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The sample autocorrelation function of non-linear time series

Basrak, Bojan

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THE SAMPLE AUTOCORRELATION FUNCTION OF NON-LINEAR TIME SERIES

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Promotor:

Co-promotor:

Beoordelingscomissie:

Prof.dr. W. Schaafsma

Dr. T. Mikosch

Prof.dr. R.A. Davis

Prof.dr. H.G. Dehling

Prof.dr. C. Klüppelberg

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