Thermodynamic Properties of Propane. III. A Reference Equation of State for Temperatures from the Melting Line to 650 K and Pressures up to 1000 MPa

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An equation of state is presented for the thermodynamic properties of propane that is valid for temperatures from the triple point temperature (85.525 K) to 650 K and for pressures up to 1000 MPa. The formulation can be used for the calculation of all thermodynamic properties, including density, heat capacity, speed of sound, energy, and saturation properties. Comparisons to available experimental data are given that establish the accuracy of calculated properties. The approximate uncertainties of properties calculated with the new equation are 0.01 % to 0.03 % in density below 350 K, 0.5 % in heat capacities, 0.03 % in the speed of sound between (260 and 420) K, and 0.02 % in vapor pressure above 180 K. Deviations in the critical region are higher for all properties except vapor pressure.

Introduction

Characteristics of Propane. Propane (C₃H₈, R-290) is the third alkane in the saturated hydrocarbon (paraffin) series starting with methane. Propane is a gas at atmospheric conditions and can be compressed into a liquid for transportation. As a commodity in this state, it is often termed liquefied petroleum gas (LPG) and contains small amounts of propylene, butane, and butylene. Because it can be stored as a liquid at atmospheric temperatures, propane has a huge advantage over natural gas, which must be highly compressed to store the same amount of energy in a similar sized tank.

Propane is extracted from natural gas processing or from the removal of light hydrocarbons in oil recovery. Propane is nontoxic but is considered an asphyxiate in large doses. It is used in many applications, primarily as a fuel, but also as a propellant or chemical feedstock in the production of other chemicals, including propyl alcohol. It is the third most common vehicle fuel after gasoline and diesel and has a lower greenhouse gas emission than that typical of motor fuels.

Propane is becoming popular as a refrigerant as traditional refrigerants are being replaced due to their ozone depletion potential or global warming potential. Propane is one of the so-called "natural refrigerants", a group that also includes water, carbon dioxide, and ammonia. It can be used in its pure form or mixed with isobutane. Some applications mix propane with other refrigerants to improve the oil solubility.

With so many industrial and scientific uses, propane has been widely measured to characterize its chemical, thermal, caloric, and combustion properties. Numerous experimental studies have been carried out over the full temperature and pressure range of nearly all applications. In the thermodynamics arena, experimental data are available for density, vapor pressure, speed of sound, virial coefficients, heat capacities, enthalpies, and enthalpies of vaporization as given in refs 1 to 186. These data

have been used over the last century to develop many equations of state to describe the gas phase, the liquid phase, or the full surface of state of propane. The work presented here represents the latest development on equations of state for propane and is part of an international collaboration between the Ruhr-University in Bochum, the Helmut-Schmidt University of the Federal Armed Forces in Hamburg, and the National Institute of Standards and Technology in Boulder to characterize the properties of ethane (Bücker and Wagner¹⁸⁷), propane (this work), and the butanes (Bücker and Wagner¹⁸⁸). This work relies heavily on new measurements from these three laboratories. Pressure-density-temperature and vapor pressure measurements were made by Glos et al. 48 in Bochum and by McLinden¹²⁰ in Boulder; heat capacities and derived vapor pressures were made by Perkins et al. 139 in Boulder; and speed of sound measurements were made by Meier¹²¹ in Hamburg. These data together with other selected literature data form the basis of the new equation of state. The physical characteristics and properties of propane are given in Table 1.

Equations of State. Equations of state are used to calculate the thermodynamic properties of pure fluids and mixtures and are often expressed as a function of the pressure with independent variables of temperature and density or as a function of the Helmholtz energy with independent variables of temperature and density. Equations expressed in terms of the Helmholtz energy have the advantage that all thermodynamic properties are simple derivatives of the equation of state, and thus only one equation is required to obtain any thermodynamic property, including those that cannot be measured, such as entropy. The location of the saturation boundaries requires an iterative solution of the physical constraints on saturation (the so-called Maxwell criteria, i.e., equal pressures and Gibbs energies at constant temperature for phases in equilibrium). Equations expressed in terms of pressure require integration to calculate caloric properties such as heat capacities and sound speeds.

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Table 1. Physical Constants and Characteristic Properties of **Propane**

| symbol | quantity | value |
|-------------------|--|---|
| R | molar gas constant | 8.314 472 J·mol ⁻¹ ·K ⁻¹ |
| M | molar mass | 44.09562 g·mol ⁻¹ |
| $T_{\rm c}$ | critical temperature | 369.89 K |
| $p_{\rm c}$ | critical pressure | 4.2512 MPa |
| $ ho_{ m c}$ | critical density | 5.00 mol·dm ⁻³ |
| T_{tp} | triple point temperature | 85.525 K |
| $p_{ m tp}$ | triple point pressure | 0.00017 Pa |
| $ ho_{ m tpv}$ | vapor density at the triple point | $2.4 \cdot 10^{-10} \text{ mol} \cdot \text{dm}^{-3}$ |
| $ ho_{ m tpl}$ | liquid density at the triple point | 16.626 mol·dm ⁻³ |
| $T_{\rm nbp}$ | normal boiling point temperature | 231.036 K |
| $ ho_{ m nbpv}$ | vapor density at the normal boiling point | 0.0548 mol·dm ⁻³ |
| $ ho_{ m nbpl}$ | liquid density at the normal boiling point | 13.173 mol·dm ⁻³ |
| T_0 | reference temperature for ideal gas properties | 273.15 K |
| p_0 | reference pressure for ideal gas properties | 0.001 MPa |
| h_0^0 | reference ideal gas enthalpy at T_0 | 26148.48 J·mol ⁻¹ |
| s_0^0 | reference ideal gas entropy at T_0 and p_0 | 157.9105 J⋅mol ⁻¹ ⋅K ⁻¹ |

Equations of state are generally composed of an ideal gas contribution and a real gas contribution. The ideal gas portion is composed of the ideal gas law, $p = \rho RT$ (where p is pressure, ρ is molar density, T is temperature, and R is the gas constant), and an equation to describe the isobaric heat capacity at zero pressure. The real gas is generally composed of an analytical equation with multiple terms, with typical equations comprising 10 to 50 terms. High accuracy equations have often required more terms than those of low accuracy; however, the most recent equation by Lemmon and Jacobsen 189 for the properties of pentafluoroethane (R-125) introduced a modified functional form that allowed the magnitude of the exponents on temperature to be reduced dramatically. This allowed fitting the experimental data with fewer terms but with high accuracy. The work on R-125 was the forerunner for the development of the propane equation presented here.

