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## The velocity modulation of galaxy properties in and near clusters: quantifying the decrease in star formation in backsplash galaxies

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## ABSTRACT

Ongoing or recent star formation in galaxies is known to increase with increasing projected distance from the centre of a cluster out to several times its virial radius  $(R_y)$ . Using a complete sample ( $M_r \le -20.5, 0.02 \le z \le 0.15$ ) of galaxies in and around 268 clusters from the Sloan Digital Sky Survey's Fourth Data Release, we investigate how, at a given projected radius from the cluster centre, the stellar mass and star formation properties of a galaxy depend on its absolute line-of-sight velocity in the cluster rest frame,  $|v_{\rm LOS}|$ . We find that for projected radii  $R < 0.5 R_v$ , the fraction of high-mass non-brightest cluster galaxies increases towards the centre for low  $|v_{LOS}|$ , which may be the consequence of the faster orbital decay of massive galaxies by dynamical friction. At a given projected radius, the fraction of Galaxies with Ongoing or Recent (<1–3 Gyr) Efficient Star Formation [GORES; with EW(H $\delta$ ) > 2 Å &  $D_n 4000 > 1.5$ ] is slightly but significantly lower for low  $|v_{LOS}|$  galaxies than for their highvelocity counterparts. We study these observational trends with the help of a dark matter (DM) cosmological simulation. We classify DM particles as virial, infall and backsplash according to their present positions in  $(r, v_r)$  radial phase space and measure the frequencies of each class in cells of  $(R, |v_{LOS}|)$  projected phase space. As expected, the virial class dominates at projected radii  $R < R_{\rm y}$ , while the infall particles dominate outside, especially at high  $|v_{LOS}|$ . However, the backsplash particles account for at least one-third (half) of all particles at projected radii slightly greater than the virial radius and  $|v_{\rm LOS}| < \sigma_{\rm v} (|v_{\rm LOS}| \ll \sigma_{\rm v})$ . The deprojection of the GORES fraction leads to a saturated linear increase with radius. We fit simple models of the fraction of GORES as a function of class only or class and distance to the cluster centre (as in our deprojected fraction). While GORES account for  $18 \pm 1$  per cent of all galaxies within the virial cylinder, in our best-fitting model, they account for 13  $\pm$ 1 per cent of galaxies within the virial sphere,  $11 \pm 1$  per cent of the virial population,  $34 \pm 1$ 1 per cent of the distant (for projected radii  $R < 2R_v$ ) infall population and  $19 \pm 4$  per cent of the backsplash galaxies. Also,  $44 \pm 2$  per cent of the GORES within the virial cylinder are outside the virial sphere. These fractions are very robust to the precise good-fitting model and to our scheme for assigning simulation particle classes according to their positions in radial phase space (except for two of our models, where the fraction of GORES reaches 27  $\pm$ 4 per cent). Given the 1–3 Gyr lookback time of our GORES indicators, these results suggest that star formation in a galaxy is almost completely quenched in a single passage through the cluster.

**Key words:** galaxies: clusters: general – galaxies: evolution – galaxies: formation – galaxies: kinematics and dynamics – galaxies: starburst – galaxies: star formation.

### **1 INTRODUCTION**

The wide variety in star formation properties of galaxies is an inevitable consequence of the varied environments they inhabit. Physical properties of galaxies such as morphology (Dressler 1980), colour (e.g. Balogh et al. 2004b), luminosity (e.g. Adami, Biviano & Mazure 1998), individual spectral indices used as star formation rate (SFR) tracers, such as the equivalent width (EW) of [O II] or H $\alpha$  (e.g. Balogh et al. 2004a; Haines et al. 2006), are known to vary systematically with environment. As they leave their sparsely populated base in the *field* for the high-density regions of galaxy clusters, galaxies see their dominant stellar population become older, emission lines disappear from their spectra, complex spirals transform into more uniform spheroids and the SFR decrease by 1–2 orders of magnitude.

It is thus generally believed that the cluster environment is hostile to star formation. For example, the denser the environment, the stronger will be the stripping of interstellar gas either by the ram pressure of the intra-cluster gas (Gunn & Gott 1972) or by the tidal field of the cluster (Merritt 1983), leading to starvation for subsequent star formation (Larson, Tinsley & Caldwell 1980). So a galaxy that entered the cluster virial radius  $\sim$ 1 Gyr ago, and has since crossed the core of the cluster, should have lost its gas via either of these two effects during its passage through the cluster core (see e.g. Vollmer 2009 for the impact of ram-pressure stripping in the Virgo cluster). Moreover, in the intermediate-density environments on the cluster outskirts, mechanisms like galaxy-galaxy interactions (e.g. Moore et al. 1996) seem to dominate the process of galaxy evolution (e.g. Porter & Raychaudhury 2007; Porter et al. 2008; Mahajan, Raychaudhury & Pimbblet, in preparation). Thus, starforming infalling galaxies are expected to have distinctive properties compared to the passively evolving virialized population inside the cluster.

However, one can define an intermediate population of galaxies that have travelled through the cluster core (perhaps more than once) and have not yet had time to mix with the virialized population. These *backsplash*<sup>1</sup> galaxies would have felt the first effects of the cluster environment, but may not have evolved all the way to attain the passive properties of the virialized population. In their simulations of six clusters, Balogh, Navarro & Morris (2000) find that  $54 \pm 20$  per cent of dark matter (DM) particles at  $1-2R_{200}$  from the cluster centre have been inside the virial radius ( $R_{200}$ ) at some earlier time. Gill et al. (2005) estimate similar fractions, considering a virial radius equivalent to  $R_{100}$ , and further add that 90 per cent of such particles go as close to the cluster centre as 50 per cent of the virial radius. Mamon et al. (2004) used both analytical methods and cosmological simulations to conclude that DM particles travel through the core of the cluster out to  $1-2.5R_{100}$  on the other side.

The backsplash galaxies may contribute to the observation that the radial trends of star formation diagnostics extend to at least twice the virial radius (Balogh et al. 2000) from cluster centres. Hence, the intermediate environments found in inter-cluster filaments and on the outskirts of galaxy clusters play a key role in defining the evolutionary history of galaxies (Rines et al. 2003; Gill, Knebe & Gibson 2005; Porter & Raychaudhury 2007; Porter et al. 2008; Mahajan, Haines & Raychaudhury 2010; Mahajan et al., in preparation).

Most results indicate that the properties of galaxies evolve as they encounter denser environments, i.e. progress from the field towards the cluster. This could be due to the prevalence of smaller clusters (galaxy groups) as one approaches rich clusters, as the tidal field and possibly some mild form of ram-pressure stripping might play a similar role, as they do in more massive clusters, to deplete the gas reservoirs of galaxies. Alternatively, it is possible that the gas reserves of galaxies may be protected by the pressure of the surrounding intra-group medium (IGM) from being tidally perturbed, preventing the star formation in the galaxy from being quenched, even after spending >1 Gyr in crossing the cluster. In such a case, an increase in tides generated during the group–cluster merger may instead result in an enhancement of the SFR of group galaxies (Bekki 1999). Although such a group pre-processing scenario is yet to be confirmed, some evidence in its favour is found in recent observational studies (e.g. Oemler et al. 2009).

The main difference between the infalling and backsplash galaxies is that the former have larger apocentres, hence larger radial (3D) velocities. Hence, one expects that the backsplash galaxies will have lower absolute line-of-sight (hereafter LOS) velocities<sup>2</sup> than the infalling galaxies. One is therefore motivated to study the modulation of the radial trends of galaxy properties, with absolute LOS velocity.

In the central regions of clusters, the relative velocities of galaxies have been found to be correlated with their luminosity (e.g. Chincarini & Rood 1977; Struble 1979; Bothun & Schombert 1990; Biviano et al. 1992), morphology (de Vaucouleurs 1961; Sandage & Tammann 1976; Moss & Dickens 1977; Helou, Salpeter & Krumm 1979; Sodre et al. 1989; Biviano et al. 1992; Girardi et al. 2003, among others) and more recently spectral type (Biviano et al. 1997; Pimbblet et al. 2006). The early-type, massive and passive galaxies are found to have lower velocity dispersion relative to their latetype, star-forming counterparts. It has been shown that this velocity segregation of mass (or luminosity) in cluster galaxies is neither induced by morphological segregation nor limited to cD galaxies (Biviano et al. 1992).

There have been some efforts to study the velocity segregation in galaxy properties on the outskirts of galaxy clusters (e.g. Mohr et al. 1996; Rines et al. 2005; Pimbblet et al. 2006). In particular, Rines et al. (2005) found no significant difference in the velocity distribution of the emission-line and absorption-line galaxies with projected radii between 1 and  $2R_{200}$  in a sample of eight nearby X-ray bright clusters. However, emission-line galaxies outside the virial radius appear to have a significantly larger velocity dispersion than their absorption-line counterparts (but Rines et al. do not provide any quantitative estimate of the significance). Moreover, from fig. 6 of Rines et al., the mean velocity dispersion profile of emission-line galaxies appears significantly steeper than that of non-emissionline galaxies (this trend was not noted by the authors). Rines et al. concluded that star-forming galaxies in the infall regions are not field interlopers, which led them to reject a simple model where the truncation of star formation at low projected radius was solely caused by the efficient quenching of star formation in (backsplash) galaxies that have crossed through the cluster.

In this paper, using the very large Sloan Digital Sky Survey (SDSS), we have collected sufficient data around hundreds of clusters to analyse the differences in the distribution in *projected phase space* (projected radius *R* and absolute LOS velocity  $|v_{LOS}|$ ) of star-forming and passive galaxies at much finer resolution than previously performed. We look for and find a significant velocity modulation of the variations in stellar mass and star formation properties with projected radius. We also build simple dynamical models involving the virial, infalling and backsplash populations of galaxies to explain our results, calibrating our models and the projection effects using a cosmological simulation.

<sup>1</sup> The term *backsplash galaxies* was first coined by Gill, Knebe & Gibson (2005).

<sup>2</sup> Our absolute LOS velocities are in the cluster frame.

This paper is organized as follows. In the following section we describe the observational data set and briefly describe our star formation diagnostics. In Section 3 we present the analysis of the SDSS galaxies around clusters, focusing on the velocity modulation of radial trends in stellar mass and star formation efficiency. In Section 4 we model our results using a cosmological simulation described in Section 4.1 to classify particles into virial, infall and backsplash populations (Section 4.2). In Section 4.3, we fit simple models of the variation with physical radius of the fraction of *Galaxies with Ongoing or Recent Efficient Star formation* (hereafter GORES) for each of the three populations to the observed fraction of GORES as a function of the projected radius and LOS velocity. We discuss and summarize our results and their implications in Section 5. Throughout this paper we assume a concordance cosmology with  $\Omega_m = 0.3$ ,  $\Omega_A = 0.7$  and h = 0.7.

## 2 DATA

#### 2.1 The cluster catalogue

We selected our galaxy clusters from the 'group' catalogue compiled by Yang et al. (2007) from the Fourth Data Release (DR4) of the SDSS. Their iterative algorithm identifies first-order groups using a Friends-of-Friends (FoF) algorithm in redshift space, with a small linking length in projected space and a large one along the direction of the LOS. This algorithm thus selects potential groups at a high surface density threshold, so that groups embedded within the virial radii of more massive ones will be extracted as two (or more) separate entities. All galaxies left out by this grouping method are treated as additional potential groups (of single galaxies).

The raw luminosities and (luminosity-weighted) centres of the clusters are measured and then the luminosities (corrected for incompleteness), masses (assuming a given mass-to-light ratio) and velocity dispersions (from a mass/velocity dispersion relation) are derived. The radii  $R_{180}$ , i.e. of spheres that are 180 times denser than the critical density of the Universe, are derived from the masses. The distribution of galaxies around each group centre in projected phase space is examined to determine group membership, based upon the assumption of a projected Navarro, Frenk & White (1996, hereafter NFW) surface density profile and a Gaussian distribution of LOS velocities with dispersion independent of the projected radius. The algorithm is iterated with these new group assignments, where the mass-to-light ratio used for estimating the new mass is a function of luminosity derived from the previous iteration. The iteration continues until the membership converges. Yang et al. (2007) have tested their algorithm on mock galaxy catalogues constructed in real space and converted to redshift space.

In the present work, we define the galaxy clusters with the following criteria:

(i) redshift range:  $0.02 \le z \le 0.12$ ;

(ii) membership: at least 15 galaxies;

(iii) minimum halo mass (within  $R_{180}$ ):  $10^{14}$  M<sub> $\odot$ </sub>.

All of our chosen clusters have at least 12 galaxies ( $M_r \le -20.5$ ) with SDSS spectra within  $R_{180}$  of each cluster centre. For our chosen cosmology, the virial radius, within which the cluster may be thought to be in dynamical equilibrium, is commonly believed to be very close to  $R_{100}$  where the density is 100 times critical. In this paper, we adopt  $R_{100}$  for the virial radius, and more precisely

$$R_{\rm v} = 1.3 \, R_{180},\tag{1}$$

which, for NFW models with concentrations between 3 and 10, matches  $R_{100}$  to an accuracy of 2 per cent. This gives us a sample of 268 clusters in the SDSS DR4 footprint with median  $M_{180} \sim 10^{14.2} \,\mathrm{M_{\odot}}$ , corresponding to a median virial radius  $R_{100} = 1.5 \,\mathrm{Mpc}$  (using equation 1).

The range of 1.5 dex in cluster masses should not be a concern given that the properties of non-central (satellite) galaxies depend little on the mass of the group or cluster they live in (van den Bosch et al. 2008).

