

The settlement performance of stone column foundations

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Vibrated stone columns are frequently used as a method of reinforcing soft ground as they provide increased bearing capacity and reduce foundation settlements. Their performance in relation to bearing capacity is well documented, but there is also a need for enhanced understanding of their settlement characteristics, particularly in relation to small-group configurations. This paper presents results obtained from physical model tests on triaxial specimens 300 mm in diameter and 400 mm high. Parameters investigated include column length to diameter ratio, area replacement ratio and single/group configuration. The findings of the work are as follows. The design is flexible: settlement can equally be controlled using short columns at relatively high area replacement ratios, or longer columns at smaller area replacement ratios. An optimum area replacement ratio of 30–40% exists for the control of settlement. The settlement performance of a small column group is highly influenced by inter-column and footing interaction effects.

KEYWORDS: footings/foundations; ground improvement; model tests; reinforced soils; settlement; soil/structure interaction

On utilise fréquemment des colonnes en pierre vibrée pour le renforcement de sols tendres, car elles accroissent la capacité portante tout en réduisant le tassement des fondations. Bien que leur performances relativement à la capacité portante soit bien documentée, il est nécessaire de renforcer les connaissances sur leurs propriétés de tassement, notamment en présence de configurations de groupes restreints. La présente communication illustre les résultats obtenus à l'issue d'essais sur maquettes de 300 mm de diamètre x 400 m de haut. Parmi les paramètres examinés, on indiquera le ratio longueur /diamètre de la colonne, le ratio superficie – remplacement, et la configuration individuelle /en groupe. Les conclusions de ces travaux indiquent (i) une flexibilité conceptuelle, dans le cadre de laquelle il est possible de limiter le tassement aussi bien en utilisant des colonnes courtes avec des ratios superficie – remplacement relativement élevés qu'en utilisant des colonnes plus longues avec ratios superficie – remplacement inférieurs ; (ii) la présence d'un ratio superficie – remplacement optimum compris entre 30 et 40% pour la limitation du tassement ; et (iii) que les effets de l'interaction inter-colonnes et de la semelle influent fortement sur les caractéristiques de tassement de petits groupes de colonnes.

INTRODUCTION

The stone column technique has witnessed significant applications, due to its versatility in treating soft cohesive soils and mixed fills of variable geotechnical properties. Laboratory-based research, together with analytical modelling, numerical modelling and field observations, is well documented, and has contributed to improvements in efficiency and quality control (Hughes & Withers, 1974; Hughes *et al.*, 1975; Aboshi *et al.*, 1979; Balaam & Booker, 1981; Barksdale & Bachus, 1983; Charles & Watts, 1983; Alamgir *et al.*, 1994; Hu, 1995; Balaam *et al.*, 1977; Raju, 1997; Slocombe *et al.*, 2000; Watts *et al.*, 2000; Watts & Serridge, 2000; McKelvey, 2002; McKelvey *et al.*, 2004; Pulko & Majes, 2005; Black, 2007; Black *et al.*, 2007a, 2007b; McCabe *et al.*, 2009). Stone columns are typically employed to support large raft foundations at relatively low or moderate loading conditions. However, more recently they have also been deployed beneath small isolated pad or strip foundations. Many previous studies have focused predominantly on the aspect of bearing capacity, although a small number of these projects have presented settlement data as a secondary aspect.

The effectiveness and performance of the stone column technique is influenced by several factors, including the

column length to diameter ratio (L/d), the area replacement ratio (A_s), the column spacing (s), the stiffness of the column (E_c) and of the surrounding soil (E_s), the stress ratio of the column and soil (σ_{vc}/σ_{vs}), the number of columns beneath the footing and the method of installation (Fig. 1). Hu (1995) studied extensively the behaviour and failure mechanisms of a large group of stone columns in relation to bearing capacity, and McKelvey (2002) investigated the performance of small-group behaviour beneath pad and strip footings. The latter work revealed that short columns ($L/d < 6$) failed in end bearing, whereas longer columns ($L/d > 6$) failed by bulging. These observations agreed with previous postulations by Wood *et al.* (2000) and Hughes & Withers (1974).

Current design techniques for settlement control relate to large-group configurations, and are analysed based on the performance of an isolated column under unit cell conditions (Priebe, 1995). This approach delivers good correlation with actual observed field behaviour for infinite groups, but discrepancies exist when it is applied to small-group column configurations. This is attributed to complex group interaction effects, which make confident predictions of settlement performance problematic (McCabe *et al.*, 2009). The work reported in this paper addresses the limitations associated with previous investigations, and uses reduced scale physical models to provide valuable insight into the settlement performance of isolated and small groups of stone columns.

EQUIPMENT DEVELOPMENT, SAMPLING, COLUMN INSTALLATION AND TESTING PROGRAMME

A review of previous investigations showed that soil beds were prepared and restrained in one-dimensional consolidation chambers during foundation loading. Two issues

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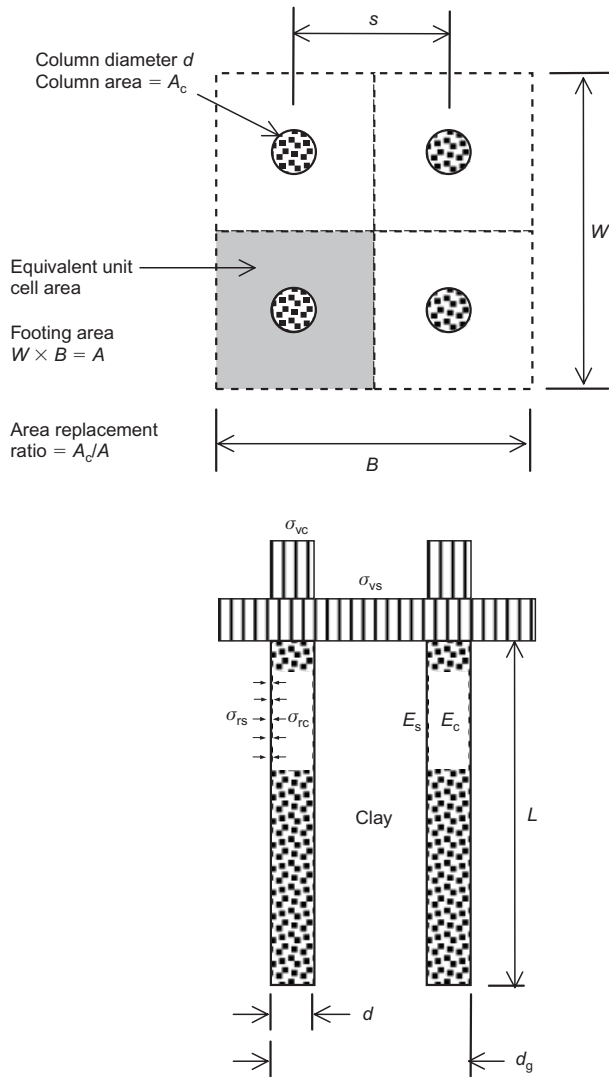


Fig. 1. Key factors affecting granular columns' performance

associated with this technique hinder the evaluation of settlement performance: (a) a lack of control of pore water pressure under foundation loading, and (b) frictional resistance, leading to non-uniform soil stiffness/strength properties. To mitigate these problems a novel protocol was adopted. Samples were initially prepared by one-dimensional consolidation, and then transferred to a large triaxial cell for re-consolidation under isotropic stress. This system allowed for the control of confining and pore water pressure, and offered the additional benefit of a non-rigid 'free' lateral boundary. The following sections describe the features of this large triaxial cell, and the associated sampling method and column installation process.

Equipment development

A large triaxial cell, capable of testing samples 300 mm in diameter by 400 mm high, was designed and constructed (Fig. 2). Several distinctive features were necessary to meet the specific criteria of the current investigation, as follows.

- (a) Independent control of vertical and lateral pressures was provided for the purpose of achieving K_0 consolidation. Confining pressure (σ_3) was applied via the cell fluid, and the vertical pressure (σ_1) was independently controlled using a rolling diaphragm type loading system located externally at the top of the cell (K_0 loading chamber) (Fig. 2). The force

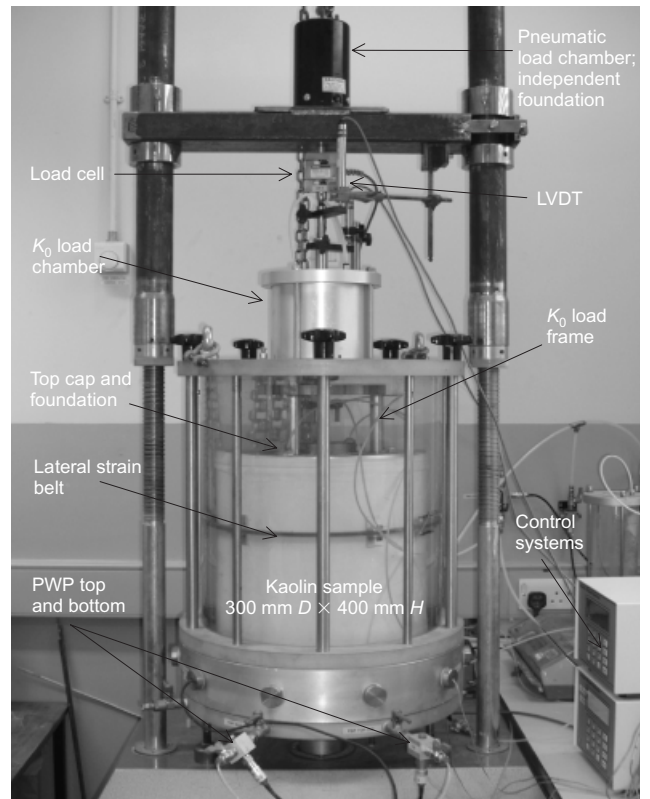


Fig. 2. Newly developed calibration triaxial cell apparatus and controlling system

- activated by this unit applied additional stress to the sample top plate by way of an internal loading frame.
- (b) Independent foundation loading was applied. Foundation loading was achieved using a small, independent 60 mm diameter footing located within the top plate (Fig. 3). A pneumatic piston located on the cross-beam of the support frame activated a ram that ran through the centre of the K_0 load chamber and load frame.

