

# The UKIRT Infrared Deep Sky Survey *ZY JHK* photometric system: passbands and synthetic colours

P. C. Hewett,<sup>1\*</sup> S. J. Warren,<sup>2</sup> S. K. Leggett<sup>3</sup> and S. T. Hodgkin<sup>1</sup>

<sup>1</sup>*Institute of Astronomy, Madingley Road, Cambridge CB3 0HA*

<sup>2</sup>*Blackett Laboratory, Imperial College of Science, Technology and Medicine, Prince Consort Road, London SW7 2AZ*

<sup>3</sup>*United Kingdom Infrared Telescope, Joint Astronomy Centre, 660 North A'ohoku Place, Hilo, HI 96720, USA*

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## ABSTRACT

The United Kingdom Infrared Telescope (UKIRT) Infrared Deep Sky Survey is a set of five surveys of complementary combinations of area, depth and Galactic latitude, which began in 2005 May. The surveys use the UKIRT Wide Field Camera (WFCAM), which has a solid angle of  $0.21 \text{ deg}^2$ . Here, we introduce and characterize the *ZY JHK* photometric system of the camera, which covers the wavelength range  $0.83\text{--}2.37 \mu\text{m}$ . We synthesize response functions for the five passbands, and compute colours in the WFCAM, Sloan Digital Sky Survey (SDSS) and two-Micron All Sky Survey (2MASS) bands, for brown dwarfs, stars, galaxies and quasars of different types. We provide a recipe for others to compute colours from their own spectra. Calculations are presented in the Vega system, and the computed offsets to the AB system are provided, as well as colour equations between WFCAM filters and the SDSS and 2MASS passbands. We highlight the opportunities presented by the new *Y* filter at  $0.97\text{--}1.07 \mu\text{m}$  for surveys for hypothetical *Y* dwarfs (brown dwarfs cooler than *T*), and for quasars of very high redshift,  $z > 6.4$ .

**Key words:** surveys – infrared: general.

## 1 INTRODUCTION

The United Kingdom Infrared Telescope (UKIRT) Infrared Deep Sky Survey (UKIDSS, Lawrence et al., in preparation) commenced on 2005 May 13, and is a set of five surveys of complementary combinations of depth and area, employing the wavelength range  $0.83\text{--}2.37 \mu\text{m}$  in up to five filters *ZY JHK*, and extending over both high and low Galactic latitude regions of the sky. The new *Z* band,  $0.84\text{--}0.93 \mu\text{m}$ , and the *Y* band,  $0.97\text{--}1.07 \mu\text{m}$ , introduced by Warren & Hewett (2002), are both characterized in this paper. It is anticipated that the surveys will take 7 years to complete. This paper characterizes the photometric system of the survey, and presents synthetic colours of a wide variety of sources. The paper is one of a set of five which provide the reference technical documentation for UKIDSS. The other four papers, described below, are Casali et al. (in preparation), Lawrence et al. (in preparation), Irwin et al. (in preparation) and Hambly et al. (in preparation).

In this paper, all quoted magnitudes are on the Vega system. We use the nomenclature *Z*, *Y*, *J*, *H* and *K* for magnitudes in the five bands used by UKIDSS; *J2*, *H2* and *K2* for the bands of the 2-Micron All Sky Survey (2MASS, Cutri et al. 2003) and *u*, *g*, *r*, *i* and *z* for the native bands of the Sloan Digital Sky Survey (SDSS, York et al. 2000) 2.5-m telescope. Vega-based magnitudes in the SDSS system have been calculated by assuming that Vega has

zero magnitude in the *u*, *g*, *r*, *i* and *z* passbands. Appropriate zero-point offsets to allow conversion to the AB system are given in Section 4.6. Quoted survey depths correspond to  $5\sigma$  significance for a point source.

The survey instrument is the Wide Field Camera (WFCAM) on UKIRT. A detailed description of the instrument is provided by Casali et al. (in preparation). The camera has four Rockwell Hawaii-II 2048<sup>2</sup> PACE arrays, with pixel scale  $0.4 \text{ arcsec}$ , giving a solid angle of  $0.21 \text{ deg}^2$  per exposure. At the time of commissioning, 2004 November, the instrument *étendue*<sup>1</sup> of  $2.38 \text{ m}^2 \text{ deg}^2$  was the largest of any near-infrared imager in the world. The Canada–France–Hawaii Telescope WIRCam instrument (Puget et al. 2004) covers a solid angle of  $0.11 \text{ deg}^2$  per exposure giving an *étendue* of  $1.22 \text{ m}^2 \text{ deg}^2$ . WFCAM is likely to remain as the near-infrared imager with the largest *étendue* in the world until completion of the near-infrared camera for the Visible and Infrared Survey Telescope for Astronomy (VISTA) (Dalton et al. 2004). Consequently, WFCAM provides the opportunity for new wide surveys, to depths substantially deeper than those reached by 2MASS. WFCAM is a common-user instrument, but it is anticipated that the majority of WFCAM observing time will be devoted to UKIDSS.

The scope, layout and broad science goals of the five components of UKIDSS are described by Lawrence et al. (in preparation).

<sup>1</sup> Product of telescope collecting area and solid angle of instrument field of view, sometimes called *grasp*.

\*E-mail: phewett@ast.cam.ac.uk

There are three surveys targeting extragalactic fields. The Large Area Survey (LAS) is a wide, relatively shallow survey that will cover  $4000 \text{ deg}^2$  from within the footprint of the SDSS, in the four bands  $YJHK$ . The depth,  $K = 18.4$ , will be some 3 mag deeper than 2MASS. The Deep Extragalactic Survey (DXS) is of intermediate depth,  $K = 21.0$ , and will cover  $35 \text{ deg}^2$  in  $J$  and  $K$ . The deepest survey is the Ultra Deep Survey (UDS), which will cover  $0.78 \text{ deg}^2$  in  $JHK$  to a depth  $K = 23.0$ . Then there are two surveys targeting Galactic fields. The Galactic Plane Survey (GPS) will cover some  $1800 \text{ deg}^2$ , defined by the sections of the Galactic-latitude band  $-5^\circ < b < +5^\circ$  that are contained within the declination limits  $-15^\circ < \delta < +60^\circ$ . This region will be imaged in  $JHK$  to a depth  $K = 19.0$ . Finally, the Galactic Clusters Survey will image 11 stellar open clusters and star formation associations, covering  $1400 \text{ deg}^2$ , in all five bands  $ZYJHK$ , to a depth  $K = 18.7$ .

For typical observing programmes, WFCAM will accumulate data at the rate of approximately 1 Tb per week. All WFCAM data are processed by an automated pipeline, described by Irwin et al. (in preparation). The pipeline flat-fields the data, subtracts the counts from the background sky, detects and parametrizes objects and performs the photometric and astrometric calibrations. The reduced frames and catalogues are ingested into the WFCAM Science Archive, described by Hambly et al. (in preparation). A process of curation results in seamless images and catalogues, matched across bands. Access to the data is through a flexible query tool, which allows SQL commands for sophisticated searches.

The present paper characterizes the photometric system defined by the WFCAM  $ZYJHK$  broad-band filters. The layout of the paper is as follows. In Section 2 we explain the design of the five passbands, in Section 3 we explain the procedure for computing synthetic colours and in Section 4 we assemble the required ingredients. In Section 5 we present the synthetic colours of a variety of non-degenerate and degenerate stars, galaxies and quasars. Finally, in Section 6 we compute colour equations between certain WFCAM, SDSS and 2MASS filters. A future paper (Hodgkin et al., in preparation) will describe the results of calibration observations with the instrument, and present the measured colour terms. These two papers, then, are similar in aim to the SDSS papers by Fukugita et al. (1996) and Smith et al. (2002).

## 2 THE WFCAM $ZYJHK$ PHOTOMETRIC SYSTEM

Extensive work on the specification of optimal passbands in the near-infrared has led to the development of the Mauna Kea Observatories (MKO) near-infrared filter set that includes  $JHKL'M'$  bandpasses (Simons & Tokunaga 2002; Tokunaga, Simons & Vacca 2002). The MKO filters have been adopted widely and the filters chosen for the WFCAM  $J$ ,  $H$  and  $K$  bands have been manufactured to the MKO specifications.

Key science goals of UKIDSS include a census of very low-temperature brown dwarfs (Section 5.2.2) and the identification of quasars with redshifts beyond the current maximum reached by SDSS,  $z = 6.4$  (Section 5.4). To enable such goals, a novel feature of UKIDSS is the extension of imaging observations to wavelengths shortward of  $1.2 \mu\text{m}$  where the availability of broad-band colours improves the discrimination between brown dwarfs and high-redshift quasars.

At the interface between conventional optical and near-infrared observations the SDSS  $z$  band has in practice become the ‘standard’ and the availability of extensive sky coverage in the  $z$  band from the SDSS is an important element for the exploitation of the UKIDSS

LAS. There is thus an argument for incorporating the SDSS  $z$  band, or a very close approximation to the band, into the UKIDSS filter set. However, while the SDSS  $z$ -band imaging is extensive, a feature of the passband is an extended tail in the response curve extending to long wavelengths. The spectral energy distributions (SEDs) of low-mass stars, brown dwarfs and high-redshift quasars involve both steeply rising flux distributions towards red wavelengths, coupled with large spectral discontinuities. As a result, the magnitude difference between the SDSS  $z$  band and a passband with a more rectangular or Gaussian transmission profile can be large for red objects. Furthermore, the form of the extended red tail in the SDSS  $z$  band is defined by the declining CCD detector quantum efficiency and is also affected by strong atmospheric absorption at  $0.93\text{--}0.97 \mu\text{m}$ , making the synthesis of a passband closely similar to the SDSS  $z$  band impractical. For these reasons a new  $Z$ -band filter has been designed for use with WFCAM. The specification involves an effective wavelength of  $0.882 \mu\text{m}$  (close to the effective wavelength of the SDSS  $z$  band), close to constant transmission over a  $0.06\text{-}\mu\text{m}$  wavelength range and cut-on and cut-off profiles very similar to the MKO  $JHK$  filters.

The wavelength interval between  $0.9$  and  $1.2 \mu\text{m}$  has, until now, been largely unexploited. The low sensitivity of most optical CCD detectors at  $\sim 1 \mu\text{m}$ , coupled with the relatively bright sky background, curtailed interest from optical astronomers. For infrared astronomers, the lack of large near-infrared detectors, which would enable wide-field surveys to be undertaken, has meant that observations at  $\sim 1 \mu\text{m}$  would be of interest in only a few specialized applications. For the first time, the technological advance represented by the commissioning of WFCAM allows wide-field observations with an instrument that possesses high throughput at  $\sim 1 \mu\text{m}$ . Scientifically, the aim of detecting bright quasars with redshifts as high as  $z = 7.2$  provides a strong motivation for obtaining broad-band observations at wavelengths between the  $Z$  and  $J$  bands.