#### 2.2 Galaxy data

The observed photometric and spectroscopic data for galaxies in this work are taken from the SDSS DR4 (Adelman-McCarthy & the SDSS collaboration 2006). We use the galaxy magnitudes, k-corrections and the corresponding galactic extinction values in the SDSS g and r bands from the New York University Value Added Galaxy Catalogue (NYU-VAGC; Blanton et al. 2005). We k-correct these magnitudes to z = 0.1, which is the median red-shift of the sample. We select galaxies that meet the following criteria:

- (i) redshift range  $0.02 \le z \le 0.15$ ;
- (ii) absolute magnitude:  $M_{\rm r} \leq -20.5$ ;
- (iii) half-light angular radius:  $\theta_{\text{eff}} \leq 5$  arcsec;
- (iv) projected separation with cluster:  $R < 2R_v$ ;
- (v) velocity relative to cluster:  $|v_{\text{LOS}} v_{\text{LOS}}^{\text{cluster}}| \le 3 \sigma_v^{\text{cluster}}$ .

Our luminosity limit roughly corresponds to  $L \ge 0.5L^*$  (given that  $M_{r,*}^{0.1} = -20.44 + 5 \log h$ ; Blanton et al. 2003), which corresponds to the apparent magnitude limit ( $r \le 17.77$ ) for the SDSS spectroscopic catalogue at z = 0.1. Our galaxy redshifts are chosen in an interval that is slightly larger than for the clusters, so as to avoid missing galaxies lying behind (or in front) of the most (least) distant clusters. The angular size criterion ensures that the spectrum obtained from the 3 arcsec SDSS fibre is a fair representation of the light from the galaxy, and does not just correspond to the passive central bulge of the galaxy.

This gives us a sample of 19 904 galaxies in or near 268 clusters covered out to 2 virial radii in projection and three times the cluster velocity dispersions along the LOS.

The cluster galaxies are compared with a sample of 21 100 field galaxies, randomly chosen to have the same redshift and luminosity distributions as those of the cluster galaxies. We require the field galaxies to lie at least 10 Mpc away from the centres of all groups with  $N \ge 5$  and halo mass  $\ge 10^{12.5} \text{ M}_{\odot}$  in the Yang et al. (2007) catalogue (this includes clusters). Since the galaxy properties depend on their distance from the nearest large structure (e.g. Mahajan et al., in preparation) out to  $\sim 3R_{200}$  ( $\lesssim 6 h_{70}^{-1}$  Mpc; e.g. Rines et al. 2003; Mahajan et al., in preparation), a linear distance of 10 Mpc (corresponding to typically 6.7  $R_v$ ) from all groups and clusters ensures that our field sample is not contaminated by the effect of any groups or clusters.

## 2.3 Star formation diagnostics

In this paper, as our principal diagnostic, we use the specific star formation rate (SFR/ $M^*$  or SSFR) of a galaxy, as estimated from the optical spectrum, by Brinchmann et al. (2004) for all galaxies belonging to the spectroscopic catalogue of SDSS DR4. From this and a few other spectral indices, namely the emission-corrected H $\delta_A$  (hereafter H $\delta$ ) EW and the 4000 Å break, estimated in a related work (Kauffmann et al. 2003), we compare the trends seen in the of different types of galaxies. Brinchmann et al. have constructed a model grid of  ${\sim}2\,\times\,10^5$ spectral synthesis models (Bruzual & Charlot 1993; Charlot & Longhetti 2001) over four main parameters spanning a range of  $-1 < \log Z/Z_{\odot} < 0.6$  in metallicity (Z),  $-4.0 < \log U < -2.0$  in ionization parameter (U),  $0.01 < \tau_v < 4.0$  in total dust extinction  $(\tau_v)$  and  $0.1 < \xi < 0.5$  in dust-to-metal ratio ( $\xi$ ). Dust attenuation is also treated with a very sophisticated model of Charlot & Fall (2000), which provides a consistent model for ultraviolet (UV) to infrared (IR) emission. They then go on to derive the values for the SFR and SFR/ $M^*$  using a Bayesian technique, considering the entire spectrum of each galaxy. The derived parameters (SFR and SFR/ $M^*$ ) are then corrected for aperture biases using photometric colours. Their analysis of line ratios is insensitive to stellar ages, SFH and the relative attenuation by dust in the gas clouds and the interstellar medium. Out of the three statistical estimates (mean, median and mode) for the probability distribution function of SFR/M\* derived for each galaxy, we used the median of the distribution in this paper, since it is independent of binning.

The spectrum of a galaxy that has experienced a burst of star formation in the recent past (1-3 Gyr ago) is expected to show a strong absorption of H $\delta$ in the optical spectrum. This is because A type stars, which significantly contribute to the H $\delta$ absorption, have a lifetime of  $\leq 1.5$  Gyr, but a burst of star formation can produce enough ionizing radiation to fill in the H $\delta$ absorption. However, as the episode of star formation ends, the H $\delta$ absorption line becomes more transparent. The EW(H $\delta$ ) has been extensively used in the literature to measure the mean stellar age of galaxies, and the elapsed time since the last major burst (e.g. Worthey & Ottaviani 1997; Kauffmann et al. 2003). At the other extreme is the 4000 Å break  $(D_n 4000)$ , which is the strongest discontinuity occurring in the optical spectrum of a galaxy, from the accumulation of absorption lines of mainly ionized metals. As the opacity increases with decreasing stellar temperature, the value of  $D_n 4000$  is the largest for old and metal-rich stellar populations. Stellar population synthesis models indicate that  $D_n$ 4000 is mostly sensitive to age, except for sub-solar metallicity populations older than 1 Gyr, where it is also strongly dependent on metallicity (Kauffmann et al. 2003).

Interestingly, the variation of H $\delta$  with  $D_n4000$  is not sensitive to metallicity or dust extinction, thus providing a good measure of SFH, such that for a given  $D_n4000$ , stronger H $\delta$  implies that the galaxy has experienced a recent burst in star formation (Kauffmann et al. 2003). In particular, the right-hand panel of Kauffmann et al.'s fig. 2 indicates that the combination of H $\delta$  > 2 Å; and  $D_n4000 <$  1.5 leads to stellar populations younger than 1 to 3 Gyr for solar and 0.2 solar metallicity populations, respectively.

# **3 VELOCITY MODULATION OF GALAXY PROPERTIES**

The key issue that we are trying to address in this paper is whether it is possible to distinguish the galaxies that have passed through the cluster core from those that are falling into it for the first time, based on observable parameters. DM simulations show that the backsplash population is most likely to be seen between 1 and  $1.5R_v$  and with velocities lower than the mean velocity of the cluster (e.g. Mamon et al. 2004; Gill et al. 2005). So, we stack together all the galaxies found in clusters within  $2R_v$  and  $|\Delta v_{\text{LOS}}| < 3\sigma_v$ , into four bins of the projected radius of width  $0.5R_v$ , and into three bins of absolute LOS velocity:  $|\Delta v_{\text{LOS}}|/\sigma_v < 1$ , 1–2 and 2–3, respectively. Below, we describe the features of these distributions for various galaxy properties with respect to one another and the field distribution.

## 3.1 Stellar mass

In Fig. 1, we plot the distribution of stellar masses for the 12 classes (three scaled velocity bins in each of the four scaled radial bins) of galaxies as described above. Due to the flux limit of SDSS, the stellar mass distribution of galaxies in Fig. 1 appears to be centred around  $M^* = 3 \times 10^{10} \,\mathrm{M_{\odot}}$  in the local Universe (also see Kauffmann et al. 2003). The most massive galaxies ( $\log M^*/\mathrm{M_{\odot}} \ge 11$ ) are mostly confined to the cores of the clusters. However, even in the core there seems to be a correlation between the relative LOS velocity of a galaxy with respect to the cluster and its stellar mass. The Kolmogorov–Smirnov<sup>3</sup> (KS) statistics show that the most massive galaxies in clusters have low velocities with respect to the cluster, and the high-velocity galaxies show an affinity for the field distribution, which is skewed towards the low-mass end. The detailed statistical comparison between different distributions is shown in Table A1.

When the brightest cluster galaxies (BCGs) are excluded, there is no mass segregation in clusters relative to the field (von der Linden et al. 2010). To explore the inter-dependence of  $M^*$ ,  $R_v$  and LOS velocity of galaxies in clusters, we repeated our analysis by excluding the BCGs from the clusters. Contrary to von der Linden et al. (2010), we find that the different distributions still show similar trends: in the inner regions of clusters the most massive galaxies have the lowest absolute LOS velocities (see Table A2).

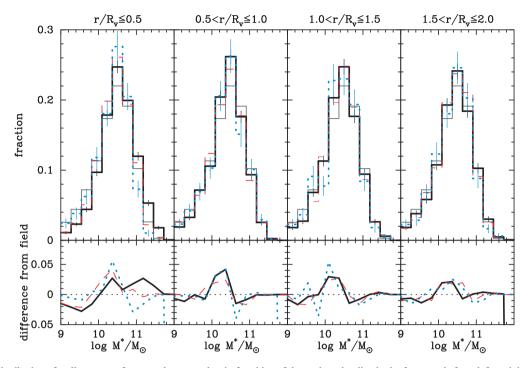
To analyse mass segregation in a different way, in Fig. 2 we show the fraction of high-stellar mass galaxies as a function of the projected radius in three bins of absolute LOS velocity, discarding BCGs. Fig. 2 confirms our impression that mass segregation is present, but only at  $R < 0.5 R_v$ , and only for the low and intermediate  $|v_{LOS}|$  galaxies.

The difference in low- and high-mass velocity distributions in the projected cluster core is not simply caused by the BCGs, which are excluded from Fig. 2 (see also Table A2). While Biviano et al. (1992) also found that high-mass non-BCGs had lower absolute LOS velocities, we find that this is limited to galaxies within  $0.5R_v$ . In other words, we find that *the high absolute LOS velocity galaxies show no mass segregation*, in contrast with the global luminosity segregation found by others (e.g. Adami et al. 1998; von der Linden et al. 2010), when no cuts are made on absolute LOS velocity galaxies are much rarer than their intermediate- and low-velocity counterparts). We discuss mass segregation amongst cluster galaxies further in Section 5.1.

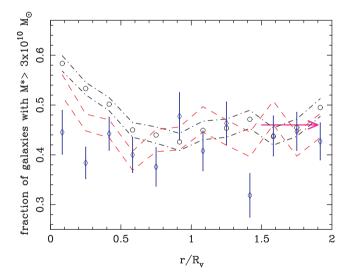
## 3.2 Galaxy colours

Broad-band photometric colours are widely used as proxies for the star formation activity of galaxies. In this paper, we use the 'colour offset', which is the difference between the  $(g - r)^{0.1}$  (extinction-corrected) colour of a galaxy and that of the red sequence (RS) for a galaxy of the same magnitude, where the RS is fitted by stacking all the cluster galaxies together. In Fig. 3 we plot the distribution of the colour offset for all 12 classes of galaxies.

<sup>3</sup> The null hypothesis for the KS test is that both the distributions being compared are drawn from the same parent distribution, i.e. if the two distributions are identical, the probability (p) of the null hypothesis being satisfied is unity.



**Figure 1.** The distribution of stellar masses for our galaxy samples, in four bins of the projected radius in the four panels from left to right. The solid black, dashed red and dotted blue distributions represent absolute LOS velocity bins  $|v_{LOS}|/\sigma_v = 0-1$ , 1–2 and 2–3, respectively. The *thin grey distribution* denotes the field. The bottom panels show the difference between the binned cluster distributions and that of the field. The error bars are Poissonian. In the flux-limited SDSS, galaxies in the local Universe have their  $M^*$  distribution centred around  $M^* = 3 \times 10^{10} \,\mathrm{M_{\odot}}$  (Kauffmann et al. 2003). A significant fraction of galaxies with  $M^* \ge 10^{11} \,\mathrm{M_{\odot}}$  are found only in the core of galaxy clusters. Interestingly, the low absolute LOS velocity galaxies in the cores are the ones which are more massive, while the high-velocity galaxies mostly inhabit the low-mass end.



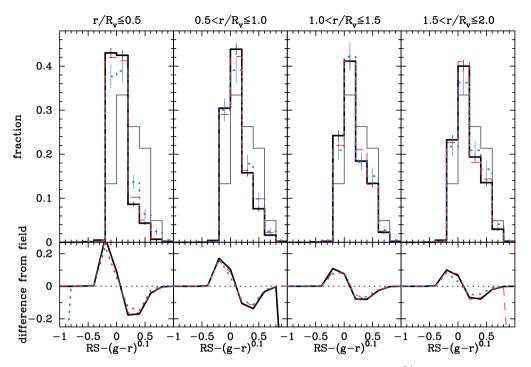
**Figure 2.** The fraction of high stellar mass galaxies  $(M^* \ge 3 \times 10^{10} \text{ M}_{\odot})$ , with BCGs removed), plotted as a function of scaled radius from the cluster centre. The low  $(0-1 \sigma_v)$  and high  $(> 2 \sigma_v)$  absolute velocities (shown as black circles and blue diamonds, respectively), and the  $\pm 1 \sigma$  range (from binomial statistics), are shown as black dash–dotted lines, red dashed lines and blue error bars, for the low, intermediate  $(1-2 \sigma_v)$  and high LOS absolute velocities, respectively. The magenta arrow indicates the field value.

The low-velocity galaxies in cluster cores are found to have the reddest colours, indicative of their passive evolution. But interestingly, even within the cores, the difference between the colours of high- and low-velocity galaxies indicates statistically significant different distributions (see Table A3). Out to  $2R_v$ , the distribution of the colour offset for the field galaxies is very different from that of the galaxies residing in and around clusters. This might suggest that the broad-band colours could be very easily modulated by slight changes in the local and/or global environment, and are hence not very well suited for the study of evolutionary trends amongst galaxies (see also Mahajan et al. 2010, in preparation). As discussed below, on the outskirts of clusters  $(1-1.5R_v)$  the trends seen for broad-band colours are consistent with those seen for spectroscopic parameters.

## **3.3** Diagnostics of specific star formation rate and star formation history

It has been shown that the SFR of galaxies is a function of their stellar mass (e.g. Noeske et al. 2007b). So in this work we prefer to use the specific star formation rate (SFR/ $M^*$ ) to quantify the *current* star formation activity in a galaxy. In Fig. 4, we plot the distributions of SFR/ $M^*$ , as estimated by Brinchmann et al. (2004), for all the galaxies in the spectroscopic galaxy catalogue of the SDSS DR4.

