

THE SCUBA-2 COSMOLOGY LEGACY SURVEY: ALMA RESOLVES THE REST-FRAME FAR-INFRARED EMISSION OF SUB-MILLIMETER GALAXIES

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ABSTRACT

We present high-resolution ($0\prime.3$) Atacama Large Millimeter Array $870\ \mu\text{m}$ imaging of 52 sub-millimeter galaxies (SMGs) in the Ultra Deep Survey field to investigate the size and morphology of the sub-millimeter (sub-mm) emission on 2–10 kpc scales. We derive a median intrinsic angular size of $\text{FWHM} = 0\prime.30 \pm 0\prime.04$ for the 23 SMGs in the sample detected at a signal-to-noise ratio (S/N) > 10 . Using the photometric redshifts of the SMGs we show that this corresponds to a median physical half-light diameter of 2.4 ± 0.2 kpc. A stacking analysis of the SMGs detected at $S/N < 10$ shows they have sizes consistent with the $870\ \mu\text{m}$ bright SMGs in the sample. We compare our results to the sizes of SMGs derived from other multi-wavelength studies, and show that the rest-frame $\sim 250\ \mu\text{m}$ sizes of SMGs are consistent with studies of resolved ^{12}CO ($J = 3-2$ to $7-6$) emission lines, but that sizes derived from 1.4 GHz imaging appear to be approximately two times larger on average, which we attribute to cosmic ray diffusion. The rest-frame optical sizes of SMGs are around four times larger than the sub-millimeter sizes, indicating that the star formation in these galaxies is compact relative to the pre-existing stellar distribution. The size of the starburst region in SMGs is consistent with the majority of the star formation occurring in a central region, a few kiloparsecs in extent, with a median star formation rate surface density of $90 \pm 30 M_{\odot}\ \text{yr}^{-1}\ \text{kpc}^{-2}$, which may suggest that we are witnessing an intense period of bulge growth in these galaxies.

Key words: galaxies: high-redshift – galaxies: starburst

1. INTRODUCTION

Nearly 20 years after their discovery, there is still debate about the nature of the population of luminous, but highly dust-obscured sources detected at high redshifts in sub-millimeter and millimeter surveys. The observational data suggest that the $850\ \mu\text{m}$ detected sub-millimeter galaxies (SMGs) lie at a median redshift $z = 2.5 \pm 0.2$ (Simpson et al. 2014, see also Chapman et al. 2005; Wardlow et al. 2011; Yun et al. 2012; Smolčić et al. 2012; Weiß et al. 2013) and are powered by bursts of star formation in relatively massive, gas-rich galaxies (stellar masses of $\sim 10^{11} M_{\odot}$ and gas masses of $\sim 0.5 \times 10^{11} M_{\odot}$, e.g., Hainline et al. 2011; Michałowski et al. 2012; Bothwell et al. 2013) with space densities of $\sim 10^{-5}\ \text{Mpc}^{-3}$. A modest proportion of SMGs have been shown to host an accreting super-massive black hole (e.g., Alexander et al. 2008; Pope et al. 2008; Wang et al. 2013) and many appear disturbed or irregular in high-resolution rest-frame optical imaging from the *Hubble Space Telescope* (*HST*), albeit predominantly with a low Sérsic index (e.g., Conselice et al. 2003; Chapman et al. 2003; Swinbank et al. 2010a; Targett et al. 2013; Wiklind et al. 2014; Chen et al.

2014). SMGs thus share some of the traits of local ultraluminous infrared galaxies (ULIRGs), although they are $\sim 10^3$ times more abundant at a fixed far-infrared luminosity (e.g., Chapman et al. 2005; Lindner et al. 2011; Magnelli et al. 2012; Yun et al. 2012; Swinbank et al. 2014) and appear to be more massive than these proposed analogs (e.g., Tacconi et al. 2002).

In the past decade, near-infrared (NIR) spectroscopy has also identified a population of quiescent, red galaxies at $z = 1.5-3$, which have been proposed as the potential descendants of high-redshift starbursts (SMGs). The stellar populations in these high-redshift quiescent galaxies follow a fairly tight “red-sequence,” indicating that the stellar population was formed rapidly in an intense starburst phase (e.g., Kriek et al. 2008). The high star formation rates (SFRs) of SMGs ($300 M_{\odot}\ \text{yr}^{-1}$; Magnelli et al. 2012; Swinbank et al. 2014), combined with large molecular gas reservoirs, indicate that they have the potential to form a stellar component of $10^{10}-10^{11} M_{\odot}$ in 100 Myr. Such rapid stellar mass growth at high redshift has led to speculation that SMGs may be the progenitors of both these high-redshift quiescent galaxies and local elliptical galaxies (Lilly et al. 1999; Genzel et al. 2003; Blain et al. 2004; Swinbank et al. 2006; Tacconi et al.

2008; Hainline et al. 2011; Hickox et al. 2012; Toft et al. 2014; Simpson et al. 2014).

Studies investigating this proposed evolutionary scenario typically compare properties such as the stellar mass, spatial clustering, and space densities of the population and the proposed descendants. However, each of these methods has significant associated uncertainties. In particular, the stellar masses of SMGs have been shown to be highly dependent on the assumed star formation history, with systematic uncertainties of a factor of around five on individual measurements (see Hainline et al. 2011; Michałowski et al. 2012). Studies of resolved H α and ^{12}CO emission lines indicate SMGs have dynamical masses of $(1-2) \times 10^{11} M_{\odot}$ (Swinbank et al. 2006; Alaghband-Zadeh et al. 2012; Bothwell et al. 2013), placing an upper limit on the stellar masses, but the number of SMGs with measured dynamical masses is small and the samples inhomogeneous. The spatial clustering of single-dish detected sub-mm sources has been shown to match that expected for the progenitors of local ellipticals (Hickox et al. 2012). However, these results are complicated by source blending in the coarse ($19''$) resolution single-dish sub-mm imaging (Hodge et al. 2013b), whereby the detected sub-mm source comprises of multiple individual SMGs. Finally, while the space densities of SMGs and ellipticals are in agreement, the analysis is highly dependent on the assumed duty cycle of the SMG population (e.g., Simpson et al. 2014).

The morphologies of SMGs provide an alternative, and potentially powerful, tool for testing any evolutionary connection, since the population of quiescent galaxies at high redshift appear extremely compact in rest-frame optical imaging (half-light radius $[R_e] \sim 1$ kpc; e.g., Daddi et al. 2005; Zirm et al. 2007; Toft et al. 2007; Buitrago et al. 2008; van Dokkum et al. 2008; Newman et al. 2012; Patel et al. 2013; Krogager et al. 2013). Recently, Chen et al. (2014) presented Wide Field Camera 3 (WFC3)/*HST* imaging of 48 SMGs, finding a median half-light radius of $R_e = 4.4^{+1.1}_{-0.5}$ kpc, considerably larger than the quiescent population (see also Targett et al. 2013; Wiklind et al. 2014). However, as discussed by Chen et al. (2014), the SMGs in their sample are predominantly disturbed systems, with indications that the intense star formation is triggered by merger activity (see also Frayer et al. 1999; Greve et al. 2005; Tacconi et al. 2006; Engel et al. 2010; Ivison et al. 2013). The sizes presented by Chen et al. (2014) are thus likely to over-estimate the size of the system at post-coalescence. In addition, the high SFRs of SMGs, combined with large molecular gas reservoirs, means that they have the potential to at least double their stellar mass during the starburst phase. As such, understanding the spatial distribution of the ongoing star formation is crucial to understanding the stellar distribution of the post starburst galaxy.

In the local universe ULIRGs, the proposed analogs of SMGs, appear to be compact (1–2 kpc diameter) using resolved ^{12}CO /dust/mid-infrared/radio emission (Condon et al. 1991; Downes & Solomon 1998; Soifer et al. 1999; Sakamoto et al. 2008; Rujopakarn et al. 2011; Ueda et al. 2014). At the typical redshift of SMGs ($z = 2.5$) it has only been possible to resolve the dust emission in a small number of the brightest sources. Younger et al. (2010) present observations of two bright SMGs ($S_{870} = 13$ mJy and 18 mJy) using the Sub-millimeter Array (SMA). Both of these SMGs appear resolved in the SMA data and have a FWHM of $0''.6 \pm 0''.2$; at the typical redshifts of SMGs this corresponds to a physical size of 4–5 kpc. More recently Hodge et al. (2013b) obtained interferometric follow-up observations, with the Atacama Large Millimeter Array (ALMA), of single-

dish identified sub-mm sources. Hodge et al. (2013b) identified 99 SMGs in the $1''.6$ resolution ALMA maps, but found that only one SMG is resolved with a FWHM of 9 kpc. The remaining SMGs are unresolved, with sizes < 10 kpc (Hodge et al. 2013b).

Limited studies in the radio and CO also hint that SMGs have sizes of a few kiloparsecs in diameter (see Menéndez-Delmestre et al. 2009 for a discussion of the mid-infrared sizes of SMGs). However these studies suffer from two limitations. In ^{12}CO the resolution achieved using facilities such as the Plateau de Bure Interferometer or SMA is barely sufficient to resolve the emission to $\lesssim 3-4$ kpc, and studies indicate the SMGs are either unresolved or marginally resolved at this resolution (e.g., Tacconi et al. 2006; Engel et al. 2010). These ^{12}CO observations are also typically carried out in the higher- J transitions, which trace the denser and warmer gas, not necessarily reflecting the full extent of the gas reservoir, or star formation activity. Indeed there is evidence from spatially-resolved ^{12}CO ($J = 1-0$) observations of a small sample of SMGs that the cool gas extents of these systems are considerably larger than claimed from high- J observations (e.g., Ivison et al. 2011; Riechers et al. 2011; Hodge et al. 2013a). In contrast to studies of ^{12}CO emission, radio observations provide the resolution required to resolve SMGs at 1.4 GHz with eMERLIN (e.g., Biggs & Ivison 2008) or at higher frequencies with the Karl G. Jansky Very Large Array (VLA). However, such studies in the radio typically rely on the far-infrared radio correlation to identify the sub-mm sources. The identification procedure is inherently probabilistic, and as shown by Hodge et al. (2013b) the reliability and completeness of the identifications is 80% and 50 pc respectively. In addition, the form of the spatially resolved far-infrared radio correlation is still debated in the local universe, owing to the potential diffusion/leakage of the cosmic rays and the influence of magnetic fields on the resulting emission (Bicay & Helou 1990; Murphy et al. 2006, 2008). Hence translating radio sizes into star formation extents is uncertain, especially when extrapolating the results of local studies to SMGs at $z \gtrsim 2$.

In this paper, we present the results of ALMA 870 μm observations of 30 bright sub-millimeter sources. These SMGs are selected at 850 μm from the SCUBA-2 (Holland et al. 2013) Cosmology Legacy Survey of the UKIDSS Ultra Deep Survey (UDS) field, and were mapped at an angular resolution of $0''.3$ FWHM using ALMA. In this work, we focus on the sizes and morphologies of these SMGs; the catalogue and number counts will be presented in J. M. Simpson et al. (in preparation). We discuss in Section 2 our sample selection, and the ALMA 870 μm observations and their reduction. In Section 3, we present the sizes of the resolved dust emission in the SMGs, and in Section 4 we present a comparison of these typical SMGs to similar high-redshift sources and to local U/LIRGs. We give our conclusions in Section 5. Throughout the paper, we adopt a cosmology with $\Omega_{\Lambda} = 0.73$, $\Omega_{\text{m}} = 0.27$, and $H_0 = 71 \text{ km s}^{-1} \text{ Mpc}^{-1}$, in which an angular size of $1''$ corresponds to 8.5–7.5 kpc at $z \sim 1.5-3.5$. Unless otherwise stated, error estimates are from a bootstrap analysis.

2. OBSERVATIONS AND ANALYSIS

The observations discussed here targeted 30 sub-mm (850 μm) sources lying in the UKIDSS UDS field. These sources were selected from wide-field 850 μm observations of the UDS field taken as part of the SCUBA-2 Cosmology Legacy Survey (S2CLS) program with the SCUBA-2 camera on the James Clerk Maxwell Telescope. The current SCUBA-2

observations reach a typical depth of $\sigma_{850} = 1.2$ mJy across a 0.8×0.8 deg² field, and have an angular resolution of $14''.8$ FWHM. From an early version of these observations, with $\sigma_{850} = 2$ mJy, we selected a sample of 30 of the brightest sub-millimeter sources in the field, detected at $>4\sigma$ significance and hence having $850 \mu\text{m}$ flux densities of 8–16 mJy.