To this end, Warren & Hewett (2002) proposed a specification for a new  $Y$ -band filter with an effective wavelength of  $1.03 \mu\text{m}$ . Hillenbrand et al. (2002) have also defined and characterized a  $Y$ -band filter with a similar effective wavelength but a substantially greater width. The rationale for the choice of the narrower  $Y$  band involves avoiding the wavelength region that suffers from significant atmospheric absorption by adopting a blue cut-on wavelength of  $\simeq 0.97 \mu\text{m}$ . At the red end of the passband, the onset of very strong emission from OH lines occurs at  $1.07 \mu\text{m}$ . This increases the signal from the sky background significantly and the Warren & Hewett  $Y$ -band cut-off wavelength is chosen to be  $\simeq 1.07 \mu\text{m}$  in order to reduce the effect of the sky background. The narrower passband also has the significant advantage of allowing improved discrimination between high-redshift quasars and T dwarfs, by some 0.15 mag. The narrower  $Y$ -band specification has therefore been adopted for the UKIDSS  $Y$ -band filter and several other observatories have also decided to incorporate the narrower  $Y$ -band specification in their filter sets (A. Tokunaga, private communication).

## 3 SYNTHETIC PHOTOMETRY

All calculations of magnitudes and colours have been undertaken using the SYNPHOT package in the Space Telescope Science Data Analysis System. The mean flux density,  $f_\lambda(P)$ , in a broad passband defined by a dimensionless bandpass throughput function,  $P(\lambda)$ , is calculated as

$$f_\lambda(P) = \frac{\int P(\lambda) f_\lambda(\lambda) \lambda d\lambda}{\int P(\lambda) \lambda d\lambda}, \quad (1)$$

where  $f_i(\lambda)$  is the flux density of the target object (SYNPHOT User Guide 1998<sup>2</sup>). The associated zero-point is calculated by evaluating the same expression for a spectrophotometric standard star, Vega in our case, ‘observed’ using the identical passband function  $P(\lambda)$ . The technique is thus differential in nature and mimics the procedure undertaken when performing actual photometric observations, calibrated by observations of standard stars. The shape of the throughput function is the key element in the calculation, although, for all but the most pathological of target SEDs, errors in the form of the throughput function cancel to first order because the zero-point defined by the standard star is calculated using the same throughput function.

SYNPHOT employs a reference SED for Vega from Bohlin & Gilliland (2004). Since in the system of the UKIRT Faint Standards (Hawarden et al. 2001), which will be used to calibrate UKIDSS, Vega has zero magnitude in *J*, *H* and *K*, whereas in the Johnson *UBV* system Vega has non-zero magnitudes, care must be taken in defining zero-points. *In this paper the zero-points in all the UKIDSS, SDSS and 2MASS bands are defined by Vega having zero magnitude.* Zero-point offsets to the AB system used to bring the SDSS bands on to the Vega system are provided in Section 4.6. Transfer to a system in which Vega has non-zero magnitude (as is the case for some near-infrared systems) can be achieved by a simple zero-point shift.

### 3.1 Accuracy of zero-points

*We assume that the spectrum of Vega provided by Bohlin & Gilliland (2004) is an accurate representation of the true SED.* Employing this spectrum as the basis for the calculations presented here ensures that the results are reproducible by others. If an improved determination of the Vega spectrum becomes available it would therefore be a simple matter to compute adjustments to any quantities provided here.

Extensive work has been undertaken to determine the absolute flux distribution of Vega from the ultraviolet through near-infrared wavelengths (e.g. Cohen, Wheaton & Megeath 2003; Bohlin & Gilliland 2004) but uncertainty at the 2 per cent level remains (see Tokunaga & Vacca 2005, for a recent discussion). A particular concern is whether the near-infrared absolute fluxes of Vega should be increased by  $\simeq 2$  per cent relative to those in the optical. While the basis for the calculation of the magnitudes and colours presented here is clear, i.e. the Bohlin & Gilliland Vega spectrum has zero magnitude for all passbands, if systematic offsets in magnitude or colour at the few per cent level are an issue for a particular application, careful reference should be made to the above emphasized statements on the zero-points definition and the adopted SED for Vega.

## 4 RESPONSE FUNCTIONS

Passband response functions have been computed by taking into consideration all wavelength-dependent quantities, including atmospheric absorption, mirror reflectivity, filter transmission and array quantum efficiency. Wavelength-independent quantities are irrelevant for synthesizing colours, but have been included by normalizing the computed curves to the measured total system throughput established from observations of standard stars. This result is preliminary, and the overall wavelength-independent normalization applied is subject to revision.

### 4.1 Atmospheric transmission

The effect of atmospheric transmission was quantified using the ATRAN code (Lord 1992). Models were generated over the wavelength range 0.8–2.5  $\mu\text{m}$  with a resolution of 3  $\text{\AA}$  using atmospheric parameters appropriate for observations from Mauna Kea. Using four values for the airmass (1.0, 1.3, 1.6 and 2.0) and four values for the precipitable water vapour (1.0, 2.0, 3.0 and 5.0 mm) resulted in a total of 16 models. The vast majority of the UKIDSS observations are expected to be performed at airmass  $\leq 1.3$  with a water column of  $\simeq 1.0$  mm. However, more extreme airmass values and water columns up to 5 mm were included to allow investigation of the passband behaviour both in poor conditions on Mauna Kea and for sites with much larger values of precipitable water vapour, such as those employed for 2MASS. The impact of Rayleigh scattering and aerosol scattering (Hayes & Latham 1975) on the shape of the passbands is insignificant given our target photometric accuracy and no attempt has been made to include their effects.

### 4.2 Telescope, instrument and detector

Light entering the telescope undergoes three reflections from aluminium-coated mirrors (telescope primary, telescope secondary and one reflection within WFCAM) before reaching the detectors. The variation in reflectivity at short infrared wavelengths, relevant for the *Z* and *Y* bands, is significant and three reflections from aluminium have been incorporated in the calculation of the passbands using data from Hass & Hadley (1963).

Transmission measurements over the wavelength range of interest for the remaining optical components within the WFCAM instrument show no variations exceeding 1 per cent, and constant transmission, independent of wavelength, has therefore been adopted.

The quantum efficiency of the Rockwell Hawaii-II 2048  $\times$  2048 HgCdTe detectors increases approximately linearly with wavelength. The change across the individual passbands amounts to only a few per cent but the variation in quantum efficiency has been incorporated in the calculation of the passbands using data for a typical device (Table 1). The measurements at 1.2, 1.6 and 2.2  $\mu\text{m}$  are the values supplied by the manufacturer, multiplied by 0.8. This factor accounts for an error in the computed gain used by the manufacturer, as a consequence of covariance between pixels. To obtain the remaining values in the table, the relative quantum efficiency across the interesting wavelength range was measured by the WFCAM team (Casali et al., in preparation), and the values were normalized to the manufacturer’s points. We have interpolated between the points in the table, with the quantum efficiency assumed to be constant for wavelengths  $> 2.2 \mu\text{m}$ .

### 4.3 Filters

The filter transmission curves are from laboratory measurements at 10- $\text{\AA}$  intervals, made by the WFCAM team. The measurements were undertaken at room temperature. The dependence of the filter cut-on and cut-off wavelengths as a function of temperature was measured by the manufacturers. Filter transmission curves appropriate for the operating temperature (120 K) of the WFCAM instrument were then

**Table 1.** Wavelength dependence of array detector quantum efficiency (q.e.).

$\lambda \mu\text{m}$	0.8	0.9	1.0	1.1	1.2	1.4	1.6	2.2
q.e.	0.53	0.55	0.54	0.54	0.54	0.57	0.62	0.61

<sup>2</sup> [http://www.stsci.edu/resources/software\\_hardware/stsdas/synphot](http://www.stsci.edu/resources/software_hardware/stsdas/synphot)

derived by us by applying the measured temperature dependence at the cut-on and cut-off wavelengths, with linear interpolation adopted for wavelengths between the two reference points. For the Z filter the measured temperature dependence was consistent with no change and the transmission profile measured at room temperature was used. At the other extreme, the K filter exhibits a shift of  $\approx 0.035 \mu\text{m}$ , or  $\sim 10$  per cent of the bandwidth, and the use of the temperature-corrected profiles is important when calculating passbands.

The transmission measurements were undertaken from  $0.4 \mu\text{m}$  out to beyond  $3.0 \mu\text{m}$ , where the WFCAM detectors possess no sensitivity. With the exception of an insignificant narrow ‘blue leak’ of height 1 per cent at  $\approx 0.792 \mu\text{m}$  for the Y filter, no leaks above the 0.1 per cent specification requirement were present in any of the filter transmission curves.

The transmission curves presented here are derived from a single filter in each band – four filters per band are necessary to cover the detector arrays in WFCAM – but intercomparison of the four transmission curves in each band shows that the variations between filters produce differences in the photometry of at most 0.01 mag.

#### 4.4 Summary: WFCAM system throughput curves

Fig. 1 shows the *ZYJHK* passband transmission curves for (i) no atmosphere, (ii) typical atmospheric conditions, airmass 1.3 and 1.0 mm of precipitable water vapour, and (iii) extreme atmospheric conditions, airmass 2.0 and 5.0 mm of precipitable water vapour.

The MKO *JHK* filter transmissions were developed with the aim of minimizing the effects of variable atmospheric transmission due primarily to the change in the water content of the atmosphere. The same philosophy was adopted in the design of the new Z and Y filters. The result is a reassuring stability of the UKIDSS *ZYJHK* system over a wide range of atmospheric conditions. There are essentially no differences in the photometry at the  $>0.01$  mag level for objects with non-pathological SEDs for observations made through precipitable water-vapour columns of  $\leq 3.0$  mm and at airmasses in the range 1.0–1.6.

The insensitivity of the WFCAM *ZYJHK* system to atmospheric properties is evident from consideration of observations of the full range of stellar types included in the Bruzual–Persson–Gunn–

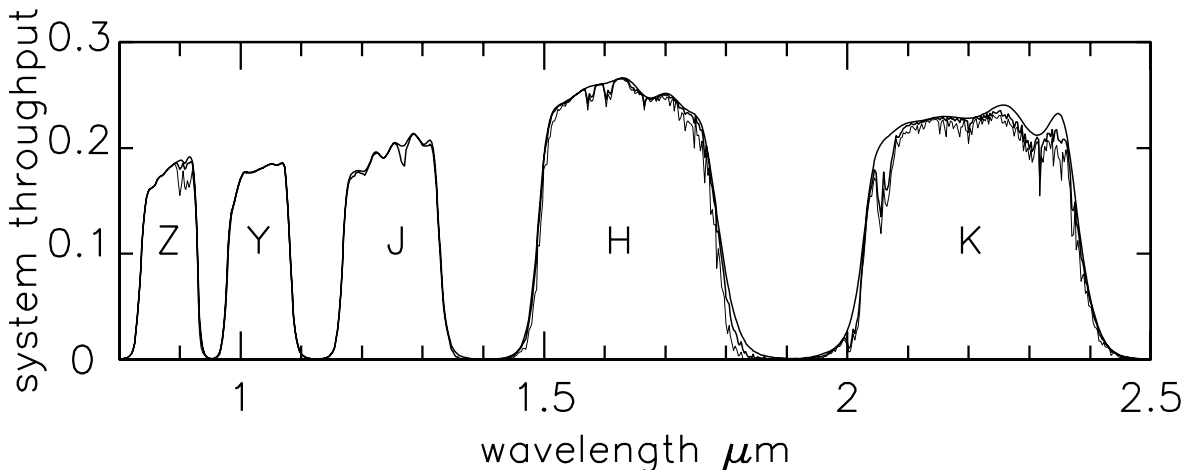
Stryker (BPGS) atlas (Section 5.1.1). Even for observations made at an airmass of 2.0 through an extreme atmospheric model for Mauna Kea that includes 5.0 mm of water vapour (Fig. 1), only in the Z band, for a narrow range of stellar type (M6–M8), are differences in the photometry that exceed  $>0.01$  mag level evident. The differences in the Z band, compared to observations made in excellent conditions, amount to no more than 0.015 mag for the narrow range of late-M spectral types. Similarly, for the adopted quasar SED (Section 5.4), observations made through the extrema of the atmospheric models differ by less than 0.02 mag for redshifts  $z < 6.2$ . Only at redshifts ( $z \sim 6.5$ ) where the very strong spectral discontinuity at  $\text{Ly}\alpha$  1216 Å coincides with the atmospheric absorption at 9000–9200 Å in the Z band does the photometry differ by more than 0.1 mag, reaching a maximum of 0.2 mag.