As expected, the cluster galaxies within  $0.5 R_v$  have their log SFR/*M*<sup>\*</sup> distributions heavily skewed towards the lower end, indicating passive evolution. Interestingly though, the high end of the values of SFR/*M*<sup>\*</sup> in the cluster core, and almost at all radii out to  $1.5 R_v$ , mostly belongs to galaxies with high velocities. KS statistics show the difference between the lowest and the highest velocity galaxy distributions to be statistically significant in the core ( $<0.5 R_v$ ) and on the cluster outskirts ( $1-1.5 R_v$ ; see Table A4). The field distribution is significantly different from all other classes of galaxies, becoming indistinguishable from the high-velocity galaxies only in the outermost radial bin.



**Figure 3.** Same as Fig. 1 but for the 'colour offset' of cluster galaxies, i.e. the difference between the  $(g - r)^{0.1}$  colour of a galaxy and the RS colour for a galaxy of the same magnitude. Galaxies bluer than the fitted RS (see text) have positive values of the offset on the *x*-axis. The build-up of the blue tail of the distribution outwards from the cluster core is clearly seen. Interestingly, even in the outermost radial bin  $(1.5-2R_v)$ , there are more RS galaxies than the field. This shows that physical processes, dependent on environment, efficiently modify properties of galaxies in regions with densities in between the two extremes characterizing cluster cores and the field.

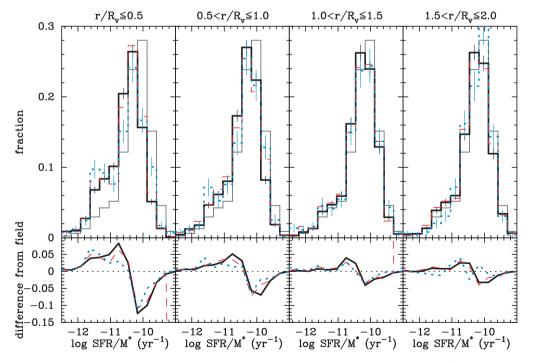
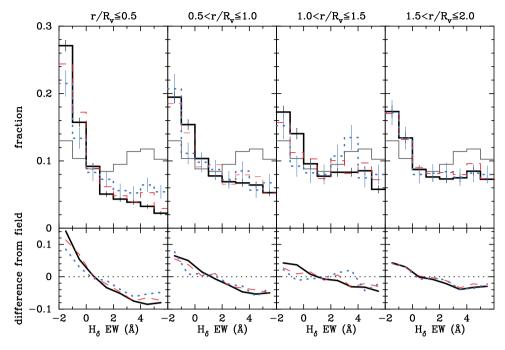


Figure 4. Same as Fig. 1 but for SFR/ $M^*$ . As expected, the cluster distributions are skewed towards the low log SFR/ $M^*$  end in the core region, but only a small tail of galaxies with low log SFR/ $M^*$  is seen in the outer radial bins.



**Figure 5.** Same as Fig. 1 but for EW(H $\delta$ ). This plot complements the results in Fig. 5. The field distribution shows a clear bimodality around 2 Å. The galaxies in the core of the cluster, most of which are evolving passively, do not show absorption in H $\delta$ . It is interesting to note that the high-velocity galaxies in the innermost bins, which are likely to be the newest entrants in the core, are also the ones which are most likely to have experienced a burst of star formation as indicated by relatively high EW(H $\delta$ ). This trend in velocity classes continues out to  $2R_v$ , where the difference between the field and the low-velocity galaxies is minimum. The difference between the highest (blue) and the lowest velocity (black) galaxies is statistically significant in all radial bins out to  $1.5 R_v$ .

Figs 5 and 6 show the distributions of EW(H $\delta$ )<sup>4</sup> and  $D_n$ 4000 for the galaxies in 12 different cells of projected phase space (three scaled absolute LOS velocities times four scaled projected radii), and compare them with the distribution of field galaxies. The EW(H $\delta$ ) distribution of the cluster galaxies is strikingly different from that of the field galaxies, the latter showing a bimodality at EW(H $\delta$ ) ~2 Å (also see Table A5). In the cluster cores, the galaxies with the highest velocities, which are most likely to have fallen in recently (Table 1), are the ones that also show H $\delta$  in absorption [EW(H $\delta$ ) > 0]. This suggests that their likelihood of experiencing a burst of star formation within the last ~1–3 Gyr is relatively higher than their low-velocity counterparts. The KS test shows that the difference between the EW(H $\delta$ ) distributions of the highest and the lowest absolute LOS velocity galaxies is statistically significant at all radii within 1.5  $R_v$  (Table A5).

The amplitudes of the 4000 Å break in SDSS galaxy spectra show very different distributions for the highest and lowest classes of  $|v_{\text{LOS}}|$ , both in the core ( $<0.5 R_v$ ) and on the periphery (1–1.5  $R_v$ ) of the clusters. However, the distributions of  $D_n$ 4000 in the 0.5–  $1 R_v$  bin are only very marginally dissimilar, with  $\sim$ 10 per cent probability of the null hypothesis being satisfied (see Table A6).

We now take advantage of the fact that together H $\delta$  and  $D_n4000$  yield a good constraint on the SFHs (Kauffmann et al. 2003) of galaxies. In Fig. 7 we show the SFHs of galaxies with different absolute LOS velocities in bins of increasing cluster-centric radius.

For clarity, we only plot the two extreme absolute LOS velocity classes ( $|v_{LOS}| < \sigma_v$  and  $|v_{LOS}|/\sigma_v = 2-3$ ). The distribution of the low  $|v_{LOS}|$  galaxies, in this plot of EW(H $\delta$ )versus  $D_n$ 4000, is dominated by the passive sequence (lower right) at low projected radii, and becomes increasingly bimodal with increasing cluster-centric radius. The same evolution occurs for the high  $|v_{LOS}|$  galaxies, but is less bimodal at large projected radius. On the other hand, the high absolute LOS velocity galaxies span the entire available parameter space equally at all distances. According to the stellar population study of Kauffmann et al. (see their fig. 3), this is an indication that the SFH is more continuous in the low  $|v_{LOS}|$  galaxies. We discuss these trends in the context of the relative fraction of the infalling and backsplash galaxies, and the fraction of star-forming galaxies as a function of cluster-centric distance in Section 5.

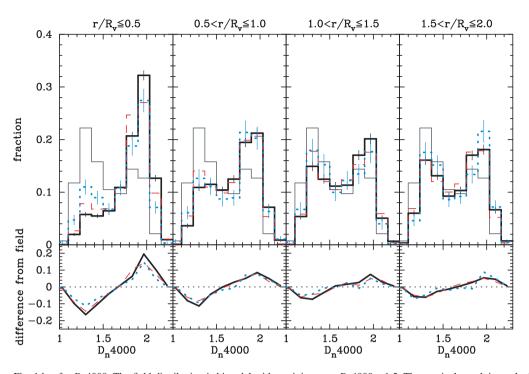
We now refer to galaxies with EW(H $\delta$ ) > 2 and  $D_n4000 < 1.5$  as GORES, following the assumption that a galaxy that experienced efficient star formation  $\lesssim 1-3$  Gyr ago is likely to show these features prominently in its spectrum. Our choice of EW(H $\delta$ ) and  $D_n4000$  thresholds is based on the bimodality seen in the field distributions (Figs 5 and 6).

Fig. 8 shows how the fraction of GORES,  $f_{\text{GORES}}$ , varies with the projected radius and absolute LOS velocity. The generally increasing radial trend of  $f_{\text{GORES}}$  is clearly modulated by  $|v_{\text{LOS}}|$ : at all projected radii, the value of  $f_{\text{GORES}}$  is higher (lower) for high (low)  $|v_{\text{LOS}}|$ .

## 4 MODELLING THE VELOCITY MODULATION

In this section, we present simple models to quantify the observed fraction of GORES by combining theoretical predictions with the suite of galaxy properties analysed in Section 3.

<sup>&</sup>lt;sup>4</sup> Note that the negative values of EW(Hδ) do not imply Hδ line *emission* in the passive galaxies, because the EW(Hδ) values are measured from the pseudo-continuum bands, and so do not always represent the 'true' flux in the Hδ line. The pseudo-continuum bands are required because in the spectra of passive galaxies, the position of several metal lines may coincide with the Hδ line, making it virtually impossible to measure the 'true' flux (G. Kauffmann, private communication; see also Worthey & Ottaviani 1997 and Kauffmann et al. 2003).



**Figure 6.** Same as Fig. 1 but for  $D_n4000$ . The field distribution is bimodal with a minimum at  $D_n4000 \sim 1.5$ . The passively evolving galaxies in the cluster core are old and metal-rich, hence their distribution peaks at the high end of the  $D_n4000$ . However, the high-velocity galaxies in the cluster core (dotted blue line) have a distribution similar to that of field galaxies. The trend continues out to  $1.5 R_v$ , beyond which the distributions almost merge with the field. The KS statistics show the distributions of the high- and low-velocity galaxies to be statistically different at all radial distances within  $1.5 R_v$ .

Table 1. Schemes of particle classes from positions in radial phase space.

Scheme	Region	А	В	С	D
	$r/R_{\rm v}$	<1	<1	<1	>1
_	$v_{\rm r}$	$> -v_{ m r,  crit}$	$v_{r,  crit}^{(2)} \leftrightarrow v_{r,  crit}$	$< v_{ m r,crit}^{(2)}$	$v_{\rm r,crit}^{(2)} \leftrightarrow v_{\rm r,crit}$
0		Virial	Virial	Virial	Infall
1		Virial	Infall	Infall	Infall
2		Backsplash	Infall	Infall	Infall
3		Infall	Infall	Infall	Infall
4		Backsplash	Backsplash	Backsplash	Infall
5		Backsplash	Backsplash	Infall	Backsplash

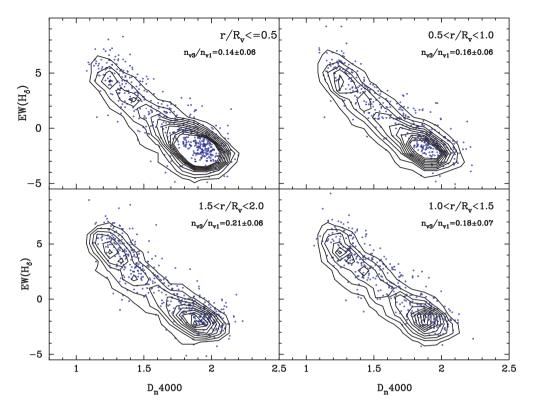
*Note.* The letters A to D correspond to the regions in Fig. 9. The symbol  $\leftrightarrow$  means 'in between'.

We build two simple models of the frequency of GORES, one in which their frequency only depends on the *class* of galaxies, i.e. whether they are part of the virialized, infall or backsplash population, and second, where the frequency of GORES depends upon class *and* the distance from the centre of the cluster. We define the three classes of galaxies in radial phase space (i.e.  $[r, v_r]$ , where *r* is the 3D radius and  $v_r$  the radial velocity) using the z = 0output of a cosmological simulation. We also use this simulation to project these quantities on to the observable *projected phase space*,  $[R, |v_{LOS}|]$ , where *R* is the projected radius.

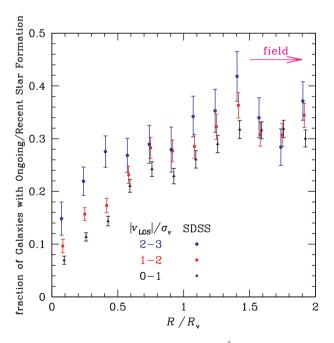
#### 4.1 Cosmological simulation

We use the high-resolution cosmological hydrodynamical simulation run by Borgani et al. (2004). To summarize, the simulation assumes a cosmological model with  $\Omega_0 = 0.3$ ,  $\Omega_{\Lambda} = 0.7$ ,  $\Omega_{b} =$  0.039, h = 0.7 and  $\sigma_8 = 0.8$ . The box size is  $L = 192 h^{-1}$  Mpc. The simulation uses 480<sup>3</sup> DM particles and (initially) as many gas particles for a DM particle mass of  $4.62 \times 10^9 h^{-1} M_{\odot}$ . The softening length was set to  $22.5 h^{-1}$  comoving kpc until redshift z =2 and fixed for subsequent epochs (i.e. at  $7.5 h^{-1}$  kpc). DM haloes were identified by Borgani et al. at redshift z = 0 by applying a standard FoF analysis to the DM particle set, with linking length 0.15 times the mean inter-particle distance. After the FoF identification, the centre of the halo was set to the position of its most bound particle. A spherical overdensity criterion was then applied to determine the virial radius,  $R_{200}$  of each halo. In this manner, 117 haloes were identified within the simulated volume, of which 105 have virial mass  $M_{200}$  greater than  $10^{14} h^{-1} M_{\odot}$ . To save computing time, the subsequent analysis was performed on a random subsample of roughly 2 million particles selected from the whole sample of 4803 particles. We deliberately chose to analyse DM particles rather than galaxies in the simulations, as we do not trust the galaxy distribution, with a homogeneous core found in these and other hydrodynamic cosmological simulations, as they conflict with the observations (Saro et al. 2006). Moreover, the particle data provide much better statistics.

A sample of 93 non-bimodal mock clusters were extracted from these simulations by Mamon, Biviano & Murante (2010), who placed their observer at 90  $h^{-1}$  Mpc of each mock cluster and added the peculiar motions to the distance with the Hubble constant value  $(H_0 = 100 \text{ km s}^{-1} \text{ Mpc}^{-1})$  corresponding to the units of positions  $(h^{-1} \text{ kpc})$ . This yields fairly regular clusters that should resemble those of Yang et al. (2007) (in the latter case, their high threshold causes multimodal clusters to be fragmented into several). We repeated the same extraction, this time by placing the observer at an infinite distance of each cluster (cylindrical projection).