2.1. ALMA Data

The data reduction and source extraction from our ALMA data is described in detail in J. M. Simpson et al. (in preparation). Here we give a brief description. The ALMA data were taken on 2013 November 1, as part of the Cycle-1 project 2012.1.00090.S. We observed all 30 sub-millimeter sources with ALMA, using 7.5 GHz of bandwidth centered at 344 GHz ($870 \mu\text{m}$; Band 7); the same frequency as the original SCUBA-2 observations. We used a “single continuum” correlator setup with four basebands of 128 dual-polarization channels each.

The phase centers for the ALMA pointings are the centroid position of the sub-millimeter source from the early SCUBA-2 map. The ALMA primary beam at this frequency is $17''.3$ FWHM, larger than the $14''.8$ FWHM of the SCUBA-2 beam and so is sufficient to recover all of the SMGs contributing to the single-dish sub-millimeter emission. The array configuration for our observations was such that the 26 ALMA 12 m antennae employed had a maximum baseline of 1250 m, and a median baseline of 200 m. This is in fact more extended than our requested compact C32-1 configuration and as a result yields a synthesized beam of $0''.35 \times 0''.25$ using Briggs weighting (robust parameter = 0.5). The maximum angular scale that our observations are sensitive to is $5''$, which as we show in Section 3.1 is an order of magnitude larger than the FWHM of the sources in our sample.

The observations of our 30 targets were split into two 15 target blocks. Each block comprises seven or eight sub-blocks of 30 s observations of 10 targets, with the targets each observed five times. The targets were randomly assigned to different sub-blocks; i.e., one source might be observed in sub-blocks 1,3,5,6,7, and another in 1,2,3,4,6. Each block has a full set of calibration observations and each 5-min sub-block is separated by a 90 s phase calibration observation and a 30 s atmospheric calibration (taken on the phase calibrator). Hence, for each map we obtained a 150 s integration. Absolute flux calibration was derived from J0238 + 166 and we used observations of the secondary phase calibrator J0217 + 014, for phase referencing. The total integration time for the project was 2.6 hr.

The data were imaged using the COMMON ASTRONOMY SOFTWARE APPLICATION (CASA version 4.2.1). As detailed in J. M. Simpson et al. (in preparation) the uv data were Fourier transformed to create a “dirty” image. We then applied the same procedure adopted by Hodge et al. (2013b): a tight clean box was placed around all $>5\sigma$ emission in each map and these were cleaned down to a depth of 1.5σ . The final cleaned maps have a median angular resolution of $0''.35 \times 0''.25$ (P.A. ~ 55 deg), using Briggs weighting (robust parameter = 0.5), and a median rms of $\sigma_{870} = 0.21$ mJy beam⁻¹ (with a range from 0.19–0.24 mJy beam⁻¹). We inspect our maps and find that we do not detect any sources at sufficiently high signal-to-noise ratio (S/N) to reliably self-calibrate.

To construct the master catalog, and ensure that the extended flux from the SMGs is recovered, we repeated the imaging procedure described above, but using natural weighting, and

applying a Gaussian taper to the data in the uv plane. Applying a Gaussian taper means that a lower weighting is given to visibilities at large distances in the uv plane, producing a map with a larger synthesized beam, hence with less emission resolved out, at the expense of higher noise. The resulting maps have a median angular resolution of $0''.8 \times 0''.65$, and median rms of $\sigma_{870} = 0.26$ mJy beam⁻¹. Hence two sets of maps were created; “detection” maps with a synthesized beam of $\sim 0''.8$ FWHM and “high-resolution” maps at $\sim 0''.3$ FWHM.

To construct our catalog, we identify sources within the ALMA primary beam FWHM that are detected at $>4\sigma$ in the $0''.8$ FWHM “detection” maps, and extract both the peak flux density and the total flux density in a $0''.8$ radius aperture for each SMG. We search for sources outside the ALMA primary beam FWHM, but do not find any statistically significant detections (see J. M. Simpson et al. in preparation). In total we identify 52 SMGs above 4σ in the 30 ALMA maps, at $0''.8$ FWHM resolution. These SMGs have a range of $870 \mu\text{m}$ flux density of 1–14 mJy and we recover the single-dish SCUBA-2 with a median ratio of $S^{\text{SCUBA2}}/S^{\text{ALMA}} = 1.04 \pm 0.05$. As the analysis presented in this paper is focused on the size distribution of SMGs, we cut our SMG sample at a higher significance limit to provide sufficiently high S/Ns for the SMGs to reliably measure their sizes. As we show below, this corresponds to $S/N \geq 10$ ($S_{870} \gtrsim 4$ mJy) at $0''.8$ resolution, which reduces our sample to 27 SMGs. In order to check the measured fluxes of these sources we also used the IMFIT routine in CASA to model each SMG and find good agreement between the model and aperture derived flux densities ($S^{\text{Model}}/S^{\text{Aperture}} = 1.02 \pm 0.01$). Where appropriate in the following analysis, we will also use the average properties of the remaining 25 SMGs with $S_{870} \lesssim 4$ mJy to test for trends with flux density across the whole sample.

Given the relatively bright $\gtrsim 8$ mJy flux limit used to select our target sample, we need to be aware of the potential influence of gravitational lensing (e.g., Blain 1996; Chapman et al. 2002).¹⁶ Indeed, we identify four examples of potential gravitationally lensed sources in our bright SMG sample: UDS 109.0, UDS 160.0, UDS 269.0, and UDS 286.0. All of these sources appear to be close to, but spatially offset from, galaxies at $z \lesssim 1$ (Figure 1). If these sources are lensed then their apparent sizes need to be corrected for lens amplification. However, they all appear singly imaged (with no sign of multiple images at our sensitive limits) and as we have no precise estimates of their redshifts or the masses of the foreground lenses, it is impossible to reliably determine this correction. We therefore highlight these four SMGs in Figure 1, and note that the derived sizes for these sources are likely to be over-estimated. When discussing the properties of our sample we do not include the potentially lensed sources in the analysis, and so our final sample consists of 23 SMGs detected at $S/N > 10\sigma$.

2.2. Robustness of Imaging

As we show in Section 3.1, most of the SMGs in our sample are resolved in the $0''.3$ resolution ALMA maps. However, we now perform two tests to ensure that an error in the calibration

¹⁶ Lensing models predict that our sample contains 1–2 SMGs that are lensed with an amplification factor >2 (e.g., Paciga et al. 2009). However, we note that the prediction is based on the Chapman et al. (2005) redshift distribution for SMGs, which does not contain the high-redshift tail of sources seen in other SMG redshift distributions (e.g., Yun et al. 2012; Smolčić et al. 2012; Weiß et al. 2013; Simpson et al. 2014). Hence the prediction for the number density of lensed sources is likely to be a lower limit.

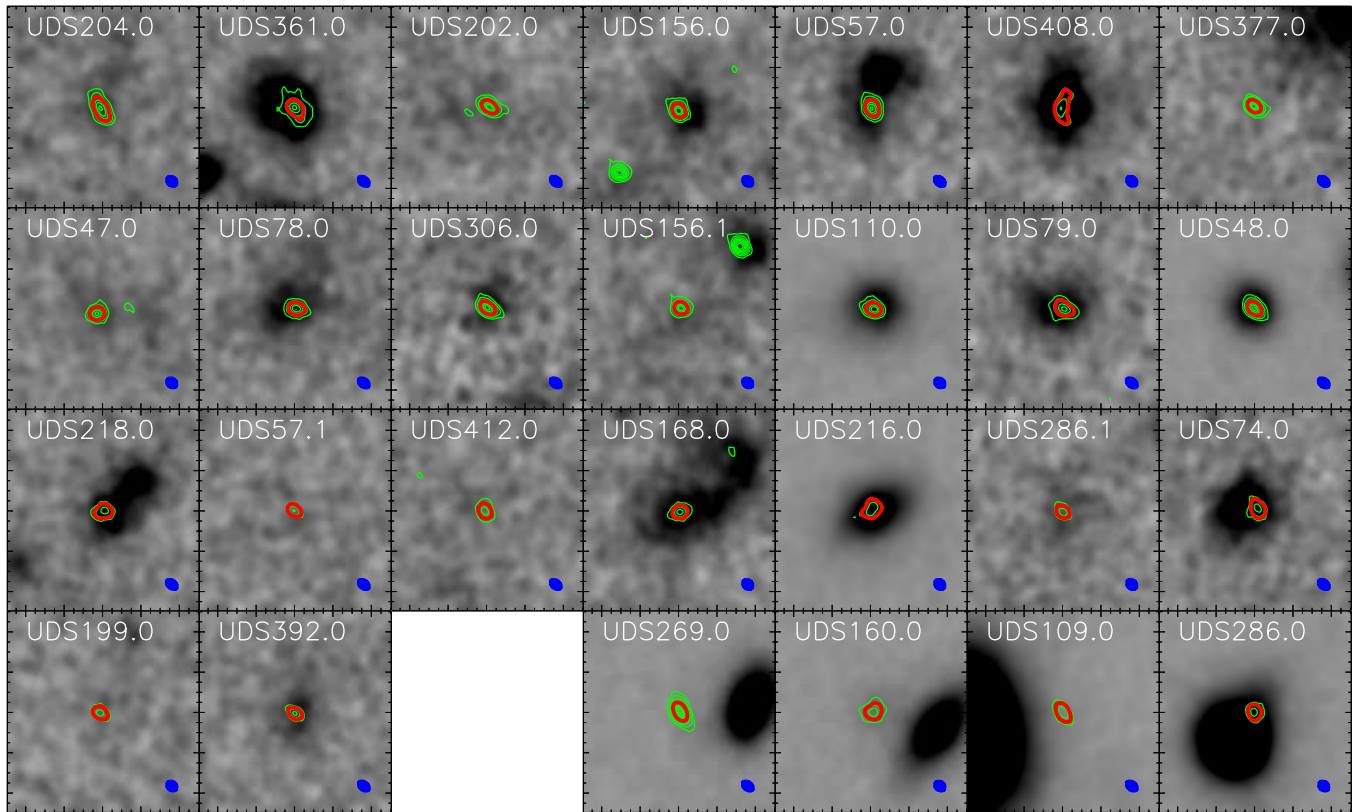


Figure 1. Grayscale K -band images of the 27 bright ($S/N > 10\sigma$) ALMA-identified SMGs in our sample. The images are in order of decreasing $870 \mu\text{m}$ flux density, except for the final four panels, which are classed as potentially lensed SMGs (images are separated by a blank panel). Each panel is $5'' \times 5''$ and we contour the ALMA maps over the images of the galaxies. The green contours on each image represent ALMA $870 \mu\text{m}$ emission at $4, 8, 12, \dots \times \sigma$, and a single red contour represents where the ALMA $870 \mu\text{m}$ surface brightness is 50% of the peak value; for an ideal point source this contour should be identical to the size of the ALMA beam FWHM (bottom right of each panel). We note that the red contour appears more extended than the beam, indicating that these SMGs are resolved in the $0''.3$ resolution ALMA data. Overall, 15% of the SMGs are not detected in the K -band imaging (5σ detection limit 25.0 mag).

of the raw data does not drive our conclusion that the sources are resolved.

The observing strategy for our targets was such that each SMG was observed five separate times through the observing block, with phase calibration observations between each repeat observation. First, we test for variations in the source size as a function of time, as might be expected if the phase solution applied to the data does not correctly model fluctuations. To do so, we separately image each repeat observation of UDS 204.0, the brightest SMG in our sample (the integration time is sufficient to detect the source at 8σ – 10σ in an individual scan). The SMG appears resolved in all five images, with an intrinsic source size in the range $0''.52$ – $0''.63$, and all sizes consistent within the associated 1σ uncertainties ($\sim 0''.05$).

Second, we reclassify an observation of the phase calibrator as a science target observation in the observing sequence and repeat the calibration of the data set. If an error in the calibration of the raw data, due to phase variations, are causing the SMGs in our sample to appear resolved, then the phase calibrator will also appear resolved in this scan. We image this phase calibrator scan in the same manner as the SMG observations and model the emission using the IMFIT routine. In the individual scan the phase calibrator has an intrinsic size of $\text{FWHM} = 0''.06 \pm 0''.01$, which is marginally higher than the intrinsic size measured in an image combining all scans ($\text{FWHM} = 0''.03 \pm 0''.01$). However, by removing a phase calibrator scan we have introduced a 10 minute gap in our calibration observations, which is double that used throughout the observations. Hence any difference in the

size of the phase calibrator should be classed as an upper limit on the uncertainty due to errors in the phase calibration of the data. Taken together these tests indicate that the SMGs in our sample do not appear resolved due to errors in the calibration of the raw data.