Synthetic photometry for such truly unusual SEDs observed through the most extreme atmospheric models can be obtained using the appropriate transmission curves. However, for the calculations presented in this paper we have adopted the passband transmission curves based on observations at an airmass of 1.3 through an atmosphere with 1.0 mm of precipitable water vapour, typical of the conditions under which the majority of UKIDSS data are likely to be obtained. These default *ZYJHK* passband transmissions are provided in Tables 2–6 (in the electronic version of the paper only), each of which lists in column 1 the wavelength in  $\mu\text{m}$  and in column 2 the fractional throughput.

#### 4.5 SDSS and 2MASS passbands

The SDSS passbands are based on data obtained by J. Gunn to calculate the ‘2001 June’ version of the SDSS passbands, which were kindly supplied by X. Fan. The passbands are identical to those provided online with the recent SDSS Data Release 4 (SDSS DR4). The passbands are appropriate for the observation of point sources from Apache Point Observatory at an airmass of 1.3.

The 2MASS passbands were derived by taking the relative spectral response curves given by Cohen et al. (2003), dividing by wavelength and renormalizing to produce a transmission function,  $P(\lambda)$ , as employed in equation (1).



**Figure 1.** Transmission curves, from above atmosphere to detector, for the WFCAM filter set. Three curves are shown for each band. The upper, thick curve is for no atmospheric absorption. The middle, thick curve is for the default atmospheric conditions (1.3 airmass, 1.0 mm water), and the lower, thin curve is for extreme atmospheric conditions (2.0 airmass, 5.0 mm water). These curves have been computed on the basis of measurement or modelling of the relevant wavelength-dependent quantities. An overall wavelength-independent normalization has been applied to match the photon count rate measured for standard stars with the instrument. The calculation is preliminary and the wavelength-independent normalization is subject to revision.

**Table 7.** Conversion to AB magnitude.

Band	$\lambda_{\text{eff}}$ ( $\mu\text{m}$ )	$S$ (Jy)	Flux density ( $\text{W m}^{-2} \mu\text{m}^{-1}$ )	AB offset
<i>u</i>	0.3546	1545	$3.66 \times 10^{-8}$	0.927
<i>g</i>	0.4670	3991	$5.41 \times 10^{-8}$	−0.103
<i>r</i>	0.6156	3174	$2.50 \times 10^{-8}$	0.146
<i>i</i>	0.7471	2593	$1.39 \times 10^{-8}$	0.366
<i>z</i>	0.8918	2222	$8.32 \times 10^{-9}$	0.533
<i>Z</i>	0.8817	2232	$8.59 \times 10^{-9}$	0.528
<i>Y</i>	1.0305	2026	$5.71 \times 10^{-9}$	0.634
<i>J</i>	1.2483	1530	$2.94 \times 10^{-9}$	0.938
<i>H</i>	1.6313	1019	$1.14 \times 10^{-9}$	1.379
<i>K</i>	2.2010	631	$3.89 \times 10^{-10}$	1.900

#### 4.6 AB system offsets

In Table 7, we list the filters and provide in column 2 the computed effective wavelength, defined according to Schneider, Gunn & Hoessel (1983) (see equation 3 in Fukugita et al. 1996). Columns 3 and 4 list the flux density of an object spectrum, of constant flux density in both Jy and  $\text{W m}^{-2} \mu\text{m}^{-1}$ , over each passband, that corresponds to zero magnitude. The former quantity is quantified in another way in column 5, as the magnitude offset to convert the Vega-based magnitudes on to the AB-magnitude system (Oke & Gunn 1983), where we have used the definition  $\text{AB}_v = -2.5 \log f_v (\text{erg s}^{-1} \text{cm}^{-2} \text{Hz}^{-1}) + 48.60$ . The values for the *J*, *H* and *K* bands computed by Tokunaga & Vacca (2005), for the MKO system, are virtually identical. This is a coincidence, however, as they employed a slightly different SED for Vega, and a different zero-point of the AB system, these two differences closely cancelling each other.

### 5 SYNTHETIC COLOURS OF STARS, GALAXIES AND QUASARS

In this section, we use the apparatus described in Sections 3 and 4, to synthesize colours of a wide range of sources – stars, galaxies and quasars – to illustrate the colours of the types of objects expected to appear in the surveys. The following subsections detail the origins of the spectra, and tabulate the results for each class of object. Fig. 2 (for brown dwarfs, stars and quasars) and Fig. 3 (for galaxies) illustrate the *Z*, *Y*, *J*, *H* and *K*, colours which are discussed in the relevant subsections that follow. Because of the wide range of computed colours, in each of the two figures the left-hand set of panels and the right-hand set of panels show the same two-colour diagrams at different scales. As discussed in Section 4.4 all calculations presented employ the passband transmission functions appropriate to observations at airmass 1.3 through an atmosphere with 1.0 mm of precipitable water vapour.

The results shown here may be reproduced by taking the tabulated passband transmissions,  $P(\lambda)$  (Tables 2–6), and evaluating the quantity  $f_\lambda(P)$  defined in equation (1), for a particular object SED (provided in the form  $f_\lambda(\lambda)$ ). The zero-point is derived by performing the same calculation for the Vega spectrum from Bohlin & Gilliland (2004). Colours in the same system may be computed for any object of specified SED by following this procedure.

#### 5.1 Non-degenerate stars: the BPGS spectrophotometric atlas, and additional M dwarfs

##### 5.1.1 BPGS spectrophotometric atlas

The BPGS atlas is a data base of spectrophotometry of 175 stars, of a wide range of spectral type and luminosity class,

spanning the optical and near-infrared wavelength range. The atlas itself is unpublished, but is available at, for example, <http://www.stsci.edu/hst/observatory/cdbs/bpgs.html>. The optical spectra comprise the Gunn–Stryker atlas (Gunn & Stryker 1983). Most of the near-infrared data come from Strecker, Erickson & Witteborn (1979), while the remainder are unpublished. Stars 1–12, 70–77, 173 and 174 have been omitted from the calculations due to incomplete wavelength coverage. Stars 169 and 170 were also excluded because of an apparent mismatch between the amplitudes of the optical and near-infrared spectra.

The synthesized colours of the BPGS stars are provided in Table 8 (a sample is included in the printed version of the paper; the full table is published electronically only). The first 12 columns list colours from *u* to *K*, and columns 13–15 list successively the spectral classification, the BPGS reference number and the name of the star, taken from Gunn & Stryker (1983), if provided.

##### 5.1.2 Additional M dwarfs

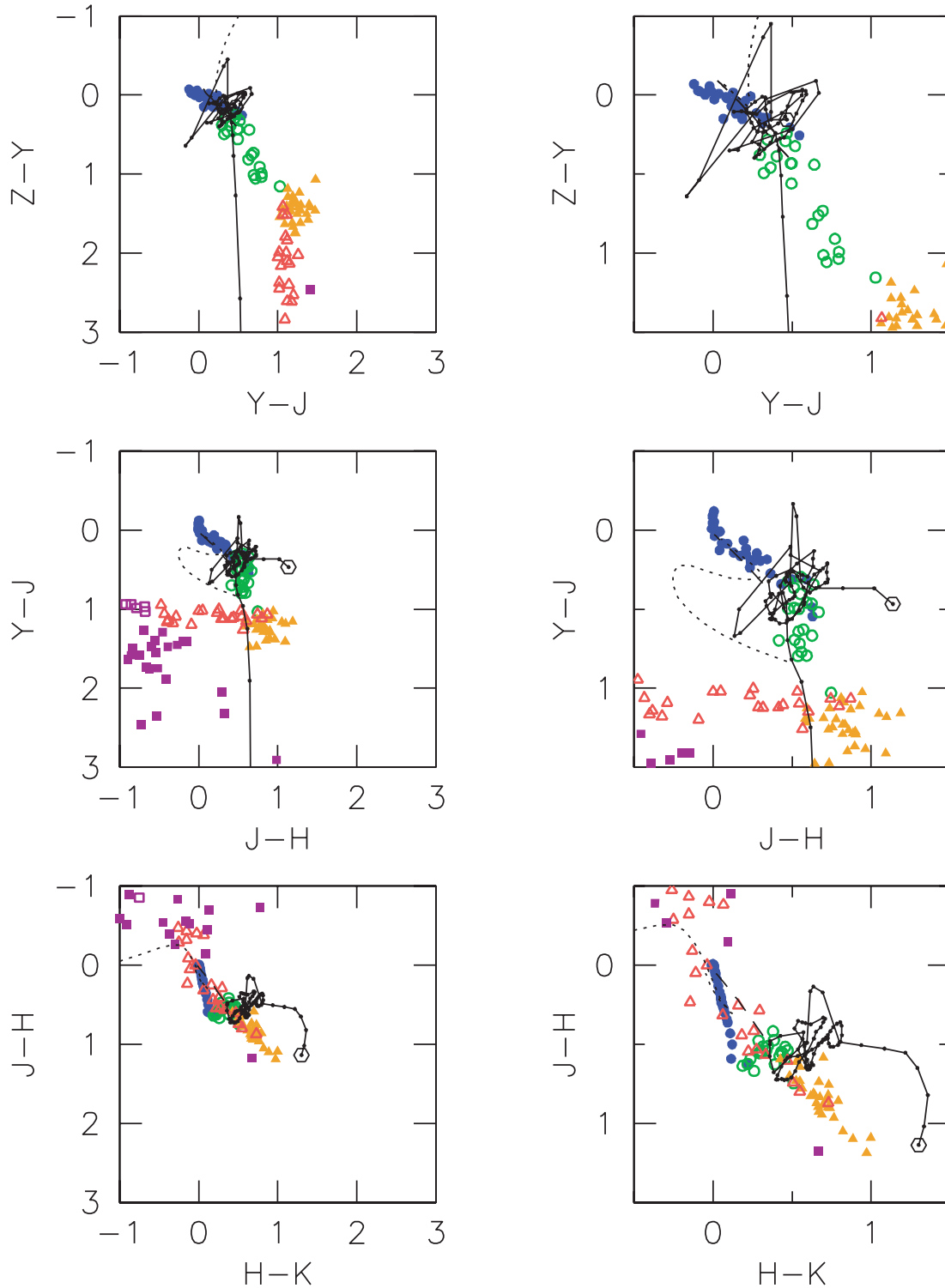
The BPGS atlas contains spectra of only six M dwarfs. Therefore, we have supplemented the list with spectra of 15 M dwarfs covering the wavelength range *i* to *K*, collated from the following references: Geballe et al. (2002), Hawley, Gizis & Reid (1996), Henry, Kirkpatrick & Simons (1994), Kirkpatrick, Henry & Simons (1995), Leggett et al. (2000a, 2001, 2002a), McLean et al. (2003) and Reid, Hawley & Gizis (1995). In Table 9, columns 1–9 provide colours over the range *i* to *K*, column 10 gives the *K*-band absolute magnitude,  $M_K$ , with the source of the parallax determination indicated, column 11 provides the spectral classification and column 12 the object name. In a few cases the spectrum does not cover the entire *i* band, and the *i* – *z* entry is consequently blank. The spectra were observed in a small number (e.g. three) of sections, each spectrophotometrically calibrated. To account for differential slit losses, the sections of spectra were calibrated absolutely using published photometry, in *J*, *H* and *K*, and frequently in a wide *Z* filter that covers the entire range of the WFCAM *Z* and *Y* filters. The result is that our synthesized colours to a large extent simply reproduce the published colours in the *J*, *H* and *K* bands, whereas colours that include the *i*, *Z* and *Y* bands involve a degree of interpolation or extrapolation, and therefore will be less accurate. The uncertainties in the spectral fluxes (at wavelengths within the WFCAM photometric passbands) are typically 3 per cent. Deviations between the measured *JHK* colours and the slopes of the spectra are 1–5 per cent. Hence, the errors in the predicted colours of the M dwarfs, and the L and T dwarfs discussed in Section 5.2.1, are expected to be 0.03–0.06 mag.

