

DEVELOPMENTS IN GEOTECHNICAL ENGINEERING 47

# THEORETICAL FOUNDATION ENGINEERING

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(5.129).

Example 5.11. Refer to Example 5.10. Other quantities remaining the same, if  $H=3$  m determine  $\beta_{cr}$ .

Solution.

$$\theta = \cos^{-1} \left[ 1 - \left( \frac{H\gamma}{\sigma} \right) \frac{(1 - \sin\phi)}{2 \tan^2(45 + \phi/2)} \right]$$

So

$$\begin{aligned} \theta &= \cos^{-1} \left[ 1 - \frac{(3)(17.5)}{16} \frac{1 - \sin 12^\circ}{2 \tan^2(45 + 12/2)} \right] \\ &= \cos^{-1} \left[ 1 - \frac{(3.281)(0.792)}{3.05} \right] = \cos^{-1}(0.148) = 81.49^\circ \end{aligned}$$

However

$$\theta_c = 90 - \phi = 90 - 12 = 68^\circ$$

So,  $\theta > \theta_c$ . Now,  $\theta = 81.49^\circ = \theta''$ . Substituting  $\phi = 12^\circ$  and  $\theta'' = 81.49^\circ$  in Eq. (5.130) gives

$$\begin{aligned} \beta_{cr} &= \tan^{-1} \left\{ \frac{(3)(17.5)}{16} \times \right. \\ &\quad \left. \frac{\cos 12(1 - \sin 12)}{2(1 + \sin 12) \left[ \left( \frac{\pi}{180} 81.49 \right) - \sin 81.49 - \pi/2 + \left( \frac{\pi}{180} 12 \right) + \cos 12^\circ \right]} \right\} \\ &= 87^\circ \end{aligned}$$

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