In our analysis in Section 3.1, we use the IMFIT routine in CASA to fit an elliptical Gaussian model (convolved with the synthesized beam) for the $870 \mu\text{m}$ emission from each SMG. However, before applying this approach to the bright SMGs in our sample, we now test the reliability of the fits as a function of S/N using simple simulated galaxies. To do so, we create 20,000 elliptical Gaussian model sources with a uniform distribution of peak S/N from 4 to 30 (covering the range of SMGs in our full sample) and a major-axis size distribution that is uniform from $0''$ to $1''$. The model sources are distributed uniformly in S/N at $0''.8$ resolution, reflecting the selection function of our full SMG catalog. In order to use realistic noise maps we add these models to a randomly chosen position in one of the residual (source-subtracted) ALMA maps.

We use CASA to fit an elliptical Gaussian to each injected model source and derive the best-fit size for each. We note that the IMFIT routine can return a point source solution if this is the best model. For each model parameter we calculate the fractional offset between the input model value and the recovered value. As expected we find that the precision of the recovered parameters is a function of S/N . To ensure that the sizes we derive for the SMGs are reliable we define a selection limit that the 1σ spread in $(\text{FWHM}^{\text{Model}} - \text{FWHM}^{\text{True}}) / \text{FWHM}^{\text{True}} < 0.3$, i.e.,

68% of the model sources are recovered with a fractional error less than 30%. We find that this requirement is met for sources that are detected at a $S/N \geq 10$, which is the justification for our use of this limit to define the bright SMG sample analyzed in this paper.

These simulations also indicate a small bias in the recovered size for sources with S/N between 10σ and 30σ of $(FWHM^{\text{Model}} - FWHM^{\text{True}})/FWHM^{\text{True}} = 0.018 \pm 0.002$ (1σ spread of ± 0.14), which we have not corrected for in the following analysis. The simulations also allow us to investigate the resolution limit of our maps, by determining the true size of a model source for which the `IMFIT` routine returns a point source best-fit solution. For SMGs with $S/N = 10$ – 30 we find that 90% of the model sources that are best fit by point source models using `IMFIT` actually have a “true” size $\leq 0''.18$ (i.e., smaller than half the size of the beam major axis). Hence, we can be confident that any SMGs that have a point source best-fit model have a size $\leq 0''.18$, and we adopt this as an upper limit for the size of the unresolved SMGs.

2.3. Multi-wavelength Properties

During our analysis we use archival multi-wavelength information on this well-studied field. An extensive analysis of the multi-wavelength properties of the SMG sample will be presented in C.-J. Ma et al. (in preparation), but for the purposes of this paper we use two pieces of information from that work: constraints on the likely redshifts of the SMGs using photometric redshifts; and estimates of their far-infrared luminosities.

First, we use the photometric redshift catalog of this field produced by the UKIDSS UDS team, which is based on a K -band selected sample of sources. To briefly summarize, photometric redshifts are determined for each field source by fitting template spectral energy distributions (SEDs) to the observed $UBVRi'z'JHK$ and IRAC 3.6 and 4.5 μm photometry, using the public SED fitting code `EAZY` (Brammer et al. 2008). Excellent agreement is found between the photometric and spectroscopic redshifts for 2146 sources in the field, with a median dispersion of $(z_{\text{phot}} - z_{\text{spec}})/(1 + z_{\text{spec}}) = 0.03$ (see Hartley et al. 2013; Mortlock et al. 2013).

Matching the SMG catalog to the photometric redshift sample finds 19 matches within $1''$ of the 23 bright SMGs, which leaves four of the SMGs without redshift information. We also searched for IRAC counterparts for the four SMGs without photometric redshifts and find that three have detections in the IRAC imaging; however, the limited number of photometric bands available for all of these sources mean it is impossible to derive precise photometric redshifts. Simpson et al. (2014) argue that these NIR-faint SMGs typically lie at higher redshifts than the optical/NIR-brighter SMGs, and so we adopt their approach and assign these sources a redshift of $z = 4 \pm 1$.

To derive the FIR luminosities of the SMGs we exploit the *Herschel* SPIRE imaging (Pilbratt et al. 2010; Griffin et al. 2010) of the field at 250, 350, and 500 μm , along with the precise position of the ALMA source to deblend and extract flux densities for the SMGs. Following the approach of Swinbank et al. (2014), they use a prior catalog of sources detected at 24 μm or 1.4 GHz, along with the ALMA source positions, to model the sources contributing to the map flux in the vicinity of each SMG. Having extracted flux densities or limits in the three SPIRE bands, along with the ALMA 870 μm flux density, they fit a library of model SED templates (see Swinbank et al. 2014), to the FIR-photometry and determine the best-fit template. We integrate the best-fit SED from 8 to 1000 μm to derive the total

far-infrared luminosity of each SMG. If an SMG is undetected in the *Herschel* 250, 350, and 500 μm imaging, then the far-infrared luminosity is treated as an upper limit. We measure a median far-infrared luminosity for the 23 SMGs in our sample of $L_{\text{FIR}} = (5.7 \pm 0.7) \times 10^{12} L_{\odot}$, and a median dust temperature of $T_{\text{d}} = 32 \pm 3$ K. We find that 5/11 and 10/14 SMGs detected at $S/N = 5\sigma$ – 10σ and $S/N = 4\sigma$ – 5σ , respectively, are undetected in the *Herschel* 250, 350, and 500 μm imaging. We stack the *Herschel* SPIRE maps for these subsets and derive an average $L_{\text{FIR}} = 3.6_{-0.9}^{+0.8} \times 10^{12} L_{\odot}$ and $L_{\text{FIR}} = 2.7_{-0.6}^{+1.6} \times 10^{12} L_{\odot}$ for the $S/N = 5\sigma$ – 10σ and $S/N = 4\sigma$ – 5σ subsets, respectively.

3. RESULTS

3.1. Resolved Dust Emission

We show the ALMA maps with a $0''.3$ FWHM resolution synthesized beam for the 27 $S/N \geq 10$ SMGs in Figure 1. These are presented as contours overlaid on K -band grayscale images, to allow the reader to make a qualitative comparison of the size and shape of the contour corresponding to the half-peak-flux level and the corresponding size for the synthesized beam. We see evidence in a majority of the SMGs that the sub-millimeter emission appears to be more extended than would be expected for an unresolved source with the same peak flux, with several examples also showing structure on smaller scales (e.g., UDS 74.0, UDS 216.0, UDS 218.0, UDS 361.0, UDS 408.0).

To quantitatively test if the SMGs are resolved in our data we initially perform two non-parametric tests. First we compare the peak flux of each source in the $0''.8$ FWHM observations to the higher resolution $0''.3$ FWHM imaging (note that the maps are calibrated in Jy beam^{-1}). The peak flux of the SMGs is lower in the $0''.3$ resolution maps, with a median ratio of $S_{\text{pk}}^{0.3}/S_{\text{pk}}^{0.8} = 0.65 \pm 0.02$, and a 1σ range of ± 0.04 . A drop in the peak flux density between the sources imaged at different resolutions indicates that flux from each SMG is indeed more resolved in the higher-resolution imaging. We note that a 40% reduction in the peak flux between the $0''.3$ and $0''.8$ resolution imaging corresponds to an intrinsic source size of $\sim 0''.3$.

As a second test we compare the total flux density in an aperture for each source to the peak flux density at both $0''.3$ and $0''.8$ FWHM resolution. We convert each map into units of Jy pixel^{-1} and measure the “total” flux density in a $0''.8$ radius aperture. The ratio of the peak-to-total flux density is 0.50 ± 0.03 at $0''.3$ FWHM resolution, compared to 0.83 ± 0.03 at $0''.8$ FWHM. This supports the conclusion that the bulk of the bright SMGs are resolved by ALMA at 870 μm with a $0''.3$ FWHM synthesized beam, and suggests that the average angular size of the population is $0''.3$ – $0''.4$. We note that the aperture fluxes of the SMGs measured in the $0''.3$ and $0''.8$ imaging are in good agreement, with a median ratio of $S_{\text{Aper}}^{0.3}/S_{\text{Aper}}^{0.8} = 1.02 \pm 0.03$.

We next investigate whether the SMGs appear resolved in the uv plane, rather than in the image plane, compared to the calibrator sources used for our observations (which are expected to be unresolved). For each source we align the phase center of the map to the position of the SMG or calibrator source, and extract the amplitudes for each source as a function of uv distance. The amplitudes represent the observed flux of the source on different angular scales in the image plane, with the longest baseline providing information on the smallest angular scales that our observations are sensitive to. For an ideal point source the amplitudes should be constant with uv distance. As

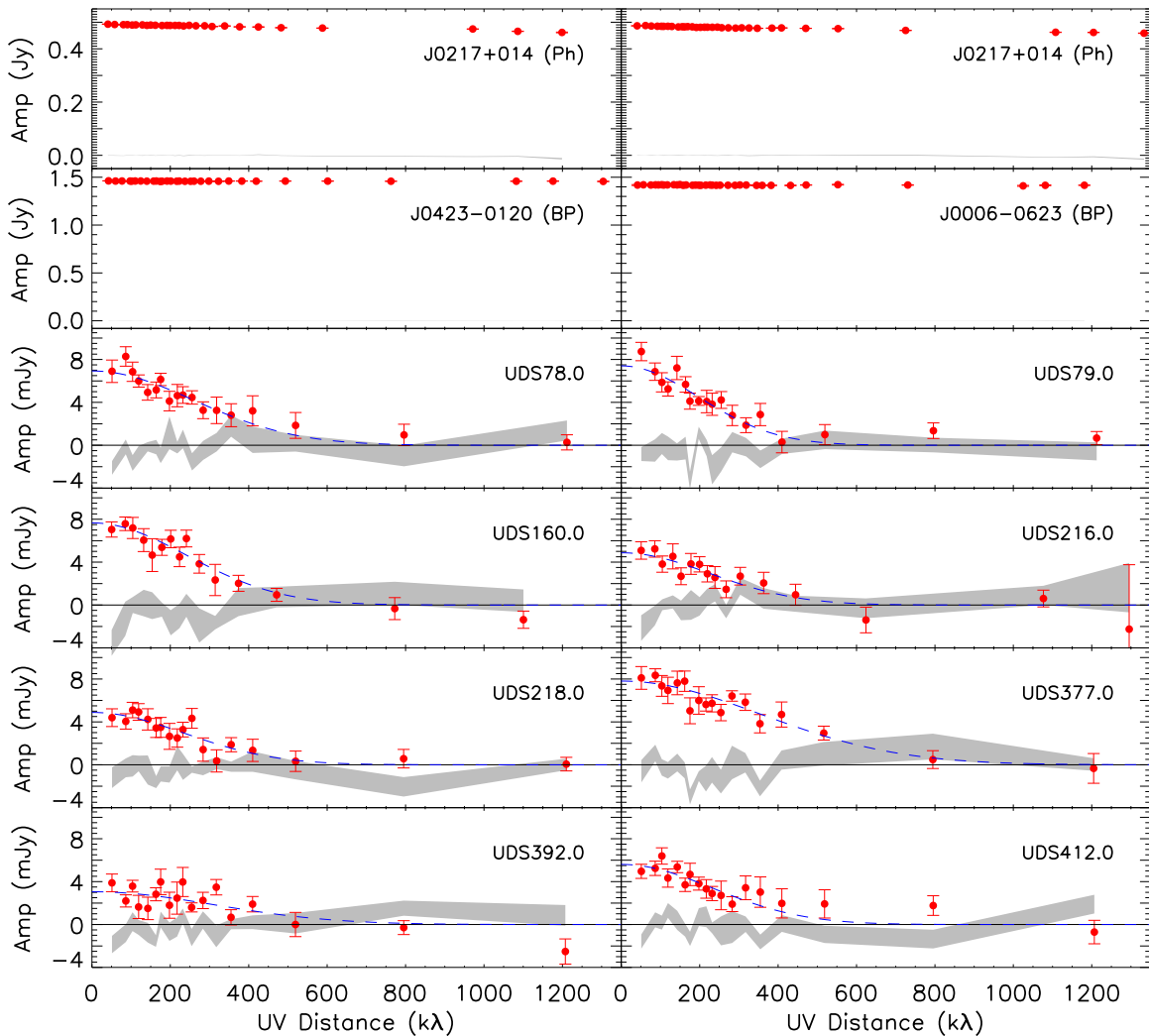


Figure 2. Components of the complex visibility vs. uv distance for the phase (Ph) and bandpass (BP) calibrators from both measurement sets (top), and an example eight SMGs from our sample (lower panels). The real components of the complex visibilities are plotted as data points, while the 1σ range of the imaginary components is shown as a gray shaded region. Both the real and imaginary components are plotted on the same scale on the left axis. The amplitudes of both sets of calibrators are relatively flat with uv distance, indicating that they are unresolved point sources, although we note a marginal drop in the flux of the phase calibrator, which suggests it is weakly resolved. In contrast the amplitudes for seven of the SMGs decline strongly with uv distance, confirming our conclusion that these sources are resolved in the sub-mm imaging at $0''.3$ resolution. We plot on each SMG a dashed line representing the best-fitting Gaussian to the amplitudes. We note that our measurements of the size and flux density of these SMGs in the image plane are consistent with the Gaussian fits to the amplitudes (the median ratio in size is $\text{FWHM}^{uv} / \text{FWHM}^{\text{image}} = 0.9 \pm 0.2$).