In Fig. 2, the colours of BPGS dwarfs covering the range of spectral types from O to K are plotted as blue filled circles. M dwarfs are plotted as green open circles, and extend the colour sequence displayed by the O to K dwarfs to redder colours.

#### 5.2 Degenerate stars: L and T dwarfs, model Y dwarfs and cool white dwarfs

##### 5.2.1 L and T dwarfs

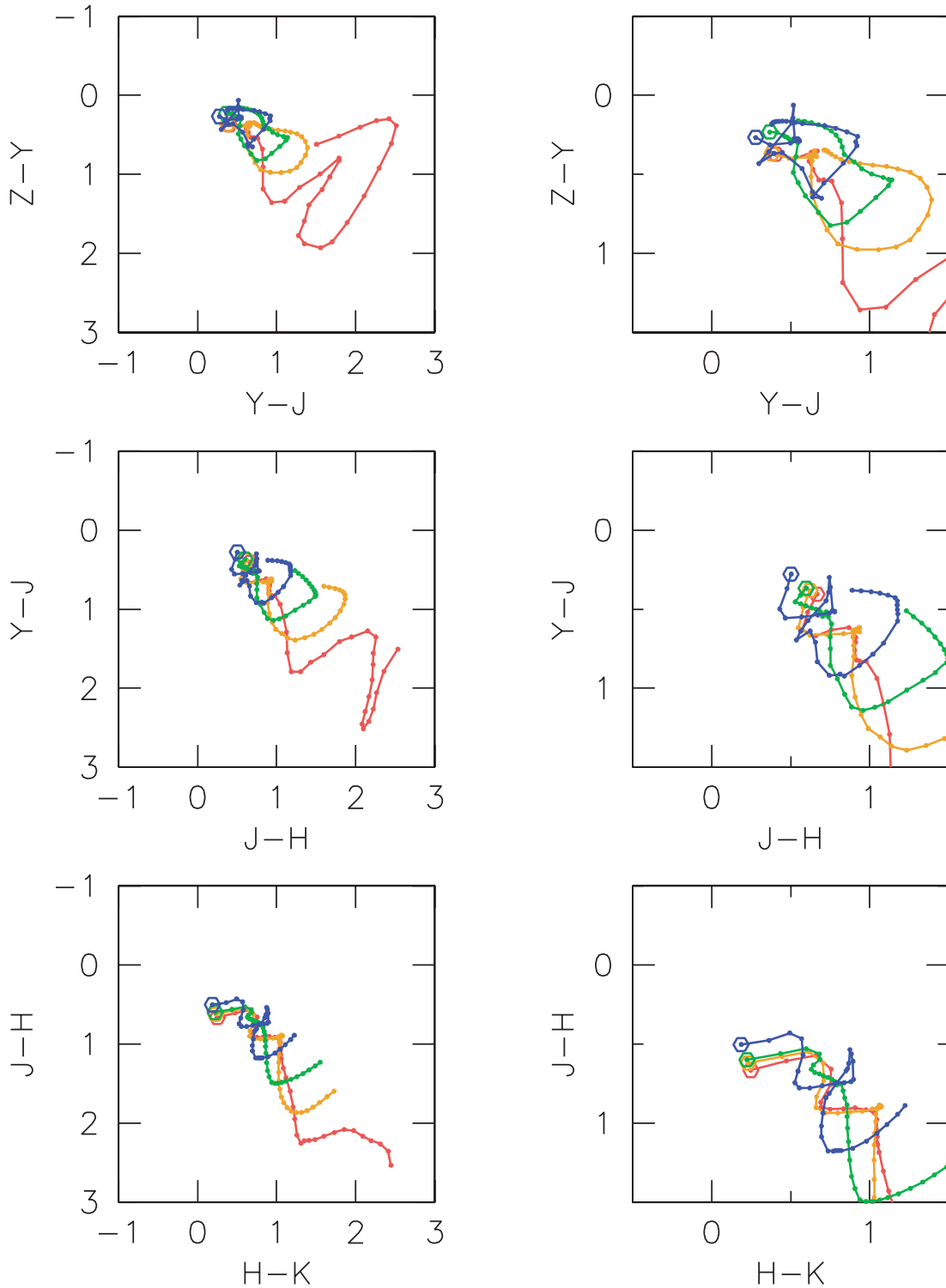
Colours of 30 L dwarfs and 22 T dwarfs have been computed from spectra covering the wavelength range *i* to *K*, collated from the following references: Burgasser et al. (2003), Chiu et al. (2006), Cruz et al. (2003), Fan et al. (2000a), Geballe et al. (1996, 2001, 2002), Kirkpatrick, Beichman & Skrutskie (1997), Kirkpatrick et al. (1999b, 2000), Knapp et al. (2004), Leggett et al. (2000b, 2001, 2002a,b), Liebert et al. (2000), McLean et al. (2003), Reid et al.



**Figure 2.** Top to bottom, three two-colour diagrams of stellar sources, cycling through the colour sequence  $Z - Y$ ,  $Y - J$ ,  $J - H$  and  $H - K$ . Each right-hand panel is a  $2 \times$  expanded view of part of the corresponding left-hand panel. Key: BPGS O–K dwarfs, blue filled circles; M dwarfs, green open circles; L dwarfs, orange filled triangles; T dwarfs, red open triangles; Burrows model cool brown dwarfs, purple filled squares; Marley model cool brown dwarfs, purple open squares; quasars  $0 < z < 8.5$ ,  $\Delta z = 0.1$ , solid black line,  $z = 0$  marked by open hexagon; H white dwarfs, dotted black line; He white dwarfs, dashed black line.

(2001), Schultz et al. (1998), Strauss et al. (1999), Tinney et al. (1998) and Tsvetanov et al. (2000). In Table 10, columns 1–9 provide colours over the range  $i$  to  $K$ , column 10 gives the  $K$ -band absolute magnitude,  $M_K$ , with the source of the parallax determination indicated, column 11 provides the spectral classification and

column 12 lists the object name. As with the M dwarfs, in a few cases the spectrum does not cover the entire  $i$  band, and the  $i - z$  entry is consequently blank. The accuracy of the synthetic colours that include the  $i$ ,  $Z$  and  $Y$  bands is subject to the same remarks made above in relation to the M dwarfs.



**Figure 3.** Top to bottom, three two-colour diagrams of HYPERZ galaxy templates, redshift range  $0 < z < 3.6$ ,  $\Delta z = 0.1$ , cycling through the colour sequence  $Z - Y$ ,  $Y - J$ ,  $J - H$  and  $H - K$ . Each right-hand panel is a  $2\times$  expanded view of part of the corresponding left-hand panel. Key: E red, Sbc orange, Scd green, Im blue. For all curves  $z = 0$  is marked by an open hexagon.

The colours of very cool stars, of spectral type M, L and T, across the WFCAM bands, deserve comment. In the  $J - H$  versus  $H - K$  two-colour diagram, Fig. 2, moving down the brown dwarf sequence, the early L stars first extend the O to M colour sequence to redder colours. Moving to cooler temperatures the colours reverse and track back up the colour sequence, becoming successively bluer,

until the coolest T dwarfs are bluer than O stars (due to the presence of strong absorption bands of water, methane and pressure-induced  $H_2$ ; see e.g. Burgasser et al. 2002; Geballe et al. 2002). The consequence is that over a broad temperature range, from mid-L to mid-T, the  $J - H$  versus  $H - K$  two-colour diagram is ineffective for distinguishing brown dwarfs from hydrogen burning stars.

**Table 8.** Colours of selected stars from the BPGS atlas.

$u - g$	$g - r$	$r - i$	$i - z$	$Z - z$	$Z - Y$	$Y - J$	$J - H$	$H - K$	$J - J2$	$H - H2$	$K - K2$	Class	BPGS no.	Name
-0.456	-0.066	-0.029	0.031	-0.012	-0.069	-0.120	0.006	-0.002	0.007	0.000	-0.001	B9V	13	HD189689
-0.043	-0.010	0.011	0.034	-0.010	-0.027	-0.094	0.000	-0.008	0.009	0.002	-0.002	A0V	14	THETA-VIR
-0.133	-0.019	0.027	0.040	-0.002	-0.023	-0.084	-0.003	-0.007	0.009	0.001	-0.002	B9V	15	NU-CAP
-0.012	-0.002	0.005	0.000	-0.008	-0.056	-0.021	0.003	-0.007	0.003	0.001	-0.002	A2V	16	HR6169
-0.068	-0.002	0.017	0.036	-0.002	-0.022	-0.010	-0.008	0.001	0.006	0.001	-0.002	A1V	17	HD190849A

Note: The full table is published in the electronic version of the paper. A portion is shown here for guidance regarding its form and content.

**Table 9.** Colours of selected additional M dwarfs. A machine-readable version of this table is available in the electronic version of the paper.