Most equations of state that are explicit in the Helmholtz energy are made up of a combination of up to four different types of terms. The two most common are simple polynomial terms, $\rho^d T^t$ (where d and t are exponents in the polynomial terms), polynomial terms with the addition of an exponential part, $\rho^d T^t \exp(-\rho^l)$, Gaussian bell-shaped terms (which will be explained later), and nonanalytical terms that are present in only a few high accuracy equations and will not be discussed in this work. Further information is given by Span and Wagner. 190 Equations have almost always required high values of the exponent t to accurately calculate the properties of the fluid. These high values have led to some extremely unphysical behavior of the equation within the two-phase portion of the fluid. Although this area is not encountered in typical usage, it can cause problems with poorly written root solving routines and introduces false roots for two-phase states that appear to have a lower energy state and thus a more favorable state as compared with the true properties of the fluid. Various mixture models use states in the two-phase region of at least one of the pure fluid components in the calculation of the mixture properties, and in such applications, it is important that the twophase region be well behaved. The modification of the functional form in the R-125 work expanded the exponential terms to include a temperature dependency, $\rho^d T^t \exp(-\rho^l) \exp(-T^m)$. This final piece allowed much lower values on the exponent t, which resulted in a more physically correct functional form and removed the possibility of false two-phase state points.

The work on propane continued the research into a functional form that can more correctly represent the true physical properties. The new term introduced in the R-125 equation was not used in this work, but rather emphasis was placed on redefining the usage of the Gaussian bell-shaped terms so that they would describe the change in the critical region, allowing the polynomial terms to model only the vapor and liquid states away from the critical region. This produced a similar effect in that the magnitude of the exponent t was greatly reduced.

Although pure compounds generally exist as an identifiable fluid only between the triple point temperature at the low extreme and the dissociation limit at the other extreme, every effort has been made to shape the functional form of the equation of state so that it extrapolates well to extreme values of temperature, pressure, and density. For example, at low temperatures, virial coefficients should approach negative infinity, and at extremely high temperatures and densities, isotherms should not cross one another and pressures should not be negative. Although such conditions exceed the physical limits of a normal fluid, there are applications that may extend into such regions, and the equation of state should be capable of describing these situations. Calculated properties shown here at extreme conditions that are not defined by experiment are intended only for qualitative examination of the behavior of the equation of state, and reliable uncertainty estimates cannot be established in the absence of experimental data.

Propane has a very low reduced triple point temperature $(T_{tp}/$ $T_{\rm c}$) of 0.23 that makes it a prime candidate for corresponding states applications. There are only a handful of other fluids, such as 1-butene, that have slightly lower values. In addition, a substantial quantity of high accuracy measurements is available for propane, allowing a reference equation of state to be developed. This reference equation of state can then be used in corresponding states models (described below) to predict properties of a host of other fluids. Since nearly all other fluids have reduced triple point temperatures higher than propane, all calculations for other fluids will be at states where experimental data were used to develop the propane surface.

Phase Equilibria of Propane

The single most important state of any fluid in the development of equations of state is the critical point. This point becomes the reducing parameter for the equation and defines liquid and vapor states, as well as supercritical states that behave like gases (when the density is less than the critical density) and like liquids (when the density exceeds the critical density). Nearly all fluids show similar behavior when their properties are scaled by the critical parameters. The law of corresponding states uses this aspect to predict properties for any fluid by mapping the surface of an unknown substance onto that for a well-known substance. The prediction can be improved as additional experimental data become available.

The triple point of a fluid defines the lowest temperature at which most substances can remain in the liquid state. Below this temperature only solid and gas states are possible in most applications, and the boundary between these states is known as the sublimation line. The melting (or freezing) line describes the boundary between the liquid and solid states for temperatures above the triple point. Equations of state such as that described here can calculate the properties at the melting point in the liquid phase but cannot calculate properties of the solid phase.

Critical and Triple Points. Critical parameters for propane have been reported by numerous authors and are listed in Table 2 (temperatures are given on ITS-90). The difficulties in the

Table 2. Summary of Critical Point Parameters

| | | $T_{ m c}$ | p_{c} | $ ho_{ m c}$ |
|--|------|------------|------------------|----------------------|
| author | year | K | MPa | mol∙dm ⁻³ |
| Abdulagatov et al. ² | 1996 | 369.96 | | 5.044 |
| Abdulagatov et al. ³ | 1995 | 369.948 | | 4.995 |
| Ambrose and Tsonopoulos ⁵ | 1995 | 369.83 | 4.248 | 4.989 |
| Barber ⁸ | 1964 | 369.693 | 4.261 | 5.13 |
| Barber et al.9 | 1982 | 369.995 | 4.26 | 5.063 |
| Beattie et al. 12 | 1935 | 369.934 | 4.2567 | 5.13 |
| Brunner ¹⁵ | 1985 | 369.955 | 4.243 | |
| Brunner ¹⁶ | 1988 | 369.885 | 4.26 | |
| Chun et al. ²⁵ | 1981 | 369.695 | 4.261 | 5.128 |
| Clegg and Rowlinson ²⁸ | 1955 | 369.784 | 4.2486 | 4.92 |
| Deschner and Brown ³⁶ | 1940 | 369.974 | 4.2658 | 5.08 |
| Glowka ⁴⁹ | 1972 | 369.725 | 4.3529 | 5.025 |
| Gomez-Nieto and Thodos ⁵¹ | 1977 | 369.945 | 4.2567 | |
| Hainlen ⁵⁷ | 1894 | 375.124 | 4.9143 | |
| Higashi ⁶⁴ | 2004 | 369.818 | 4.2465 | 5.148 |
| Holcomb et al.70 | 1995 | 369.77 | 4.244 | 4.996 |
| Honda et al. ⁷² | 2008 | 370.01 | 4.26 | 5.035 |
| Horstmann et al. ⁷³ | 2001 | 369.7 | 4.25 | |
| Jou et al. ⁸⁰ | 1995 | 369.75 | 4.27 | |
| Kay ⁸⁵ | 1964 | 369.924 | 4.2557 | |
| Kay and Rambosek ⁸⁶ | 1953 | 369.79 | 4.2492 | 5.122 |
| Kratzke ⁹⁸ | 1980 | 369.775 | 4.239 | |
| Kratzke ⁹⁷ | 1983 | 369.825 | 4.246 | 4.955 |
| Kreglewski and Kay ¹⁰⁰ | 1969 | 369.994 | 4.2603 | 5.125 |
| Kuenen ¹⁰² | 1903 | 370.124 | 4.3468 | |
| Lebeau ¹⁰⁶ | 1905 | 370.624 | 4.5596 | |
| Maass and Wright ¹¹⁴ | 1921 | 368.723 | | |
| Matschke and Thodos116 | 1962 | 369.862 | 4.2568 | |
| Matteson ¹¹⁷ | 1950 | 369.935 | 4.2568 | 4.976 |
| Mousa ¹²⁷ | 1977 | 369.715 | 4.2537 | 4.853 |
| Mousa et al. 128 | 1972 | 369.715 | 4.2537 | 4.853 |
| Olszewski ¹³² | 1895 | 370.124 | 4.4583 | |
| Opfell et al. 133 | 1956 | 369.946 | 4.2548 | 4.987 |
| Reamer et al. 144 | 1949 | 369.957 | 4.2568 | 5.003 |
| $Roof^{148}$ | 1970 | 369.797 | 4.2492 | |
| Sage and Lacey ¹⁵⁰ | 1940 | 369.679 | 4.2885 | 5.272 |
| Sage et al. 151 | 1934 | 373.235 | 4.4354 | 5.268 |
| Scheeline and Gilliland ¹⁵⁴ | 1939 | 372.013 | 4.3851 | |
| Sliwinski ¹⁶¹ | 1969 | 369.816 | | |
| Thomas and Harrison ¹⁶⁸ | 1982 | 369.825 | 4.2471 | 4.955 |
| Tomlinson ¹⁷⁰ | 1971 | 369.797 | | 4.914 |
| Yasumoto et al. ¹⁷⁸ | 2005 | 369.84 | 4.247 | 4.898 |
| Yesavage et al. 180 | 1969 | 369.957 | 4.2541 | |
| this work | 2009 | 369.89 | 4.2512 | 5.00 |
| | | | | |