**Figure 7.** The distribution of galaxies having the highest  $(|v_{LOS}|/\sigma_v = 2 - 3;$  blue points) and the lowest  $(|v_{LOS}| < \sigma_v;$  black contours) absolute LOS velocity relative to the cluster, in bins of increasing (scaled) radius (clockwise from top left). The innermost contour represents a density of 100, decreasing by 10 at every subsequent level. The fractions in the top right corner of each panel show the ratio of the numbers in the two classes of galaxies shown, and the scatter in it. Barring the innermost radial bin, the distribution of high-velocity galaxies remains the same, although the distribution of the virialized galaxies tends to become bimodal with increasing (scaled) radius.



**Figure 8.** The fraction of GORES [EW(H $\delta$ ) > 2Å and  $D_n4000 < 1.5$ ] versus projected radius in bins of absolute LOS velocity:  $0-1\sigma_v$  (black triangles),  $1-2\sigma_v$  (red squares) and  $> 2\sigma_v$  (blue pentagons), slightly shifted along the *x*-axis for clarity. The magenta arrow indicates the GORES fraction in the field ( $R > 3R_v$ ).

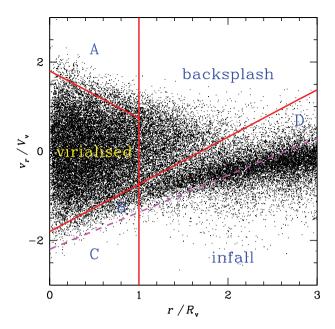
#### 4.2 Classification schemes

Ideally, one should define the virial, infall and backsplash classes by following the orbits of the particles (Gill et al. 2005), but this task is beyond the scope of the present article. Instead, we define the classes using the present-day radial phase-space distribution of particles. Particles that are outside the virial radius, and travelling at velocities lower than the critical velocity, are falling into the cluster for the first time, while particles outside the virial radius with higher velocities must have crossed the cluster at least once.

Sanchis, Łokas & Mamon (2004) have analysed the distribution of DM particles in the radial phase space  $(r, v_r)$  at z = 0, for a cluster-mass halo in a dissipationless cosmological *N*-body simulation (256<sup>3</sup> particles in a box of 150  $h^{-1}$  Mpc width). Their fig. 1 (see also Mamon et al. 2004) suggests that the separation of particles belonging to the infall, backsplash and virialized populations can be written with a critical radial velocity delimiting the infall regime from the other two classes:

$$\frac{V_{\rm r,\,crit}}{V_{\rm v}} = -1.8 + 1.06 \,\left(\frac{r}{R_{\rm v}}\right).$$
 (2)

Fig. 9 shows the distribution of DM particles in the stack of 93 clusters in radial phase space  $(r, v_r)$ . Overplotted are the cuts of Sanchis et al. (2004) designed to separate the virialized, infall and backsplash classes of particles (equation 2). The particles within the virial radius with large absolute radial velocities have uncertain classes.



**Figure 9.** Radial phase-space distribution of DM particles of the stack of 93 regular mock clusters from the cosmological hydrodynamical simulation of Borgani et al. (2004). The units of radius and radial velocity are the virial radius  $r_{100}$  and the circular velocity at that radius, respectively. The critical velocity separating infall from backsplash population (long diagonal red line) is given in equation (2). The short diagonal line represents the negative critical velocity threshold (see Section 4). For clarity, only one out of 550 particles of the original simulation is plotted. Region A is virialized in Schemes 0 and 1, infall in Scheme 3 and otherwise backsplash. Region B is virialized in Scheme 0, infall in Schemes 1 to 3, otherwise backsplash. Region C is virialized in Scheme 0, backsplash in Scheme 4, otherwise infall. Region D is backsplash in Scheme 5, otherwise infall (see Table 1).

We devise several Schemes to identify the three classes of particles (we refer to fig. 6 in Bertschinger 1985 for a schematic view of the trajectories of particles in radial phase space). Table 1 summarizes these schemes. The rapidly infalling particles with  $r < r_v$  might represent the low-end tail of the radial velocity distribution of the virial class, which we denote by Scheme 0, or might indeed be part of the infall class (Schemes 1 to 3), or may even be mainly populated by particles on their second infall, i.e. backsplash class (Scheme 4). The rapidly expanding particles with  $r < r_v$  might again represent the high-end tail of the radial velocity distribution of the virial class (Schemes 0 and 1), or the backsplash class (Schemes 2 and 4), or the infall class (if the star-forming properties of galaxies in this region of radial phase space reflect those of the rapidly infalling class within the virial radius; Scheme 3). Scheme 0 corresponds to maximum virialization while Scheme 3 corresponds to maximum infall.

Although Fig. 9 is based upon a very different simulation (hydrodynamical instead of dissipationless and with three times better mass resolution) and on a stacked halo instead of a single one, it shows that the critical radial velocity of equation (2) is fully adequate to distinguish between infalling and backsplash particles in the stacked mock cluster obtained from the cosmological hydrodynamical simulation analysed here.

One may argue that the red solid line separating the infall and backsplash classes is too high and that we may be missing an important fraction of backsplash particles at high r and low  $v_r$ . We thus created a *maximum backsplash* Scheme 5, where we consider

the critical velocity

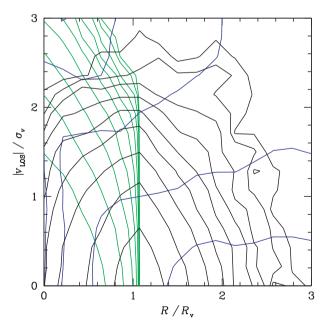
$$\frac{v_{\rm r,\,crit}^{(2)}}{V_{\rm v}} = -2.2 + 0.83 \,\left(\frac{r}{R_{\rm v}}\right). \tag{3}$$

This is shown as the magenta dashed line in Fig. 9: particles with  $v_r < v_{r, \, crit}^{(2)}$  are infalling; other particles are backsplash or virial according to Scheme 4 applied with  $v_{r, \, crit}$ .

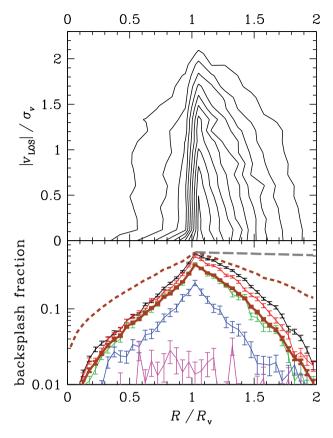
The cosmological simulation provides us with a unique way of measuring the frequency of the three classes of particles (galaxies) in projected phase space. We translate velocities from  $V_v = V_{100}$  to the observable cluster velocity dispersion,  $\sigma_v$ , noting that the stacked cluster has a velocity dispersion (limited to the aperture  $r < R_v$ ) of 0.65  $V_v$ , as measured in the hydrodynamical simulation by Mamon et al. (2010), and within 5 per cent of what is expected for isotropic NFW models of clusters (appendix A of Mauduit & Mamon 2007).

Fig. 10 shows the fractions of the three classes in projected phase space. The virialized particles are necessarily at radii  $r < R_v$ , the infalling particles prefer large projected distances and high velocities, while the backsplash particles are mostly found just around the virial radius and have *low absolute LOS velocities*. This preference of backsplash galaxies for low  $|v_{LOS}|$  is an immediate consequence of their lower radial velocities (Section 1) and has also been noted by Gill et al. (2005).

In the top panel of Fig. 11, we show the contours for the fraction of particles that are backsplash, while the bottom panel provides the fraction of backsplash particles versus projected radius in wide bins of absolute LOS velocity. The two plots of Fig. 11 indicate that the fraction of backsplash particles reaches a maximum of 54 per cent just outside the virial radius at very low  $|v_{LOS}|$  for Scheme 3 (75 per cent for Scheme 5). At high  $|v_{LOS}|$ , the fraction

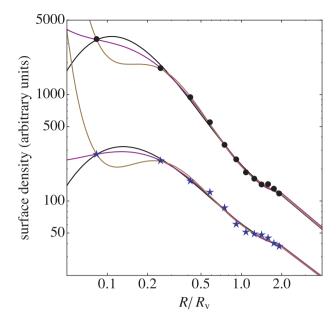


**Figure 10.** Density in projected phase space of virial (green), infall (blue) and backsplash (black contours) particles of the stacked mock cluster with our preferred model (Scheme 3, see Fig. 9). The contours are logarithmically spaced by a factor of 2.3, and the same set of contours is used for all three classes: the highest contours are on the lower left (virial), lower right (infall) and bottom (backsplash), where the latter two classes only reach the second highest contour of the virial class.



**Figure 11.** Upper panel: contours in projected phase space of the fraction of particles of the stacked mock cluster that contribute to the backsplash class (Scheme 3; see Fig. 9). Contours are linearly spaced from 0.05 to 0.5 going downwards. Lower panel: fraction of backsplash particles in bins of absolute LOS velocity: 0–0.5 (top, black), 0.5–1.0 (red), 1.0–1.5 (green), 1.5–2.0 (blue) and >2.0  $\sigma_v$  (bottom, magenta), and summed over all LOS velocities  $<3\sigma$  (thick brown). The dashed thick brown curve shows the maximum backsplash fraction (for  $|v_{LOS}| < 3\sigma_v$ ) from Scheme 5 while the long-dashed thick grey line is the relation deduced from observations by Pimbblet (2011) (see Section 5.3).

of backsplash particles is symmetric relative to the virial radius. However, at low  $|v_{\rm LOS}|$ , the fraction is skewed towards higher values beyond the virial radius (see e.g. curve representing all particles with  $|v_{\rm LOS}| < 3 \sigma_v$  in the bottom panel of Fig. 11). Indeed, at projected radii smaller than the virial radius, the backsplash particles must be in the foreground or background of the virial sphere, and geometric effects typically cause their 3D velocities to be aligned with the LOS, making it difficult to obtain small absolute LOS velocities. These trends are confirmed in Table 2, which lists the fractions of the three classes of particles in cells of projected phase space.



**Figure 12.** Surface density of all galaxies (top) and of GORES (bottom). The symbols are the data (filled black circles for all galaxies and blue stars for GORES). The black, purple and brown curves represent the polynomial fits of log  $\Sigma$  versus log *R* for orders 3, 4 and 5, respectively. The data were extrapolated beyond  $2R_v$  with power-law fits to the outermost three data points.

#### 4.3 Models

#### 4.3.1 Global deprojection

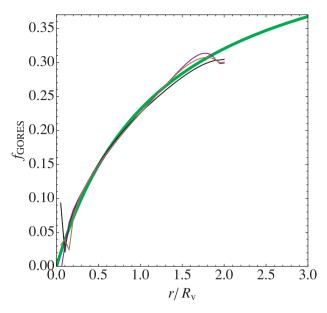
We first directly deproject the observed fractions of GORES, regardless of the LOS velocity. Expressing the global (summing over the velocity bins) observed fraction of GORES as  $g_{\text{GORES}}(R) = N_{\text{GORES}}(R)/N_{\text{tot}}(R)$ , we can deduce the surface densities,  $\Sigma(R) = N(R)/(2\pi R dR)$  of GORES and of all galaxies. Since the projected number profiles  $N_{\text{GORES}}(R)$  and  $N_{\text{tot}}(R)$  are fairly noisy, we fit a polynomial to log  $\Sigma$  versus log R and extrapolate the data beyond the last point by a power law, whose slope is fit on the last three points. Fig. 12 shows the surface density profiles and their polynomial fits. While the fits diverge dramatically at low R, they match remarkably well at high R (better than analogous fits of log  $\Sigma$ versus R, not shown in Fig. 12 for clarity). One can now perform Abel inversion to deduce the space densities

$$\nu(r) = -\frac{1}{\pi} \int_{r}^{\infty} (\mathrm{d}\Sigma/\mathrm{d}R) / \sqrt{R^2 - r^2} \,\mathrm{d}R \tag{4}$$

of GORES and all galaxies, and finally obtain the deprojected fraction of GORES by dividing the two space densities. Fig. 13 shows the resultant deprojected fraction of GORES, obtained with the orders 3 to 5 polynomial fits of  $\log \Sigma$  versus  $\log R$  (Fig. 12). Fig. 13

**Table 2.** The fraction of virialized (v), infall (i) and backsplash (b) particles of the stacked mock cluster in cells of projected phase space with Scheme 3.

$r/R_{\rm v}$		0-0.5			0.5–1			1–1.5			1.5–2	
$ v_{\rm LOS} /\sigma_v$	v	i	b	v	i	b	v	i	b	v	i	b
0-1	0.89		0.03	0.49	0.33	0.18	0.00			0.00	0.93	0.07
1-2 2-3	0.83 0.69	0.16 0.31	$0.02 \\ 0.00$	0.40 0.16	0.48 0.83	0.11 0.01	0.00 0.00		0.19 0.01	0.00 0.00	0.97 1.00	0.03 0.00



**Figure 13.** Deprojected fractions of GORES (using equation 4). Thin curves show the results obtained by polynomial fits of the log surface density versus log *R* (orders 3, 4 and 5 in black, purple and brown, respectively). The thick green curve represents equation (5) with  $f_0 = 0.52$  and  $a = 1.26 R_v$ , obtained by a  $\chi^2$  fit to the order of 4 polynomial fit of log  $\Sigma$  versus log *R* (purple curve), with *r* linearly spaced between 0.05 and  $2 R_v$ .

also shows a  $\chi^2$  fit of equation (5) to the deprojected fraction of GORES obtained from the order of 4 polynomial fit of log  $\Sigma$  versus log *R*, using

$$f_{\rm GORES}(r) = f_0 \frac{r}{r+a}.$$
(5)

We see that the simple, saturated linear model provided in equation (5), with asymptotic GORES fraction  $f_0 = 0.52$  and *quenching radius for efficient star formation* (hereafter quenching radius)  $a = 1.26R_v$ , is a decent representation of the deprojected profile for  $f_{\text{GORES}}$ . While this deprojection leads to an asymptotic value of  $f_{\text{GORES}} = 0.52$ , equation (5) yields  $f_{\text{GORES}} = 0.44$  at our typical minimum projected radius for field galaxies (6.7 $R_v$ ), very close to their observed fraction of 0.45.