The foundation was instrumented with two pressure cells (2000 kPa range) to monitor the contact pressure (Fig. 3), one located at the centre of the footing (PT1), and the other at a radius of 18 mm (PT2). A third pressure cell (PT3)

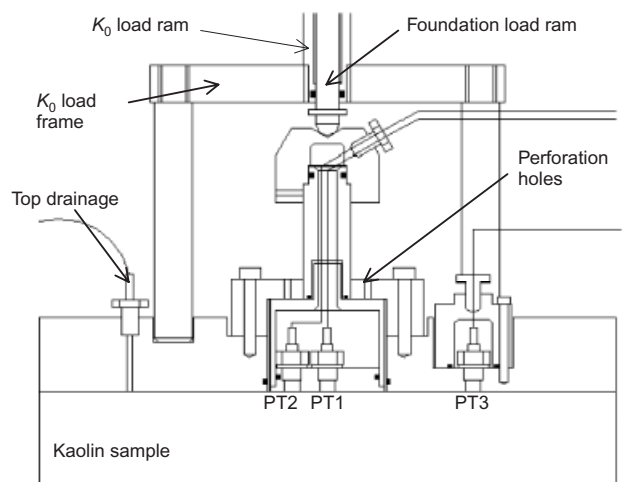


Fig. 3. Dual loading device: surcharge and independent foundation loading

(1000 kPa range), located away from the foundation, measured the vertical stress in the surrounding soil.

Displacement of the independent foundation and top plate (surrounding clay) were measured using separate 50 mm and 20 mm stroke linear variable differential transformer (LVDT) devices respectively. Cell pressure, pore water pressure and the pneumatic load chamber to apply independent foundation loading were controlled using automatic pressure controllers. Radial displacement of the sample during K_0 and foundation loading was monitored using a submersible 10 mm LVDT mounted on a lateral strain calliper, based on the original configuration proposed by Menzies (1976). This was located 120 mm from the top of the sample. All instrumentation was interfaced with a 16-channel data logger (MPX 3000) for data acquisition.

Sampling

The standard approach used by many researchers to make large samples is similar to a Rowe cell configuration (Rowe & Barden, 1966). This particular technique works satisfactorily in shorter consolidation chambers; however, difficulties have been reported, such as over-stretching of the bellows, and loss of consolidation pressure (Anderson *et al.*, 1991; McKelvey, 2002; Navaneethan, 2003; Ahmadi & Robertson, 2004). To mitigate this problem, a simple arrangement was adopted whereby the seal between the piston and the consolidation chamber was achieved using an inflatable O-ring (Fig. 4(a)).

The consolidation chamber (Fig. 4(b)) was fabricated from a polyethylene mains water pipe, machined to leave a bore of 300 mm and height of 900 mm. The top and bottom plates of the chamber were manufactured from aluminium, and were fitted with porous filter discs and drainage facilities. A pressure cell was located in the base plate to monitor the earth pressure at the base of the chamber. The piston plate was manufactured from polyvinyl chloride (PVC), and was 298 mm in diameter by 60 mm thick. A bicycle tube (inflatable O-ring) was located in a groove, as shown in Fig. 4(a), and was connected to a regulated air line so that it could be inflated to achieve a seal between the piston and the chamber. Drainage was allowed from the base of the sample.

Samples were prepared by consolidating kaolin slurry,

prepared at a water content of 1.5 times the liquid limit (70%), to a vertical pressure of 150 kPa. This pressure was adequate to produce quality repeatable samples with undrained shear strength, $c_u = 35$ kPa. Silicone grease was smeared on the inner cylindrical surface to reduce friction; this also aided sample extrusion after consolidation. Internal earth pressure measurements recorded at the base of the chamber during consolidation indicated that the pressure reduced from 157 kPa (7 kPa more than the applied pressure due to self-weight of the slurry) to 98 kPa at the end of consolidation. This would imply that the clay at the bottom (from where the drainage was allowed) was slightly over-consolidated, as a result of unloading arising from frictional resistance. Further evidence to support this observation was determined from the void ratio of the spoil removed during column installation along the depth of the sample. As highlighted, variation of sample strength and stiffness with depth was present in previous experimental investigations; however, the effects of this in the current work are reduced, as the sample was reconsolidated under isotropic stress.

Consolidation of 95% was achieved in approximately 14 days, after which the consolidation and tube pressures were reduced with the drainage line closed. Using a specially fabricated sampling table, specimens were extruded from the consolidation chamber into position on the triaxial base, resting on a vertical mobile table (Fig. 4(c)), and trimmed to 400 mm high using a wire saw.

Column installation

Various methods of column installation, ranging from pre-forming frozen columns to forced intrusion and replacement/compaction, were considered as part of this investigation (Black, 2007). Pre-forming resulted in reduced column density upon thawing. Forced intrusion was more representative of actual field installation, as it displaced the surrounding soil, generating densification (Egan *et al.*, 2008), but the technique was difficult to implement in a small-scale model; furthermore, trial tests generated suction during removal of the poker which caused collapse of the cavity. Replacement was also trialled; although the technique is not entirely representative of field conditions, it proved to produce columns of excellent consistency, and has been adopted for the present research.

The holes were carefully bored using helical augers, which rotated at a constant speed of 19 rev/min, with a vertical penetration of 25 mm. Granular aggregate (crushed basalt) was then introduced to the cavity in stages, and compacted using a 1.0 kg metal rod free-falling through a fixed distance of 50 mm for a series of 10 blows. The aggregate was of uniform grading, with particle size in the range 1.18–2.36 mm, and was in keeping with a 1:30 scale prototype. The average dry column density was calculated as $1648 \text{ kg/m}^3 \pm 2\%$, based on the assumption of constant cavity volume during installation. It is evident that some degree of cavity expansion will occur during compaction, and therefore this measurement was strictly used as a means of ensuring quality control between tests. Compaction of the same aggregate into a rigid container of a known volume showed that the dry density was approximately 1550 kg/m^3 , implying that the installation of columns in the clay bed would have resulted in a 6% increase in cavity volume.

Each column was completed by infiltrating with de-aired water, and the placement of a thin layer of fine sand. This layer was vital to ensure that the pressure cells beneath the footing were subjected to a uniformly distributed load (UDL) rather than a point load from the crushed aggregate. Additional material characteristics for kaolin and basalt aggregate are provided in Table 1.

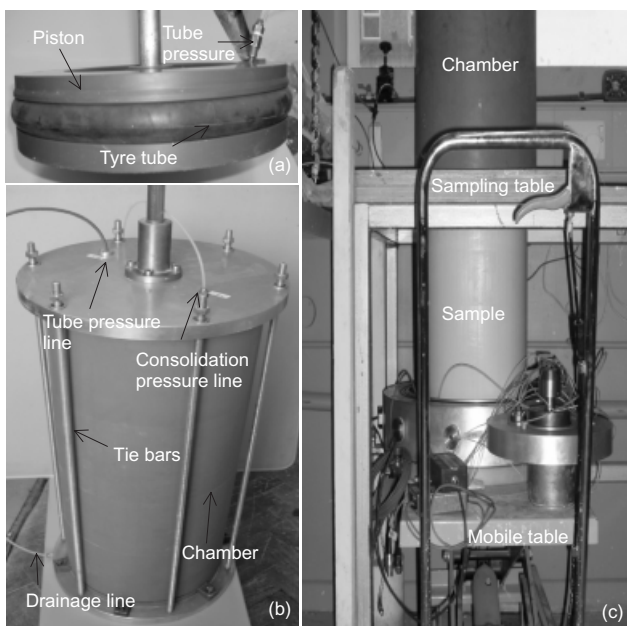


Fig. 4. (a) Innovative piston sealing arrangement; (b) consolidation chamber; (c) sample extrusion

Table 1. Material properties

Material	Property	Value
Clay: Speswhite kaolin clay	Particle size: μm	< 63
	Liquid limit: %	68
	Plastic limit: %	34
	Plasticity index: %	34
	Modulus of elasticity, E' : kN/m^2	4
	Friction angle, ϕ : degrees	22
	Undrained shear strength: kN/m^2	35
	Compression index, C_c	0.47
	Swelling index, C_s	0.12
	Basalt aggregate: crushed basalt, uniformly graded	Particle size: mm
Modulus of elasticity, E' : kN/m^2		30
Friction angle, ϕ : degrees		43

Testing programme

The testing programme focused on assessing the effects of A_s , L/d and the number of columns beneath the footing (Table 2). The diameters for the column under isolated column conditions were 25 mm, 32 mm and 38 mm, which correspond to area replacement ratios of 17%, 28% and 40% beneath the 60 mm footing respectively. For the group configuration, three columns of 18 mm and 22 mm diameter were adopted, as these provided A_s values correlating with the single column of 28% and 40%. Three column lengths – 125 mm, 250 mm and 400 mm – were considered, which represent H_c/H_s ratios of 0.31, 0.62 and 1 respectively (where H_c and H_s are the lengths of the column and sample respectively). $H_c/H_s = 1$ represents a fully penetrating column; $H_c/H_s < 1$ represents a floating column. Initial saturation of the sample was conducted, to eliminate air voids trapped in the column during installation. This was followed by consolidation of the sample under a confining pressure of 275 kPa and back-pressure of 200 kPa, which lasted for approximately 4 days, whereas for reinforced samples drainage accelerated to 2 days when a fully penetrating column was present.

Isotropic confinement was followed by K_0 consolidation, where the total vertical and horizontal stresses were increased to 341 kPa and 300 kPa from 275 kPa, representing a K_0 of 0.71. This was conducted in order to produce more realistic field stress conditions, and allow for surcharge during independent footing load. In addition, under K_0

consolidation the configuration is representative of the unit cell concept, and enables further analysis under this consideration. The required stress path to achieve K_0 consolidation was determined using stress path apparatus on a small specimen, 50 mm in diameter and 100 mm high, which was extracted from the larger sample after the initial one-dimensional consolidation. This stress path was approximately linear, and was imposed on the 300 mm diameter sample in the large triaxial cell by ramping the horizontal and vertical stresses at the required rates. This procedure was adopted as the control software did not incorporate real-time feedback to execute complex stress path loading.