$i - z$	$Z - z$	$Z - Y$	$Y - J$	$J - H$	$H - K$	$J - J2$	$H - H2$	$K - K2$	$M_K$	Class	Name
0.576	0.021	0.323	0.519	0.668	0.260	-0.034	0.020	-0.008	5.3 <sup>a</sup>	M1	GI 229A
-	-0.014	0.292	0.458	0.593	0.237	-0.040	0.020	-0.038	8.2 <sup>b</sup>	M3	LHS 5327
0.973	0.032	0.432	0.498	0.543	0.303	-0.037	0.026	-0.019	7.8 <sup>b</sup>	M3.5	GJ 1001A
0.966	0.017	0.440	0.640	0.541	0.337	-0.053	0.026	-0.025	8.1 <sup>a</sup>	M3.5	GI 15B
1.147	0.023	0.432	0.492	0.514	0.316	-0.044	0.021	-0.052	8.2 <sup>a</sup>	M4	GI 699
0.957	0.055	0.559	0.496	0.476	0.288	-0.040	0.028	-0.029	6.9 <sup>b</sup>	M4.5	GI 630.1A
0.858	0.078	0.815	0.628	0.571	0.421	-0.040	0.027	-0.032	9.0 <sup>b</sup>	M5.5	GJ 1002
1.508	0.113	1.056	0.718	0.548	0.433	-0.049	0.034	-0.031	9.5 <sup>b</sup>	M5.5	GJ 4073
1.337	0.077	0.733	0.694	0.516	0.457	-0.048	0.031	-0.035	8.5 <sup>b</sup>	M5.5	GJ 1245A
1.170	0.060	0.761	0.667	0.627	0.391	-0.052	0.025	-0.024	8.4 <sup>b</sup>	M5.5	GI 905
1.550	0.089	0.909	0.771	0.559	0.439	-0.050	0.029	-0.024	9.1 <sup>b</sup>	M6	GI 406
-	0.037	1.012	0.698	0.417	0.380	-0.064	0.029	-0.053	8.7 <sup>b</sup>	M6	LHS 5328
1.720	0.120	1.036	0.794	0.593	0.455	-0.055	0.034	-0.025	9.7 <sup>b</sup>	M6.5	GJ 3855
1.559	0.092	0.992	0.796	0.538	0.472	-0.065	0.037	-0.026	9.7 <sup>b</sup>	M7	VB 8
2.299	0.157	1.154	1.028	0.747	0.511	-0.051	0.034	-0.016	-	M8.5	SDSS J225529.09-003433.4

<sup>a</sup>ESA (1997); <sup>b</sup>van Altena, Lee & Hoffleit (1995).

A two-colour diagram involving  $Z$ , such as  $Z - J$  versus  $J - H$ , separates the two populations. Nevertheless, very deep observations would be required in  $Z$  to detect the coolest T dwarfs, which have  $Z - J \sim 4$ . The  $Y$  band provides a compromise solution. In the  $Y - J$  versus  $J - H$  diagram, plotted in the middle panels in Fig. 2, it is seen that brown dwarfs have approximately constant  $Y - J \sim 1.2$ , redder than the M stars, while the  $J - H$  colour (or  $J - K$ ) separates the L dwarfs from the T dwarfs.

### 5.2.2 Model Y dwarfs

The current coolest known T dwarf is 2MASS J0415-0935 (Burgasser et al. 2002). The synthetic colours for this object are included in Table 10. The star has  $T_{\text{eff}} \sim 700$  K (Golimowski et al. 2004), and spectral type T9 (Knapp et al. 2004) in the Geballe et al. (2002) classification scheme, revised to T8 by Burgasser, Burrows & Kirkpatrick (2006). Cooler brown dwarfs no doubt exist, but will be difficult to find, because of their very low luminosities. One of the main goals of UKIDSS is to discover such stars. At some temperature a new spectral sequence is expected to appear, possibly associated with the emergence of  $\text{NH}_3$  in the spectrum, and the nomenclature Y dwarf has been suggested (Kirkpatrick et al. 1999a; Kirkpatrick 2000). In order to develop a strategy for finding brown dwarfs cooler than  $T_{\text{eff}} \sim 700$  K we have computed synthetic colours from the model spectra of Burrows, Sudarsky & Lunine (2003), which cover masses in the range  $1-10 M_{\text{Jup}}$ , and ages  $10^{8.0-9.7}$  yr. In Table 11, columns 1-9 provide predicted colours over the range  $i$  to  $K$ , column 10 the  $K$ -band absolute magnitude,  $M_K$ , and columns 11-14 list, respectively, the model mass, age,  $T_{\text{eff}}$  and surface gravity.

Table 12 lists colours computed from similar models by Marley et al. (2002; 2004, private communication). Columns 1-10 in Ta-

ble 12 contain the identical information to that for the models of Burrows et al. (2003) given in Table 11, while columns 11 and 12 specify the temperature and surface gravity for the models given by Marley et al. These models are for  $T_{\text{eff}}$  of 700 and 600 K, and surface gravities  $\log g$  of 4.48, 5.00 and 5.48  $\text{cm s}^{-2}$ , and so sample masses around 15, 30 and 60  $M_{\text{Jup}}$  aged 0.4-0.6, 3.0-4.6 and  $\geq 13$  Gyr, respectively. Although the  $Y - J$  colours of the Marley models are bluer than the Burrows models, the general trends are similar - very late T and Y dwarfs will have  $Y - J$  redder than M dwarfs ( $Y - J > 0.8$ ) while  $J - H$  will be extremely blue ( $J - H < -0.2$ ).

The synthetic colours for the models of warmer temperature, which overlap in temperature with the coolest known T dwarfs, are in reasonable agreement with the measured colours of the T dwarfs (Fig. 2), giving some confidence in the synthetic colours of the cooler objects. The range of masses and ages considered give rise to a wide range of predicted colours. The models, however, all suggest that the coolest brown dwarfs continue getting bluer in the near-infrared with decreasing  $T_{\text{eff}}$  for  $T_{\text{eff}} > 400$  K. Burrows et al. (2003) describe the reddening at cooler temperatures to be due to the appearance of water clouds and, more importantly, the collapse of flux on the Wien tail.

Spectral changes occur at temperatures hotter than 400 K: the alkali lines are expected to disappear below 500 K, and at 600 K  $\text{NH}_3$  is expected to be detectable at the blue edge of the  $H$ - and  $K$ -band peaks (Burrows et al. 2003). The appearance of  $\text{NH}_3$  in the near-infrared may signal the next spectral type after T, i.e. Y, as discussed above. WFCAM will allow candidate very late T and Y dwarfs to be identified from their blue  $J - H$  colours; these objects will be followed up spectroscopically. The LAS should find several brown dwarfs later than T8 in the first 2 years of the survey. Adopting a detection limit of  $K = 18.4$ , the LAS should detect dwarfs as cool



**Table 10.** Colours of selected L and T dwarfs. A machine-readable version of this table is available in the electronic version of the paper.

$i - z$	$Z - z$	$Z - Y$	$Y - J$	$J - H$	$H - K$	$J - J2$	$H - H2$	$K - K2$	$M_K$	Class	Name
2.077	0.100	1.069	1.476	0.643	0.549	-0.085	0.041	-0.016	10.5 <sup>a</sup>	L1	2MASS J03454316+2540233
1.996	0.188	1.322	1.193	0.610	0.527	-0.073	0.045	0.007	10.0 <sup>a</sup>	L1	2MASS J07464256+2000321AB
2.165	0.232	1.419	1.412	1.092	0.997	-0.096	0.058	-0.020	-	L3	2MASS J00283943+1501418
-	0.251	1.460	1.289	0.819	0.729	-0.094	0.056	-0.024	-	L3	SDSS J111320.16+343057.9
2.064	0.187	1.385	1.397	0.850	0.718	-0.088	0.055	-0.020	11.3 <sup>a</sup>	L3	DENIS-P J1058.7-1548
2.137	0.248	1.503	1.366	0.896	0.665	-0.085	0.048	-0.011	11.5 <sup>b</sup>	L3	GD 165B
2.138	0.215	1.458	1.472	0.733	0.550	-0.100	0.055	-0.004	11.3 <sup>a</sup>	L4	2MASS J00361617+1821104
-	0.168	1.235	1.274	0.899	0.728	-0.102	0.057	-0.017	-	L4.5	SDSS J085116.20+181730.0
2.337	0.254	1.418	1.263	0.857	0.792	-0.093	0.056	-0.015	11.4 <sup>b</sup>	L4.5	LHS 102 B
2.139	0.231	1.392	1.291	0.902	0.738	-0.096	0.058	-0.017	-	L4.5	SDSS J083506.16+195304.4
2.719	0.214	1.359	1.230	0.821	0.643	-0.096	0.054	-0.013	11.8 <sup>c</sup>	L5	SDSS J053951.99-005902.0
2.789	0.196	1.443	1.062	0.810	0.636	-0.102	0.056	0.004	11.4 <sup>a</sup>	L5.5	DENIS-P J0205.4-1159AB
-	0.317	1.577	1.383	0.963	0.764	-0.101	0.056	-0.017	-	L5.5	SDSS J134203.11+134022.2
2.884	0.181	1.411	1.158	1.186	0.971	-0.105	0.057	-0.029	12.6 <sup>c</sup>	L5.5	SDSS J010752.33+004156.1
1.472	0.194	1.375	1.195	0.778	0.563	-0.111	0.052	-0.009	-	L5.5	SDSS J020608.97+223559.2
2.949	0.196	1.616	1.182	1.097	0.884	-0.094	0.056	-0.024	12.7 <sup>a,c</sup>	L6	2MASS J08251968+2115521
-	0.230	1.419	1.261	0.730	0.525	-0.107	0.052	-0.011	-	L6	SDSS J103321.92+400549.5
-	0.188	1.286	1.126	0.738	0.669	-0.105	0.062	-0.011	-	L6	SDSS J162255.27+115924.1
2.494	0.257	1.615	1.284	0.885	0.695	-0.103	0.057	-0.011	11.1 <sup>a</sup>	L6	DENIS-P J1228.2-1547AB
1.317	0.298	1.501	1.246	0.756	0.732	-0.086	0.048	-0.028	-	L6	SDSS J065405.63+652805.4
-	0.390	1.747	1.229	0.834	0.675	-0.107	0.054	-0.013	-	L6.5	SDSS J141659.78+500626.4
-	0.202	1.280	1.188	0.699	0.484	-0.100	0.053	-0.013	-	L6.5	SDSS J142227.25+221557.1
3.105	0.168	1.461	1.160	1.049	0.822	-0.108	0.056	-0.009	12.9 <sup>a</sup>	L7.5	2MASS J16322911+1904407
-	0.173	1.184	1.125	0.594	0.425	-0.113	0.058	-0.021	-	L7.5	SDSS J112118.57+433246.5
-	0.176	1.406	1.112	0.928	0.667	-0.112	0.057	0.004	12.3 <sup>c</sup>	L8	SDSS J003259.36+141036.6
-	0.247	1.631	1.089	0.827	0.618	-0.124	0.060	-0.004	-	L9	SDSS J100711.74+193056.2
3.089	0.198	1.470	1.133	0.870	0.653	-0.107	0.055	-0.013	-	L9	2MASS J09083803+5032088
3.201	0.197	1.542	1.025	0.942	0.688	-0.117	0.060	0.034	-	L9	2MASS J03105986+1648155
1.765	0.354	1.738	1.215	0.587	0.546	-0.112	0.052	-0.008	-	L9.5	SDSS J080531.80+481233.0
-	0.272	1.664	1.193	0.583	0.698	-0.143	0.050	-0.001	-	L9.5	SDSS J151114.66+060742.9
2.605	0.184	1.513	1.066	0.870	0.730	-0.135	0.062	-0.004	-	T0	SDSS J085834.64+325629.1
3.044	0.220	1.517	1.114	0.799	0.550	-0.125	0.058	-0.003	12.0 <sup>c</sup>	T0	SDSS J042348.57-041403.5
-	0.148	1.410	1.066	0.743	0.506	-0.140	0.058	0.001	-	T0	SDSS J120747.17+024424.8
1.527	0.422	2.133	1.148	0.604	0.472	-0.153	0.057	0.023	-	T1	SDSS J103931.35+325625.5
1.903	0.276	1.787	1.097	0.546	0.224	-0.147	0.059	0.045	-	T1.5	SDSS J090900.73+652527.2
3.684	0.310	2.020	1.257	0.567	0.332	-0.179	0.067	0.041	-	T2	SDSS J075840.33+324723.4
4.712	0.325	1.989	1.021	0.534	0.275	-0.168	0.063	0.054	13.1 <sup>c,d</sup>	T2	SDSS J125453.90-012247.4
1.550	0.223	1.835	1.121	0.414	0.258	-0.170	0.053	0.058	-	T2.5	SDSS J143945.86+304220.6
-	0.280	2.048	1.004	0.255	0.160	-0.151	0.056	0.064	-	T3	2MASS J12095613-1004008
-	0.313	2.100	1.119	0.287	0.295	-0.193	0.062	0.046	-	T3	SDSS J153417.05+161546.1
3.352	0.296	1.991	1.105	0.443	0.183	-0.187	0.057	0.056	12.8 <sup>c,d</sup>	T3	SDSS J102109.69-030420.1
-	0.390	2.157	1.044	0.234	-0.144	-0.179	0.045	0.076	-	T3	SDSS 120602.51+281328.7
1.976	0.509	2.608	1.122	0.317	0.062	-0.212	0.070	0.090	-	T3.5	SDSS J121440.94+631643.4
-	0.487	2.447	1.020	0.050	-0.108	-0.188	0.049	0.107	-	T4	2MASS J22541892+3123498
4.590	0.491	2.526	1.198	-0.090	-0.131	-0.211	0.046	0.119	13.7 <sup>a,c,d</sup>	T4.5	2MASS J05591914-1404488
3.357	0.423	2.372	1.021	0.001	-0.038	-0.203	0.048	0.104	-	T4.5	SDSS J092615.38+584720.9
-	0.612	2.836	1.091	-0.288	-0.251	-0.222	0.041	0.110	-	T4.5	SDSS J135852.68+374711.9
4.009	0.477	2.614	1.178	-0.321	-0.152	-0.258	0.038	0.131	15.4 <sup>a,c,d</sup>	T6	SDSS J162414.37+002915.6
4.120	0.307	2.397	1.141	-0.382	0.066	-0.262	0.036	0.138	15.1 <sup>c,d</sup>	T6.5	SDSS J134646.45-003150.4
4.291	0.567	3.006	1.164	-0.399	-0.023	-0.254	0.016	0.103	15.6 <sup>e</sup>	T7	GI 229B
4.545	0.618	3.083	0.946	-0.474	-0.259	-0.284	0.031	0.155	16.7 <sup>e</sup>	T7.5	GI 570D
4.261	0.582	3.093	1.061	-0.433	-0.152	-0.296	0.034	0.152	17.0 <sup>c</sup>	T8	2MASS J04151954-0935066