Note that although the constraints from potential SDSS fibre collisions leads to underestimated surface density profiles at low projected radii, this bias in surface density should affect both the total and GORES surface densities in a similar (multiplicative) way (equation 4). Hence the effect of fibre collisions on the ratio of GORES to total space densities should be minor.

We now refine the models accounting for the LOS velocity modulation of  $f_{\text{GORES}}(R)$ , using the dynamical classes of the galaxies (virial, infall and backsplash).

#### 4.3.2 Model 1: constant recent starburst fraction per class

Suppose that for each of the three classes of galaxies (virial, infall and backsplash), the fraction of galaxies which experienced a recent ( $\leq 1-3$  Gyr) starburst (GORES) is independent of the 3D radius and radial velocity. Let these three fractions be  $f_v$ ,  $f_i$  and  $f_b$ , respectively (we drop the subscript 'GORES' from f for clarity.).

The fraction of GORES in a cell  $(R, v_z)$  of projected phase space can then be written as

$$g_{\text{GORES}}(R_i, v_j) = \sum_{\alpha} f_{\alpha} p(\alpha | R_i, v_j),$$
(6)

 Table 3. Best-fitting parameters for the three galaxy classes with the six schemes for the model of constant GORES fraction per class.

	$r < R_{\rm s}$	v AND				
Scheme	$v_{\rm r} < v_{ m r,crit}$	$v_{\rm r} > -v_{\rm r,crit}$	$f_{v}$	$f_{i}$	$f_{b}$	$\chi^2_{\nu}$
0	Virial	Virial	0.11	0.33	0.26	4.6
1	Infall	Virial	0.10	0.34	0.24	3.5
2	Infall	Backsplash	0.10	0.33	0.28	2.9
3	Infall	Infall	0.10	0.34	0.23	2.7
4	Backsplash	Backsplash	0.09	0.32	0.32	3.0
5	Backsplash*	Backsplash	0.10	0.33	0.30	2.9

*Notes.*  $\chi^2_{\nu}$  is the  $\chi^2$  per degree of freedom. The errors are typically 0.01 on  $f_v$  and  $f_i$  and 0.04 on  $f_b$ . In Scheme 5, the extreme negative velocities for  $r < R_v$  correspond to infall galaxies. \*region D in Fig. 9.

where  $p(\alpha | R_i, v_j)$  is the fraction of particles of class  $\alpha$  within the cell  $(R_i, v_j)$  of projected phase space (as in Table 1, but with finer radial bins).

One can then perform a  $\chi^2$  fit between the observed and predicted fractions of GORES  $g_{\text{GORES}}(R_i, v_j)$  over all cells  $(R_i, v_j)$ , using the conditional probabilities for each class,  $p(\alpha|R_i, v_j)$ , derived from the cosmological simulation. We assume binomial error bars on the observed values of  $g_{\text{GORES}}(R_i, v_j)$  and that the  $p(\alpha|R_i, v_j)$  derived from the cosmological simulation are perfectly known. Furthermore, we use the six schemes for the three populations, changing the class within the cluster virial sphere for the extreme velocities  $|v_r| >$  $|v_{r, \operatorname{crit}}(r)|$  as explained in the caption of Fig. 9. Table 3 shows the best fits for each of these six population schemes.

The best-fitting predictions for the scheme with the lowest reduced  $\chi^2$  (hereafter  $\chi^2_{\nu}$ ), Scheme 3 (where both the very positive and very negative radial velocity objects within the virial sphere are considered to be part of the infall population), provide a reasonable match to the observed fractions of GORES in bins of projected phase space. But  $\chi^2_{\nu} = 2.7$  for this best-fitting model suggests that the model itself can be improved.

## 4.3.3 Model 2: recent starburst fractions increasing with physical radius

In our second model, we suppose that the fraction of GORES is no longer constant per class, but varies with physical radius r as in equation (5), varying the normalization and scale for each class:

$$f_{\alpha}(r) = f_{\alpha} \frac{r/R_{\nu}}{r/R_{\nu} + a_{\alpha}},\tag{7}$$

i.e. rising roughly linearly with radius for  $r < a_{\alpha}$ , and saturating to an asymptotic value  $f_{\alpha}$  at large radii. The predicted fractions of GORES is then

$$g_{\text{GORES}}(R_i, v_j) = \sum_{\alpha} p(\alpha | R_i, v_j) \sum_k f_{\alpha}(r_k) q(r_k | R_i, v_j, \alpha), \quad (8)$$

where  $q(k|R_i, v_j, \alpha)$  is the fraction of the particles of class  $\alpha$  in the cell of projected phase space  $(R_i, v_j)$  that are in the *k*th bin of physical radius. The physical radial bins are expressed as  $r_k = R_i \cosh u_k$ , where  $u_k$  is linearly spaced from 0 to  $\cosh^{-1}r_{\text{max}}/R_i$ , using  $r_{\text{max}} = 50 R_v$ .

Table 4 shows the new set of fits. The first set of lines shows the fits when we force the same quenching radius for the three classes:  $a_v = a_i = a_b$ . Again, Scheme 3 provides the lowest  $\chi^2_v$ , which is now 1.6 (in comparison with 2.7 for the f = constant model). So with the inclusion of just one extra parameter, the radially varying model fits the data much better. This is confirmed with both the *F*-test and

Table 4. Best-fitting parameters for the three galaxy classes with the four schemes for models of radially varying GORES fraction.

	$r < R_{\Lambda}$	AND													
Scheme	$v_{\rm r} < v_{\rm r,crit}$	$v_{\rm r} > -v_{ m r,crit}$	$f_{\rm v}$	$f_{i}$	$f_{b}$	$a_{\rm v}$	ai	ab	$\chi^2_{\nu}$	F	$P_F$	ΔAICc	$P_{\rm AICc}$		
0	Virial	Virial	0.32	0.38	0.35	0.58	0.58	0.58	2.0	46	0	87	0		
1	Infall	Virial	0.24	0.37	0.29	0.36	0.36	0.36	1.8	31	0	55	0		
2	Infall	Backsplash	0.21	0.36	0.30	0.28	0.28	0.28	1.7	24	0	39	0		
3	Infall	Infall	0.19	0.36	0.26	0.22	0.22	0.22	1.6	24	0	36	0		
4	Backsplash	Backsplash	0.23	0.35	0.35	0.35	0.35	0.35	1.8	24	0	40	0		
5	Backsplash*	Backsplash	0.22	0.36	0.34	0.31	0.31	0.31	1.8	22	0	37	0	AIC-AIC(3)	Р
0	Virial	Virial	0.41	0.35	1.00	0.88	0.27	4.79	2.0	0.6	0.56	-3	_	11.8	0.003
1	Infall	Virial	0.34	0.34	0.36	0.72	0.00	1.23	1.6	3.6	0.04	5.7	0.06	7.6	0.02
2	Infall	Backsplash	0.30	0.33	0.21	0.62	0.00	0.00	1.5	3.8	0.03	5.5	0.06	4.4	0.11
3	Infall	Infall	0.29	0.34	0.39	0.62	0.00	1.40	1.2	5.7	0.01	8.3	0.02	_	_
4	Backsplash	Backsplash	0.26	0.37	0.28	0.50	0.55	0.00	1.6	3.1	0.06	4.1	0.13	5.4	0.07
5	Backsplash*	Backsplash	0.27	0.35	0.27	0.53	0.19	0.00	1.6	2.8	0.08	3.4	0.19	5.7	0.06

Notes. The upper portion is for fits in which  $a_v = a_i = a_b$  is enforced, while the lower portion is for fits with fully free scale radii. The errors are typically 0.01 on  $f_v$  and  $f_i$  and 0.04 on  $f_b$ . In Scheme 5, the extreme negative velocities for  $r < R_v$  are infall. The best-fitting Scheme 3 is highlighted in bold. F and  $P_F$  represent the F-test statistic that the fit with the scheme is significantly better than that of the previous model [f(r) with  $a_v = a_i = a_b$  versus f = cst for the upper panel and general f(r) versus f(r) with  $a_v = a_i = a_b$  for the lower panel] and the associated probabilities of a larger value of F appearing by chance.  $\Delta AICc$  and  $P_{AICc}$  represent the same quantities with the Akaike criterion (AIC =  $\chi^2 + 2k$ , for k parameters; Akaike 1974) modified for finite size samples [AICc =  $\chi^2 + 2k n/(n - k - 1)$ , for k parameters and n data points, Hurvich & Tsai 1989]. The final two columns for the lower panel provide the Akaike statistic testing whether the fit for Scheme  $\neq 3$  is as good as Scheme 3 and its associated probability that a larger value of AICc occurs by chance.

the Akaike Information Criterion for finite sample (AICc; Akaike 1974; Hurvich & Tsai 1989) criterion (Table 4). Note that the cosmic variance on the finite number of clusters has been incorporated in the errors. The value of quenching radius *a* is low in Scheme 3, which indicates that it is not that far from the model with constant fraction of GORES per class. The top panel of Fig. 14 shows the observed fractions of GORES together with the best fits with Scheme 3 for both the constant fraction per class and radially varying models with  $a_v = a_i = a_b$ . Both models capture the initial rise of the GORES fraction with the projected radius and subsequent saturation, as well as the velocity modulation, even though the fit is not excellent.

In the next set of fits, shown in the bottom six rows of Table 4, we lift the assumption of  $a_v = a_i = a_b$ . The best-fitting reduced  $\chi^2$  values are now  $\leq 1.6$  for Schemes 1–5, with an often significant improvement of the fit (despite the two extra parameters) over the radially varying model with the same scale parameters (see the Ftest statistic in Table 4). The F-test indicates that the improvement is significant with the inclusion of two extra parameters (three scales instead of a unique one). Using the Akaike criterion, which reduces here to  $\triangle AIC = \triangle AIC = \triangle \chi^2$ , with associated probability P = $\exp(-\Delta AIC/2)$ , we conclude that Scheme 3, which still leads to the lowest  $\chi^2_{\mu} = 1.2$ , is a significantly better fit than Scheme 0 (99.7 per cent confidence) and marginally significantly better fit than Schemes 4 (93 per cent confidence) and 5 (94 per cent confidence). Although a decent fit to the data, this best-fitting model still predicts too low values of  $f_{\text{GORES}}$  for high absolute LOS velocity galaxies within half virial radius of the clusters. Interestingly, the best-fitting model (Scheme 3) predicts a constant GORES fraction for the infall class galaxies  $(a_i = 0)$ , while the next best-fitting model (Scheme 2) predicts that both infall and backsplash populations have a constant GORES fraction ( $a_i = a_b = 0$ ).

#### **5 DISCUSSION**

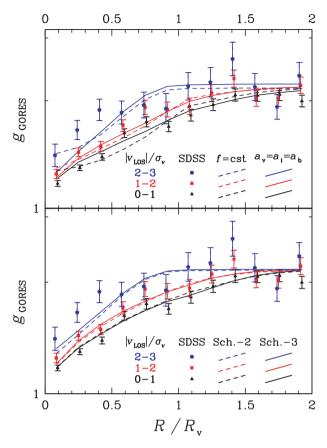
This paper is a unique analytical effort to explore the variations in the spectral and physical properties of different dynamical classes of galaxies residing in similar environments projected on the observed sky (projected radius and absolute LOS velocity), and to interpret these differences. We draw a sample of ~20 000 galaxies  $(M_{\rm r} \leq -20.5)$  found within  $2R_{\rm v}$  and  $|\Delta v_{\rm LOS}| < 3 \sigma_{\rm v}$  of 268 galaxy clusters, and a similar sample of field galaxies for this purpose. All the galaxies are taken from the SDSS DR4 spectroscopic galaxy catalogue.

#### 5.1 Velocity segregation of stellar mass

Three physical mechanisms might explain the excess of high-mass galaxies in the cluster cores amongst the low-velocity galaxies (Fig. 2): cluster tides, two-body relaxation and dynamical friction. We examine in turn each one of these.

Tidal effects from the cluster gravitational field (predicted by Merritt 1983; Mamon 1992; Gnedin, Hernquist & Ostriker 1999, clearly seen in cosmological simulations by Ghigna et al. 1998, and measured through gravitational lensing by Natarajan et al. 2009) will be most effective on slowly moving galaxies, because these have more time to feel the cluster tides. Even though stars are less affected by tides than the more extended DM haloes, simulations of a live dwarf spiral galaxy orbiting a spiral galaxy  $\sim 100$  times more massive, with fixed gravitational potential (Klimentowski et al. 2009) or live N-body system (Łokas et al. 2010), indicate that, at each pericentric passage, over 35 per cent (Klimentowski et al.) to 67 per cent (Łokas et al.) of the stars of a spiral galaxy are tidally stripped. Tides will thus transform massive galaxies into low-mass ones, and low-mass galaxies into even lower mass ones. So tides cause a decrease in the fraction of high-mass galaxies, which disagrees with the trend seen in Fig. 2.

If two-body relaxation can lead to energy equipartition in the cluster cores, then the high-mass galaxies will move slower (in 3D). So the fraction of high-mass galaxies among the low 3D velocity ones should increase with decreasing cluster-centric radius. Hence, the fraction of high-mass galaxies among the low absolute LOS velocity should also increase with decreasing radius. However, the same argument would lead us to predict that the fraction of high-mass galaxies among the high-velocity ones should decrease with decreasing radius, and instead Fig. 2 shows no such trend. Therefore, the trend in Fig. 2 cannot be due to two-body relaxation, unless some



**Figure 14.** Same as Fig. 8, with best-fitting models overplotted. Top: the dashed and solid curves show the best-fitting Scheme 3 models (Tables 3 and 4) assuming no radial dependence (using equation 6) and the radially varying one of equation (7), forcing  $a_v = a_i = a_b$ , using equation (8), respectively. Bottom: best-fitting radially varying model (equation 7) with free values of  $a_v, a_i$  and  $a_b$ , for Schemes 2 (dashed) and 3 (solid). The schemes are defined in Tables 3 and 4.

other process is increasing the fraction of high-mass galaxies among the high-velocity ones within the cluster core.