Figure 5 presents the lateral displacement response during K_0 loading for samples TS-01, TS-07 and TS-10. It is evident that the simplified approach to achieve K_0 proved successful for TS01 (unreinforced), as the imposed stress path resulted in virtually zero lateral strain; however, in reinforced tests the intended true K_0 stress path was not fully achieved, as slight lateral straining occurred (Fig. 5, TS-07 and TS-10; negative values represent contraction). This is attributed to variation in stiffness of the stone column and surrounding clay: therefore the applied stress path is referred to as the apparent K_0 path in the remainder of the paper. The implications of this apparent K_0 path and the consequence of lateral straining will be discussed later. In all column tests, the lateral strains experienced during the apparent K_0 loading were below 0.1%.

The third and final stage of testing involved applying

Table 2. Test schedule

Test	Column configuration	Column length, L : mm	Column diameter, d : mm	Area replacement ratio, A_s : %	L/d ratio	
TS-01	Unreinforced	N/A	N/A	N/A	N/A	
TS-02	Isolated	125	25	17	5.0	
TS-03	Isolated	250	25	17	10.0	
TS-04	Isolated	400	25	17	16.0	
TS-05	Isolated	125	32	28	3.9	
TS-06	Isolated	250	32	28	7.8	
TS-07	Isolated	400	32	28	12.5	
TS-08	Isolated	125	38	40	3.3	
TS-09	Isolated	250	38	40	6.6	
TS-10	Isolated	400	38	40	10.5	
TS-11	Group	250	18 × 3	40	13.8	4.1*
TS-12	Group	400	18 × 3	28	22.2	6.6*
TS-13	Group	250	22 × 3	28	11.3	4.1*
TS-14	Group	400	22 × 3	40	18.1	6.6*

*Calculated using L/d_g , where d_g = group diameter.

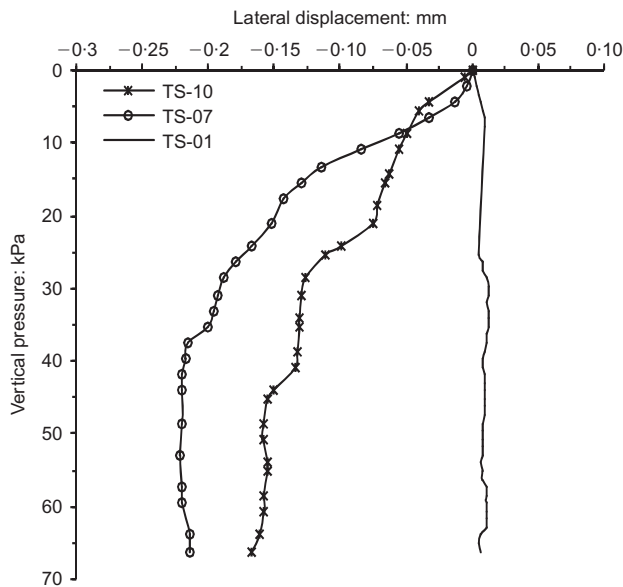


Fig. 5. Lateral displacement response during K_0 loading for a sample reinforced with fully penetrating columns $H_c/H_s = 1$

independent foundation loading under drained conditions. To determine an appropriate loading rate, a trial test was performed on an unreinforced sample, in which foundation load was applied at a loading rate of 1 kPa/h while drainage through the top of the sample was not permitted; 2 kPa of excess pore water pressure developed. In reinforced tests, drainage capacity was enhanced, due to the presence of a stone column, together with top drainage being permitted. Therefore the trial loading rate of 1 kPa/h was deemed sufficient to ensure fully drained conditions.

RESULTS AND DISCUSSION

Due to the complexity and extent of the investigation, it is not possible to present all the data generated as part of the study. Therefore the authors have chosen to provide information that emphasises the most significant findings from the research. The aspects examined in detail in the remainder of this paper are

- performance of samples during initial and K_0 consolidation
- performance of the foundation reinforced by a single column
- performance of the foundation reinforced by a group of three columns
- settlement control using stone columns.

Performance of samples during initial and apparent K_0 consolidation

The unit cell configuration assumes that an end bearing column and the surrounding clay are strained equally in the vertical direction, while zero lateral displacement is maintained at the outer boundary. On the basis of the above description, the apparent K_0 consolidation stage was considered as a close approximation to a unit cell, as the lateral strains were small. As the full sample cross-sectional area is loaded (by way of the 300 mm rigid top plate) during the apparent K_0 consolidation, the effective area replacement ratio is recalculated for the single column diameters of 25 mm, 32 mm and 38 mm as 0.7%, 1.1% and 1.6% respectively. Note that during the foundation loading stage the column diameters above reflect area replacement ratios of 17%, 28%

and 40% respectively beneath the isolated 60 mm diameter footing.

Figure 6 shows the vertical displacement plotted against the vertical stress for samples with fully penetrating columns of diameters 25 mm, 32 mm and 38 mm, and the unreinforced sample. The axial strains experienced by the composite samples (TS-04, TS-07 and TS-10) were 0.77%, 0.72% and 0.54% for area replacement ratios of 0.7%, 1.1% and 1.6% respectively, compared with 1.5% for the unreinforced sample. This yields settlement improvement factors n , defined as the ratio between untreated (S_{ut}) and treated (S_t) settlement, of 1.9, 2.1 and 2.8 respectively, which are greater than those determined by Priebe (1995) of 1.04, 1.06 and 1.10 respectively, based on Poisson's ratio of the soil, $\nu'_s = 0.33$ and friction angle for granular material, $\phi'_c = 45^\circ$. Apart from scale effects, a possible explanation for these differences could relate to the fact that Priebe (1995) does not account for foundation rigidity, and is based on flexible footing conditions.

Figures 7(a) and 7(b) show the pressure–displacement characteristics of samples installed with partially penetrating columns having H_c/H_s ratios of 0.31 and 0.62 and column diameters of 32 mm and 38 mm respectively. It is evident that settlement reduces as the depth of treatment increases for similar values of area replacement ratio. The test data presented in Fig. 7 relate to samples reinforced with a partially penetrating column. Although this does not adhere strictly to the traditional concept of the unit cell configuration, Balaam *et al.* (1977) have shown that, under these conditions, total settlement can be estimated by summing the individual settlements of the reinforced and unreinforced portions. Neglecting small stress variations at the reinforced and unreinforced boundary caused by stress concentrations at the column base, and assuming that the vertical pressure distribution is reasonably uniform across the entire length of the unreinforced sample, the relevant strains experienced by each component can be linearly interpolated from observations of strain made on the two extreme sample conditions of a fully penetrating reinforced and unreinforced sample. The results yielded good correlation between the measured and predicted settlements using this approach. Small variations are attributed to the different boundary conditions between the samples used to generate settlement predictions:

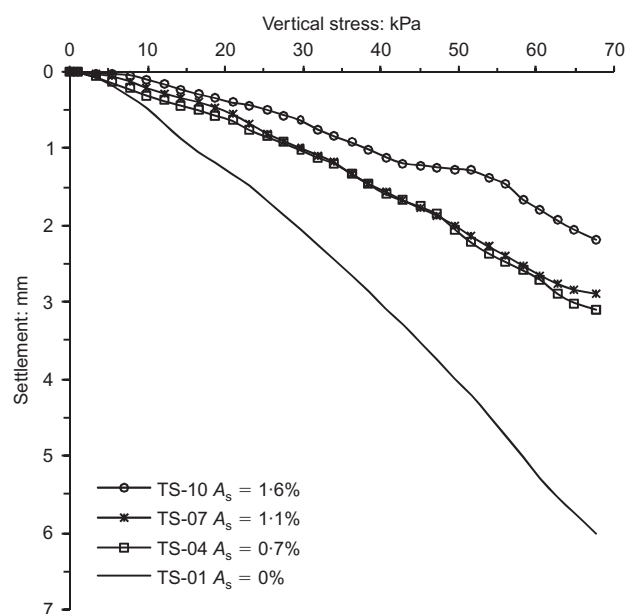


Fig. 6. Settlement under unit cell consideration for $H_c/H_s = 1$ with increasing area replacement ratio

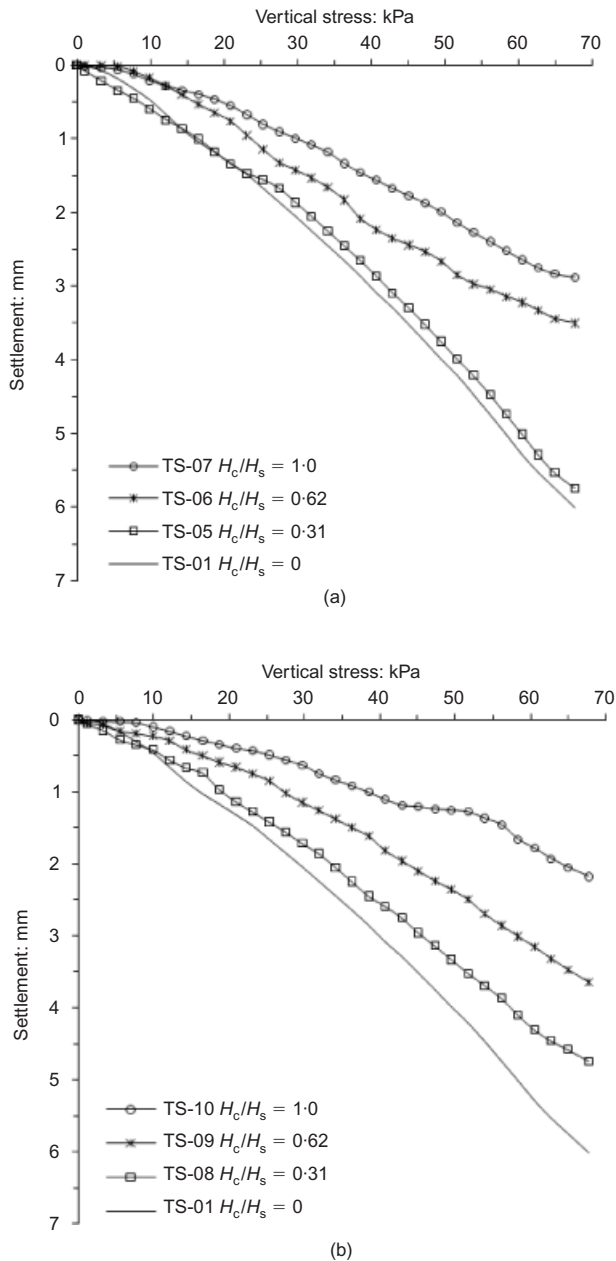


Fig. 7. Settlement under unit cell consideration with varying area replacement ratio: (a) $A_s = 1.1\%$; (b) $A_s = 1.6\%$

for example, fully rigid restraints were provided by the top plate and pedestal in the extreme conditions, compared with the flexible interface boundary that exists for the partially penetrating condition.