<sup>a</sup>Dahn et al. (2002); <sup>b</sup>van Altena et al. (1995); <sup>c</sup>Vrba et al. (2004); <sup>d</sup>Tinney, Burgasser & Kirkpatrick (2003); <sup>e</sup>ESA (1997).

as 450 K at 10 pc in all  $YJH$  bands (column 10 in Tables 11 and 12). This temperature limit translates to a lower-mass limit of  $10 M_{\text{Jup}}$  for an assumed age of 1–5 Gyr.

Should young, nearby, even cooler objects be detected in the  $Y$  and  $J$  bands, Fig. 4 shows that the model  $Y - J$  colours are approximately constant with temperature down to 400 K, then move rapidly redder. Stellar objects redder than  $Y - J = 2$  would be extremely cool, and very interesting objects indeed. Possible contaminants in-

clude carbon stars, distinguishable using other colours, and quasars of very high redshift,  $z > 7.8$ , which are expected to be extremely rare. Although model colours of elliptical galaxies become very red in  $Y - J$  at high redshift  $z > 2.8$  (see below), this is only true of an unevolving spectrum. For realistic formation of redshifts, such extreme colours would not be seen. For the model cool brown dwarfs, a similar trend with temperature is seen in the  $Z - J$  colour, but a selection limit  $Z - J > 5$  would be required, which would involve

**Table 11.** Colours of Burrows et al. (2003) model T and Y cool dwarfs. A machine-readable version of this table is available in the electronic version of the paper.

$i - z$	$Z - z$	$Z - Y$	$Y - J$	$J - H$	$H - K$	$J - J2$	$H - H2$	$K - K2$	$M_K$	Mass ( $M_{\text{Jup}}$ )	$\log t$ (yr)	$T_{\text{eff}}$ (K)	$\log g$ ( $\text{cm s}^{-2}$ )
4.215	2.247	5.829	2.464	-0.729	0.782	-0.277	0.070	0.100	23.3	1	8.0	290	3.23
8.595	4.556	8.391	4.345	1.175	0.667	-0.323	0.077	0.103	31.3	1	8.5	216	3.27
11.662	6.062	9.928	5.510	2.278	-3.478	-0.377	0.082	0.055	43.5	1	9.0	159	3.32
3.238	1.000	4.193	1.548	-1.018	0.194	-0.272	0.073	0.110	20.0	2	8.0	386	3.53
4.162	2.130	5.626	2.349	-0.529	-0.117	-0.293	0.074	0.105	24.4	2	8.5	283	3.57
8.348	4.314	8.043	4.105	1.325	-1.464	-0.347	0.080	0.109	33.8	2	9.0	208	3.60
12.773	5.796	9.630	6.817	3.962	-2.575	-0.345	0.072	-0.121	45.8	2	9.5	149	3.63
13.659	5.121	8.968	8.828	5.572	-2.164	-0.117	-0.088	-0.514	49.2	2	9.7	134	3.64
4.782	0.612	3.530	1.264	-0.696	0.129	-0.289	0.074	0.133	16.9	5	8.0	588	3.92
4.417	0.835	3.898	1.509	-1.134	-0.448	-0.290	0.078	0.116	19.7	5	8.5	426	3.96
3.338	1.510	4.767	1.879	-0.414	-1.031	-0.302	0.077	0.112	23.7	5	9.0	312	3.99
7.888	3.889	7.526	4.021	1.910	-1.984	-0.350	0.083	0.117	32.5	5	9.5	225	4.02
10.624	5.149	8.955	5.397	3.329	-1.306	-0.357	0.094	0.112	36.7	5	9.7	197	4.03
4.661	0.443	3.062	1.288	-0.454	0.114	-0.292	0.071	0.137	15.8	7	8.0	703	4.07
4.715	0.769	3.778	1.487	-0.833	-0.261	-0.291	0.080	0.125	18.2	7	8.5	507	4.12
2.923	0.888	3.860	1.468	-0.592	-0.998	-0.294	0.078	0.115	21.6	7	9.0	369	4.15
4.418	2.109	5.423	2.318	0.326	-2.213	-0.327	0.078	0.116	27.3	7	9.5	267	4.18
5.737	2.799	6.199	2.905	0.982	-3.279	-0.345	0.078	0.119	30.8	7	9.7	234	4.19
4.190	0.301	2.457	1.409	-0.147	0.092	-0.288	0.074	0.132	14.6	10	8.0	859	4.24
5.044	0.646	3.501	1.398	-0.553	-0.159	-0.292	0.077	0.134	16.8	10	8.5	620	4.29
4.491	0.787	3.733	1.638	-0.892	-0.877	-0.298	0.081	0.120	19.7	10	9.0	447	4.32
3.621	0.690	3.364	1.035	-1.054	-2.160	-0.318	0.076	0.118	24.1	10	9.5	325	4.35
3.848	1.730	4.914	2.042	0.297	-2.128	-0.326	0.078	0.120	26.1	10	9.7	284	4.36
4.924	0.703	3.555	1.546	-0.539	-0.446	-0.294	0.081	0.130	17.3	15	9.0	593	4.52
4.117	0.680	3.448	1.582	-0.854	-1.502	-0.307	0.081	0.122	21.0	15	9.5	414	4.56
2.807	0.802	3.568	1.409	-0.197	-1.903	-0.309	0.080	0.122	22.8	15	9.7	359	4.57
5.172	0.640	3.379	1.475	-0.390	-0.367	-0.293	0.076	0.132	16.3	20	9.0	686	4.66
4.465	0.709	3.493	1.732	-0.661	-1.190	-0.302	0.085	0.125	19.4	20	9.5	483	4.71
4.095	0.642	3.323	1.584	-0.752	-1.671	-0.310	0.083	0.124	21.0	20	9.7	421	4.72
5.107	0.516	3.015	1.452	-0.269	-0.295	-0.290	0.073	0.130	15.4	25	9.0	797	4.80
4.762	0.733	3.517	1.747	-0.517	-0.915	-0.298	0.085	0.126	18.2	25	9.5	555	4.83
4.578	0.698	3.429	1.752	-0.624	-1.344	-0.304	0.086	0.125	19.6	25	9.7	483	4.85

**Table 12.** Colours of Marley et al. (private communication) model cool dwarfs. A machine-readable version of this table is available in the electronic version of the paper.

$i - z$	$Z - z$	$Z - Y$	$Y - J$	$J - H$	$H - K$	$J - J2$	$H - H2$	$K - K2$	$M_K$	$T_{\text{eff}}$ (K)	$\log g$ ( $\text{cm s}^{-2}$ )
6.027	0.651	3.467	0.849	-1.093	-1.034	-0.294	0.072	0.135	18.2	600	4.48
5.848	0.694	3.359	0.937	-0.919	-1.779	-0.296	0.074	0.131	18.7	600	5.00
5.806	0.730	3.269	0.970	-0.680	-1.762	-0.294	0.073	0.125	18.7	600	5.48
5.908	0.560	3.237	0.942	-0.854	-0.749	-0.289	0.067	0.136	16.9	700	4.48
5.942	0.666	3.287	0.985	-0.786	-1.279	-0.291	0.070	0.129	17.3	700	5.00
5.976	0.779	3.341	1.031	-0.673	-1.402	-0.288	0.068	0.121	17.5	700	5.48

Note: the model spectra extend only to 2.4  $\mu\text{m}$  and the  $H - K$  and  $K - K2$  colours may be in error by up to 0.02 mag.

unreasonably long integrations in the Z band. Caution is required, however, as the model colours are subject to uncertainty, and other authors (Baraffe et al. 2003; Marley, private communication) find somewhat different trends.