experimental determination of the critical parameters and impurities in the samples cause considerable differences among the results obtained by the various investigators. The critical density is difficult to determine accurately by experiment because of the infinite compressibility at the critical point and the associated difficulty of reaching thermodynamic equilibrium. Therefore, reported values for the critical density are often calculated by extrapolation of rectilinear diameters with measured saturation densities or by correlating single-phase data close to the critical point.

Figures 1, 2, and 3 show the critical temperature, pressure, and density as a function of the year that they were published. It is interesting to note how the differences between the reported values and the true critical point cannot be described as a function of the year published. With the availability of new high accuracy density data in the critical region, we allowed the reducing parameters (critical point) of the equation of state to be determined simultaneously with the other coefficients and exponents in the equation (as explained later). This is one of the first successful attempts to accurately derive the critical temperature and density solely from fitting experimental data for both the single phase and saturated states of a substance during the fitting process (also see Schmidt and Wagner¹⁹¹). Other such equations used critical parameters taken from a single experimental source. During many months of fitting, the range of the fitted values for the reducing parameters was

monitored closely. For temperature, it ranged from (369.86 to 369.92) K but was most stable around 369.89 K. This latter value was chosen as the critical temperature of propane. The critical density was also monitored closely and stayed remarkably centered around a value of 5.00 mol·dm⁻³, which was taken as the final value for the critical point. The critical pressure was determined from the final equation of state as a calculated point at the critical temperature and density. The resulting values of the critical properties are

$$T_c = (369.89 \pm 0.03) \,\mathrm{K}$$
 (1)

$$\rho_{\rm c} = (5.00 \pm 0.04) \,\text{mol} \cdot \text{dm}^{-3}$$
 (2)

and

$$p_c = (4.2512 \pm 0.005) \,\text{MPa}$$
 (3)

where all uncertainties are estimated as 2σ combined values. These values should be used for all property calculations with the equation of state.

Figure 4 shows calculations of the saturation properties from the equation of state very close to the critical point. The rectilinear diameter (the average of the saturated liquid and vapor densities) is also shown to be linear on this scale as it approaches the critical density value of 5.00 mol·dm⁻³ (as expected). In recent work on equations of state, including some of the equations in the work of Lemmon and Span, 192 where equations of state were presented for 20 different fluids, the shape of the rectilinear diameter was checked to ensure that it was linear in the critical region. Cases where this line curved to the left or right indicated incorrect representation of the critical region properties, and either the critical density was modified or the values of the saturation states were changed until the rectilinear diameter was linear. This was especially important for fluids with limited or low accuracy data in the critical region because the high flexibility in the equation resulted in properties that were often incorrect. Adjusting the saturation lines and critical density so that the rectilinear diameter was linear resulted in much better representation of the critical properties, as is shown in this

The triple point temperature of propane was measured by Perkins et al. 139 by slowly applying a constant heat flux to a frozen sample contained within the cell of an adiabatic calorimeter and noting the sharp break in the temperature rise, resulting in

$$T_{\rm tp} = 85.525 \,\mathrm{K}$$
 (4)

Pavese and Besley¹⁹³ also measured the triple point temperature and reported a value of 85.528 K. The triple point pressure is extremely low and very difficult to measure directly, and thus it was calculated from the equation of state with a value of p_{tn} = 0.00017 Pa.

Vapor Pressures. The boundaries between liquid and vapor are defined by saturation states, and ancillary equations can be used to give good estimates. These ancillary equations are not required when a full equation of state is available since application of the Maxwell criteria to the equation of state can yield the saturation states. This criteria for a pure fluid requires finding a state in the liquid and a state in the vapor that have the same temperature, pressure, and Gibbs energy. The ancillary equations can be used to give close estimates for the pressure and densities required in the iterative procedure to find the saturation states.

Table 3 summarizes the available experimental data for propane, including vapor pressures. Data labeled as "TRC" were

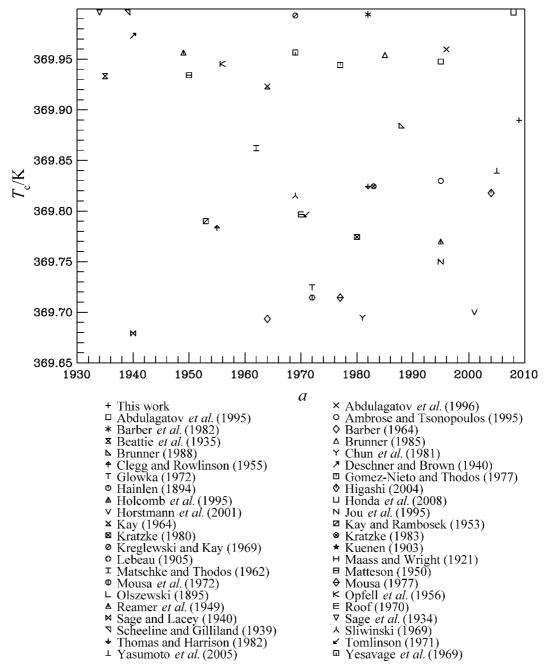


Figure 1. Reported critical temperatures T_c of propane as a function of the year a published.