During the apparent K_0 consolidation, the change in stress acting on the column and surrounding soil beneath the sample top plate was monitored. Fig. 8 displays the results obtained for a sample reinforced with 28 mm diameter columns of length 125 mm, 250 mm and 400 mm. The increase in vertical stress applied to generate the apparent K_0 loading was 66 kPa: this agrees well with the uniform increase in stress observed beneath the plate in the unreinforced sample (Fig. 8(a)). However, because of variations in stiffness characteristics in the reinforced specimens, the stress increase measured on the column (PT1) and surrounding clay (PT3) varied. In nearly all tests the magnitude of stress on the column was found to increase with respect to area replacement ratio and column length: this is highlighted

for TS-02 to TS-04 in Figs 8(b)–8(d). Furthermore, as the magnitude of the vertical stress increase on the clay during the apparent K_0 consolidation was lower than originally intended, some degree of lateral contraction would be anticipated as the horizontal confining stress increased at the previous predetermined rate. This shows good correlation with the lateral displacement measurements recorded at the sample boundary shown in Fig. 5, and with other tests within the series.

Performance of foundation reinforced by a single column

State of the composite sample prior to foundation loading.

Figure 8 highlighted the stress variation on the column and clay beneath the rigid plate during the apparent K_0 consolidation stage. If the stress concentration on the column were to be significant during this phase, then frictional resistance might have mobilised prior to application of the actual foundation loading. Mobilisation of strength occurs predominantly as a result of differential displacement; however, internal compression of the granular material along the column length maintains displacement compatibility with the consolidating clay. Consequently it is most probable that mobilisation of strength will be more prevalent where the column is floating, where discontinuity could occur as a result of the column penetrating into the underlying soft clay. The maximum difference in the stress recorded between the column and the soil beneath the top plate was approximately 120 kPa (Fig. 8(c)). It is this stress variation that may contribute to the possible mobilisation of shear strength; however, based on the column geometry, it can be shown that a pressure difference of approximately 600 kPa is required for full mobilisation of the side friction. Since the maximum observed measurement is significantly less, it can be concluded that side friction and end bearing were not mobilised in any significant way prior to the main loading. Similar findings were observed for the 32 mm and 38 mm diameter partially penetrating columns.

Further evidence to substantiate the above argument is observed in Fig. 9, which presents the contact stress measured with respect to the vertical displacement throughout the entire three stages of loading (isotropic compression, apparent K_0 and foundation loading). It is clear that there is no evidence to suggest any significant mobilisation of capacity at the end of the apparent K_0 stage; however, it can be said that the column was, to some extent, 'prestressed'. This occurrence is not unlike the full-scale application, as the compaction process during installation often results in the column being prestressed.

Settlement reduction. The ultimate undrained bearing capacity for the 60 mm diameter footing was determined to be 320 kPa. Assuming a factor of safety of 2, the allowable bearing capacity is 160 kPa. This pressure conforms to typical working loads for vibro columns in practice, and therefore it is an appropriate stress level for the evaluation settlement performance in the model tests.

During the isolated foundation loading stage, the column diameters adopted represent area replacement ratios of 17%, 28% and 40% beneath the footing diameter of 60 mm. Fig. 10(a) shows the relationship between bearing pressure and settlement for $A_s = 17\%$ at H_c/H_s ratios of 0.31, 0.62 and 1.0, for tests TS-02, TS-03 and TS-04 respectively. Similar figures for $A_s = 28\%$ and $A_s = 40\%$ are shown in Figs 10(b) and 10(c). While noting that increasing the column length resulted in enhanced load-carrying capacity, the settlement at a bearing pressure of 160 kPa was the main focus of the present work and discussion in this paper. The relevant

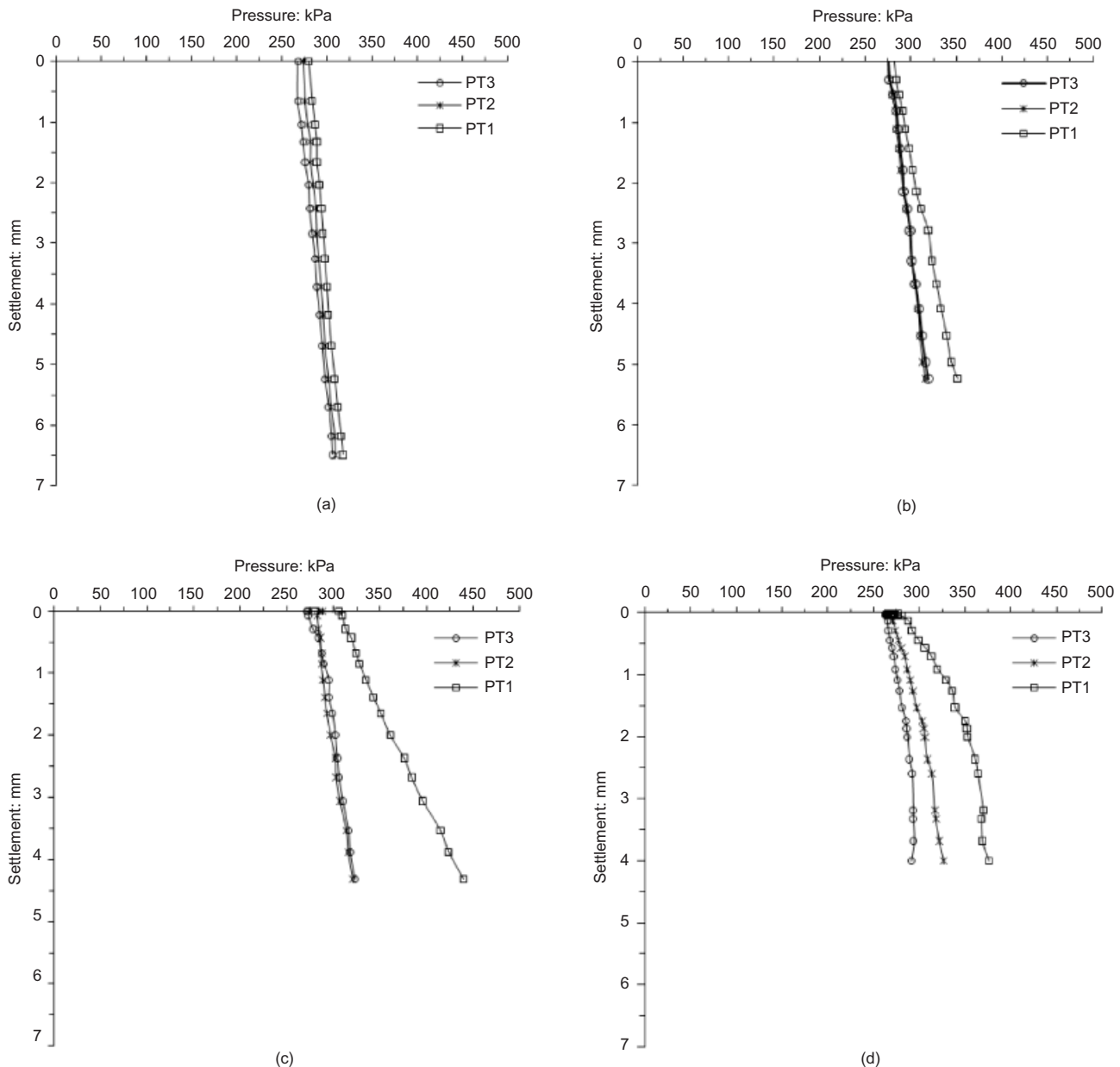


Fig. 8. Total pressure distribution recorded at locations PT1, PT2 and PT3 for total plate displacement during isotropic compression and K_0 loading for: (a) unreinforced sample (TS-01), and sample reinforced with 25 mm diameter column of increasing length; (b) $H_c/H_s = 0.31$ (TS-02); (c) $H_c/H_s = 0.62$ (TS-03); (d) $H_c/H_s = 1$ (TS-04)

settlements and corresponding settlement improvement factors are provided in Table 3. The settlement improvement factor is also plotted with respect to L/d ratio for all values of A_s in Fig. 11(a). It is evident that n increases with respect to L/d ratio for each area replacement ratio, although it appears that increasing the column geometry beyond $L/d = 8-10$ offers little significant improvement, particularly at lower A_s values of 17% and 28%. This agrees favourably with findings previously published by McKelvey (2002), who postulated a critical L/d ratio of 6 in relation to bearing capacity performance for physical model tests. More enhanced improvement in n was observed at $A_s = 40\%$ when L/d exceeded 8, although the relative rate of increase also diminishes with increasing L/d .

The settlement improvement factors are also plotted with respect to area replacement ratio in Fig. 11(b). It is evident that the settlement improvement factor increases with area replacement ratio in a significant manner; however, there

appears to be a threshold A_s level for improvement of between 30% and 40%, particularly when the column is non-end-bearing. This is consistent with observations reported by Wood *et al.* (2000) for a large-group configuration. When compared with predicted values of n from Priebe (1995) in Fig. 12, it is evident that the observed experimental results are somewhat higher than expected. A possible explanation for this could be the confinement provided as a consequence of the rigid nature of the surcharge boundary condition provided by the sample top plate.