### 5.2.3 Cool white dwarfs

Model spectra of white dwarfs have been provided by P. Bergeron (see e.g. Bergeron et al. 2005, and references therein, and the web page <http://www.astro.umontreal.ca/~bergeron/CoolingModels/>) and used to calculate colours over the range  $u$  to  $K$ . The models are for pure H and pure He atmospheres, with surface gravity

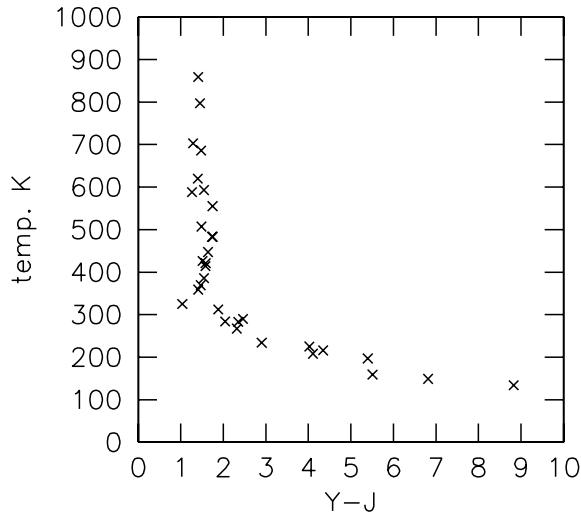
$\log g = 8$ . Tables 13 and 14 provide the colours in columns 1–12, column 13 provides the  $K$ -band absolute magnitude and column 14 the effective temperature. (Samples of the tables are included in the printed version of the paper; the full tables are published electronically only.)

Fig. 2 shows that while He-atmosphere white dwarfs are difficult to distinguish from main-sequence stars, hydrogen-rich white dwarfs become blue in  $J - H$  at  $T_{\text{eff}} < 5000\text{K}$ . This is due to the onset of pressure-induced molecular hydrogen absorption in these high-pressure atmospheres. White dwarfs can be used as chronometers, as their cooling after the planetary nebula stage is reasonably well understood. The age of the Galactic disc has been

**Table 13.** Colours of pure H atmosphere model white dwarf spectra of different effective temperature.

$u-g$	$g-r$	$r-i$	$i-z$	$Z-z$	$Z-Y$	$Y-J$	$J-H$	$H-K$	$J-J2$	$H-H2$	$K-K2$	$M_K$	$T_{\text{eff}}$ (K)
1.632	0.932	-2.161	-0.054	-0.147	-1.709	0.832	0.467	-2.569	-0.045	-0.139	-0.036	23.937	1500
1.410	1.204	-1.555	-0.076	-0.124	-1.496	0.747	0.243	-1.871	-0.057	-0.107	-0.032	22.053	1750
1.238	1.334	-1.008	-0.106	-0.105	-1.313	0.668	0.072	-1.341	-0.058	-0.083	-0.033	20.559	2000
1.091	1.391	-0.517	-0.128	-0.091	-1.152	0.587	-0.061	-0.963	-0.054	-0.066	-0.034	19.380	2250
0.962	1.401	-0.092	-0.113	-0.078	-0.998	0.507	-0.154	-0.681	-0.046	-0.051	-0.031	18.390	2500

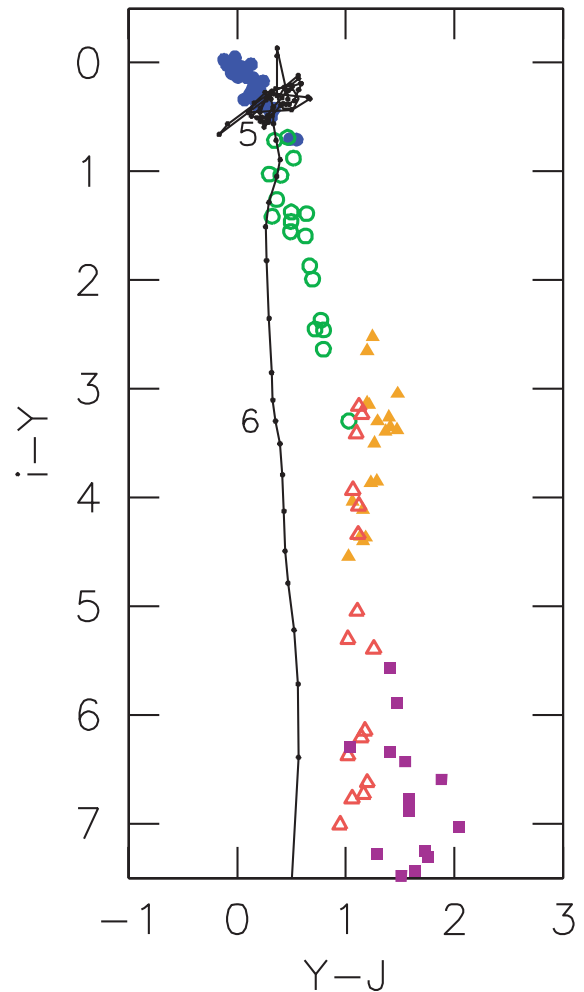
Note: The full table is published in the electronic version of the paper. A portion is shown here for guidance regarding its form and content.

**Figure 4.** Temperature–colour relation of model cool brown dwarfs.

constrained by the coolest disc white dwarfs (Liebert, Dahn & Monet 1988; Oswalt et al. 1996), and if halo white dwarfs can be identified, the age of the halo could also be constrained. This is especially true of the H-rich white dwarfs, as He atmospheres are less opaque and allow the white dwarf to cool rapidly – a He-rich dwarf will be a Gyr or more younger than a H-rich dwarf with the same temperature (e.g. Bergeron, Leggett & Ruiz 2001). Fig. 9 of Bergeron et al. (2005) shows that most white dwarfs known have  $T_{\text{eff}} > 4000$  K and, based on tangential velocity and temperature, are most likely to be (thick) disc dwarfs younger than  $10^{10}$  yr. The LAS will be able to detect 4000-K H-rich white dwarfs out to around 60 pc, and 3000-K H-rich white dwarfs to 20 pc. While these objects are very rare, they occupy a unique region of the  $J-H$  versus  $Y-J$  diagram and will be easy to identify and important to follow up.

### 5.3 Galaxies: HYPERZ templates and the Kinney–Mannucci spectra

We have computed synthetic colours of galaxies over the redshift range  $0 < z < 3.6$ , with a step size  $\Delta z = 0.1$ , by redshifting unevolving locally measured template spectra of different galaxy types. Predictions for the  $u$  and  $g$  colours at high redshift require the adoption of a model for the effects of intervening absorption. While such a model is employed to make predictions for the quasar SEDs (Section 5.4), galaxy colours at high redshift based on unevolved ultraviolet galaxy SEDs are of limited utility and the  $u$ - and  $g$ -band simulations are confined to redshifts  $z \leq 1.7$  and  $\leq 2.5$ , respectively. We have used two published sets of templates, as detailed below, and a summary of the tabular information available in machine-readable form is given in Table 15.

**Figure 5.** Two-colour diagram illustrating colours of stars, brown dwarfs and quasars. Key: BPGS O–K dwarfs, blue filled circles; M dwarfs, green open circles; L dwarfs, orange filled triangles; T dwarfs, red open triangles; Burrows model cool brown dwarfs, purple filled squares; quasars  $0 < z < 8.5$ ,  $\Delta z = 0.1$ , solid black line, with redshifts 5 and 6 marked. In this plot, quasars  $6 < z < 7.2$  are identifiable as bluer than L and T dwarfs in the  $Y-J$  colour. Note that the Marley model cool brown dwarfs all have  $i-Y > 7.5$  and so lie off the plot.

#### 5.3.1 HYPERZ templates

The first set of templates are the extended Coleman, Wu & Weedman (1980) spectra that are supplied with and used by the HYPERZ photometric redshift code (Bolzonella, Miralles & Pelló 2000). The original spectra given by Coleman et al. (1980) cover the wavelength range  $1400 < \lambda < 10000$  Å, and were extended by

**Table 14.** Colours of pure He atmosphere model white dwarf spectra of different effective temperature.

$u - g$	$g - r$	$r - i$	$i - z$	$Z - z$	$Z - Y$	$Y - J$	$J - H$	$H - K$	$J - J2$	$H - H2$	$K - K2$	$M_K$	$T_{\text{eff}}$ (K)
1.994	2.123	1.111	0.691	0.028	0.394	0.476	0.444	0.316	-0.029	0.013	-0.016	13.858	3500
1.723	1.915	0.975	0.591	0.022	0.326	0.415	0.388	0.276	-0.026	0.011	-0.014	13.710	3750
1.464	1.715	0.851	0.504	0.017	0.268	0.363	0.341	0.243	-0.024	0.010	-0.013	13.583	4000
1.211	1.526	0.741	0.430	0.013	0.219	0.320	0.301	0.216	-0.021	0.009	-0.011	13.471	4250
0.960	1.346	0.645	0.368	0.009	0.178	0.284	0.269	0.192	-0.020	0.008	-0.010	13.373	4500

Note: The full table is published in the electronic version of the paper. A portion is shown here for guidance regarding its form and content.

**Table 15.** List of tables containing predicted galaxy and quasar colours.

Table no.	Description
Table 16	Colours of redshifted HYPERZ E galaxy
Table 17	Colours of redshifted HYPERZ Sbc galaxy
Table 18	Colours of redshifted HYPERZ Scd galaxy
Table 19	Colours of redshifted HYPERZ Im galaxy
Table 20	Colours of redshifted Kinney–Mannucci E galaxy
Table 21	Colours of redshifted Kinney–Mannucci S0 galaxy
Table 22	Colours of redshifted Kinney–Mannucci Sa galaxy
Table 23	Colours of redshifted Kinney–Mannucci Sb galaxy
Table 24	Colours of redshifted Kinney–Mannucci Sc galaxy
Table 25	Colours of redshifted blue model quasar
Table 26	Colours of redshifted average model quasar
Table 27	Colours of redshifted red model quasar

Bolzonella et al. (2000) to both shorter and longer wavelengths using synthetic spectra created with the GISSSEL98 code (Bruzual & Charlot 1993). The synthetic colours for, respectively, the template E, Sbc, Scd and Im spectra are provided in Tables 16–19 (in the electronic version of the paper only). In each table, column 1 lists the redshift and columns 2–12 list colours in the  $u$  to  $K$  bands. Blank entries correspond to redshift ranges where colours would be affected by intergalactic absorption. Table 15 summarizes the contents of the tables containing the predicted colours for the various galaxy and quasar template spectra.

The redshift tracks of the  $ZYJHK$  colours of the four spectra are plotted in Fig. 3. The effect of redshift is, as a rule, to shift the spectra redward of the locus of stars, i.e. towards the bottom right-hand side in each plot. We chose to redshift unevolving templates as this gives an idea of the envelope within which galaxy colours lie at any redshift. But the use of an old stellar population (the E spectrum) to define the red boundary of the colour distribution becomes unrealistic by redshift  $z = 2$ . Therefore objects discovered in the region of colour space traced by the E spectrum at high redshift are more likely to be dusty galaxies, not represented by the templates used here.

### 5.3.2 Kinney–Mannucci spectra

The second set of templates are the spectra created by Mannucci et al. (2001), by combining their near-infrared averaged spectra with the ultraviolet–optical template spectra of Kinney et al. (1996). The synthetic colours for, respectively, the template E, S0, Sa, Sb and Sc spectra are provided in Tables 20–24 (in the electronic version of the paper only). In each table, column 1 lists the redshift and columns 2–12 list colours in the  $u$  to  $K$  bands. Blank entries correspond to redshift ranges where colours would be affected by intergalactic ab-

sorption or where the template SEDs provide incomplete coverage. The latter restriction is confined to colours involving  $K$  at  $z = 0$  as the spectra of Mannucci et al. (2001) reach only 2.4  $\mu\text{m}$ , where the WFCAM  $K$  filter still has significant transmission.