taken from Frenkel et al.194 and are explained in the data comparison section. The vapor pressure can be represented with the ancillary equation

$$\ln\left(\frac{p_{\sigma}}{p_{c}}\right) = \frac{T_{c}}{T} [N_{1}\theta + N_{2}\theta^{1.5} + N_{3}\theta^{2.2} + N_{4}\theta^{4.8} + N_{5}\theta^{6.2}]$$
(5)

where $N_1 = -6.7722$, $N_2 = 1.6938$, $N_3 = -1.3341$, $N_4 = -3.1876$, $N_5 = 0.94937$, $\theta = (1 - T/T_c)$, and p_σ is the vapor pressure. This equation is a modification of the equation first proposed by Wagner¹⁹⁵ in 1974. The original form of the equation has been used to model the vapor pressures for a large number of substances. The exponents on the first two terms are fixed by theory as explained by Wagner or by Lemmon and Goodwin. 196 In the modified form, the exponents on the last three terms are substance specific, and when accurate data are available, the exponents can be fitted nonlinearly to produce an equation with very low uncertainties. In this work, the values of the coefficients and exponents were determined simultaneously with nonlinear fitting techniques. The values of the critical parameters are given above in eqs 1 to 3.

Saturated Densities. Table 3 summarizes the saturated liquid and vapor density data for propane. The saturated liquid density can be represented by the ancillary equation

$$\frac{\rho'}{\rho_c} = 1 + N_1 \theta^{0.345} + N_2 \theta^{0.74} + N_3 \theta^{2.6} + N_4 \theta^{7.2}$$
 (6)

where $N_1 = 1.82205$, $N_2 = 0.65802$, $N_3 = 0.21109$, $N_4 = 0.21109$ 0.083973, $\theta = (1 - T/T_c)$, and ρ' is the saturated liquid density. The saturated vapor density can be represented by the equation

$$\ln\left(\frac{\rho''}{\rho_{\rm c}}\right) = N_1 \theta^{0.3785} + N_2 \theta^{1.07} + N_3 \theta^{2.7} + N_4 \theta^{5.5} +$$

$$N_5\theta^{10} + N_6\theta^{20}$$
 (7)

where $N_1 = -2.4887$, $N_2 = -5.1069$, $N_3 = -12.174$, $N_4 = -30.495$, $N_5 = -52.192$, $N_6 = -134.89$, and ρ'' is the saturated vapor density. Values calculated from the equation of state with the Maxwell criteria were used in developing eq 7. The values of the coefficients and exponents for eqs 6 and 7 were determined with nonlinear least-squares fitting techniques.

Functional Form of the Equation of State

Modern equations of state are often formulated with the Helmholtz energy as the fundamental property with independent variables of density and temperature

$$a(\rho, T) = a^{0}(\rho, T) + a^{r}(\rho, T)$$
(8)

where a is the Helmholtz energy, $a^0(\rho,T)$ is the ideal gas contribution to the Helmholtz energy, and $a^{\rm r}(\rho,T)$ is the residual Helmholtz energy, which corresponds to the influence of intermolecular forces. Thermodynamic properties can be calculated as derivatives of the Helmholtz energy. For example, the pressure is

$$p = \rho^2 \left(\frac{\partial a}{\partial \rho}\right)_T \tag{9}$$

Additional equations are given in Appendix A.

In modern applications, the functional form is explicit in the dimensionless Helmholtz energy, α , with independent variables of dimensionless density and temperature. The form of this equation is

$$\frac{a(\rho, T)}{RT} = \alpha(\delta, \tau) = \alpha^{0}(\delta, \tau) + \alpha^{r}(\delta, \tau)$$
 (10)

where $\delta = \rho/\rho_c$ and $\tau = T_c/T$.

Properties of the Ideal Gas. The Helmholtz energy of the ideal gas is given by

$$a^0 = h^0 - RT - Ts^0 (11)$$

The ideal gas enthalpy is given by

$$h^{0} = h_{0}^{0} + \int_{T_{0}}^{T} c_{p}^{0} dT$$
 (12)

where c_p^0 is the ideal gas heat capacity. The ideal gas entropy is given by

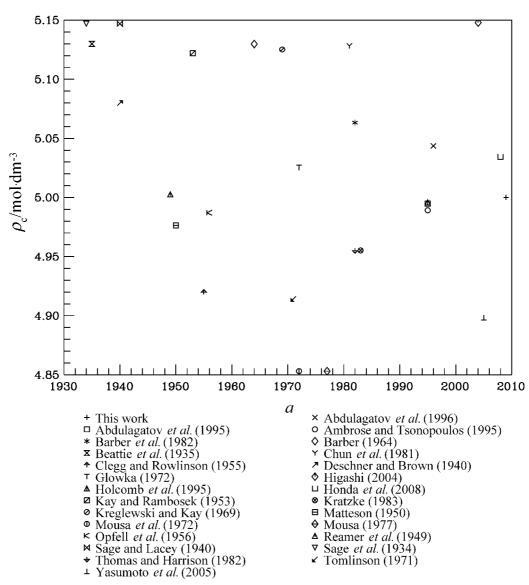


Figure 2. Reported critical densities ρ_c of propane as a function of the year a published.

$$s^{0} = s_{0}^{0} + \int_{T_{0}}^{T} \frac{c_{p}^{0}}{T} dT - R \ln \left(\frac{\rho T}{\rho_{0} T_{0}} \right)$$
 (13)

where ρ_0 is the ideal gas density at T_0 and p_0 [$\rho_0 = p_0/(T_0R)$], and T_0 and p_0 are arbitrary reference states. Combining these equations results in the following equation for the Helmholtz energy of the ideal gas

$$a^{0} = h_{0}^{0} + \int_{T_{0}}^{T} c_{p}^{0} dT - RT - T \left[s_{0}^{0} + \int_{T_{0}}^{T} \frac{c_{p}^{0}}{T} dT - R \ln \left(\frac{\rho T}{\rho_{0} T_{0}} \right) \right]$$
(14)

The ideal gas Helmholtz energy is given in dimensionless form by

$$\alpha^{0} = \frac{h_{0}^{0}\tau}{RT_{c}} - \frac{s_{0}^{0}}{R} - 1 + \ln\frac{\delta\tau_{0}}{\delta_{0}\tau} - \frac{\tau}{R} \int_{\tau_{0}}^{\tau} \frac{c_{p}^{0}}{\tau^{2}} d\tau + \frac{1}{R} \int_{\tau_{0}}^{\tau} \frac{c_{p}^{0}}{\tau} d\tau$$
(15)

where $\delta_0 = \rho_0/\rho_c$ and $\tau_0 = T_c/T_0$. The ideal gas Helmholtz energy is often reported in a simplified form for use in equations of state as

$$\alpha^{0} = \ln \delta - a_{1} \ln \tau + \sum a_{k} \tau^{i_{k}} + \sum a_{k} \ln[1 - \exp(-b_{k}\tau)]$$
(16)

where standard models to describe the ideal gas heat capacity have been assumed.