Figures 13(a)–(c) highlight the change in pressure measured by PT1 during the foundation loading stage for each area replacement with increasing H_c/H_s ratio. It can be seen that the change in pressure above the column (PT1) was significantly influenced by the column length. For all values of A_s there appears to be no significant difference between the pressure observed at PT1 for the unreinforced sample and that for the sample reinforced with a 125 mm

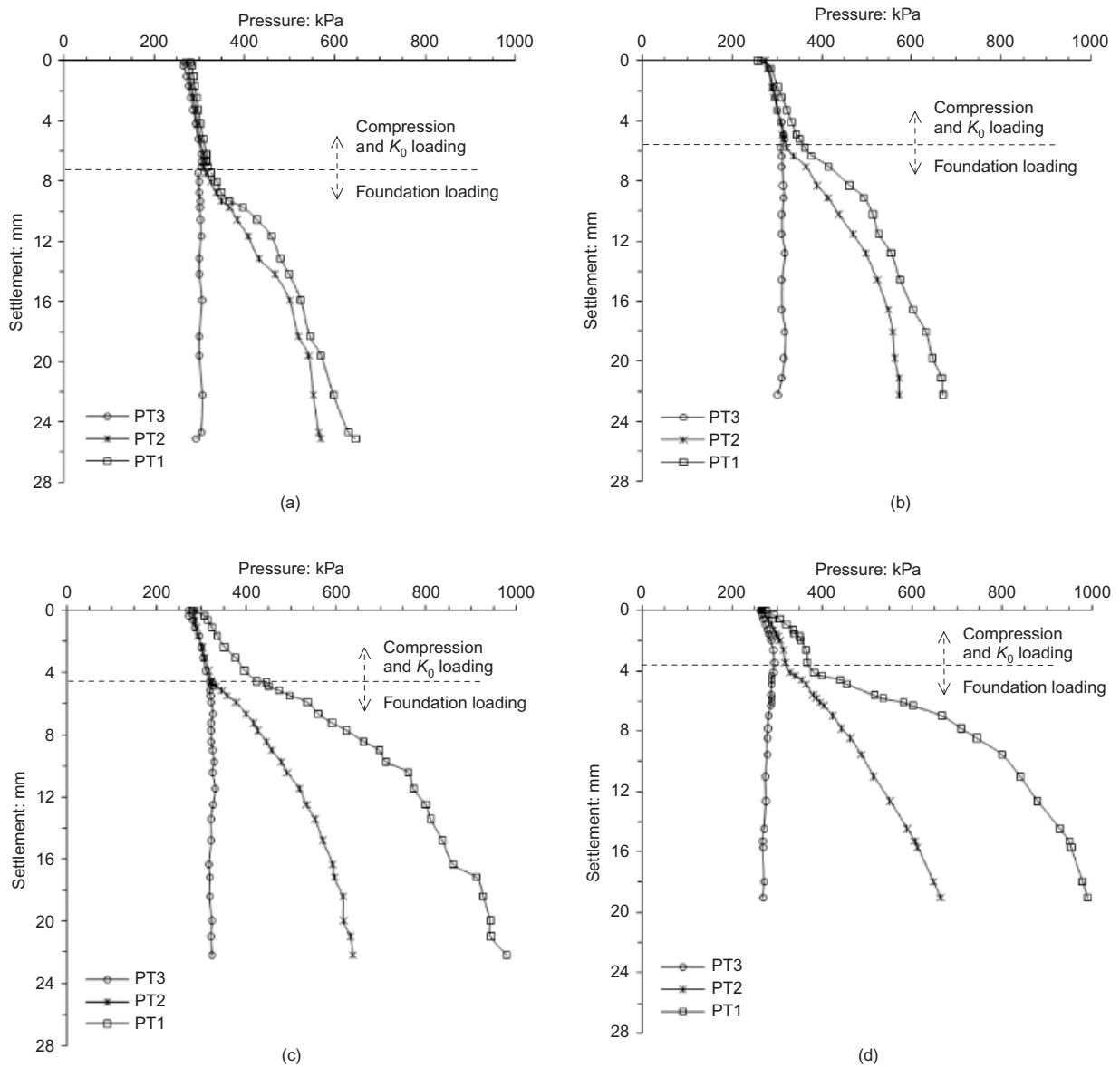


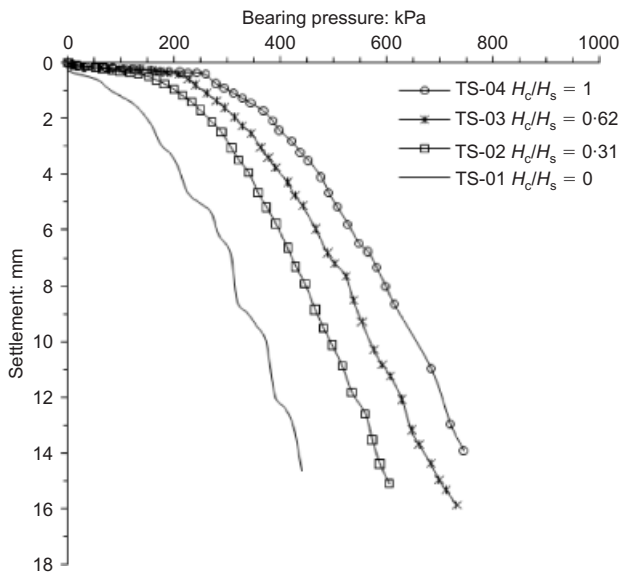
Fig. 9. Total pressure distribution recorded at locations PT1, PT2 and PT3 during isotropic compression, K_0 loading and foundation loading for: (a) unreinforced sample (TS-01), and sample reinforced with 25 mm diameter column of increasing length; (b) $H_c/H_s = 0.31$ (TS-02); (c) $H_c/H_s = 0.62$ (TS-03); (d) $H_c/H_s = 1$ (TS-04)

column ($H_c/H_s = 0.31$). This implies that the shorter column may be acting as a rigid friction pile, and is exhibiting 'end bearing' failure and consequently not contributing significantly towards the load capacity or mitigating settlement. Larger pressure differences at PT1 were recorded once the column geometry (L/d) exceeded the critical length and are attributed to greater column capacity arising from bulging.

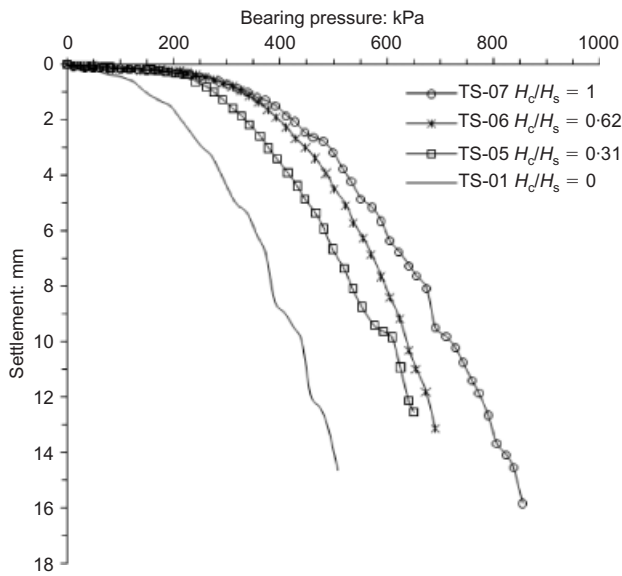
The lateral displacements observed during foundation loading at 120 mm below the top plate are reported for tests TS-01, TS-02 and TS-03 in Fig. 14(a) for $A_s = 17\%$. For the short column ($H_c/H_s = 0.31$), the sample contracted laterally in the early stage of the loading (up to a displacement of 6.5 mm) by 0.022 mm, and this was followed by continued expansion as the loading continued. The maximum radial expansion at the termination of loading was 0.038 mm. The initial contraction and reduced radial expansion observed in this case further substantiate the hypothesis, based on the variation of pressure, that shorter columns behaved as load transfer elements, and failed in end bearing. For the longer

column ($H_c/H_s = 0.62$, representing an L/d ratio of 10), greater expansion of the reinforced sample than in the unreinforced condition was recorded. Column bulging would be more a predominant failure mechanism, and the lateral displacement measurements support this. Similar findings relating to sample contraction and expansion were also observed for $A_s = 28\%$ and 40% (Figs 14(b) and Fig. 14(c) respectively).

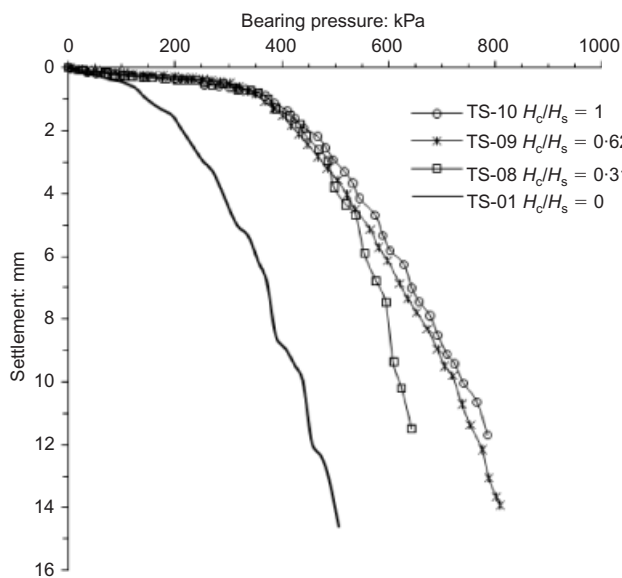
Further confirmation of column failure modes was also obtained from the deformed column profiles observed by sample dissection after each test (Fig. 15). It is shown in Fig. 16 that the base displacement of the column decreases with increasing column L/d , is negligible for $L/d > 8$, and disappears completely at $L/d \approx 10$. Furthermore, in TS-02 and TS-05 the magnitude of base displacement observed is 50% of the final foundation displacements of 15.9 mm and 12.5 mm respectively. This increases considerably in TS-08 to almost 90%, which again emphasises that short columns with low L/d ratio failed in end bearing, despite the occurrence of some internal column compression.