Figure 2 demonstrates we do indeed recover an effectively flat distribution for both the phase and bandpass calibrators.

In Figure 2, the amplitudes as a function of uv distance for the eight SMGs, which are the sole sources detected in their respective ALMA maps (restricting the sample in this way removes any complications due to modeling and subtracting other sources in the primary beam). The amplitudes of seven of the SMGs clearly decrease with increasing uv distance. A single SMG, UDS 392.0, appears to be only marginally resolved on the longest baselines (our analysis in the image plane identifies this SMG as unresolved, see Figures 2 and 3). We fit the amplitudes for each SMG with a single Gaussian component and determine the equivalent size in the uv plane. The model fits in the uv and image planes are consistent, and derive a median size ratio between the image- and uv -derived sizes of $\text{FWHM}^{uv} / \text{FWHM}^{\text{image}} = 0.9 \pm 0.2$ and a median flux density ratio $S^{\text{image}} / S^{uv} = 1.1 \pm 0.1$. In 2–3 of the SMGs the flux density does not fall to zero on baselines $\gtrsim 600$ kλ, indicating that there

is unresolved flux in these sources on an angular scale of $\lesssim 0''.3$, but this unresolved component comprises $\lesssim 10\%$ of the total flux density.

Given that our non-parametric tests indicate that the SMGs are resolved in our $0''.3$ imaging, we now chose to fit a more complex model to the sources. Using the IMFIT routine we determine the best-fit elliptical Gaussian model for the 23 SMGs in our bright sample ($S/N > 10\sigma$). The free parameters of the model are position; peak flux density; major and minor axis; and position angle. The median intrinsic size of the 23 SMGs is $0''.30 \pm 0''.04$ (deconvolved FWHM of the major axis), and one SMG is modeled as a point source; as the intrinsic sizes of the sources are comparable to the beam we choose to focus our analysis on the FWHM of the major axis. The median χ^2 for the elliptical Gaussian fit is 38.3 ± 1.4 , and the number of degrees of freedom of the fit is 33 (we define beam to be the size of the resolution element). If we fit each SMG with a point source model then the median difference in χ^2 between the

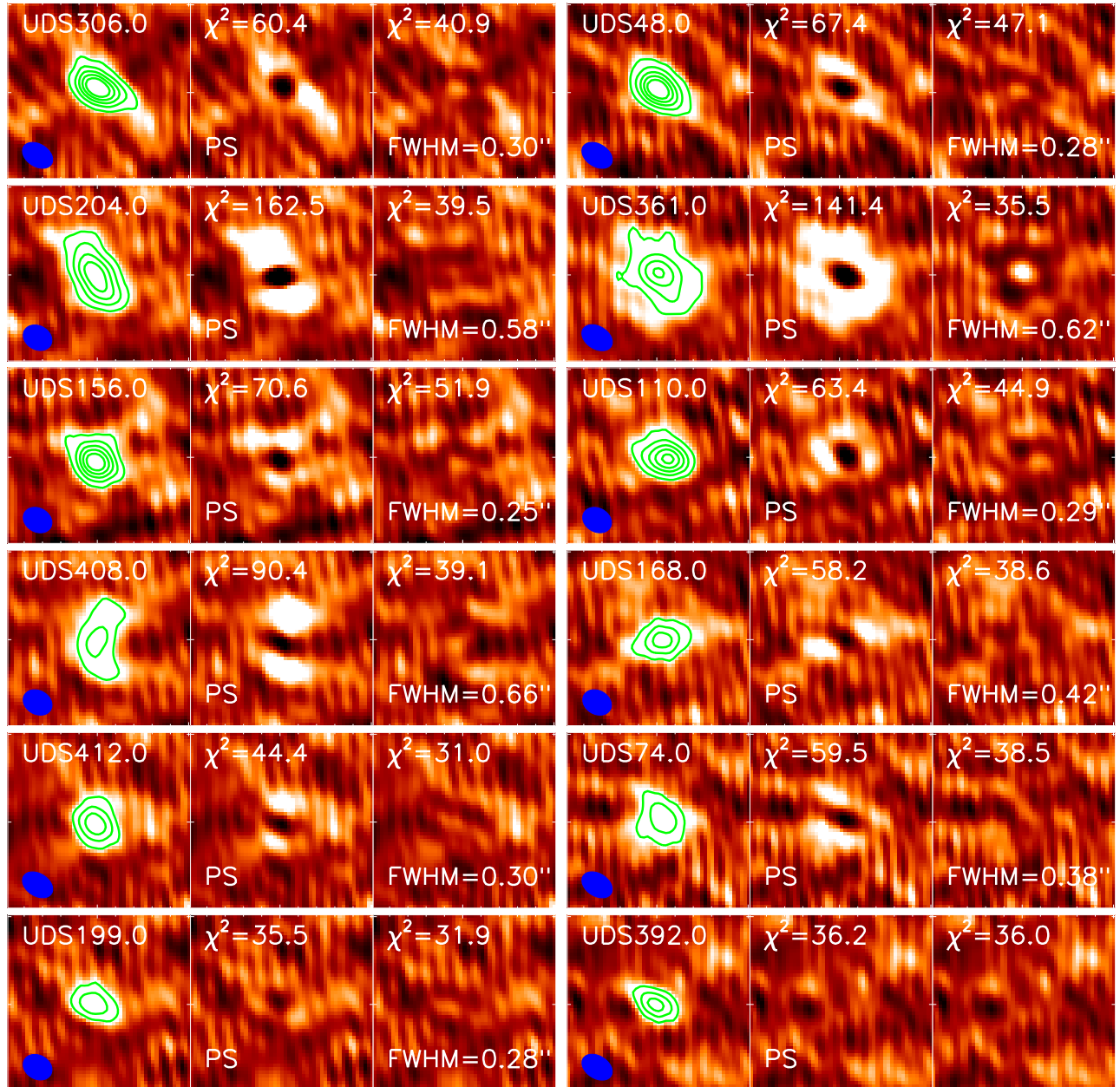


Figure 3. Examples showing $2'' \times 2''$ images of our high-resolution $870 \mu\text{m}$ maps ($0''.3$; left) alongside the residuals from fitting a point source model (PS; middle of each set of three panels) and an elliptical Gaussian model (resolved; right) for 12 example SMGs in our sample. The green contours represent $870 \mu\text{m}$ emission at 4, 8, 12, ... $\times \sigma$, and the color-scale in each image is clipped at $\pm 3\sigma$. The ALMA beam is shown in the bottom left of the left-hand column. The SMGs presented here are chosen such that they span the full range in detection significance for the sample, and are a fair representation of the data quality of our ALMA maps. In 11 of these images there are significant residuals when fitting a point source model to the $870 \mu\text{m}$ emission, indicating that these sources are resolved in our ALMA maps. In contrast we highlight UDS392.0, which is well described by a point source model and is classed as unresolved in our analysis. For the full sample of 23 SMGs the median difference in χ^2 between the best-fit extended and point-source model is $\Delta\chi^2 = 20 \pm 2$. We find that 22/23 SMGs are resolved in our $0''.3$ resolution imaging, and derive a median angular size for the sample of $0''.30 \pm 0''.04$ (deconvolved FWHM of the major axis).

best-fit extended and point-source model is $\Delta\chi^2 = 20 \pm 2$ (see Figure 3).¹⁷

The top panel of Figure 4 shows the sizes of the SMGs as a function of their $870 \mu\text{m}$ flux density. The dispersion of the $870 \mu\text{m}$ sizes is small and there is no clear trend in the size of the

dust emission region with $870 \mu\text{m}$ flux density. We note however that the two SMG with $S_{870} \sim 12$ mJy in the sample are around two times larger than the median of the sample. While this may be interpreted as a weak trend in the size of SMGs with $870 \mu\text{m}$ flux density we caution against a strong conclusion, given the limited sample size at these fluxes. We also show the sizes of two bright SMGs ($S_{870} = 13$ mJy and 18 mJy) presented by Younger et al. (2010). These SMGs were observed with the SMA and both appear marginally resolved in the uv plane, with sizes of $0''.6 \pm 0''.2$ (deconvolved FWHM). While the size measurements for these sources have large associated uncertainties, they are consistent with the sizes presented here.

¹⁷ We also determined the best-fit Gaussian model for the SMGs in the $0''.8$ imaging but find that 65% are unresolved, consistent with our results from the higher resolution ($0''.3$) imaging. The resolved sources in the $0''.8$ imaging have a median FWHM ratio between the two sets of imaging of $\text{FWHM}^{0.8}/\text{FWHM}^{0.3} = 1.2 \pm 0.1$, however, we strongly caution that we have not included upper limits in this calculation, and hence the ratio will be biased towards higher values.