Properties of the Real Fluid. Unlike the ideal gas, the real fluid behavior is often described with empirical models that are only loosely supported by theoretical considerations. Although it is possible to extract values such as second and

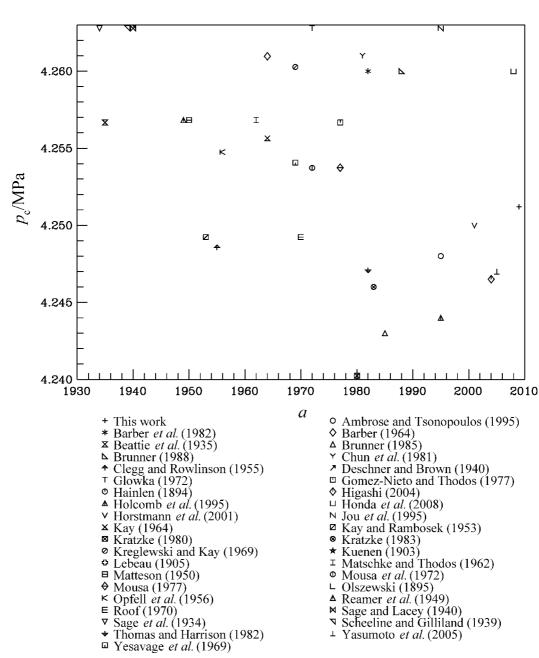


Figure 3. Reported critical pressures p_c of propane as a function of the year a published.

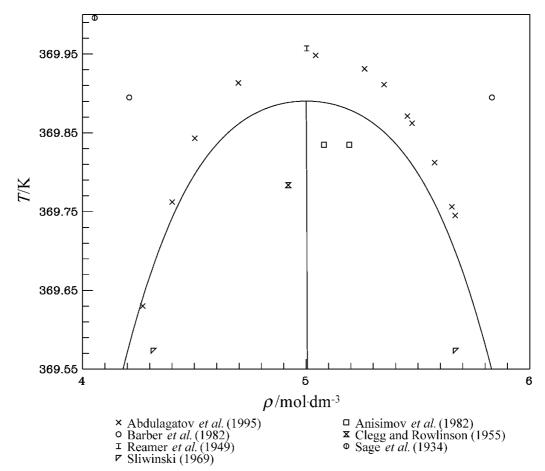


Figure 4. Saturation data in the critical region, the phase boundaries calculated from the Maxwell criteria, and the rectilinear diameter (average of the saturation values) as a function of density ρ and temperature T.

third virial coefficients from the fundamental equation, the terms in the equation are empirical, and any functional connection to theory is not entirely justified. The coefficients of the equation depend on the experimental data for the fluid and are constrained by various criteria explained elsewhere in this manuscript and in the works of Span and Wagner¹⁹⁷ and Lemmon and Jacobsen. 189

The common functional form for Helmholtz energy equations of state is

$$\alpha^{r}(\delta,\tau) = \sum N_k \delta^{d_k} \tau^{t_k} + \sum N_k \delta^{d_k} \tau^{t_k} \exp(-\delta^{l_k})$$
 (17)

where each summation typically contains 4 to 20 terms and where the index k points to each individual term. The values of t_k should be greater than zero, and d_k and l_k should be integers greater than zero. The functional form used in this work contains additional Gaussian bell-shaped terms

$$\alpha^{r}(\delta, \tau) = \sum_{k} N_{k} \delta^{d_{k}} \tau^{t_{k}} + \sum_{k} N_{k} \delta^{d_{k}} \tau^{t_{k}} \exp(-\delta^{l_{k}}) + \sum_{k} N_{k} \delta^{d_{k}} \tau^{t_{k}} \exp(-\eta_{k} (\delta - \varepsilon_{k})^{2} - \beta_{k} (\tau - \gamma_{k})^{2})$$
(18)

These terms were first successfully used by Setzmann and Wagner¹⁹⁸ for the methane equation of state. In that work, these terms are significant only near the critical point and rapidly go to zero away from the critical point. As such, they are extremely sensitive but powerful in modeling the properties of fluids in the critical region, especially for densities; their ability to model caloric properties (e.g., the steep increase of c_v near the critical point) is limited. As explained by Wagner and Pruss, ¹⁹⁹ the strong sensitivity of these terms made it difficult to determine the values automatically in the optimization and nonlinear fitting process. Thus, they determined these parameters based on comprehensive precalculations, and only two of them were fitted at a time in their nonlinear regression.

In this work, because linear optimization was not used, the coefficients and exponents of the Gaussian bell-shaped terms were fitted simultaneously with all of the other parameters in the equation of state. The terms had to be monitored closely to ensure that irregular behavior did not creep into the equation, as was evident by plots of heat capacities or speeds of sound. Initially, the values of η and β were forced to be in the same range as values in other equations reported by Wagner's group. However, the fitting algorithm tended toward much smaller values, indicating that these terms would be numerically significant over a broader range of temperature and density. The final values of these two coefficients in this work are significantly different from those of other equations, except for the very last term in the equation.

Most multiparameter equations of state have shortcomings that affect the determination of phase boundaries, the calculation of metastable states within the two-phase region, and the shapes of isotherms in the low-temperature vapor phase. These can be traced to the magnitude of t in τ^t in eq 17. As the temperature goes to zero, τ^t goes to infinity for values of t > 1, causing the pressure to increase rapidly to infinity. The effect is more pronounced for higher values of t. The primary use of terms with high values of t is for modeling the area around the critical region, where the properties change rapidly. Outside the critical region, the effect is dampened out with the δ^d contribution in