(a)



(b)



(c)

Fig. 10. Footing pressure–settlement response of sample reinforced with columns of various area replacement and H_c/H_s ratios: (a) $A_s = 17\%$; (b) $A_s = 28\%$; (c) $A_s = 40\%$

Table 3. Settlement improvement factor during foundation loading

Test no.	Settlement: mm	Improvement factor, n
TS-01	1.50	1.00
TS-02	0.40	3.75
TS-03	0.28	5.36
TS-04	0.26	5.77
TS-05	0.23	6.49
TS-06	0.22	6.82
TS-07	0.21	7.14
TS-08	0.29	5.24
TS-09	0.23	6.52
TS-10	0.20	7.50

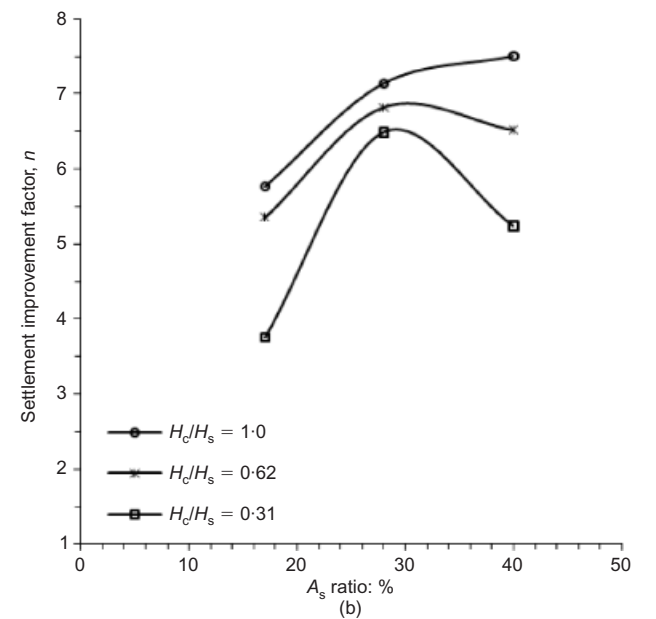
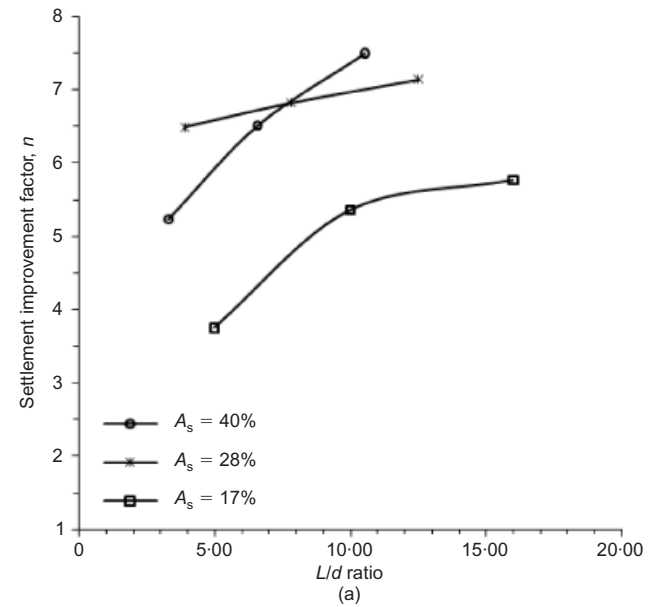


Fig. 11. Settlement improvement factor plotted against: (a) L/d ratio; (b) A_s ratio

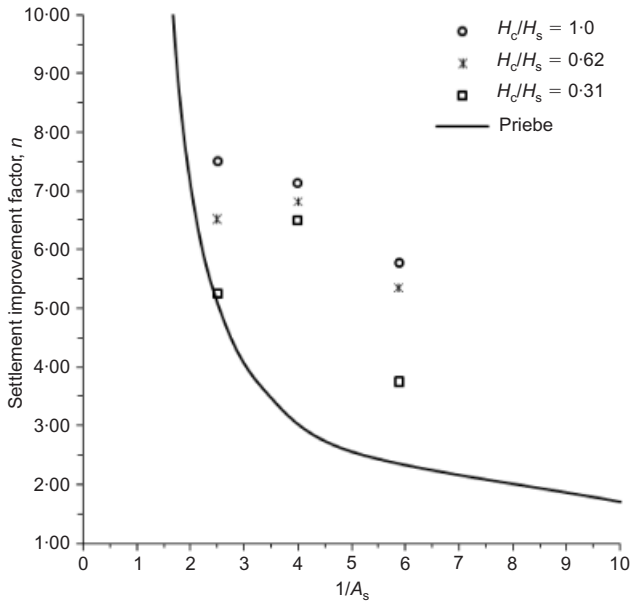


Fig. 12. Settlement improvement factor compared with that of Priebe (1995)

Performance of foundations supported on column groups

The performance of a small group of three columns, 18 mm and 22 mm in diameter (corresponding to $A_s = 28\%$ and 40%) and 250 mm and 400 mm long, were evaluated using the same test configuration as described above. Fig. 17(a)–(d) presents the pressure–settlement characteristics for the small-group configuration, compared with that of the corresponding single column at matching A_s and length. The overall load-carrying capacity of the foundation supported on the group of columns is generally similar to that of a single column at the same area replacement ratio, with the exception of small variations at low bearing pressures. The settlement of the foundation at the target bearing pressure (160 kPa) for the group $A_s = 28\%$ and 40% at $H_c/H_s = 0.62$ is 0.46 mm and 0.39 mm respectively, which represents settlement improvement factors of 3.2 and 3.8. These n values, and those determined for $H_c/H_s = 1.0$ in the group configuration, are plotted in Fig. 18. For direct comparison the corresponding single-column n values are also included. It is evident that the performance of the group is not as good as that of the corresponding single column, and it is interesting that this reduction is more significant when the column is not end bearing.

The effect of block failure arising due to group interaction is well documented in relation to pile foundations (Poulos, 1968; Poulos & Mattes, 1974; Meyerhof, 1976). Examination of the excavated column profiles showed that similar behaviour is prevalent in partially penetrating groups of stone columns ($H_c/H_s = 0.62$). Redefining the L/d ratio to account for group behaviour by replacing the individual column diameter (d) with that of the effective group diameter ($d_g = 60$ mm) produces revised L/d_g ratios for the group configuration at $A_s = 28\%$ and 40% of 4 and 6 respectively. These values are similar to the critical column length previously defined for a single column condition by Hughes & Withers (1974) and McKelvey (2002). Lateral contraction of the sample boundary for the partially penetrating column group ($H_c/H_s = 0.62$), similar to that previously described for the isolated column, provides additional supporting evidence to support the block failure mechanism observations.

Figure 19 shows the pressure recorded by PT1 and PT2 during the foundation loading for TS-12 and 14. Under

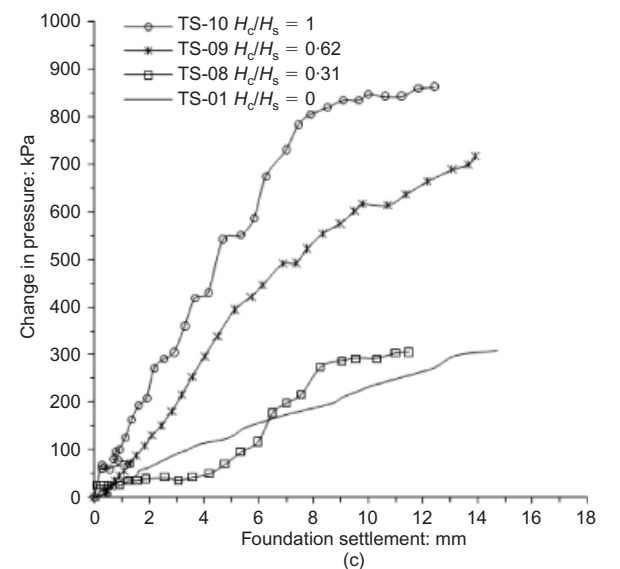
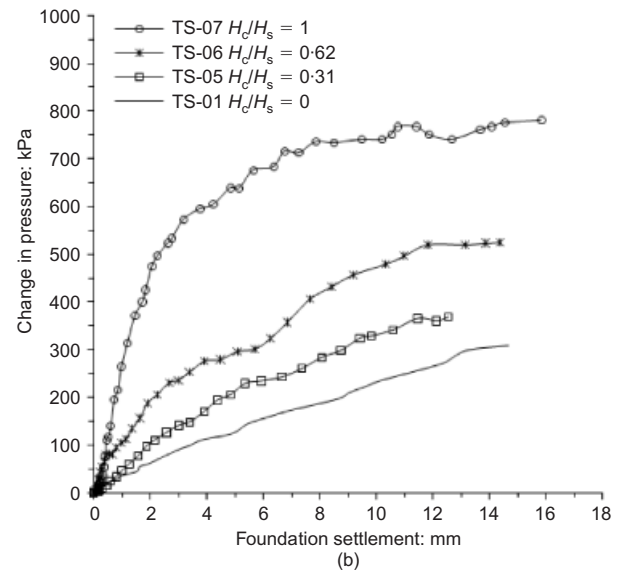
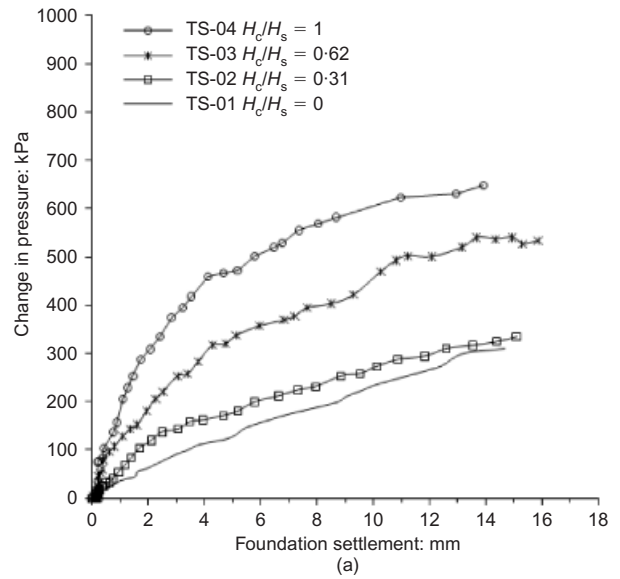