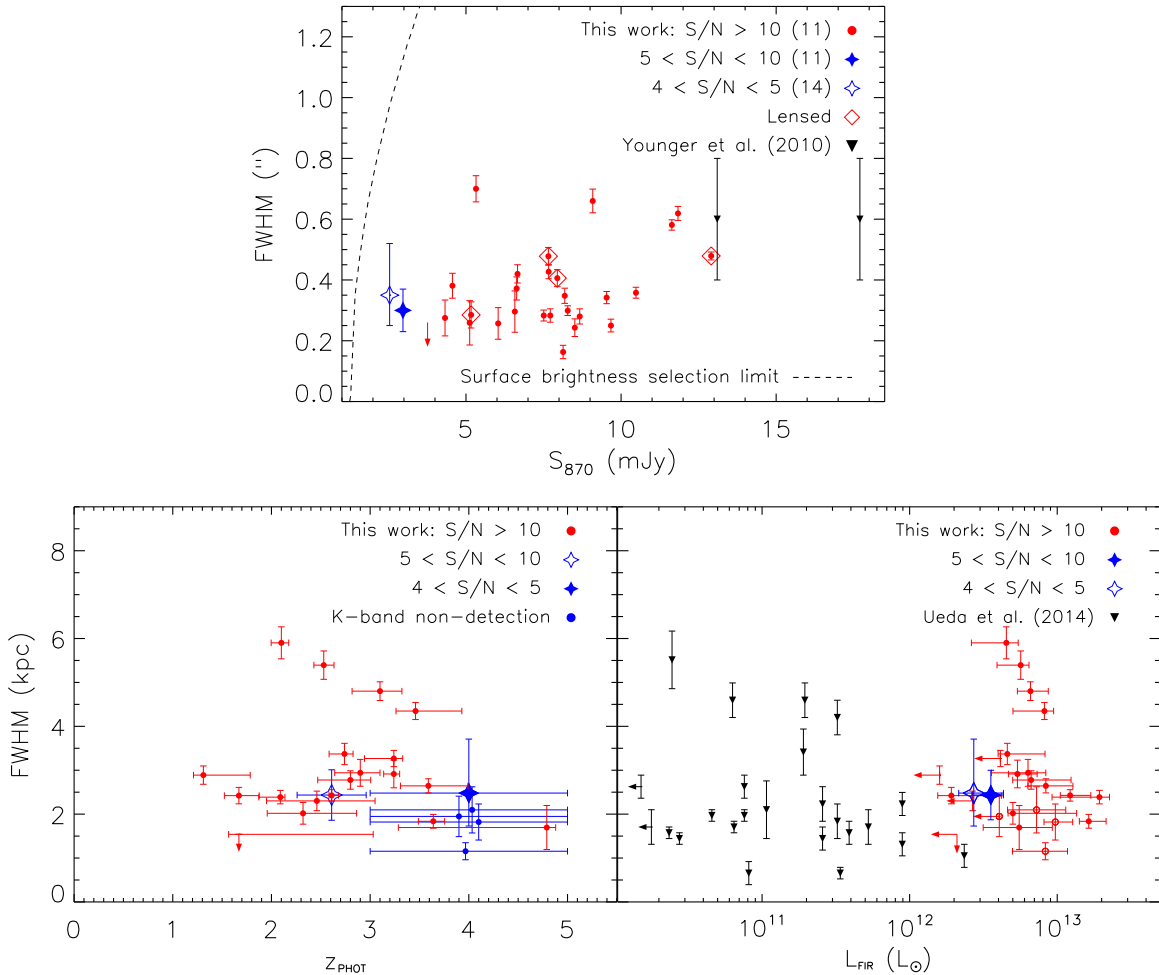


Figure 4. Top: Angular size distribution of the $870\ \mu\text{m}$ emission from SMGs as a function of their $870\ \mu\text{m}$ flux density. A dashed line represents our surface brightness selection limit. The 23 SMGs detected at $\geq 10\sigma$, have a median intrinsic size of $0.30 \pm 0'.04$ (deconvolved FWHM of the major axis). We stack the $870\ \mu\text{m}$ emission from SMGs detected at 5σ – 10σ and 4σ – 5σ , and show the size derived from each stack. We find that these $870\ \mu\text{m}$ faint SMGs have sizes that are on average consistent with the brighter SMG distribution. We highlight four SMGs that are potentially lensed sources, but note that these are not included in our analysis. For comparison we show the sizes of two bright SMGs measured from observations with the SMA (Younger et al. 2010). Bottom left: Physical size of SMGs as function of redshift. Four SMGs in our sample do not have a photometric redshift, and we fix the redshift of these sources at $z = 4 \pm 1$ (the redshifts are offset in the plot). The potentially lensed SMGs are not shown on this figure. The median physical size of the 23 SMGs in the sample is $\text{FWHM} = 2.4 \pm 0.2\ \text{kpc}$, and we do not find a trend in the physical size with redshift. From our stacking analysis we measure an average physical size for the SMGs detected at $S/N = 5\sigma$ – 10σ of $2.4 \pm 0.6\ \text{kpc}$, consistent with our results for the $870\ \mu\text{m}$ brighter SMGs. We also show the results of stacking the 14 SMGs detected at $S/N = 4\sigma$ – 5σ , but note that 8/14 sources in the stack do not have a photometric redshift. Bottom right: Physical size of the SMGs in our sample as a function of FIR luminosity. The 23 SMGs shown have a median FIR luminosity of $L_{\text{FIR}} = (5.7 \pm 0.7) \times 10^{12}\ L_{\odot}$, and a median physical size of $\text{FWHM} = 2.4 \pm 0.2\ \text{kpc}$. We do not find a trend between L_{FIR} and the physical size of the SMGs. For comparison we also show the sizes of local “merger-remnants” measured from interferometric observations of the ^{12}CO ($J = 1-0/2-1/3-2$) molecular emission line. These local galaxies have a median size of $1.9 \pm 0.2\ \text{kpc}$, and are marginally smaller than the SMGs presented here. As the “low”- J ^{12}CO typically exceeds the size of the star forming region, the star formation in SMGs appears to be considerably more extended than in local U/LIRGs.

To search for trends in our sample over a larger dynamical range we have also used the fainter SMGs detected in our ALMA maps. While the individual sizes measured for these galaxies have significant uncertainties, we can attempt to derive a typical size for samples of faint SMGs via stacking (this is reasonable as the synthesized beam does not vary significantly between observations; the beam major and minor axes vary by at most $0'.03$ and $0'.02$, respectively, across the full sample). We split the fainter 25 SMGs into roughly equal sub-samples detected at $S/N = 5\sigma$ – 10σ (median $S_{870} = 3.1 \pm 0.5\ \text{mJy}$) and $S/N = 4\sigma$ – 5σ (median $S_{870} = 2.6 \pm 0.3\ \text{mJy}$), containing 11 and 14 SMGs, respectively. We stack the $0'.3$ FWHM maps of these sub-samples and use `IMFIT` to measure the size of the stacked profile. We derive sizes of $0'.30 \pm 0'.07$ and $0.35^{+0.17}_{-0.10}$ for the two sub-samples, respectively. The errors on the measured size of each subset are derived by bootstrapping the maps included in the stacks and repeating the analysis. These results indicate

that at least on average the 1–4 mJy SMGs in our full sample have the same size distribution as those with observed $870\ \mu\text{m}$ flux densities of 4–15 mJy sources (see Figure 4).

4. DISCUSSION

4.1. Physical Size of SMGs

The 23 SMGs detected at $>10\sigma$ in our sample have a median angular FWHM of $0'.30 \pm 0'.04$. For each SMG we use the photometric redshift to convert the measured angular diameter into an intrinsic physical scale, and derive that the median physical size of the SMGs is $2.4 \pm 0.2\ \text{kpc}$ (FWHM of the major axis). As shown in Figure 4, the distribution has a narrow interquartile range of 1.8–3.2 kpc, indicating that the dispersion in the sizes of our sample of SMGs is small. We use the results of our stacking analysis to derive an average physical size of $2.4 \pm 0.6\ \text{kpc}$ and $2.5^{+1.2}_{-0.7}\ \text{kpc}$, at a median redshift of

$z = 2.6 \pm 0.4$ and $z = 4 \pm 1$, for the $S/N = 5\sigma$ – 10σ and $S/N = 4\sigma$ – 5σ subsets, respectively, indicating no trend in the size of SMGs with redshift. An important caveat of this result is that only one SMG in our sample has a photometric redshift of $z \gtrsim 3.5$. Four SMGs do not have a photometric redshift and it is likely that these sources lie at $z \sim 4$ (see Simpson et al. 2014); however, the uncertainties on these redshifts are large. At $z = 4$ these SMGs have a distribution of physical FWHM from <1.3 – 2.1 kpc, and are consistent with the lower redshift SMGs in the sample. However, if they instead lie at $z = 6$, then the range of FWHM is <1.1 – 1.7 kpc, and these sources would be smaller than all but one $z < 4$ SMG.

Recently Weiß et al. (2013) discussed that evolution in the size of SMGs with redshift is a possible explanation for the discrepancy between the redshift distribution of lensed and unlensed SMGs. As 60% of the SMGs presented by Weiß et al. (2013) lie at $z > 3.5$ we cannot investigate this claim further. However, we note that for the *unlensed* SMGs presented here, we do not find any evolution in the sizes of the $870 \mu\text{m}$ emitting region at $z < 3.5$.

4.1.1. Comparison of the Multi-wavelength Sizes of SMGs

We now compare the $870 \mu\text{m}$ sizes presented here to the sizes of SMGs measured from observations at different wavelengths. First, we compare our results to a sample of 12 SMGs (median $S_{850} = 6.8 \pm 0.6$ mJy) with deconvolved sizes measured from $0''.5$ resolution 1.4 GHz/VLA imaging (Biggs & Ivison 2008). In their analysis Biggs & Ivison (2008) fit an elliptical Gaussian model to the 1.4 GHz emission from each SMG, deriving a median angular size of $\text{FWHM} = 0''.64 \pm 0''.14$. At the redshifts of these SMGs this angular size corresponds to a median physical size of $\text{FWHM} = 5.3 \pm 1.1$ kpc. Four SMGs in their sample do not have a redshift and we set these to the median redshift of the sample ($z = 2$; consistent with the radio-detected SMGs in Simpson et al. 2014). Hence the 1.4 GHz sizes for the SMGs presented by Biggs & Ivison (2008) are about two times larger than the $870 \mu\text{m}$ sizes presented here.

It is important to initially note that the radio counterparts to the sub-mm emission presented in Biggs & Ivison (2008) were identified via a probabilistic approach using the far-infrared radio correlation. As shown by Hodge et al. (2013b) these identifications are 80% reliable, and so we might expect that two or three of the radio sources presented in Biggs & Ivison (2008) are not the true counterpart to the sub-mm emission. However, we do not know if such mis-identifications are likely to be biased towards galaxies with larger, or smaller, sizes at 1.4 GHz.

Another possible explanation for the discrepancy between the radio and far-infrared sizes of SMGs is that the diffusion length of cosmic rays (~ 1 – 2 kpc) is expected to be larger than the diffusion length of far-infrared photons (~ 100 pc), due to magnetic fields efficiently transporting cosmic rays through the host galaxy. Murphy et al. (2008) present a study of 18 local star-forming galaxies with resolved imaging at $70 \mu\text{m}$ and 1.4 GHz. They show that the radio emission from these galaxies can be modeled as the convolution of the far-infrared emission with an exponentially declining kernel, with an e -folding length of the kernel of 1 – 2 kpc (see also Bica & Helou 1990; Murphy et al. 2006). We convolve the median $870 \mu\text{m}$ size of the SMGs with this exponential kernel and find that the FWHM of the convolved profile is 3.8 – 5.2 kpc, showing that the radio sizes of Biggs & Ivison (2008) are likely consistent with our $870 \mu\text{m}$ sizes.

The galaxies presented by Murphy et al. (2008) are “normal” star-forming galaxies, with SFRs three orders of magnitude lower than the SMGs presented here. The e -folding length of the kernel has been shown to depend on both SFR density and morphology, with high SFR densities and irregular galaxies having lower e -folding lengths (Murphy et al. 2008). In both of these situations ordered magnetic fields are disrupted, allowing cosmic ray electrons to stream more freely out of the galaxy, resulting in a shorter scale length. As such, we caution that a scale length of 1 – 2 kpc might be an over-estimate of the appropriate scale length for the radio emission from SMGs.

Next we compare the $870 \mu\text{m}$ sizes of SMGs to the sizes of SMGs measured from ^{12}CO emission lines. Engel et al. (2010) present a compilation (including new observations) of the sizes of SMGs measured from resolved ^{12}CO ($J = 3$ – $2/4$ – $3/6$ – $5/7$ – 6) emission lines (see also Tacconi et al. 2006, 2008). Deriving a median size for the sample is challenging, as the upper limits on the size of unresolved SMGs are typically similar to the sizes of the resolved sources. Treating the unresolved sources as point sources, the median size of the sample is $\text{FWHM} = 2.3 \pm 1.1$ kpc, but this rises to 3.7 ± 0.6 kpc if upper limits are taken as the “true” source size. In our analysis we have not included the sizes taken from Bothwell et al. (2010), as it is not clear that these sizes have been deconvolved for the beam.

In the study by Engel et al. (2010) the ^{12}CO -emission lines are often either unresolved, or marginally resolved, with sizes constrained at only 1σ – 2σ . The sizes are also measured from ^{12}CO emission lines across a range of rotational transitions, from $J = 2$ – 1 to 7 – 6 , and we note that there is ongoing debate over whether emission from different transitions traces the same molecular gas (Weiß et al. 2007; Panuzzo et al. 2010; Bothwell et al. 2013; Narayanan & Krumholz 2014). Due to these issues we simply note that the sizes derived from *moderate- J* transitions of ^{12}CO are broadly consistent with the median $870 \mu\text{m}$ size of the SMGs in our sample.

Finally, we compare our results to the sizes of SMGs derived from high-resolution *HST* NIR imaging. Chen et al. (2014) recently presented *H*-band/*HST* imaging (rest-frame optical imaging) of 48 SMGs. These SMGs were drawn from the ALESS sample (Hodge et al. 2013b), and have precise $\lesssim 0''.3$ identifications from ALMA $870 \mu\text{m}$ observations. Chen et al. (2014) fit a Sérsic profile to the *H*-band emission, deriving a median half-light radius of $R_e = 4.4^{+1.1}_{-0.5}$ kpc (see also Targett et al. 2013; Wiklind et al. 2014). As recommended by Chen et al. (2014), we have restricted their sample to the 17 SMGs with an apparent *H*-band magnitude < 24 mag and a photometric redshift between $z_{\text{phot}} = 1$ – 3 , which ensures that the size distribution is complete (median $S_{850} = 4.0 \pm 0.6$ mJy). The Sérsic profiles fitted by Chen et al. (2014) are more complicated than the Gaussian profiles used in our analysis, but we note that a Gaussian profile corresponds to a Sérsic profile with Sérsic index $n = 0.5$. If we convert our $870 \mu\text{m}$ sizes to a half-light radius we find that the SMGs have a median $R_e = 1.2 \pm 0.1$ kpc in the sub-millimeter. As we show in Section 4.3.1 the half-light radius of the best-fit Sérsic profile to the stacked $870 \mu\text{m}$ emission from the SMGs is consistent with the median size from the elliptical Gaussian fit. The optical sizes of the SMGs are about four times larger than the $870 \mu\text{m}$ dust emitting region, and as can be seen in Figure 5 the distribution of NIR sizes has considerably more dispersion than the $870 \mu\text{m}$ sizes. The compact nature of the star formation means that it is plausible we are observing bulge growth in the form of obscured star formation. However, to test this hypothesis requires