The time required by dynamical friction to make the orbits of galaxies decay towards the cluster centre scales as  $v^3/m$ , where v is the 3D velocity of the galaxy of mass m. Therefore the most massive and slowly moving galaxies should have their orbits decay the most, and be brought to even lower (projected) radius. So dynamical friction should boost the fraction of high-mass slow-moving galaxies in the cluster core. Moreover, the effects of dynamical friction should be weak for the rapidly moving galaxies. This explains the lack of trend in the fraction of high-mass galaxies with the projected radius for the galaxies with large absolute LOS velocities.

For dynamical friction (and tides), the high-velocity galaxies act little, if one assumes a population in virial equilibrium. Now, the infalling galaxies also tend to have high absolute radial velocities (Fig, 9), hence high absolute LOS velocities (e.g. Table 2), in fact even higher than the virialized population. So the same argument applies to the infalling galaxies: their velocities are too high to be seriously affected by dynamical friction or tides.

We note that the two-body relaxation time-scale is independent of galaxy mass *m*, while the dynamical friction time-scale varies as 1/m. It is easy to show that the ratio of two-body relaxation time to dynamical friction time scales as  $\langle m \rangle /m$ . Thus, the lack of high-velocity low-mass galaxies in the inner bin of projected radii in Fig. 2, in contrast with the excess expected from two-body relaxation, is not inconsistent with the excess of high-mass galaxies at low radii observed in Fig. 2 and expected from dynamical friction.

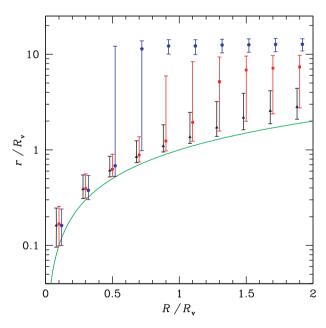
Is dynamical friction efficient enough to increase the fraction of high-mass galaxies towards the centre among the slowly moving galaxies? We adopt the dynamical friction time-scale that Jiang et al. (2008) carefully calibrated with a cosmological hydrodynamical simulation:

$$t_{\rm df} \simeq 1.4 \, \frac{M(r)/m}{\ln[1+M(r)/m]} \, \frac{r}{v_c(r)} \,,$$
(9)

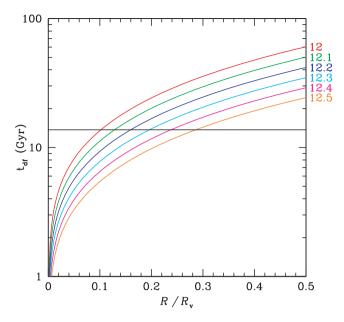
where *m* is the galaxy mass (with its tidally stripped DM halo) and  $v_c(r) = \sqrt{GM(r)/r}$  is the circular velocity at radius *r*. Equation 9 incorporates the effects of elongated orbits and tidal stripping. One would like to have an idea of the physical radius of each galaxy given its projected radius and absolute LOS velocity. Fig. 15 shows the distribution of physical radii given the projected radii in our adopted bins of absolute LOS velocity.

The physical radii of the low absolute LOS velocity galaxies are close to their projected radii, so that these low-velocity galaxies can be used to deproject radial trends. But high absolute LOS velocity galaxies appear to systematically lie very far from the virial sphere (typically  $10 R_v$ ).

Using the relation  $r \approx 1.3R$  from Fig. 15, we can estimate the dynamical friction time as a function of the projected radius. Fig. 16 indicates that a galaxy (along with its dark halo) must have a total mass of at least  $10^{12.45} \,\mathrm{M_{\odot}}$ , for the orbital decay time, at  $R = 0.25 R_v$ , to be smaller than the age of the Universe. In comparison, Yang, Mo & van den Bosch (2009, their table 4) found that in the SDSS, central group/cluster galaxies of mass  $3 \times 10^{10} \,\mathrm{M_{\odot}}$ , resides in haloes of mass  $10^{12.2} \,\mathrm{M_{\odot}}$ . Also, according to table 4 of Yang et al., central haloes of mass  $10^{12.45} \,\mathrm{M_{\odot}}$  have corresponding galaxy masses of  $10^{10.66} \,\mathrm{M_{\odot}}$ , i.e. 45 per cent above our galaxy mass threshold. We therefore conclude that the dynamical friction might indeed be just sufficiently effective to explain the trends in Fig. 2. However, the DM halo of a galaxy extends further out than its



**Figure 15.** Physical radius versus projected radius for particles of stacked mock cluster (medians with error bars for quartiles) in bins of absolute LOS velocity:  $0-1 \sigma_v$  (black triangles),  $1-2 \sigma_v$  (red squares) and  $2-3 \sigma_v$  (blue pentagons). The green curve shows r = R.



**Figure 16.** Time-scale for orbital decay by dynamical friction versus projected radius for galaxies of log total mass (in solar masses, including the tidally stripped DM halo) of (from top to bottom, labelled on right) 12 (red), 12.1 (green), 12.2 (blue), 12.3 (cyan), 12.4 (magenta) and 12.5 (orange), orbiting an NFW cluster of scale radius  $0.19R_v$  and mass  $M_V \equiv M_{100} = 1.9 \times 10^{14} M_{\odot}$  (corresponding to the median mass of  $M_{180} = 10^{14.2} M_{\odot}$  of the SDSS clusters studied here) within the virial radius  $R_v \equiv R_{100} = 1.5 \text{ Mpc}$ . The time-scale is estimated using equation (9) assuming that r = 1.3R as inferred from our cosmological simulation (see Fig. 15). The age of the Universe is shown as the horizontal line.

stellar component, so haloes are tidally stripped in a more efficient manner (e.g. Klimentowski et al. 2009). This means that the ratio of total to stellar mass of cluster galaxies is lower than for field galaxies. One would therefore expect the actual halo masses to be lower than inferred for the central galaxies, from table 4 of Yang et al. (2009), and thus the orbital decay times by dynamical friction to be somewhat longer.

#### 5.2 The star-forming galaxies

The distributions of specific SFR, broad-band colour and amplitude of the 4000 Å break show statistical differences with absolute LOS velocity at almost all radii out to  $R < 1.5 R_v$  (Figs 3, 4 and 6; Tables A3, A4 and A6, respectively). However, the field component shows a bimodal distribution in EW(H $\delta$ ) (Fig. 5) and  $D_n$ 4000 (Fig. 6) around 2 Å and 1.5, respectively. This is in agreement with the bimodality of these two diagnostics when plotted in terms of stellar mass, luminosity or concentration (Kauffmann et al. 2003). We adopt these thresholds to define a galaxy as a recent starburst galaxy (GORES) if it has EW(H $\delta$ ) > 2 Å and  $D_n$ 4000 < 1.5.

As expected, the fraction of GORES drops within the virial radius  $R_v$  for all velocity classes (Fig. 8). But the fraction of GORES is modulated by the absolute LOS velocity: at a given projected radius, galaxies with higher  $|v_{LOS}|$  have higher fractions of GORES. For the high absolute LOS velocity galaxies, the fraction of star-forming galaxies declines rapidly but only well within the core region ( $\leq 0.5 R_v$ ). This once again strengthens our interpretation that the high-velocity galaxies are the youngest members of the core, having recently fallen in.

A curious feature occurs in the radial variation of both highmass (Fig. 2) and GORES fractions (Fig. 8): the galaxies with high absolute LOS velocity show a marginally significant peak (dip) in the fraction of GORES (high-mass galaxies) at  $1.5 R_y$ . If this feature is not a statistical fluke, it may be reflecting the discontinuity seen in SFR of cluster galaxies at the physical radius where infalling and virialized galaxies meet. However, this is expected to occur closer to the virial radius and our simple models involving the virial, infall and backsplash populations do not lead to any discontinuity of  $f_{\text{GORES}}$  at 1.5  $R_{y}$  (Fig. 14). An explanation may require a model going beyond spherical symmetry, e.g., with large-scale filaments feeding clusters (see Porter & Raychaudhury 2007; Porter et al. 2008; Mahajan et al., in preparation). For the benefit of the reader, we emphasize that the enhancement seen in the SFR of galaxies seems to occur in a very narrow region only. This observation is very interesting and still being explored. It might prove useful to distinguish between the backsplash and infall galaxies.

Given the  $M^*$ -SSFR anti-correlation (e.g. Mamon, Parker & Proust 2001; Noeske et al. 2007a; Damen et al. 2009), the peak in the fraction of low-mass galaxies might be directly linked to the enhancement of SFR in infalling galaxies on the outskirts of clusters before the environmental effects in clusters predominate (Porter & Raychaudhury 2007; Porter et al. 2008).

While the projected radii of the low absolute LOS velocity particles in the stacked mock cluster underestimate only slightly their physical radii (Fig. 15), our cosmological simulation indicates that the high absolute LOS velocity particles with projected radii R > $0.8 R_v$  have very large physical radii (typically over 10 virial radii). This implies that the observed fraction of GORES for the high absolute LOS velocity bin at  $R > R_v$  should be the same as that of the field, but this is not what is observed (Fig. 8). One cannot resort to cosmic variance to explain this discrepancy, given the large number of clusters used in our analysis of the SDSS observations (268) and in the simulations (93), and we cannot find any other convincing explanation for this dichotomy.

#### 5.3 Identifying backsplash galaxies

The analysis of the z = 0 output of DM particles in our cosmological hydrodynamical simulation allows us to distinguish backsplash particles, whose positions in radial phase space imply that they previously crossed their parent (mock) clusters from virialized particles (within the virial sphere) and the remaining infall particles (which are actually expanding away from their clusters when they are beyond the turnaround radius of  $\simeq 3.5 R_v$ ). Our analysis in projected phase space indicates that the best place to detect backsplash particles is just beyond the virial radius and at very low velocities. With Scheme 3, the backsplash fraction reaches 54 per cent (bottom panel of Fig. 11) for the lowest absolute LOS velocity bin. With the maximum backsplash Scheme 5, it reaches 75 per cent for the lowest  $|v_{LOS}|$  bin.

Pimbblet (2011) compared the distribution of SSFRs of galaxies with  $0.3 < |v_{LOS}|/\sigma_v < 0.5$ , attributed to the infall class with the full distribution. This led him to predict that the fraction of backsplash galaxies decreases as  $f_b = 0.61-0.052 R/R_v$ . Such a trend (grey line in the bottom panel of Fig. 11) appears inconsistent with the backsplash fractions predicted from our cosmological simulation, even with our maximum backsplash Scheme 5. It is difficult to understand how one would find that as many as half of all galaxies at 2 virial radii (the maximum projected radius in the analysis of Pimbblet) from clusters are backsplash. Backsplash galaxies typically only bounce out to 1–2 virial radii (Mamon et al. 2004). Yet, the high fraction of backsplash galaxies found by Pimbblet agrees with the 54  $\pm$  20 per cent fraction of backsplash particles that Gill et al. (2005) found in the range of projected radii 1 <  $R/R_v$  < 2 from their cosmological simulations. In our Schemes 0–4, we find that only 17  $\pm$  1 per cent<sup>5</sup> of the particles in this range of the projected radius (with  $|v_{LOS}| < 3\sigma_v$ ) are backsplash particles. However, our backsplash fraction amongst DM particles is marginally consistent with the higher fraction found by Gill et al. Even in the maximum backsplash Scheme 5 (partly motivated by Pimbblet's high backsplash fraction, but only marginally consistent with the observed fraction of GORES), we find only 40  $\pm$  1 per cent of the particles in the same range of the projected radius are backsplash. This is apparently inconsistent with that from Gill et al.'s simulations.

Part of our disagreement with Pimbblet on the fraction of backsplash galaxies in the range  $1 < R/R_v < 2$  may be caused by the narrow range of  $|v_{LOS}|/\sigma_v$  used by him to select the infall galaxies.

## 5.4 The quenching of star formation in 3D: infalling versus backsplash galaxies

The SDSS spectroscopy provides the means to address the role of the dynamical classes (virial, infall and backsplash) in shaping the properties of galaxies by studying the spectral features as a function of both projected radius *and* absolute LOS velocity.

Beyond the well-known radial dependence of galaxy properties in clusters, our analysis highlights the velocity modulation of these trends for the parameters SFR/ $M^*$ , EW(H $\delta$ ) and the  $D_n$ 4000. All trends with the projected radius are amplified with increasing absolute LOS velocity. As can be seen in Fig. 15, the effect of  $|v_{LOS}|$ effectively adding to the projected radius is not trivial. Nevertheless, as qualitatively expected from the Hubble flow, in every bin of the projected radius the higher absolute LOS velocities lead to a higher physical radius.

In Section 3 we find observational evidence to support the statistical differences between the low-velocity  $(|v|_{\text{LOS}} \le \sigma_v)$  and the high-velocity ( $2 < |v_{\text{LOS}}|/\sigma_v \le 3$ ) galaxies on the outskirts of clusters (1–1.5  $R_v$ ). KS tests between the different distributions in the clusters and in the field show statistically significant differences between the low- and high-velocity galaxies between 1 and 1.5 $R_v$ in SFR/ $M^*$ , EW(H $\delta$ ) and the  $D_n$ 4000 (Tables A1–A6).

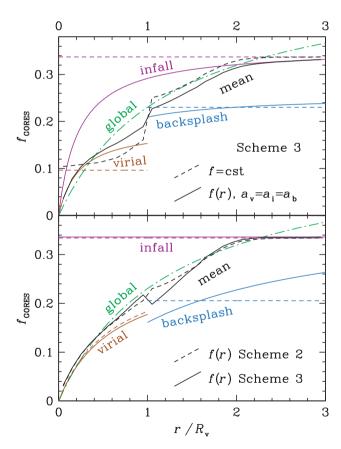
Despite the noisiness of the variations with the projected radius of the numbers of galaxies and of GORES, we have been able to deproject the fraction of GORES to show that it is well fit (Fig. 13) by a saturated linear model (equation 5). Such a model applied in turn to the three different classes of galaxy populations (virialized, infalling and backsplash) with the same quenching radius  $(a_v =$  $a_i = a_b$  provides an adequate fit to the variation of GORES with the projected radius in three bins of absolute LOS velocity (top four rows of Table 4 and upper panel of Fig. 14). The model reproduces the rise with projected radius and the higher fractions for higher absolute LOS velocities. Similar models with free star formation quenching radii fit the data even better (bottom four rows of Table 4 and lower panel of Fig. 14). In particular, the radius-dependent model where galaxies within the virial sphere  $(r < R_v)$  with radial velocity  $|v_r| > |v_{r, crit}|$  are considered to be infalling provides the best fit to the data (Section 4.3, Fig. 9 and Table 4).