Table 3. Summary of Experimental Data for Propane

| | | | temperature range | pressure range | density range | |
|--|--------------|---------------|-------------------------------|--|--|----------------|
| author | year | no. of points | (T/K) | (p/MPa) | $(\rho/\text{mol}\cdot\text{dm}^{-3})$ | $AARD^a$ (% |
| | | Ideal G | as Isobaric Heat Capaciti | ies | | |
| Beeck ¹³ | 1936 | 4 | 273 to 573 | | | 4.36 |
| Chao et al. ²² | 1973 | 19 | 50 to 1500 | | | 0.22 |
| Dailey and Felsing ³¹ | 1943 | 8 | 344 to 693 | | | 0.591 |
| Ernst and Büsser ⁴² | 1970 | 4 | 293 to 353 | | | 0.205 |
| Esper et al. ⁴³ | 1995 | 26 | 230 to 350 | | | 0.297 |
| Goodwin and Lemmon ⁵² | 1995 | 14 | 265 to 355 | | | 1.02 |
| He et al. ⁶² | 2002 | 4 | 293 to 323 | | | 0.206 |
| Kistiakowsky et al. ⁹² | 1940 | 14 | 148 to 259 | | | 0.523 |
| Kistiakowsky and Rice ⁹³ | 1940 | 4 | 272 to 369 | | | 0.361 |
| Scott ¹⁵⁶ | 1974 | 8 | 272 to 369 | | | 0.282 |
| Trusler and Zarari ¹⁷² Yesavage ¹⁷⁹ | 1996 1968 | 7 7 | 225 to 375 339 to 422 | | | 0.028 0.646 |
| Tesavage | 1700 | , | | | | 0.040 |
| TRC (Frenkel et al.) ¹⁹⁴ | | 120 | Vapor Pressures 130 to 426 | 0.00002 to 4.25 | | 1.54 |
| Barber et al. ¹⁰ | 1982 | 18 | 329 to 370 | 1.94 to 4.23 | | 0.48 |
| Beattie et al. 12 | 1935 | 17 | 323 to 348 | 1.71 to 2.85 | | 0.018 |
| Bobbo et al. 14 | 2002 | 5 | 248 to 295 | 0.203 to 0.875 | | 0.095 |
| Burrell and Robertson ¹⁸ | 1916 | 16 | 149 to 229 | 0.0004 to 0.101 | | 18.3 |
| Calado et al. ¹⁹ | 1997 | 13 | 175 to 211 | 0.003 to 0.037 | | 0.786 |
| Carruth and Kobayashi ²¹ | 1973 | 12 | 97.6 to 179 | 10^{-8} to 0.005 | | 13.9 |
| Chun ²⁴ | 1964 | 10 | 348 to 367 | 2.85 to 4.09 | | 0.6 |
| Clark ²⁶ | 1973 | 10 | 327 to 370 | 1.88 to 4.21 | | 0.494 |
| Clegg and Rowlinson ²⁸ | 1955 | 9 | 323 to 370 | 1.72 to 4.25 | | 0.184 |
| Coquelet et al. ²⁹ | 2003 | 17 | 277 to 353 | 0.536 to 3.13 | | 0.108 |
| Dana et al. ³² | 1926 | 43 | 210 to 323 | 0.037 to 1.71 | | 0.512 |
| Delaplace ³⁵ | 1937 | 27 | 90.2 to 126 | 10^{-8} to 0.00001 | | 40.9 |
| Deschner and Brown ³⁶ | 1940 | 36 | 302 to 370 | 1.05 to 4.26 | | 0.996 |
| Djordjevich and Budenholzer ³⁸ | 1970 | 6 | 128 to 255 | 0.00001 to 0.259 | | 6.92 |
| Echols and Gelus ⁴⁰ | 1947 | 4 | 134 to 250 | 0.00003 to 0.215 | | 11.6 |
| Francis and Robbins ⁴⁵ | 1933 | 34 | 301 to 337 | 1.05 to 2.4 | | 4.72 |
| Giles and Wilson ⁴⁷ | 2000 | 4 | 273 to 333 | 0.474 to 2.12 | | 0.144 |
| Glos et al. ⁴⁸ | 2004 | 5 | 130 to 170 | 0.00002 to 0.002 | | 0.741 |
| Glos et al. ⁴⁸ | 2004 | 17 | 180 to 340 | 0.005 to 2.43 | | 0.002 |
| Hainlen ⁵⁷ | 1894 | 13 | 240 to 375 | 0.182 to 4.91 | | 6.76 |
| Hanson et al. ⁵⁸ | 1952 | 4 | 270 to 330 | 0.425 to 2 | | 0.225 |
| Harteck and Edse ⁵⁹ | 1938 | 145 | 163 to 232 | 0.001 to 0.107 | | 0.846 |
| Higashi et al. ⁶⁵ Hipkin ⁶⁶ | 1994 | 8 4 | 283 to 313 | 0.644 to 1.38 | | 0.891 |
| Hirata et al. ⁶⁷ | 1966 1969 | 5 | 267 to 366 197 to 273 | 0.385 to 3.92 | | 1.25 0.728 |
| Ho et al. ⁶⁹ | 2006 | 6 | 273 to 313 | 0.016 to 0.476 0.474 to 1.37 | | 0.728 |
| Holcomb et al. 70 | 1995 | 19 | 240 to 364 | 0.149 to 3.79 | | 0.198 |
| Holcomb and Outcalt ⁷¹ | 1998 | 4 | 290 to 350 | 0.769 to 2.95 | | 0.198 |
| Honda et al. ⁷² | 2008 | 4 | 320 to 369 | 1.6 to 4.23 | | 0.164 |
| Im et al. ⁷⁷ | 2006 | 6 | 313 to 363 | 1.37 to 3.77 | | 0.201 |
| Kahre ⁸¹ | 1973 | 5 | 278 to 328 | 0.548 to 1.88 | | 0.581 |
| Kay ⁸³ | 1970 | 10 | 332 to 368 | 2.07 to 4.14 | | 0.41 |
| Kay ⁸⁴ | 1971 | 9 | 332 to 390 | 2.07 to 4.83 | | 0.438 |
| Kayukawa et al. ⁸⁷ | 2005 | 13 | 240 to 360 | 0.148 to 3.55 | | 0.102 |
| Kemp and Egan ⁸⁹ | 1938 | 12 | 166 to 231 | 0.002 to 0.103 | | 0.252 |
| Kim and Kim ⁹⁰ | 2005 | 8 | 253 to 323 | 0.244 to 1.71 | | 0.08 |
| Kim et al. ⁹¹ | 2003 | 8 | 253 to 323 | 0.244 to 1.72 | | 0.134 |
| Kleiber ⁹⁵ | 1994 | 3 | 255 to 298 | 0.261 to 0.949 | | 0.034 |
| Kratzke ⁹⁸ | 1980 | 14 | 312 to 368 | 1.33 to 4.07 | | 0.05 |
| Kratzke and Müller ⁹⁹ | 1984 | 5 | 300 to 357 | 1.01 to 3.36 | | 0.01 |
| Laurance and Swift ¹⁰⁵ | 1972 | 10 | 311 to 344 | 1.3 to 2.64 | | 0.068 |
| Lee et al. 107 | 2003 | 7 | 268 to 318 | 0.408 to 1.53 | | 0.313 |
| Lim et al. 110 | 2004 | 4 | 273 to 303 | 0.475 to 1.08 | | 0.103 |
| Lim et al. 111 | 2004 | 6 | 268 to 313 | 0.408 to 1.36 | | 0.362 |
| Lim et al. 112 | 2006 | 13 | 268 to 323 | 0.408 to 1.71 | | 0.228 |
| Maass and Wright ¹¹⁴ | 1921 | 6 | 230 to 250 | 0.114 to 0.269 | | 15.3 |
| Manley and Swift ¹¹⁵ | 1971 | 5 | 244 to 311 | 0.176 to 1.3 | | 0.177 |
| McLinden ¹²⁰ | 2009 | 38 | 270 to 369 | 0.431 to 4.18 | | 0.017 |
| Miksovsky and Wichterle ¹²² | 1975 | 6 | 303 to 369 | 1.08 to 4.19 | | 0.269 |
| Miranda et al. 123 | 1976 | 5 | 266 to 355 | 0.385 to 3.28 | | 0.66 |
| Miyamoto and Uematsu ¹²⁵ | 2006 | 8 | 280 to 369 | 0.583 to 4.18 | | 0.082 |
| Mousa ¹²⁷ | 1977 | 11 | 335 to 370 | 2.2 to 4.25 | | 0.496 |
| Niesen and Rainwater ¹³⁰ | 1990 | 4 | 311 to 361 | 1.3 to 3.63 | | 0.08 |
| Noda et al. 131 | 1993 | 4 | 273 to 293 | 0.473 to 0.836 | | 0.182 |
| Outcalt and Lee ¹³⁵ Park and Jung ¹³⁶ | 2004 | 12 | 260 to 360 | 0.311 to 3.55 | | 0.064 |
| Park and ling | 2002 | 5 | 273 to 313 | 0.475 to 1.37 | | 0.049 |
| Doub at al 137 | 2007 | _ | | | | |
| Park et al. ¹³⁷ Perkins et al. ¹³⁹ | 2007 2009 | 5 53 | 273 to 313 85.5 to 241 | 0.472 to 1.37 $10^{-8} \text{ to } 0.154$ | | 0.298 0.162 |