Fig. 13. Change in pressure at column location recorded by PT1: (a) $A_s = 17\%$; (b) $A_s = 28\%$; (c) $A_s = 40\%$

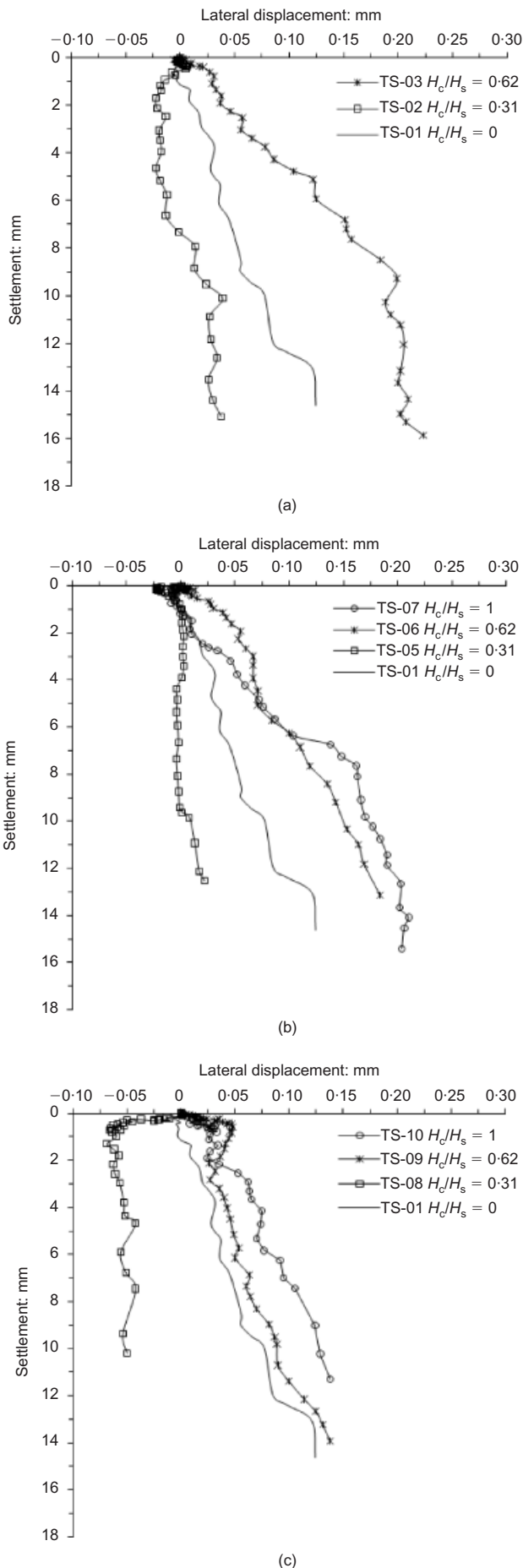


Fig. 14. Lateral strain response during foundation loading: (a) $A_s = 17\%$; (b) $A_s = 28\%$; (c) $A_s = 40\%$

group conditions, PT1 is now exposed to clay and PT2 is exposed to the stone column. The pressure recorded by PT1 is significantly higher than the pressure read by PT2; although this may be counterintuitive, based on the relative material stiffness, this particular observation can be explained by the load-carrying mechanism of stone columns. Upon loading, stone columns may undergo deformation, as they are non-rigid elements. As evidenced through sample dissection after loading in both this and previous research (Hu, 1995; McKelvey, 2002), column bulging and subsequent inter-column interactions have a significant role in controlling group stability. Enhanced lateral resistance of the clay in the central confined clay region provides improved support against column deformation, which reduces the bulging observed on the inner column surfaces. Deformations occur more readily on the outward surfaces, as the lateral pressures and soil confinement are lower beyond the edge of the foundation. As footing displacement progresses, the lateral pressure on the internal face will continue to increase, therefore generating column bending towards the weaker unsupported side.

Settlement control using stone columns

The research considered various aspects of the stone column application, which includes the area replacement ratio, L/d ratio, and small-group performance. A finding from the research is the possible existence of a threshold area replacement ratio of between 30% and 40% for settlement performance. However, it is acknowledged that this observation is currently only related directly to the test configuration, and may be not valid as a general rule in all cases, because of variations in soil shear strength and stiffness. Furthermore, it was noted that enhanced performance of the column can be achieved if the tendency to bulging is restricted. For moderate area replacement ratios the clay annulus beneath the foundation surrounding the column is also subjected to increased vertical stress for the foundation load, and hence is able to provide enhanced lateral restraint against bulging. This beneficial effect is dependent on the thickness of the annulus, and when this is significantly reduced (as in the case of larger A_s values), the overall column performance is compromised, as bulging failure occurs more readily. Similar behaviour could also contribute to the relatively reduced performance of the group as the columns were located at the edge of the footing.

From the load-displacement curves presented in Fig. 10 and the settlement improvement factors presented in Fig. 11 it is shown that there may be evidence to suggest that some degree of design flexibility exists for the design of stone columns, whereby settlement can be effectively controlled when using larger area replacement ratios and relatively short column lengths ($L/d < 6$) or long, slender columns ($L/d > 6$) at relatively small area replacement values. The authors acknowledge that this hypothesis is at present based only on limited test data; however, continued research in this respect may offer more conclusive evidence in order to substantiate the above argument fully. Nevertheless, the potential of such a finding would be invaluable in the design of stone columns in difficult site conditions, as it would allow greater flexibility in the column geometry for the treatment provided, in addition to providing advanced economic viability of the stone column technique.

The group study revealed that the pressure developed in the clay enclosed by the three columns was significantly higher than in the confining columns, and this contributed to excessive column deformation on the outer surface of the column. This observation leads to an interesting consideration: in practice it is often the case that a central column is

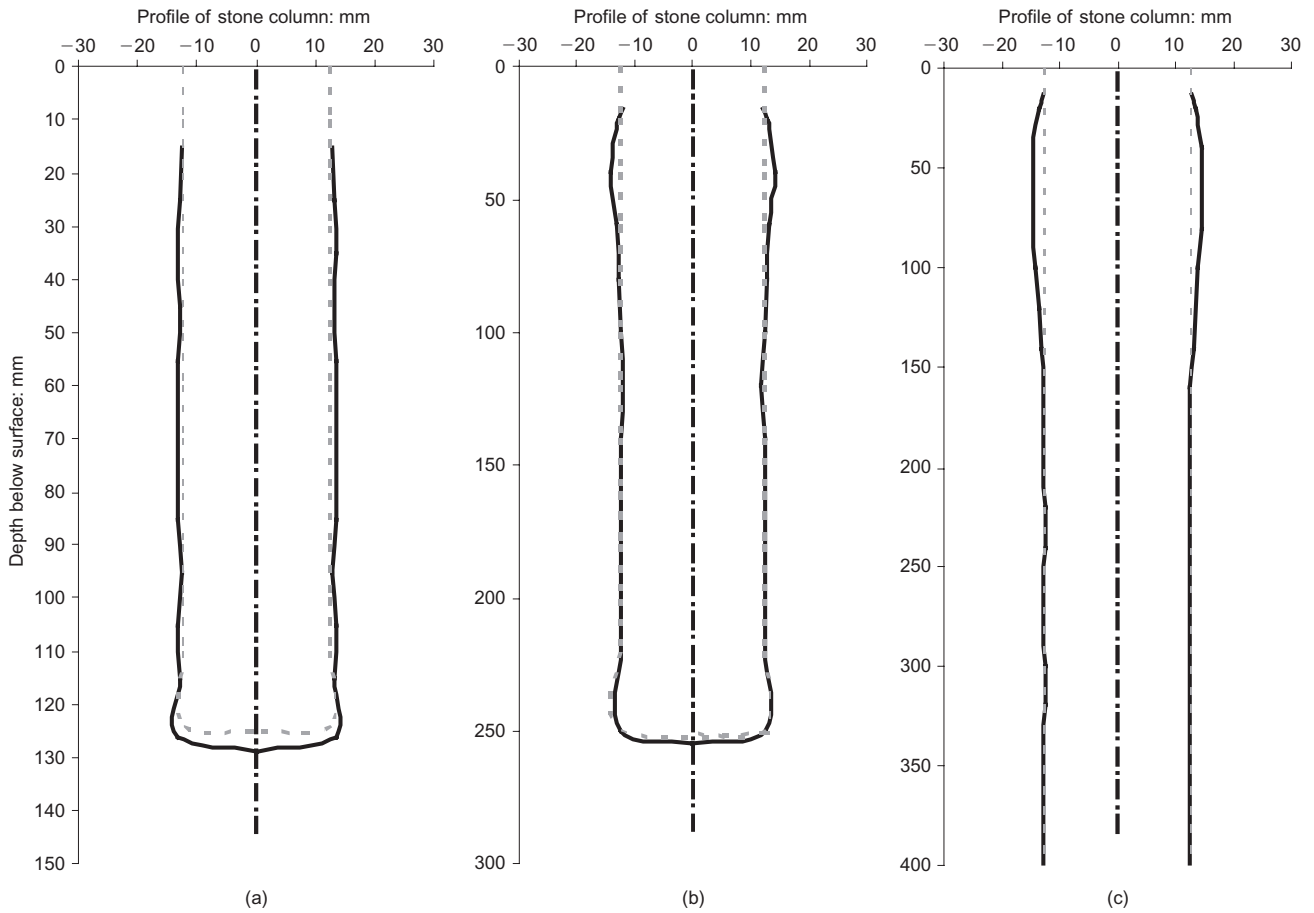


Fig. 15. Excavated column profile, $A_s = 17\%$: (a) $L/d = 5$; (b) $L/d = 10$; (c) $L/d = 16$