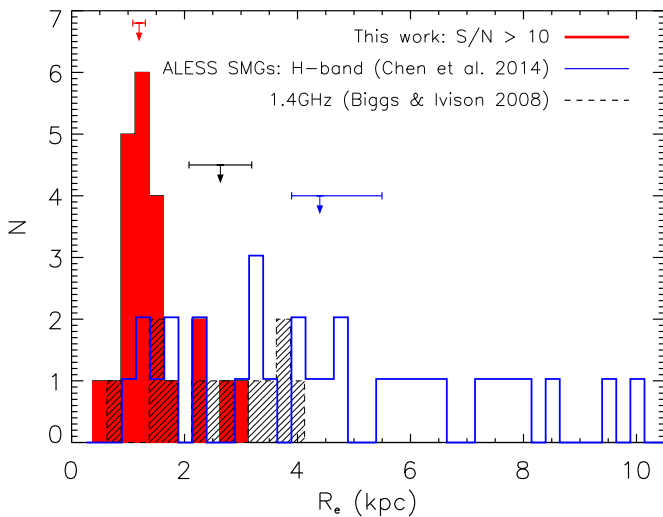


Figure 5. Comparison of the $870\ \mu\text{m}$ sizes of the SMGs in our sample, to the sizes of SMGs measured in 1.4 GHz/VLA imaging (Biggs & Ivison 2008) and H -band/ HST imaging (Chen et al. 2014). To allow a fair comparison between the samples we present all of the sizes in terms of an effective radius. The median size of the 12 SMGs identified in the 1.4 GHz imaging is $R_e = 2.6 \pm 0.6$ kpc, approximately double the median $870\ \mu\text{m}$ size of SMGs, $R_e = 1.2 \pm 0.1$ kpc. Convoluting the $870\ \mu\text{m}$ emission with a kernel of scale length 1–2 kpc, which is appropriate for modeling cosmic ray diffusion in star-forming galaxies at low redshift (Murphy et al. 2008), increases the median size of the SMGs to 3.8–5.2 kpc. Chen et al. (2014) measure a median size of $R_e = 4.4^{+1.1}_{-0.5}$ kpc from rest-frame optical HST imaging of 17 interferometrically identified SMGs at $z = 1$ –3. The H -band sizes of these SMGs are on average four times larger than the $870\ \mu\text{m}$ sizes presented here, indicating that the obscured star-forming region in SMGs is compact relative to the stellar emission.

high-resolution dust and optical imaging of the same sample of SMGs to pinpoint the location of the star formation within the host galaxy.

4.1.2. Comparison to Local U/LIRGs

We now compare the sizes of the SMGs in our sample to the sizes of local infrared-bright galaxies. Recently Ueda et al. (2014) presented a compilation of <1 kpc resolution interferometric imaging (new and archival) of ^{12}CO ($J = 1$ –0; 2–1; 3–2) emission from 30 local star-forming galaxies classified as “merger remnants.” We select galaxies from their sample with far-infrared luminosities $> 1 \times 10^{10} L_{\odot}$ ($\text{SFR} \gtrsim 1 M_{\odot} \text{yr}^{-1}$), resulting in a sample of 24 galaxies with a median $L_{\text{FIR}} = (1.4 \pm 0.1) \times 10^{11} L_{\odot}$. The sample contains one ULIRG ($L_{\text{FIR}} > 10^{12} L_{\odot}$) and 12 LIRGs ($L_{\text{FIR}} > 10^{11} L_{\odot}$). Ueda et al. (2014) measure the size of each galaxy as the radius containing 80% (R_{80}) of the total ^{12}CO flux. To ensure a fair comparison with the results presented here, we derive the correction between FWHM and R_{80} , and apply this correction to the sizes presented by Ueda et al. (2014). The sample of 24 local galaxies has a median diameter of 1.9 ± 0.2 kpc, with a 1σ dispersion of 1.3–3.4 kpc (consistent with Downes & Solomon 1998).

We caution that Ueda et al. (2014) present a sample of optically selected “merger-remnants” and although these “merger-remnants” are FIR-bright, the selection is not well-matched to the FIR-selected sample of SMGs presented here. Ueda et al. (2014) also measure the size of the sources in their sample from low - J transitions of ^{12}CO : 12 sources are observed in ^{12}CO ($J = 1$ –0) emission, 10 in ^{12}CO ($J = 2$ –1), and two in ^{12}CO ($J = 3$ –2). The lowest J transitions trace cold molecular gas, and are expected to reflect the size of the total gas reservoir, rather than the star-forming region. Indeed, studies of Arp 220,

the closest ULIRG, find that the size of the rest-frame $860\ \mu\text{m}$ emission is 50–80 pc, which is approximately two to four times smaller than the extent of the ^{12}CO ($J = 1$ –0) emission (Downes & Solomon 1998; Sakamoto et al. 2008).

The sizes of local U/LIRGs measured from low - J transitions of ^{12}CO appear marginally smaller than the $870\ \mu\text{m}$ sizes of the SMGs presented here, although the two samples are consistent within the associated uncertainties. However, as we have discussed, sizes measured from the $J = 1$ –0 transition of ^{12}CO are likely to be an upper limit on size of the star-forming region. In the absence of a sample of local ULIRGs with sizes measured at approximately the same wavelength as the SMGs in this paper, we simply note that the star-forming regions in SMGs may be significantly larger than local U/LIRGs.

4.2. Are SMGs Eddington Limited Starbursts?

The high SFRs of SMGs means that they could host regions with an extreme star formation density, which could result in very different star formation conditions to other galaxy populations. In an isolated star-forming region the radiation pressure from massive stars may provide sufficient feedback to regulate the further collapse of the giant molecular cloud. Andrews & Thompson (2011) show via the balance of radiation pressure from star formation with self-gravitation, that the maximum SFR surface density, assuming optically thick dust emission ($\tau > 1$),¹⁸ and in the absence of nuclear heating via an active galactic nucleus, is

$$\text{SFR}_{\text{max}} \gtrsim 11 f_{\text{gas}}^{-0.5} f_{\text{dg}}^{-1} M_{\odot} \text{yr}^{-1} \text{kpc}^{-2}, \quad (2)$$

where f_{gas} is the gas fraction in the star-forming region, and f_{dg} is the dust-to-gas ratio (see also Murray et al. 2005; Thompson et al. 2005; Murray et al. 2010). We adopt a dust-to-gas ratio of $f_{\text{dg}} = 1/90$ (Magnelli et al. 2012; Swinbank et al. 2014), but note that $f_{\text{dg}} = 1/50$ has also been suggested for star-forming galaxies (Kovács et al. 2006). Estimates of the dynamical masses (Swinbank et al. 2006; Alaghband-Zadeh et al. 2012), stellar masses (Hainline et al. 2011; Simpson et al. 2014) and gas masses (Bothwell et al. 2013) indicate that SMGs have typical gas fractions of $\sim 40\%$; however, this is a global property of the galaxy. As the size of the rest-frame optical emitting region in SMGs is around four times larger than the size of the star-forming region (Figure 5), it is likely that the gas fraction is considerably higher in the star-forming region. In our analysis we adopt a gas fraction of unity, i.e., gas is the dominant component, as this sets a lower limit on the maximum SFR surface density. If we adopt a gas fraction of 40% then the maximum SFR surface density would rise by 60%. Adopting these values the maximum SFR surface density predicted by Andrews & Thompson (2011) is $\sim 1000 M_{\odot} \text{yr}^{-1} \text{kpc}^{-2}$.

The 23 SMGs in our sample have a median far-infrared luminosity of $(5.7 \pm 0.7) \times 10^{12} L_{\odot}$, which corresponds to a median $\text{SFR} = 990 \pm 120 M_{\odot} \text{yr}^{-1}$ (for a Salpeter initial mass function (IMF)). To derive the SFR surface density for our

¹⁸ Andrews & Thompson (2011) state that a starburst should be treated as optically thick if the gas is above a critical surface density,

$$\Sigma_{\text{g}} \gtrsim 1200 M_{\odot} \text{kpc}^{-2}. \quad (1)$$

Here we have adopted a Rosseland mean dust opacity of $5 \text{cm}^{-2} \text{g}^{-1}$ and a dust-to-gas ratio of $f_{\text{dg}} = 90$ (see Andrews & Thompson 2011; Swinbank et al. 2014). Assuming the typical gas mass of SMGs, $4 \times 10^{10} M_{\odot}$ (Swinbank et al. 2014), then the typical gas density of SMGs is $\Sigma_{\text{g}} = 4000 M_{\odot} \text{kpc}^{-2}$.

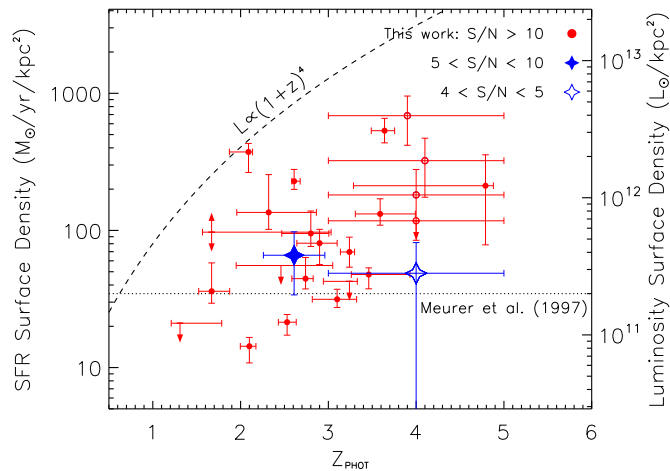


Figure 6. Star formation rate surface density of the SMGs in our sample as a function of redshift. The dashed line represents luminosity evolution $L_{\text{IR}} \propto (1+z)^4$. A dotted line shows the 90th percentile luminosity surface density for a sample of ultraviolet-selected sources (Meurer et al. 1997). The SMGs have a median star formation rate density of $90 \pm 30 M_{\odot} \text{ yr}^{-1} \text{ kpc}^{-2}$, and we note that no SMGs exceed the Eddington limit for a radiation pressure supported starburst ($\sim 1000 M_{\odot} \text{ yr}^{-1} \text{ kpc}^{-2}$; Andrews & Thompson 2011).

sample we initially divide the SFR of each SMG by a factor of two (the measured size of each SMG corresponds to the half-light radius of the profile). We show our sample in Figure 6, and assuming a uniform disk profile for the gas and cool dust distribution the median SFR surface density of the SMGs is $90 \pm 30 M_{\odot} \text{ yr}^{-1} \text{ kpc}^{-2}$. Only two SMGs have a SFR surface density above $500 M_{\odot} \text{ yr}^{-1} \text{ kpc}^{-2}$, and no SMGs exceed the maximum value predicted by Andrews & Thompson (2011).

The SMGs in our sample are forming stars at surface rate densities an order of magnitude lower than the estimated Eddington limit. However, we stress that these surface rate densities are integrated across the star-forming region (see Meurer et al. 1997). In the well-studied lensed SMG SMM J2135-0102 (Swinbank et al. 2010b) it has been shown that the star formation is in four distinct “clumps” (FWHM = 100–300 pc), located within a gas disk with a half light radius ~ 1 kpc (Swinbank et al. 2011; Danielson et al. 2011, 2013). If the star formation in the SMGs in our sample is “clumpy,” then individual regions in the gas disk may be Eddington limited, but the integrated SFR surface density will appear sub-Eddington.

Meurer et al. (1997) show that a sample of ultraviolet-selected sources (at $z = 0-3$) have a 90th percentile global luminosity surface density of $2 \times 10^{11} L_{\odot} \text{ kpc}^{-2}$ (with an associated uncertainty of a factor of three), which they interpret as an upper limit on the global luminosity surface density of a starburst. The SMGs presented here have a median global luminosity surface density of $(5.2 \pm 1.7) \times 10^{11} L_{\odot} \text{ kpc}^{-2}$, a factor of three times higher than the value found by Meurer et al. (1997; see Figure 6). A possible explanation for this discrepancy is that Meurer et al. (1997) measure half-light radii for the galaxies in their sample from ultraviolet imaging, and assume that dust attenuation is uniform across the galaxy. As discussed in Section 4.1.1 we find that the rest-frame optical half-light radii of SMG are a factor of four larger than the $870 \mu\text{m}$ dust half-light radius. The discrepancy in the optical sizes and dust sizes of SMGs indicates that there is significant differential reddening in these sources. If the ultraviolet-selected sources in (Meurer et al. 1997) suffer from similar differential reddening, then the half-light radii measured in the ultraviolet are likely to overestimate the true extent of the star formation.

4.3. Are SMGs the Progenitors of Compact Quiescent Galaxies at $z \sim 2$?

It has been suggested that an evolutionary sequence exists whereby SMGs transition into local elliptical galaxies via a quiescent galaxy phase at redshift $z \sim 2$ (e.g., Lilly et al. 1999; Genzel et al. 2003; Blain et al. 2004; Swinbank et al. 2006; Tacconi et al. 2008; Swinbank et al. 2010a; Hickox et al. 2012; Toft et al. 2014; Simpson et al. 2014; Chen et al. 2014). This evolutionary scenario has been investigated by comparing properties, such as the stellar masses, spatial clustering, and space densities of SMGs, to the properties of the proposed descendants. However, each of these methods has significant uncertainties: the stellar masses of SMGs have been shown to be highly dependent on the assumed star formation history; the number of SMGs with measured dynamical masses is small and the samples are inhomogeneous; and the spatial clustering strength of single-dish identified sub-mm sources is biased by source blending.