Table 3. Continued

| Remippersubh et al. 142 2009 6 26 36 323 0.344 to 1.72 0.199 Remore et al. 145 1996 10 315 to 370 1.38 to 426 0.334 Remore et al. 145 1996 10 315 to 370 1.38 to 426 0.334 Remore et al. 145 1997 10 315 to 370 1.38 to 426 0.334 Remore et al. 145 1998 1994 21 294 to 371 0.862 0.431 0.351 Scheeline and Gilliand 154 1999 5 315 to 372 1.41 to 4.39 1.11 Scheeline and Gilliand 154 1999 5 315 to 372 1.41 to 4.39 1.11 Scheeline and Gilliand 154 1999 5 315 to 372 1.41 to 4.39 1.11 Scheeline and Gilliand 154 1998 1906 8 173 to 343 8 0.007 to 2.9 1.03 Seeing et al. 156 Seeing et al. 157 Seeing | | | | temperature range | pressure range | density range | |
|---|--|------|---------------|---------------------------|----------------|--|-------------|
| Reamer et al. 144 1949 | author | year | no. of points | (T/K) | (p/MPa) | $(\rho/\text{mol} \cdot \text{dm}^{-3})$ | $AARD^a$ (6 |
| Reamer et al. 144 1949 | Ramiugernath et al. 142 | 2009 | 6 | 263 to 323 | 0.344 to 1.72 | | 0.194 |
| Reamer et al. 155 ger et al. 157 ger | Reamer et al. 144 | | | | | | 0.316 |
| Sage et al. 151 Schindler et a | Reamer et al. 145 | | | | | | 0.183 |
| Scheelmen and Gilliands 1519 95 315 to 372 1.41 to 4.39 1.11 Scheelmen and Gilliands 1528 1966 8 173 to 348 0.070 to 2.9 10.5 Seening et al. 1528 2008 6 273 to 223 0.476 to 1.77 0.200 2.5 Seening et al. 1529 2008 6 273 to 223 0.476 to 1.77 0.200 2.5 Seening et al. 1529 2008 6 273 to 223 0.476 to 1.77 0.200 2.5 Seening et al. 1529 2008 2008 2008 2009 2.5 Seening et al. 1529 2.5 Seening et al. | | | | 294 to 371 | | | 0.511 |
| Schindler et al. 159 | Scheeline and Gilliland ¹⁵⁴ | | | | | | |
| Scong et al. 1-99 Scong et al. | Schindler et al. 155 | | | | | | |
| Skripka et al. 160 1970 10 123 to 273 0.000005 to 0.472 4.24 1Domas and Harrison 161 1978 15 325 80 330 0.292 to 4.25 0.044 10 17 to 0.000 1.01 | Seong et al. 159 | | | | | | 0.302 |
| Fischmann Fisc | Skripka et al. 160 | | | | | | |
| Thomas and Harrison 166 1982 25 258 to 370 0.292 to 4.25 0.002 Chickner and Lossing 169 1915 13 105 to 165 10 10 0.001 13 105 to 165 10 10 0.001 13 105 to 165 10 10 0.0001 10 133 11 27 10 166 10 172 10 160 10 180 10 | Teichmann ¹⁶⁶ | 1978 | 15 | 325 to 363 | | | 0.047 |
| Tickner and Lossing 160 Libynii and Wichterler 167 1983 32 296 to 368 0.893 to 1.12 0.0156 Wichterler and Kohayashi 177 1972 9 130 to 214 0.00002 to 0.044 2.47 Yocelen and Kidnay 184 1999 5 240 to 344 0.151 to 2.64 0.582 Landini 187 1984 1995 15 8aturated Liquid Densities FRC (Frenkel et al., 194 185 285 to 363 8abdulagatiov et al., 2 1985 286 386 to 370 588 to 1870 589 to 1 | Thomas and Harrison ¹⁶⁸ | 1982 | 25 | 258 to 370 | 0.292 to 4.25 | | 0.022 |
| Lebyti and Wicherler 16 18 18 32 296 to 368 0.893 to 4.12 0.156 | Fickner and Lossing 169 | | | 105 to 165 | | | |
| Wichterle and Kohayashi ¹⁷ 1972 9 130 to 214 0,00002 to 1,044 2.47 (orongi ¹²² 1928 12 161 to 312 0,001 to 1,33 11.77 (orongi ¹²³ 1964 13 273 to 347 0,155 to 0,199 0.482 (angle and Kidnay ¹⁴⁴ 1999 5 240 to 344 0,151 to 2,64 0.582 (angle and Kidnay ¹⁴⁴ 1996 13 273 to 347 0,155 to 0,199 0.442 (bagaine and Kidnay ¹⁴⁴ 1978 15 8 Marratel Liquid Densities **TRC (Frenckle et al.) ¹⁶⁴ 1982 5 5 271 to 370 5,04 to 10.9 0.599 (angle and kidnay ¹⁴⁴ 1982 5 271 to 370 5,04 to 10.9 0.599 (angle angle angl | Jchytil and Wichterle ¹⁷³ | | | | | | 0.156 |
| 1.77 1.77 1.76 1.76 1.77 1.76 | Wichterle and Kobayashi 177 | | | | | | |
| fuection and Kidnay **8. 1999 5 240 to 344 0.151 to 2.64 0.382 25 2007 13 241 to 247 0.155 to 0.199 0.645 25 2007 13 241 to 247 0.155 to 0.199 0.645 25 2007 | Young ¹⁸² | | | | | | |
| Sambring et al. 1964 13 | Yucelen and Kidnav ¹⁸⁴ | | | | | | |
| Saturated Liquid Densities | Zanolini ¹⁸⁵ | | | | | | |