In contrast, a simpler model, where the fraction of GORES is a constant that only depends on the class of galaxy population, does not provide an adequate fit (Table 3), even if it also reproduces these qualitative trends (Fig. 14).

The ability of Scheme 3 to better fit the SDSS data than the other three schemes suggests that the high absolute *radial* velocity galaxies within the virial sphere, both infalling and outflowing, retain their fraction of GORES. However, our best-fitting model with Scheme 2 is also an adequate fit, so the model with quenching at pericentre is also consistent with the data.

In the constant GORES fraction model with Scheme 3, the GORES fraction in the backsplash class is half-way between the analogous values for the virial and infalling populations, suggesting that one passage through the cluster environment causes half the quenching of star formation. We now consider the deprojected models to assess how star formation is quenched at a unique radius where the three classes can be compared: the virial radius.

Fig. 17 shows how the best-fitting models predict the fraction of GORES as a function of the 3D radius. We first note that for the constant  $f_{\text{GORES}}$  per class model, the mean variation of  $f_{\text{GORES}}$  (top panel of Fig. 17) departs more strongly from the global trend found by the global deprojection (Section 4.3.1) than do the mean variations with the other models. This reinforces the view that the constant  $f_{\text{GORES}}$  per class model does not reproduce our data well.



**Figure 17.** Fraction f(r) of GORES versus physical radius, for the virial (brown), infall (purple) and backsplash (blue-grey) populations, their mean (using the cosmological simulation to determine the radial variation of the densities of the three classes, black) and the global deprojection (green dash-dotted curve). Top: best-fitting constant (dashed lines) and radially increasing (equation 5) with  $a_v = a_i = a_b$  (solid curves), both with Scheme 3. Bottom: best fit radially increasing (equation 5) with free star formation quenching radii for Schemes 2 (dashed) and 3 (solid curves).

<sup>&</sup>lt;sup>5</sup> The errors in our fractions of backsplash particles are from 50 bootstraps on the 93 haloes of the cosmological simulation.

**Table 5.** Quenching at  $r = R_v$  (models with free quenching radii).

Scheme	$f_{\rm GORES}^{\rm vir}(R_{\rm v})$	$f_{\rm GORES}^{\rm inf}(R_{\rm v})$	$f_{\rm GORES}^{\rm bsp}(R_{\rm v})$	Quenching
0	0.22	0.28	0.17	1.7
1	0.19	0.34	0.16	1.3
2	0.18	0.33	0.21	0.9
3	0.18	0.34	0.16	1.1
4	0.17	0.24	0.28	-0.7
5	0.18	0.30	0.27	0.2

*Note.* The last column lists  $Q = (f_{\text{GORES}}^{\text{inf}} - f_{\text{GORES}}^{\text{bsp}})/(f_{\text{GORES}}^{\text{inf}} - f_{\text{GORES}}^{\text{vir}})$ , which measures the effectiveness of quenching of the backsplash population relative to the infall and virial ones. The best-fitting Scheme 3 is highlighted in bold.

With the radially dependent model of the GORES fraction with equal quenching scale radii, again with Scheme 3, the fraction of GORES in the backsplash population at  $r = R_v$  is intermediate between those of the infalling and virialized populations, although closer to the virialized one (top panel of Fig. 17).

Table 5 displays the fraction of GORES at the surface of the virial sphere ( $r = R_v$ ) for the better-fitting radially varying models with free quenching radii. The backsplash quenching factor,  $Q = (f_{\text{GORES}}^{\text{inf}} - f_{\text{GORES}}^{\text{bsp}})/(f_{\text{GORES}}^{\text{inf}} - f_{\text{GORES}}^{\text{vir}})$ , should lie between 0 (no quenching: backsplash and infall have the same GORES fraction at a given radius) and 1 (full quenching: backsplash and virial have the same GORES fraction at a given r). The values above unity imply that the fraction of GORES in the backsplash population lying on the virial sphere is lower than the corresponding fraction of the virial population at the same location. This leads to the unphysical result that on the virial sphere backsplash galaxies are more passive than the virialized ones.

For our best-fitting Scheme 3, Q = 1.1 is just above unity, i.e. the backsplash and virialized populations on the virial sphere have very similar fractions of GORES,<sup>6</sup> while for the second best fitting Scheme 2, Q = 0.9 (see bottom panel of Fig. 17). On the other hand, for Scheme 4, Q is much smaller than 0: the fraction of GORES for galaxies lying on the virial sphere is higher for the backsplash galaxies than for the infall population. This again appears to be an unphysical result, which leads us to disregard Scheme 4 (which fits the data worse than Scheme 3, but with only marginal significance; see Table 4). This suggests that *the backsplash galaxies are strongly quenched relative to the infalling ones*, at least half the way from infalling to virialized galaxies at  $r = R_v$  (for Scheme 5, which is only marginally consistent with the data) to nearly fully quenched to the level of virialized galaxies (Schemes 3 and 2).

In contrast, using hydrodynamical cosmological simulations of the Local Group, Knebe et al. (2011) find that the luminosity function of backsplash galaxies is similar to that of the infalling galaxies and that the total mass within the radius containing the outermost stars divided by the luminosity is higher for infalling galaxies than for backsplash galaxies. The first result suggests little quenching of star formation as dwarf galaxies cross through the virial sphere of the Milky Way, while the second result suggests inverse quenching, that is that backsplash galaxies have higher luminosity per unit mass. However, star formation in  $10^{12} \, M_{\odot}$  galaxies falling into  $10^{14} \, M_{\odot}$  clusters should be similar to the quenching of star formation in dwarf galaxies of mass  $10^{10} \, M_{\odot}$  falling into the Milky Way virial sphere. What is more surprising is that fig. 5 of Knebe et al. (2011) indicates that galaxies in the virialized class have higher luminosity for

given internal velocity dispersion than galaxies in the infall class. Analysing the residuals of luminosity versus velocity dispersion relative to the mean global trend, we deduce that the higher luminosity of virialized galaxies compared to infall galaxies of the same velocity dispersion is statistically significant (with 99.9 per cent confidence using a KS test, and by typically two magnitudes). The backsplash population on the other hand is intermediate but not inconsistent with either the virial or the infall populations. The higher luminosities of the virial population of simulated dwarfs appear to contradict the observed positive luminosity–radius correlation found for luminous virialized galaxies with cluster-centric distances above  $\gtrsim 0.1R_v$  from their parent rich clusters (Adami et al. 1998).

The quest for the physical mechanism responsible for this quenching is beyond the scope of this paper, be it tidal stripping, ram-pressure stripping, harassment, starvation or pre-processing in groups. For instance, van den Bosch et al. (2008) argue that the lack of dependence of galaxy colour on cluster mass is evidence against the dominance of ram-pressure stripping and harassment.

We note that in our two best-fitting models (Schemes 3 and 2), the fraction of GORES in infalling galaxies is independent of their physical distance to the cluster. Our best-fitting model requires a scheme (like our Scheme 3) where galaxies within the virial sphere with high outgoing velocities are equivalent to the infalling galaxies within the same volume (those with strong negative velocities). This together with the comparison of GORES fraction at the virial radius suggests that the star formation in galaxies is quenched on a timescale comparable to the time taken for a galaxy to bounce out of a cluster and reach its virial radius. This time-scale corresponds to about 1 to 2 Gyr, which is very close to the lookback time to which our joint  $H\delta$ – $D_n$ 4000 GORES diagnostic is most sensitive (Section 2.3). Correcting for this lookback time, one concludes that star formation in a galaxy is nearly fully quenched in a single passage through the cluster.

Of course, there will be a variety of orbital pericentres for the infalling galaxies, leading to different degrees of quenching. But the typical high elongations found for orbits in Acold dark matter simulations (Ghigna et al. 1998) suggest that orbits with large pericentres will be rare.

We find that  $17.9 \pm 0.4$  per cent<sup>7</sup> of the galaxies within the *virial* cylinder (projected radii  $R < R_v$  and  $|v_{LOS}| < 3\sigma_v$ ) are GORES. This can be compared to the fraction of blue galaxies within the virial cylinder: we find that  $20.3 \pm 0.4$  per cent of the galaxies with  $R < R_v$  are 0.2 mag bluer than the RS (this fraction is fairly consistent with the ~78 per cent of SDSS cluster galaxies that Yang, Mo & van den Bosch 2008 find to lie on the RS). So, within the virial cylinder, the fraction of GORES is roughly  $88 \pm 0.5$  per cent of the fraction of blue galaxies, although some blue galaxies are not GORES and some GORES are not blue (Mahajan & Raychaudhury 2009).

In comparison, using the same cosmological simulation as in the present article, Mamon et al. (2010) recently showed that  $23 \pm 1$  per cent of galaxies within the virial cylinder are outside the virial sphere. As discussed by Mamon et al., the match between fraction of blue galaxies and fraction of cluster interlopers is probably a coincidence since some galaxies within the cluster sphere must be blue and some interlopers must be RS galaxies in projected groups.

<sup>&</sup>lt;sup>6</sup> Forcing Q = 1 in our fit leads to  $\chi^2_{\nu}$  only 0.003 higher for Scheme 3.

<sup>&</sup>lt;sup>7</sup> The errors here and below on the fractions of GORES are binomial and do not incorporate cosmic variance.

Table 6. Fractions of GORES.

Model	Scheme	Virial cylinder	Virial sphere	Virial class	Infall class	Backsplash class
Range		$R < R_v$	$r < R_v$	$(r < R_v)$	$R < 2R_v$	$R < 2R_v$
f = cst	3	0.17	0.12	0.10	0.34	0.23
$a_{\rm v} = a_{\rm i} = a_{\rm b}$	3	0.17	0.13	0.11	0.33	0.22
f(r)	1	0.17	0.13	0.12	0.34	0.19
f(r)	2	0.17	0.13	0.11	0.33	0.21
$f(\mathbf{r})$	3	0.17	0.13	0.11	0.34	0.19
f(r)	4	0.17	0.13	0.11	0.32	0.26
f(r)	5	0.17	0.13	0.11	0.34	0.27
SDSS	-	0.176	-	-	-	-

*Notes.* The last six models are our best-fitting ones ( $\chi_{\nu}^2 \leq 1.6$ ). The best-fitting scheme 3 is highlighted in bold. Note that the fractions of GORES within the virial cylinder slightly underestimate the observed fraction, but are consistent with it within the 1 per cent errors.

With our models, we can estimate the fraction of GORES within the *virial sphere* using the average of the mean fractions f(r)(Fig. 17) weighted by  $r^2$  times the galaxy number density profile, v(r) measured in our cosmological simulation. Results given in Table 6 indicate that for our three best-fitting models (see Table 4), *the fraction of GORES within the virial sphere is*  $13 \pm 1$  per cent. We then predict the fraction of blue galaxies within the virial sphere to be  $13/0.88 = 15 \pm 2$  per cent.

Now, while most galaxies within the virial sphere are part of the virial population, some are infalling (Schemes 1 to 3) or backsplash (Scheme 2). Yet, we can proceed even further and estimate the fraction of GORES among the virialized class, again using our cosmological simulation to perform the calibration. As seen in Table 6, the fraction of GORES among the virialized class is not zero, but typically  $11 \pm 1$  per cent. We also predict that the fraction of blue galaxies among the virialized population is  $11/0.88 = 12.5 \pm 2$  per cent. Moreover, Table 6 indicates that the fraction of GORES among the  $R < 2R_v$  infall galaxies is  $34 \pm 1$  per cent while among the backsplash galaxies the fraction of GORES is typically  $20 \pm 4$ per cent (for Schemes 3, 2 and 1) or perhaps as high as  $27 \pm 4$  per cent (Schemes 4 and 5).

The presence of GORES among the virialized class might be caused by those low-metallicity galaxies for which our  $H\delta - D_n 4000$  estimator of recent efficient star formation has a lookback time as long as 3 Gyr (Section 2.3). Alternatively, these GORES might be the consequence of star formation triggered by rapid flybys and rare ongoing direct (satellite–satellite) mergers in clusters.

Finally, our statistics lead us to conclude that a fraction  $0.13 \times (1 - 0.23)/0.18 = 0.56$  of the GORES within the virial cylinder is within the virial sphere, so that  $44 \pm 2$  per cent of GORES within the virial cylinder are outside the virial sphere, for all good-fitting schemes.

Note that the asymptotic behaviour of the best-fitting models disagrees with the field value by at least 10 per cent. One may think that this discrepancy may be due to a different set of environmentdependent phenomenon become efficient in modulating galaxy properties at  $R > 2R_v$  from the centres of clusters, or to the oversimplified models we used to deproject the fraction of GORES. However, according to the cosmological simulation we analysed here, the high absolute LOS velocity galaxies at  $R > R_v$  ought to lie at similar very far distances from the cluster centres (12 virial radii; see Fig. 15) as the field galaxies. Therefore, the discontinuity in the observed fraction of GORES between these galaxies and the field is puzzling and remains an open question.

### 5.5 Epilogue

In summary, our work shows that the galaxy properties in and around clusters are functions of not only stellar mass and local environment (e.g. Haines et al. 2007; von der Linden et al. 2010), but also of absolute LOS velocity. With these velocities, it is then statistically feasible to segregate the infalling and backsplash galaxies at any cluster-centric radius, including cluster outskirts. This velocity modulation will be better seen in the properties of the relatively low mass galaxies, because they are the first ones to be influenced by any changes in their immediate environment (see Mahajan, Haines & Raychaudhury 2011 for such an effect seen in the nearby Coma cluster). It would be worthwhile to extend our analysis using other indicators of very recent star formation to (1) confirm our conclusion that the quenching of star formation occurs in a single passage through the cluster, and (2) assess the fraction of galaxies with very recent star formation among the virialized population. The survival of low-mass galaxies and of star formation in galaxies of all mass, as they pass through the cluster core, leads us to important issues that should also be addressed with high-resolution cosmological hydrodynamical simulations.