Here we use sizes to test this evolutionary link, since a distinctive feature of the population of quiescent galaxies at redshift $z = 1-3$ is that they are extremely compact, with half-light sizes of $\sim 1 \text{ kpc}^{19}$ (e.g., Daddi et al. 2005; Zirm et al. 2007; Toft et al. 2007; Buitrago et al. 2008; van Dokkum et al. 2008; Newman et al. 2012; Patel et al. 2013; Krogager et al. 2013). A morphological analysis of SMGs thus provides an alternative route to investigating the proposed evolutionary sequence.

We construct a sample of spectroscopically confirmed quiescent galaxies at $z \sim 2$, to compare to SMGs, by combining the samples presented by van Dokkum (2008) and Krogager et al. (2013). The galaxies in these samples have spectroscopically confirmed 4000 Å/Balmer breaks, indicative of an old ($\gtrsim 0.5-1$ Gyr) stellar population, assuming no age-dependent dust reddening. Both studies use the code GALFIT to fit a Sérsic profile to the H -band emission from each galaxy. The combined sample of 24 quiescent galaxies has a median half-light radius of $R_e = 1.5 \pm 0.2 \text{ kpc}$ and a median Sérsic index of $n = 3.3 \pm 0.7$. The stellar masses of these galaxies are estimated to be $\gtrsim 10^{11} M_{\odot}$ and the median redshift of the sample is $z = 2.2 \pm 0.1$. The age of the stellar population in these quiescent galaxies (0.5–1 Gyr) means that their progenitors likely lie at $z = 2.5-3$ consistent with the redshift distribution of SMGs (Toft et al. 2014; Simpson et al. 2014). We note that the half-light radii of the spectroscopically confirmed quiescent galaxies in our comparison sample are consistent with the sizes measured for a large sample of color-selected quiescent galaxies at a similar redshift ($z = 1.5-2.5$; Patel et al. 2013).

As discussed in Section 4.1.1, Chen et al. (2014) show that the unobscured rest-frame optical light in SMGs has a median half-light size of $R_e = 4.4_{-0.5}^{+1.1} \text{ kpc}$ and Sérsic index of $n = 1.2 \pm 0.3$. In contrast, the quiescent galaxies in our comparison sample have a median half-light radius of $R_e = 1.5 \pm 0.2 \text{ kpc}$, significantly smaller than the rest-frame optical half-light radius of SMGs. The median Sérsic index of the SMGs is also significantly lower than the quiescent galaxies, indicating that a significant transformation of the light profile (and potentially stellar mass distribution) of SMGs is required if they are indeed the progenitors of the quiescent galaxies in our comparison sample. A number of studies have suggested that the star formation in SMGs is triggered by merger activity: in H -band/

¹⁹ We note that mass selected samples ($M_{\star} > 5 \times 10^{10} M_{\odot}$) containing both star-forming and quiescent galaxies at $z = 1-3$, have an half-light radius (4 kpc) that is higher than, and a Sérsic index (1.5) which is lower than, our sample of quiescent galaxies (see Patel et al. 2013; Buitrago et al. 2013).

HST imaging ($82 \pm 9\%$) of SMGs have signatures of interactions and/or irregular morphologies (Chen et al. 2014), and the low Sérsic index n measured for the population is consistent with merging systems (Kartaltepe et al. 2012); dynamical studies of resolved H α emission from SMGs find strong evidence of kinematically distinct multiple components (Swinbank et al. 2006; Alaghband-Zadeh et al. 2012); and a study of molecular line emission from SMGs finds that 75% of sources are ongoing mergers, with the remaining 25% classed as either disk or late stage mergers (Engel et al. 2010).

It is well established that mergers can induce torques that are effective at removing angular momentum from the gas in the system, allowing the gas to fall into the inner regions and potentially resulting in a kiloparsec-scale nuclear starburst (e.g., Barnes & Hernquist 1991; Mihos & Hernquist 1994). Recently, Hopkins et al. (2013) presented numerical simulations of two gas rich disk galaxies undergoing a major merger at high redshift. Hopkins et al. (2013) show that the major merger triggers an intense central starburst, with 50% of the star formation activity concentrated within a diameter of ~ 2 kpc. The simulations also demonstrate that the starburst increases the stellar surface density within the central 2 kpc diameter by two orders of magnitude. The size of the star-forming region in the SMGs presented in this work are consistent with simulations of major mergers. If the star formation in SMGs is indeed a centrally concentrated starburst then we expect a significant rise in the concentration of the stellar component, increasing the fraction of light contained in a de Vaucouleurs-like ($n = 4$) profile.

4.3.1. Sérsic Index

We now investigate whether there is evidence that the star formation in SMGs is more highly concentrated than the stellar component. First, we test whether our data have sufficiently high S/N to recover a more complex Sérsic profile.²⁰ We create 4000 model sources with a half-light size fixed at the median size of the SMGs, a range of Sérsic index from $n = 0.5$ –4 and an S/N distribution that is uniform from 10σ – 30σ . To simulate realistic noise we add these models to a randomly chosen position in one of the residual (source-subtracted) ALMA maps.

We fit a Sérsic profile to each model source using the code GALFIT (Peng et al. 2010), and find that the half-light size of the model sources is recovered accurately at all values of S/N and Sérsic index ($R_e^{\text{rec}}/R_e^{\text{input}} = 0.99 \pm 0.01$; 1σ dispersion ± 0.2). In contrast, although the Sérsic index is recovered correctly on average ($n^{\text{rec}}/n^{\text{input}} = 0.97 \pm 0.02$) the distribution has a 1σ dispersion of 0.4–2.2, indicating that measurements for individual sources are highly uncertain.²¹ Crucially, we find that the dispersion in the recovered Sérsic index is dependent on the S/N of the injected source; for $S/N > 20\sigma$ the 1σ dispersion is 0.6–1.8. As such we do not attempt to fit a Sérsic profile on a source-by-source basis, but instead stack the $870 \mu\text{m}$ emission from the 23 SMGs detected at $>10\sigma$ and use GALFIT to fit a Sérsic model to the stacked profile. The best-fit model to the stacked profile has a Sérsic index of $n = 2.5 \pm 0.4$ and a half-light radius of $R_e = 0''.17 \pm 0''.03$, where the errors are derived by bootstrapping the maps used in the stacking.

²⁰ The test we perform is to investigate the required S/N, and does not test the effects of spatial filtering on our ALMA maps, due to the configuration of the array. However, we note that the maximum angular scale that our maps are sensitive to is $5''$, which is an order of magnitude larger than the FWHM of the SMGs in our sample.

²¹ If we re-fit our model sources, but force the Sérsic index to $n = 0.5$ the median recovered half-light size is $R_e^{\text{rec}}/R_e^{\text{input}} = 0.99 \pm 0.01$, with a 1σ dispersion ± 0.15 .

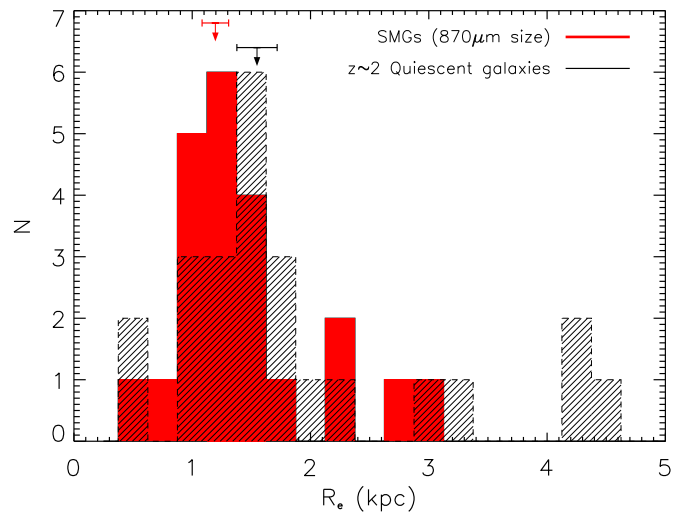


Figure 7. Comparison of the FWHM of the rest-frame FIR emission in SMGs to $z \sim 2$ quiescent galaxies, the proposed progenitors of local elliptical galaxies. The quiescent galaxies are selected to have strong 4000 \AA Balmer breaks, suggestive of an old stellar population, and are found to be compact in F160W/*HST* imaging, with a median half-light size of $R_e = 1.5 \pm 0.2$ (van Dokkum 2008; Krogager et al. 2013).

The median Sérsic index of the $870 \mu\text{m}$ emission from the SMGs is higher than the Sérsic index of the unobscured rest-frame optical light in SMGs (Chen et al. 2014, but see also Targett et al. 2013), indicating that the ongoing star formation is more centrally concentrated. As we show in Figure 7, the half-light radius of the star formation in SMGs, median $R_e = 1.2 \pm 0.1$ kpc, is comparable to the half-light radius of the quiescent galaxies in our comparison sample, $R_e = 1.5 \pm 0.2$ kpc. If we combine the average Sérsic profile of the star formation and the pre-existing stellar population, under the simple assumption that the ongoing star-formation in SMGs doubles the luminosity of the stellar component, then the half-light radius of the resulting galaxy is ~ 2 kpc. This estimated half-light radius of the post-starburst SMGs is still marginally larger than median half-light radius of $z \sim 2$ quiescent galaxies. However, as shown by Chen et al. (2014) ($82 \pm 9\%$) of SMGs have signs of either merger activity or disturbed morphologies, and it is likely that the size measured for the ongoing merger is larger than the size of the galaxy at post-coalescence. In addition, the contribution of the stars formed in the SMG phase to the luminosity of the post-starburst galaxy is highly dependent on the mass of stars formed and the relative ages of the stars formed in the starburst and the pre-existing stellar population. The half-light radius of the ongoing, extreme, star formation in SMGs is comparable to the half-light radius of high-redshift compact quiescent galaxies, indicating that the ongoing star formation may explain the transformation required in the proposed evolutionary scenario from an intense starburst phase (SMG) to a local elliptical galaxies, via a compact quiescent galaxy at $z \sim 2$.

5. CONCLUSIONS

In this paper we have presented high-resolution ($0''.3$) ALMA imaging of 52 SMGs in the UDS field. The main conclusions from our work are as follows.

1. We fit an elliptical Gaussian model to the $870 \mu\text{m}$ emission from 23 SMGs detected at $S/N > 10\sigma$. The median diameter, deconvolved from the beam, of these 23 SMGs is $\text{FWHM} = 0''.30 \pm 0''.04$, and the distribution has a

- narrow interquartile range of $0'.26$ – $0'.42$. Two SMGs in our sample (10%) are best fit by a point source model, and have an upper limit on their size of $<0'.18$. We stack the $870\ \mu\text{m}$ emission from SMGs detected at $S/N = 4\sigma$ – 5σ and $S/N = 5\sigma$ – 10σ , measuring an average size of $0.35^{+0.17}_{-0.10}''$ and $0'.30 \pm 0'.07$ for each subset, respectively, consistent with the brighter examples.
2. Using photometric redshifts we convert the angular diameter of each SMG to a physical scale. The median physical FWHM of the 23 SMGs detected at $S/N > 10\sigma$ is 2.4 ± 0.2 kpc, and again the distribution has a narrow interquartile range of 1.8–3.2 kpc. We investigate the size of the rest-frame FIR-emission region in SMGs, but do not find a trend with either redshift or $870\ \mu\text{m}$ flux density.
 3. We compare the $870\ \mu\text{m}$ sizes of the SMG presented in this work to the sizes of SMGs measured at 1.4 GHz. The median FWHM of these SMGs is 5.1 ± 1.1 kpc, which is about two times larger than the median $870\ \mu\text{m}$ size presented here. We convolve the median $870\ \mu\text{m}$ profile of the SMGs with an exponentially declining kernel, with a scale length of 1–2 kpc, appropriate for modeling the radio and far-infrared emission in local star-forming galaxies (Murphy et al. 2008). The convolved profile has a FWHM = 3.8–5.2 kpc, showing that the radio sizes may be consistent with our sub-millimeter sizes. However, we caution that as stated by Murphy et al. (2008) the scale length of the convolution kernel may be sensitive to the SFR and morphology of the galaxy.
 4. We also compare the sizes we derive for the $870\ \mu\text{m}$ emission region in SMGs to the sizes of SMGs measured from observations of resolved “moderate”- J ^{12}CO emission lines. Treating the upper limits in the CO studies as point sources, the median FWHM for the sample is 2.3 ± 1.1 kpc (rising to 3.7 ± 0.6 kpc if upper limits are taken as detections). Thus, the cool gas estimates of the sizes are consistent with the $870\ \mu\text{m}$ sizes measured here.
 5. The pre-existing stellar population in SMGs has a half-light radius of $4.4^{+1.1}_{-0.5}$ kpc, as measured from rest-frame optical *HST* imaging (Chen et al. 2014), which is about four times larger than the extent of the ongoing star formation. The high dust content of SMGs means that the starburst component is likely to be missed in rest-frame optical imaging, while their prodigious SFRs mean they have the potential to transform their stellar mass distribution. Hence, we expect the post-starburst galaxy to be compact, with a smaller half-light radius than the pre-existing stellar population.
 6. SMGs are slightly larger than local far-infrared bright galaxies (U/LIRGs), with low- J molecular gas sizes for the latter, median FWHM = 1.9 ± 0.2 kpc. However, these gas-derived sizes are likely to be larger than the far-infrared extents of the local galaxies, meaning the SMGs are probably physically larger systems.
 7. The 23 SMGs in our sample have a median star formation rate of $\text{SFR} = 1170 \pm 160 M_{\odot} \text{ yr}^{-1}$ (for a Salpeter IMF), and a median star formation density of $90 \pm 30 M_{\odot} \text{ yr}^{-1} \text{ kpc}^{-2}$. The Eddington limit for a radiation pressure regulated starburst is $\sim 1000 M_{\odot} \text{ yr}^{-1} \text{ kpc}^{-2}$ (Andrews & Thompson 2011). Hence, the SMGs in our sample have integrated SFR densities that are on average an order of magnitude lower than the Eddington limit. We suggest that this is due to the star formation occurring in “clumps,” which may be Eddington limited, but appear sub-

Eddington when integrated across the whole star formation region.