The redshift tracks of the Kinney–Mannucci spectra mostly follow closely the HYPERZ tracks for similar spectral classes.

### 5.4 Quasars in the redshift range $0 < z < 8.5$

Given the extended wavelength range covered by the passbands ( $u$  through  $K$ ) and the large redshift range of interest for the quasars,  $0 < z < 8.5$ , a quasar SED covering the rest-frame wavelength range  $500 < \lambda < 25\,000 \text{ \AA}$  is required. High signal-to-noise ratio composite spectra from large quasar surveys (Francis et al. 1991; Brotherton et al. 2001; Vanden Berk et al. 2001) provide information for the wavelength range  $1000 \lesssim \lambda \lesssim 7000 \text{ \AA}$  but additional constraints are needed to model the full wavelength range. The relatively simple model SED employed here has been constructed using the emission-line properties of the Large Bright Quasar Survey (LBQS) composite spectrum (Francis et al. 1991) combined with a parametric continuum model. A more complete description of the quasar model SED and the data used to determine the parameters is given in Maddox & Hewett (2006) but an outline is given here.

The quasar SED model parameters were defined by requiring the model to reproduce the median colours in  $ugrizJ2H2K2$  of a sample of 2708 quasars, magnitudes  $i < 17.4$  and redshifts  $0.1 \leq z \leq 3.6$ , with unresolved morphologies, from the SDSS DR3 quasar catalogue (Schneider et al. 2005), 90 per cent of which possess 2MASS  $JHK$  detections. The ‘continuum’ is represented by a power law in frequency,  $F(\nu) \propto \nu^\alpha$  with  $\alpha = -0.3$  for  $\lambda < 12\,000 \text{ \AA}$  and  $\alpha = -2.4$  for  $\lambda \geq 12\,000 \text{ \AA}$ . A modest contribution from Balmer continuum radiation is included to model the excess flux needed at  $\sim 3000 \text{ \AA}$ . Emission-line contributions from the LBQS composite spectrum (Francis et al. 1991) over the wavelength range  $1000\text{--}6000 \text{ \AA}$  are included, along with  $H\alpha$  from an extended version of the LBQS composite, and the addition of a Paschen  $\alpha$  line. The  $H\alpha$  strength in the composite is derived from low-luminosity objects and it is necessary to incorporate a reduction in the equivalent width of  $H\alpha$  as a function of luminosity, i.e. a Baldwin effect (Baldwin 1977), with a dependence  $EW(H\alpha) \propto L_{\text{QSO}}^{-0.2}$ , to reproduce the behaviour of the median  $JHK$  colours as  $H\alpha$  passes through the near-infrared passbands over the redshift range  $1 \lesssim z \lesssim 3$  (where QSO means quasi-stellar object).

Given the primary redshift range of interest for the UKIDSS survey is at  $z > 6$ , the effects of intergalactic absorption are incorporated by including the absorption from an infinite optical-depth Lyman-limit system at  $912 \text{ \AA}$  in the quasar rest frame, i.e. there is no flux below  $912 \text{ \AA}$  in the quasar rest frame. Absorption due to  $\text{Ly}\alpha$ ,  $\text{Ly}\beta$  and  $\text{Ly}\gamma$  transitions in the  $\text{Ly}\alpha$  forest is included using data from Songaila (2004), which extend to a redshift of  $z = 6.5$ . At

redshift  $z = 6.5$  there is almost no flux shortward of 1216 Å, and rather than attempting an unconstrained extrapolation of the absorption behaviour to higher redshifts the absorption applicable at  $z = 6.5$  has been applied at all redshifts  $z > 6.5$ . In practice, the adoption of the  $z = 6.5$  absorption for higher redshifts means that colours involving  $Z$  and  $Y$  (e.g.  $Y - J$ ) will represent blue limits. However, the amplitude of the discontinuity at 1216 Å is such that such colours are already extremely red (reaching 8 mag) and additional absorption will simply increase the amplitude of the continuum breaks relevant to the detection of quasars at  $z > 6.5$ . Those interested in the  $u$ -band colours of quasars at redshifts  $1.8 < z < 3.5$  will likely wish to apply a more sophisticated Monte Carlo approach to simulating the effects of different sightlines through the intergalactic medium. A somewhat steeper power-law index below the Ly $\alpha$  line would also provide an improved fit to the median  $u$ -band colours.

The simple model quasar SED provides an exceptionally good fit to the median colours, *grizJ2H2K2*, over the full redshift range  $0.1 \leq z \leq 3.6$  and colours involving the  $u$  band to  $z \sim 2$ . To provide an indication of the effects of changing the overall shape of the quasar SED on the UKIDSS colours, ‘blue’ and ‘red’ quasar SEDs have been generated by modifying the power-law slope at  $\lambda < 12000$  Å to  $\alpha = 0.0$  and  $-0.6$ , respectively.

The model colours of the blue, average and red model quasar spectra, respectively, are provided in Tables 25, 26 and 27 (in the electronic version of the paper only), and cover the redshift range  $0 < z < 8.5$ , with redshift interval  $\Delta z = 0.1$ . In each table, column 1 lists the redshift, and columns 2–13 provide colours over the range  $u$  to  $K$ .

The discovery of quasars of very high redshift  $z > 6$  is another of the key goals of UKIDSS (Warren & Hewett 2002). The general principle used to find high-redshift quasars  $3 < z < 6.4$  with broad-band photometry (e.g. Warren, Hewett & Osmer 1991; Fan et al. 2000b) is to image in three bands, one ( $a$ ) blueward of redshifted Ly $\alpha$ , a second ( $b$ ) containing or just redward of Ly $\alpha$  and a third ( $c$ ) further to the red. The quasars are then red in  $a - b$ , and bluer in  $b - c$  than any stars, or brown dwarfs, that are similarly red in  $a - b$ . The most distant quasar found in the SDSS has  $z = 6.40$  (Fan et al. 2003; Iwamuro et al. 2004). At higher redshifts Ly $\alpha$  moves out of the  $z$  band, and a longer-wavelength middle filter is needed.

Unfortunately, in the standard near-infrared bands  $JHK$  quasars are redder than most stars (Warren, Hewett & Foltz 2000), and have similar colours to M stars, late L dwarfs and early T dwarfs. This means that in a search for quasars of redshift  $z > 6.4$ , a colour from the  $JHK$  bands used as the red colour  $b - c$  is not effective. As shown in Fig. 5, the  $Y$  band appears to offer a solution. The colour of the average quasar spectrum lies at least 0.5 mag bluer than L and T dwarfs in  $Y - J$  until  $z \sim 7.2$ , so that combining UKIDSS data with sufficiently deep  $i$ -band data it may be possible to discover quasars at redshifts  $z > 6.4$ .

## 6 COLOUR EQUATIONS BETWEEN WFCAM, SDSS AND 2MASS

We have used synthetic colours to compute colour equations, relating photometry in the WFCAM bands and the native SDSS 2.5-m telescope  $z$  band and 2MASS  $J2$ ,  $H2$  and  $K2$  bands, i.e. those bands with similar effective wavelengths to WFCAM bands. We used the BPGS atlas, and the additional M stars (Section 5.1.2), but excluded L and T dwarfs which follow different, more complicated, relations. We computed fits for luminosity classes III and V separately. The two fits are mostly similar for any band, but noticeably different

in the  $K$  band. The following relations allow photometric transformations between the different systems. The rms scatter in these relations is 0.01 mag or less. We remind readers that all magnitudes here are Vega based, and that Table 7 provides offsets to the AB system.

$$Z = z - 0.01 + 0.051(i - z) \quad \text{[III]} \quad (2a)$$

$$Z = z - 0.01 + 0.068(i - z) \quad \text{[V]} \quad (2b)$$

$$z = Z + 0.02 - 0.103(Z - Y) \quad \text{[III]} \quad (2c)$$

$$z = Z + 0.01 - 0.103(Z - Y) \quad \text{[V]} \quad (2d)$$

$$J = J2 - 0.01 - 0.003(J2 - H2) \quad \text{[III]} \quad (3a)$$

$$J = J2 + 0.01 - 0.067(J2 - H2) \quad \text{[V]} \quad (3b)$$

$$J2 = J + 0.02 \quad \text{[III]} \quad (3c)$$

$$J2 = J - 0.01 + 0.073(J - H) \quad \text{[V]} \quad (3d)$$

$$H = H2 + 0.01 + 0.065(H2 - K2) \quad \text{[III]} \quad (4a)$$

$$H = H2 + 0.080(H2 - K2) \quad \text{[V]} \quad (4b)$$

$$H2 = H - 0.01 - 0.063(H - K) \quad \text{[III]} \quad (4c)$$

$$H2 = H - 0.069(H - K) \quad \text{[V]} \quad (4d)$$

$$K = K2 + 0.075(H2 - K2) \quad \text{[III]} \quad (5a)$$

$$K = K2 - 0.081(H2 - K2) \quad \text{[V]} \quad (5b)$$

$$K2 = K - 0.072(H - K) \quad \text{[III]} \quad (5c)$$

$$K2 = K + 0.073(H - K) \quad \text{[V]} \quad (5d)$$

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## SUPPLEMENTARY MATERIAL

The following supplementary material is available for this article online.

**Table 2.** System throughput curve for the WFCAM *Z* filter.

**Table 3.** System throughput curve for the WFCAM *Y* filter.

**Table 4.** System throughput curve for the WFCAM *J* filter.

**Table 5.** System throughput curve for the WFCAM *H* filter.

**Table 6.** System throughput curve for the WFCAM *K* filter.

**Table 8.** Colours of selected stars from the BPGS atlas.

**Table 9.** Colours of selected additional M dwarfs.

**Table 10.** Colours of selected L and T dwarfs.

**Table 11.** Colours of Burrows et al. (2003) model T and Y cool dwarfs.

**Table 12.** Colours of Marley et al. (private communication) model cool dwarfs.

**Table 13.** Colours of pure H atmosphere model white dwarf spectra of different effective temperature.

**Table 14.** Colours of pure He atmosphere model white dwarf spectra of different effective temperature.

**Table 16.** Colours of redshifted HYPERZ E galaxy.

**Table 17.** Colours of redshifted HYPERZ Sbc galaxy.

**Table 18.** Colours of redshifted HYPERZ Scd galaxy.

**Table 19.** Colours of redshifted HYPERZ Im galaxy.

**Table 20.** Colours of redshifted Kinney–Mannucci E galaxy.

**Table 21.** Colours of redshifted Kinney–Mannucci S0 galaxy.

**Table 22.** Colours of redshifted Kinney–Mannucci Sa galaxy.

**Table 23.** Colours of redshifted Kinney–Mannucci Sb galaxy.

**Table 24.** Colours of redshifted Kinney–Mannucci Sc galaxy.

**Table 25.** Colours of redshifted blue model quasar spectrum.

**Table 26.** Colours of redshifted average model quasar spectrum.

**Table 27.** Colours of redshifted red model quasar spectrum.

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