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## APPENDIX A: KOLMOGOROV-SMIRNOV STATISTICS

In this appendix, we present tables of probabilities, from the Kolmogorov–Smirnov test, that various sub-samples of different physical quantities arise from the same parent distributions (see Section 3).

**Table A1.** KS test probabilities for the null hypothesis that pairs of subsamples have distributions of  $M^*$  arising from the same parent distribution. Columns v1, v2 and v3 correspond to  $|v_{\text{LOS}}|/\sigma_v = 0-1$ , 1–2 and 2–3, respectively. Statistically significant differences between subsample pairs are highlighted in bold.

		$R/R_{\rm v} \le 0.5$		0.5	$5 < R/R_v \le 1$	1.0	1.0	$0 < R/R_v \leq$	1.5	1.5	$5 < R/R_v \le$	2.0	Field
	v1	v2	<i>v</i> 3	v1	v2	<i>v</i> 3	v1	v2	<i>v</i> 3	v1	v2	v3	
	1	2	3	4	5	6	7	8	9	10	11	12	
1	1.0E+00	7.3E-08	2.5E-09	4.2E-20	2.9E-20	1.6E-09	1.2E-12	1.8E-09	4.1E-08	2.7E-11	1.4E-10	8.5E-06	0.0E+00
2		1.0E + 00	1.7E - 02	3.1E-03	6.2E-06	9.9E-04	5.9E-03	6.1E-02	1.2E-03	2.1E-02	5.5E-02	6.5E-02	2.6E-13
3			1.0E + 00	1.7E-01	3.6E-01	3.6E-01	4.3E-02	1.2E-01	2.6E-01	3.6E-02	3.2E-01	7.3E-01	2.6E-01
4				1.0E + 00	2.8E-02	1.3E-01	2.1E-01	7.6E-01	2.3E-01	1.4E-01	8.8E-01	6.7E-01	5.6E-07
5					1.0E + 00	6.5E-01	2.5E - 02	8.8E-02	8.9E-01	3.3E-03	3.2E-02	6.4E-01	1.3E-01
6						1.0E + 00	3.8E-02	9.9E-02	7.8E-01	2.0E-02	7.9E-02	2.6E-01	1.8E-01
7							1.0E + 00	7.9E-01	1.0E-01	9.7E-01	5.8E-01	6.7E-01	2.6E-04
8								1.0E + 00	1.5E - 01	8.4E-01	7.9E-01	8.3E-01	5.4E-03
9									1.0E + 00	4.3E-02	9.9E-02	5.2E-01	4.3E-01
10										1.0E + 00	4.9E-01	7.0E-01	5.4E-06
11											1.0E + 00	9.1E-01	3.7E-03
12												1.0E+00	3.8E-01

Table A2. Same as Table A1, but with BCGs excluded.

		$R/R_{\rm v} \le 0.5$		0.5	$\delta < R/R_{\rm v} \leq 1$	1.0	1.0	$0 < R/R_{\rm v} \leq$	1.5	1.5	$5 < R/R_{\rm v} \le 2$	2.0	Field
	v1	v2	<i>v</i> 3	v1	v2	<i>v</i> 3	v1	v2	v3	v1	v2	<i>v</i> 3	
	1	2	3	4	5	6	7	8	9	10	11	12	
1	1.0E+00	5.2E-08	6.6E-10	1.5E-20	1.2E-21	1.2E-09	6.9E-15	9.0E-10	6.5E-09	2.0E-12	9.5E-11	3.9E-06	0.0E+00
2		1.0E + 00	9.2E-03	1.5E-03	1.7E-06	2.3E-04	8.9E-04	3.6E-02	5.1E-04	4.0E-03	3.8E-02	3.8E-02	3.9E-13
3			1.0E + 00	2.0E-01	4.3E-01	2.7E-01	9.8E-02	1.3E-01	2.5E-01	4.4E-02	2.2E-01	7.4E-01	3.4E-01
4				1.0E + 00	2.3E-02	6.3E-02	5.5E-01	7.6E-01	1.7E-01	3.0E-01	8.5E-01	6.5E-01	2.6E-06
5					1.0E + 00	6.9E-01	4.6E-02	1.0E-01	8.4E-01	5.4E-03	2.5E-02	6.7E-01	5.8E-01
6						1.0E + 00	6.7E-02	7.7E-02	7.3E-01	3.4E-02	4.1E-02	2.6E-01	1.5E-01
7							1.0E + 00	9.8E-01	1.0E-01	8.9E-01	8.1E-01	7.8E-01	4.5E-03
8								1.0E + 00	1.3E-01	8.9E-01	7.3E-01	8.7E-01	1.7E-02
9									1.0E + 00	5.2E-02	6.9E-02	4.5E-01	1.9E-01
10										1.0E + 00	4.9E-01	6.8E-01	5.8E-05
11											1.0E + 00	9.0E-01	8.2E-03
12												1.0E + 00	5.3E-01

**Table A3.** Same as Table A1, but for the difference between the  $(g - r)^{0.1}$  colour and the best-fitted RS.

		$R/R_{\rm v} \le 0.5$		0.5	$5 < R/R_{\rm v} \leq 1$	1.0	1.0	$0 < R/R_{\rm v} \leq$	1.5	1.5	$5 < R/R_{\rm v} \le 2$	2.0	Field
	v1	v2	<i>v</i> 3	v1	v2	<i>v</i> 3	v1	v2	v3	v1	v2	v3	
	1	2	3	4	5	6	7	8	9	10	11	12	
1	1.0E+00	1.2E-01	1.0E-04	5.9E-30	3.4E-29	1.3E-10	0.0E+00	0.0E+00	2.0E-29	0.0E+00	0.0E+00	9.0E-27	0.0E+00
2		1.0E + 00	1.7E - 02	1.5E-16	6.1E-17	1.8E-07	1.0E - 41	7.3E-41	6.2E-23	1.4E-45	8.4E-36	7.6E-20	0.0E+00
3			1.0E + 00	5.8E-05	4.6E-06	1.6E-02	1.2E-13	4.5E-16	1.8E-12	3.9E-15	2.5E-13	2.4E-08	0.0E+00
4				1.0E + 00	5.6E-02	3.3E-01	1.3E-11	1.2E-14	3.8E-10	2.2E-15	2.2E-11	1.1E-07	0.0E+00
5					1.0E + 00	8.1E-01	1.1E-04	1.6E-07	1.3E-06	5.4E-06	1.8E-05	1.0E-04	0.0E+00
6						1.0E + 00	2.4E-03	4.1E-05	6.1E-05	8.0E-04	9.9E-04	5.5E-03	4.9E-29
7							1.0E+00	1.1E-01	1.8E-02	6.1E-01	2.7E-01	1.0E-01	0.0E+00
8								1.0E+00	3.3E-01	1.3E-01	6.5E-01	3.6E-01	1.7E-23
9									1.0E+00	5.0E-02	1.5E-01	1.5E-01	3.0E-06
10										1.0E+00	8.1E-01	4.8E-01	0.0E+00
11											1.0E + 00	5.6E-01	1.4E-31
12												1.0E+00	1.9E-16

Table A4. Same as Table A1, but for SFR/M	Table A4.	Same as	Table A1.	but for	SFR/M <sup>3</sup>
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		$R/R_{\rm v} \leq 0.5$		0.5	$5 < R/R_v \le$	1.0	1.0	$0 < R/R_{\rm v} \leq$	1.5	1.5	$\delta < R/R_{\rm v} \leq 2$	2.0	Field
	v1	ν2	<i>v</i> 3	v1	v2	<i>v</i> 3	v1	v2	<i>v</i> 3	v1	v2	<i>v</i> 3	
	1	2	3	4	5	6	7	8	9	10	11	12	
1	1.0E+00	5.8E-04	1.0E-04	1.0E-26	8.1E-28	4.7E-12	0.0E+00	5.6E-45	1.1E-22	0.0E+00	1.8E-40	1.5E-21	0.0E+00
2		1.0E + 00	1.7E-02	1.0E-08	6.2E-13	1.3E-06	4.1E-25	1.1E-25	1.2E-16	2.1E-33	1.7E-21	1.2E-14	0.0E+00
3			1.0E + 00	3.4E-03	1.4E - 02	3.1E-02	1.5E-06	1.1E-07	7.5E-08	1.0E-07	2.5E-06	3.4E-06	1.6E-21
4				1.0E + 00	6.1E-02	8.4E-02	4.1E-07	1.6E-09	4.5E-09	2.3E-11	3.2E-08	7.9E-07	0.0E+00
5					1.0E + 00	4.7E-01	6.2E-04	1.1E - 04	6.1E-06	3.0E-05	3.4E-04	1.8E-04	1.4E-26
6						1.0E + 00	9.1E-03	2.3E-02	6.3E-03	4.1E-03	1.6E-02	1.1E-02	5.5E-07
7							1.0E + 00	1.5E-01	2.5E-03	3.0E-01	7.3E-02	2.9E-02	1.9E-17
8								1.0E + 00	9.7E-02	4.6E-01	5.2E-01	4.5E-01	2.9E-05
9									1.0E + 00	1.7E-02	8.9E-02	7.5E-01	1.1E-01
10										1.0E + 00	4.3E-01	1.9E-01	2.7E-14
11											1.0E + 00	6.0E-01	1.8E-08
12												1.0E + 00	2.9E-03

**Table A5.** Same as Table A1, but for  $H\delta$ .

		$R/R_{\rm v} \leq 0.5$		0.5	$5 < R/R_v \le 1$	1.0	1.0	$0 < R/R_v \leq$	1.5	1.5	$5 < R/R_{\rm v} \le 2$	2.0	Field
	v1	v2	<i>v</i> 3	v1	v2	<i>v</i> 3	v1	v2	<i>v</i> 3	v1	v2	<i>v</i> 3	
	1	2	3	4	5	6	7	8	9	10	11	12	
1	1.0E+00	1.7E-06	7.0E-09	0.0E+00	0.0E+00	6.1E-22	0.0E+00	0.0E+00	8.9E-37	0.0E+00	0.0E+00	1.1E-27	0.0E+00
2		1.0E + 00	6.6E-04	1.4E-18	2.6E-24	9.6E-14	3.7E-38	7.7E-39	4.4E-25	1.5E-39	6.2E-35	1.6E-17	0.0E+00
3			1.0E + 00	6.0E-03	8.5E-05	2.8E-03	7.3E-07	2.8E-10	2.0E-09	2.7E-06	9.4E-08	1.2E-04	4.4E-36
4				1.0E + 00	2.4E-03	5.8E-03	7.2E-07	1.9E-11	4.4E-11	1.3E-08	3.6E-09	1.4E-04	0.0E+00
5					1.0E + 00	7.8E-01	2.0E-01	2.4E-04	2.7E-06	5.5E-02	1.3E-02	7.8E-02	1.6E-42
6						1.0E+00	2.1E-01	1.6E-02	6.4E-04	2.2E-01	7.7E-02	1.7E-01	1.0E-12
7							1.0E + 00	3.6E-02	3.6E-04	1.0E-01	3.1E-01	5.7E-01	6.1E-42
8								1.0E + 00	1.6E-01	1.8E-02	3.2E-01	4.3E-01	5.4E-13
9									1.0E + 00	9.9E-04	1.0E-02	6.6E-02	1.3E-02
10										1.0E + 00	4.1E-01	8.6E-01	1.0E-43
11											1.0E + 00	9.8E-01	9.1E-19
12												1.0E + 00	7.3E-09

**Table A6.** Same as Table A1, but for  $D_n$ 4000.

	$R/R_{ m v} \le 0.5$			$0.5 < R/R_v \le 1.0$			$1.0 < R/R_v \le 1.5$			$1.5 < R/R_{\rm v} \le 2.0$			Field
	v1	v2	<i>v</i> 3	v1	v2	<i>v</i> 3	v1	v2	<i>v</i> 3	v1	v2	<i>v</i> 3	
	1	2	3	4	5	6	7	8	9	10	11	12	
1	1.0E+00	3.5E-09	5.1E-09	0.0E+00	0.0E+00	9.8E-15	0.0E+00	0.0E+00	8.8E-35	0.0E+00	0.0E+00	1.2E-27	0.0E+00
2		1.0E + 00	1.1E - 04	3.1E-23	1.9E-23	8.4E-09	4.7E-40	6.2E-38	1.9E-24	1.4E-45	1.3E-35	5.2E-18	0.0E+00
3			1.0E + 00	8.1E-03	7.2E-05	4.7E-02	7.4E-07	9.2E-09	5.7E-09	9.0E-07	3.7E-08	8.2E-05	1.2E-34
4				1.0E + 00	2.2E-02	1.0E - 01	1.2E-06	4.8E-09	2.5E-07	1.6E-11	5.6E-09	1.9E-05	0.0E+00
5					1.0E + 00	2.8E-01	6.3E-02	8.2E-04	9.8E-05	1.0E-03	5.8E-03	1.7E - 02	0.0E+00
6						1.0E + 00	1.4E-02	5.6E-04	5.1E-05	1.7E - 02	5.2E-03	9.5E-02	1.1E-17
7							1.0E + 00	7.1E-02	7.5E-03	1.1E-01	6.9E-02	1.8E-01	0.0E+00
8								1.0E+00	2.1E-01	1.2E-01	9.4E-01	1.0E-01	7.4E-17
9									1.0E + 00	2.1E-02	1.1E-01	4.9E-02	1.3E-03
10										1.0E+00	3.5E-01	5.9E-01	2.5E-38
11											1.0E + 00	1.2E-01	1.5E-21
12												1.0E + 00	4.1E-10

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