8. The half-light radius of the ongoing star formation in SMGs is similar to the size of $z = 2.2 \pm 0.1$ quiescent galaxies, median $R_e = 1.5 \pm 0.2$. The ongoing, compact, starburst in SMGs has the potential to at least double the pre-existing stellar mass, offering an explanation of the proposed transformation of SMGs into compact, quiescent galaxies at high redshift, and thus how they fit into the evolutionary scenario proposed for local elliptical galaxies.

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All data used in this analysis can be obtained from the ALMA, ESO, *Spitzer*, and *Herschel* archives.

REFERENCES

- Alaghband-Zadeh, S., Chapman, S. C., Swinbank, A. M., et al. 2012, *MNRAS*, **424**, 2232
- Alexander, D. M., Brandt, W. N., Smail, I., et al. 2008, *AJ*, **135**, 1968
- Andrews, B. H., & Thompson, T. A. 2011, *ApJ*, **727**, 97
- Barnes, J. E., & Hernquist, L. E. 1991, *ApJL*, **370**, L65
- Bicay, M. D., & Helou, G. 1990, *ApJ*, **362**, 59
- Biggs, A. D., & Ivison, R. J. 2008, *MNRAS*, **385**, 893
- Blain, A. W. 1996, *MNRAS*, **283**, 1340
- Blain, A. W., Chapman, S. C., Smail, I., & Ivison, R. 2004, *ApJ*, **611**, 725
- Bothwell, M. S., Chapman, S. C., Tacconi, L., et al. 2010, *MNRAS*, **405**, 219
- Bothwell, M. S., Smail, I., Chapman, S. C., et al. 2013, *MNRAS*, **429**, 3047
- Brammer, G. B., van Dokkum, P. G., & Coppi, P. 2008, *ApJ*, **686**, 1503
- Buitrago, F., Trujillo, I., Conselice, C. J., & Häußler, B. 2013, *MNRAS*, **428**, 1460
- Buitrago, F., Trujillo, I., Conselice, C. J., et al. 2008, *ApJL*, **687**, L61
- Chapman, S. C., Blain, A. W., Smail, I., & Ivison, R. J. 2005, *ApJ*, **622**, 772
- Chapman, S. C., Smail, I., Ivison, R. J., & Blain, A. W. 2002, *MNRAS*, **335**, L17

- Chapman, S. C., Windhorst, R., Odewahn, S., Yan, H., & Conselice, C. 2003, *ApJ*, 599, 92
- Chen, C.-C., Smail, I., Swinbank, A. M., et al. 2014, *ApJ*, in press
- Condon, J. J., Huang, Z.-P., Yin, Q. F., & Thuan, T. X. 1991, *ApJ*, 378, 65
- Conselice, C. J., Chapman, S. C., & Windhorst, R. A. 2003, *ApJL*, 596, L5
- Daddi, E., Renzini, A., Pirzkal, N., et al. 2005, *ApJ*, 626, 680
- Danielson, A. L. R., Swinbank, A. M., Smail, I., et al. 2011, *MNRAS*, 410, 1687
- Danielson, A. L. R., Swinbank, A. M., Smail, I., et al. 2013, *MNRAS*, 436, 2793
- Downes, D., & Solomon, P. M. 1998, *ApJ*, 507, 615
- Engel, H., Tacconi, L. J., Davies, R. I., et al. 2010, *ApJ*, 724, 233
- Frayer, D. T., Ivison, R. J., Scoville, N. Z., et al. 1999, *ApJL*, 514, L13
- Genzel, R., Baker, A. J., Tacconi, L. J., et al. 2003, *ApJ*, 584, 633
- Greve, T. R., Bertoldi, F., Smail, I., et al. 2005, *MNRAS*, 359, 1165
- Griffin, M. J., Abergel, A., Abreu, A., et al. 2010, *A&A*, 518, L3
- Hainline, L. J., Blain, A. W., Smail, I., et al. 2011, *ApJ*, 740, 96
- Hartley, W. G., Almaini, O., Mortlock, A., et al. 2013, *MNRAS*, 431, 3045
- Hickox, R. C., Wardlow, J. L., Smail, I., et al. 2012, *MNRAS*, 421, 284
- Hodge, J. A., Carilli, C. L., Walter, F., Daddi, E., & Riechers, D. 2013a, *ApJ*, 776, 22
- Hodge, J. A., Karim, A., Smail, I., et al. 2013b, *ApJ*, 768, 91
- Holland, W. S., Bintley, D., Chapin, E. L., et al. 2013, *MNRAS*, 430, 2513
- Hopkins, P. F., Cox, T. J., Hernquist, L., et al. 2013, *MNRAS*, 430, 1901
- Ivison, R. J., Papadopoulos, P. P., Smail, I., et al. 2011, *MNRAS*, 412, 1913
- Ivison, R. J., Swinbank, A. M., Smail, I., et al. 2013, *ApJ*, 772, 137
- Kartalpe, J. S., Dickinson, M., Alexander, D. M., et al. 2012, *ApJ*, 757, 23
- Kovács, A., Chapman, S. C., Dowell, C. D., et al. 2006, *ApJ*, 650, 592
- Kriek, M., van der Wel, A., van Dokkum, P. G., Franx, M., & Illingworth, G. D. 2008, *ApJ*, 682, 896
- Krogager, J.-K., Zirm, A. W., Toft, S., Man, A., & Brammer, G. 2013, arXiv:1309.6316
- Lilly, S. J., Eales, S. A., Gear, W. K. P., et al. 1999, *ApJ*, 518, 641
- Lindner, R. R., Baker, A. J., Omont, A., et al. 2011, *ApJ*, 737, 83
- Magnelli, B., Lutz, D., Santini, P., et al. 2012, *A&A*, 539, A155
- Menéndez-Delmestre, K., Blain, A. W., Smail, I., et al. 2009, *ApJ*, 699, 667
- Meurer, G. R., Heckman, T. M., Lehnert, M. D., Leitherer, C., & Lowenthal, J. 1997, *AJ*, 114, 54
- Michałowski, M. J., Dunlop, J. S., Cirasuolo, M., et al. 2012, *A&A*, 541, A85
- Mihos, J. C., & Hernquist, L. 1994, *ApJL*, 431, L9
- Mortlock, A., Conselice, C. J., Hartley, W. G., et al. 2013, *MNRAS*, 433, 1185
- Murphy, E. J., Helou, G., Braun, R., et al. 2006, *ApJL*, 651, L111
- Murphy, E. J., Helou, G., Kenney, J. D. P., Armus, L., & Braun, R. 2008, *ApJ*, 678, 828
- Murray, N., Quataert, E., & Thompson, T. A. 2005, *ApJ*, 618, 569
- Murray, N., Quataert, E., & Thompson, T. A. 2010, *ApJ*, 709, 191
- Narayanan, D., & Krumholz, M. R. 2014, *MNRAS*, 442, 1411
- Newman, A. B., Ellis, R. S., Bundy, K., & Treu, T. 2012, *ApJ*, 746, 162
- Paciga, G., Scott, D., & Chapin, E. L. 2009, *MNRAS*, 395, 1153
- Panuzzo, P., Rangwala, N., Rykala, A., et al. 2010, *A&A*, 518, L37
- Patel, S. G., van Dokkum, P. G., Franx, M., et al. 2013, *ApJ*, 766, 15
- Peng, C. Y., Ho, L. C., Impey, C. D., & Rix, H.-W. 2010, *AJ*, 139, 2097
- Pilbratt, G. L., Riedinger, J. R., Passvogel, T., et al. 2010, *A&A*, 518, L1
- Pope, A., Chary, R.-R., Alexander, D. M., et al. 2008, *ApJ*, 675, 1171
- Riechers, D. A., Hodge, J., Walter, F., Carilli, C. L., & Bertoldi, F. 2011, *ApJL*, 739, L31
- Rujopakarn, W., Rieke, G. H., Eisenstein, D. J., & Juneau, S. 2011, *ApJ*, 726, 93
- Sakamoto, K., Wang, J., Wiedner, M. C., et al. 2008, *ApJ*, 684, 957
- Simpson, J. M., Swinbank, A. M., Smail, I., et al. 2014, *ApJ*, 788, 125
- Smolčić, V., Aravena, M., Navarrete, F., et al. 2012, *A&A*, 548, A4
- Soifer, B. T., Neugebauer, G., Matthews, K., et al. 1999, *ApJ*, 513, 207
- Swinbank, A. M., Chapman, S. C., Smail, I., et al. 2006, *MNRAS*, 371, 465
- Swinbank, A. M., Papadopoulos, P. P., Cox, P., et al. 2011, *ApJ*, 742, 11
- Swinbank, A. M., Simpson, J. M., Smail, I., et al. 2014, *MNRAS*, 438, 1267
- Swinbank, A. M., Smail, I., Chapman, S. C., et al. 2010a, *MNRAS*, 405, 234
- Swinbank, A. M., Smail, I., Longmore, S., et al. 2010b, *Natur*, 464, 733
- Tacconi, L. J., Genzel, R., Lutz, D., et al. 2002, *ApJ*, 580, 73
- Tacconi, L. J., Genzel, R., Smail, I., et al. 2008, *ApJ*, 680, 246
- Tacconi, L. J., Neri, R., Chapman, S. C., et al. 2006, *ApJ*, 640, 228
- Targett, T. A., Dunlop, J. S., Cirasuolo, M., et al. 2013, *MNRAS*, 432, 2012
- Thompson, T. A., Quataert, E., & Murray, N. 2005, *ApJ*, 630, 167
- Toft, S., Smolčić, V., Magnelli, B., et al. 2014, *ApJ*, 782, 68
- Toft, S., van Dokkum, P., Franx, M., et al. 2007, *ApJ*, 671, 285
- Ueda, J., Iono, D., Yun, M. S., et al. 2014, *ApJS*, 214, 1
- van Dokkum, P. G. 2008, *ApJ*, 674, 29
- van Dokkum, P. G., Franx, M., Kriek, M., et al. 2008, *ApJL*, 677, L5
- Wang, S. X., Brandt, W. N., Luo, B., et al. 2013, *ApJ*, 778, 179
- Wardlow, J. L., Smail, I., Coppin, K. E. K., et al. 2011, *MNRAS*, 415, 1479
- Weiß, A., De Breuck, C., Marrone, D. P., et al. 2013, *ApJ*, 767, 88
- Weiß, A., Downes, D., Neri, R., et al. 2007, *A&A*, 467, 955
- Wiklund, T., Conselice, C. J., Dahlen, T., et al. 2014, *ApJ*, 785, 111
- Younger, J. D., Fazio, G. G., Ashby, M. L. N., et al. 2010, *MNRAS*, 407, 1268
- Yun, M. S., Scott, K. S., Guo, Y., et al. 2012, *MNRAS*, 420, 957
- Zirm, A. W., van der Wel, A., Franx, M., et al. 2007, *ApJ*, 656, 66