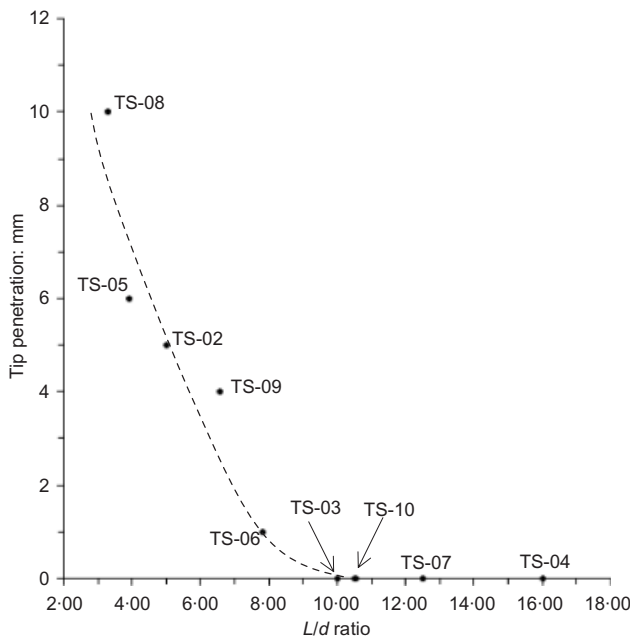


Fig. 16. Column tip penetration plotted against L/d ratio

placed in the middle of a small circular or square column group. Information determined in the present investigations raises questions regarding this configuration, as it may be superfluous to the overall group performance, although further testing is required to substantiate this.

CONCLUDING REMARKS

The work reported in this paper documented the settlement performance of a 60 mm foundation supported on soft clay treated with stone columns with different configurations of column length to diameter ratio, area replacement ratio and single/group conditions. It has been observed that settlement can equally be controlled using shorter columns at higher replacement ratios or longer columns at reduced area replacement. In addition, it is also shown that an optimum area replacement ratio of between 30% and 40% exists for the control of settlement, and that soil–structure interaction has a significant role in preventing excessive column deformations. The existence of a block mechanism in conjunction with enhanced localised stress in the enclosed soil confined by the small-group configuration proved to have a detrimental effect on settlement when compared with an isolated column. The above findings could make a significant positive contribution to current design practice, although it is acknowledged that additional model and field experiments, coupled with parametric numerical evaluation, are required to verify these conclusions.

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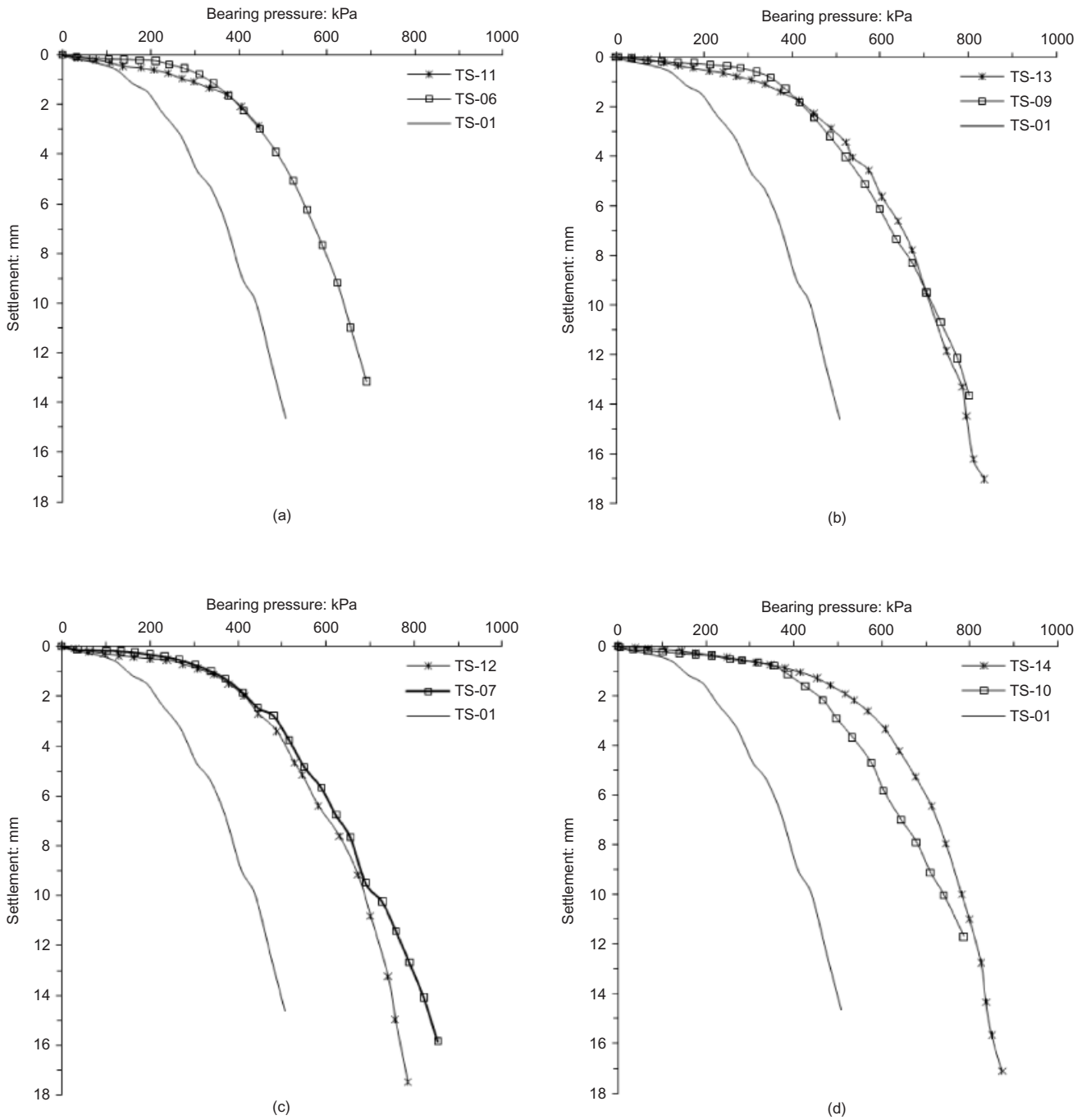


Fig. 17. Small-group performance compared with isolated column: (a) $A_s = 28\%$, $H_c/H_s = 0.62$; (b) $A_s = 28\%$, $H_c/H_s = 1.0$; (c) $A_s = 40\%$, $H_c/H_s = 0.62$; (d) $A_s = 40\%$, $H_c/H_s = 1.0$

NOTATION

A_c area of stone column
 A_s area replacement ratio
 B foundation breadth
 c_u undrained shear strength
 D foundation diameter
 d stone column diameter
 d_g effective stone column group diameter
 e void ratio
 E_s, E_c deformation moduli of soil and column
 H_c/H_s ratio of column length to sample height (soil)
 n settlement improvement factor
 K_0 coefficient of earth pressure at rest
 L column length
 L/d ratio of column length to diameter
 p' mean effective stress

Q deviator stress
 q_0 surcharge pressure
 q_u ultimate bearing pressure
 S settlement
 S_t settlement of treated soil
 S_{ut} settlement of untreated soil
 s column spacing
 W foundation width
 ν'_s Poisson's ratio of soil
 σ_{rc}, σ_{rs} radial stress in column and soil
 σ_{vc}, σ_{vs} vertical stress experienced by column and soil
 σ'_v, σ'_h vertical and horizontal effective stress
 σ_1, σ'_1 vertical total and effective stress
 σ_3, σ'_3 horizontal total and effective stress
 τ shear stress
 ϕ'_c, ϕ'_s friction angle of the column and soil

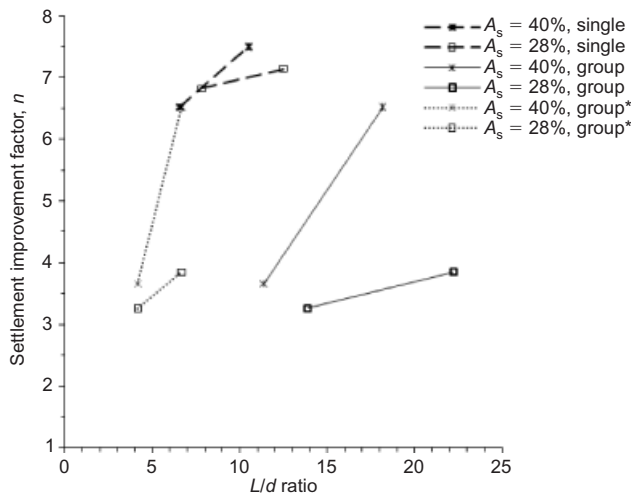


Fig. 18. Settlement improvement factor for single and a group of columns; * denotes L/d based on group diameter, d_g

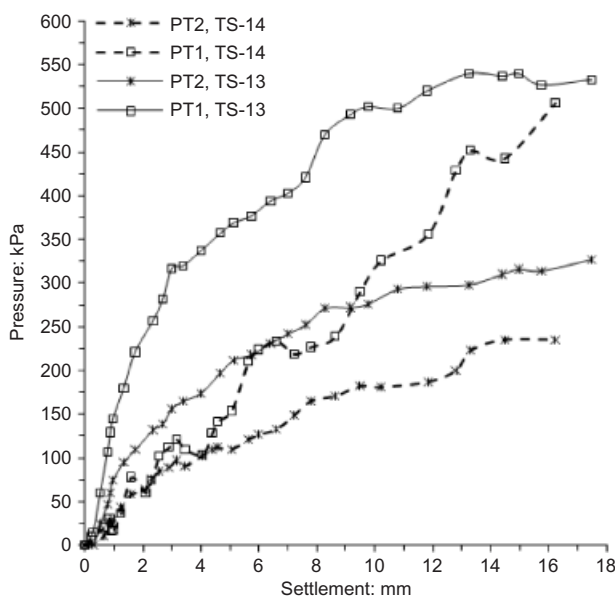


Fig. 19. Pressure recorded beneath footing in group configuration

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