| Saturated Liquid Densities Saturated Densities Saturated Liquid Densities Saturated Densities Saturate | Zhang et al. ¹⁸⁶ | | | | | | |
| Section Sect | and of all | 2007 | | | | | 0.0.0 |
| blubulgatov et al. 3 1995 26 305 to 370 5.04 to 10.9 0.599 arber et al. 6 1982 5 271 to 370 5.08 to 12 2.41 histimov et al. 6 1982 5 271 to 370 5.08 to 12 2.41 histimov et al. 6 1982 9 329 to 370 5.83 to 9.83 1.66 Tark 3 1973 5 327 to 370 4.92 to 10.2 2.92 hins et al. 2 28 to 333 9.78 to 13.3 0.162 Tark 3 1973 5 327 to 370 4.92 to 10.2 2.92 hins et al. 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 | CRC (Frenkel et al.) ¹⁹⁴ | | | - | • | 7.7 to 16.6 | 0.836 |
| Anisimov et al. 9 1982 5 271 to 370 5.08 to 12 2.41 arber et al. 9 1982 9 329 to 370 5.83 to 9.83 1.66 Larney. 9 1942 34 228 to 333 9.78 to 13.3 0.166 Larney. 9 1942 34 228 to 333 9.78 to 13.3 0.166 Larney. 9 1942 34 228 to 333 9.78 to 13.3 0.166 Larney. 9 1942 34 228 to 330 9.78 to 13.3 0.166 Larney. 9 1945 1955 9 323 to 370 49.2 to 10.2 2.92 2.92 beschner and Brown. 9 1956 12 2.73 to 32.9 9.96 to 12 0.555 2.0 sechner and Brown. 9 1940 14 303 to 368 6.64 to 11 0.975 1950 arbert. 9 1940 14 303 to 368 6.64 to 11 0.975 1950 arbert. 9 1940 1970 1970 1970 1970 1970 1970 1970 197 | | 1995 | | | | | |
| Sarber et al. 10 1982 9 329 to 370 5.83 to 9.83 1.66 Tannery 1973 1942 34 228 to 333 9.78 to 13.3 0.162 Tannery 1973 5 327 to 370 4.92 to 10.2 2.92 Dana et al. 17 1974 1975 1926 12 273 to 329 9.96 to 12 0.555 1974 1976 1976 1976 1976 1976 1976 1976 1976 | | | | | | | |
| Sameys 1942 34 228 to 333 3.78 to 13.3 0.166 Carlank 1973 5 327 to 370 6.37 to 9.9 2.59 Legg and Rowlinson 1955 9 323 to 370 4.92 to 10.2 2.92 Szechner and Brown 1940 14 303 to 368 6.64 to 11 0.975 Szechner and Brown 1940 14 303 to 368 6.64 to 11 0.975 Szechner and Brown 1940 14 303 to 368 6.64 to 11 0.975 Szechner and Brown 1940 14 303 to 368 6.64 to 11 0.975 Szechner and Brown 1940 14 303 to 368 6.64 to 11 0.975 Szechner and Brown 1940 14 303 to 368 6.64 to 11 0.975 Szechner and Brown 1940 14 303 to 368 6.64 to 11 0.975 Szechner and Brown 1940 14 303 to 368 6.64 to 11 0.975 Szechner and Brown 1940 14 303 to 368 6.64 to 11 0.975 Szechner and Brown 1940 14 303 to 368 6.64 to 11 0.975 Szechner and Brown 1940 17 16 100 to 289 11.5 to 16.3 Szechner and Brown 1967 16 278 to 361 7.76 to 11.9 0.251 Szechner and Kurata 1969 5 93.2 to 133 15.5 to 16.4 0.043 Szechner and Kurata 1969 5 93.2 to 133 15.5 to 16.4 0.043 Szechner and Kurata 1973 10 278 to 328 9.94 to 11.9 0.104 Szenkawa et al. 7 2005 13 240 to 360 7.89 to 12.9 0.078 Stosek and McKinley 200 228 to 333 15.5 to 16.4 0.033 Szenkawa et al. 7 2005 13 245 to 325 10.1 to 12.8 0.042 Szenkawa et al. 7 1942 20 228 to 333 9.78 to 13.3 0.21 Szenkawa et al. 7 1942 20 228 to 333 9.78 to 13.3 0.21 Szenkawa et al. 7 1941 | | | | | | | |
| Elark 1973 5 327 to 370 6.37 to 9.9 2.59 | Sarney ²⁰ | | | | | | |
| Display 1955 9 323 to 370 4.92 to 10.2 2.92 | Tlark ²⁶ | | | | | | |
| Dana et al. ³² 1926 12 273 to 329 9.96 to 12 0.557 bescher and Brown ³⁶ 1940 14 303 to 368 6.64 to 11 0.975 bly and Kobayashi ⁴¹ 1978 18 166 to 288 11.5 to 14.8 0.061 flost et al. ⁴⁸ 2004 27 90 to 340 9.34 to 16.5 0.003 laynes and Hiza ⁶¹ 1977 16 100 to 289 11.5 to 16.3 0.088 relegeson and Sage- ⁶³ 1967 16 278 to 361 7.76 to 11.9 0.255 lolcomb et al. ³⁰ 1995 14 313 to 364 7.42 to 10.6 0.071 lolcomb and Outcalt ²¹ 1998 4 290 to 350 8.66 to 11.5 0.026 eases and Kurata ⁷⁸ 1969 5 93.2 to 133 15.5 to 16.4 0.045 (al. ⁴⁸ 1973 10 278 to 328 9.94 to 11.9 0.104 (al. ⁴⁸ 1973 10 278 to 328 9.94 to 11.9 0.104 (al. ⁴⁸ 1973 10 278 to 328 9.94 to 11.9 0.104 (al. ⁴⁸ 1973 10 278 to 328 9.94 to 11.9 0.104 (al. ⁴⁸ 1973 10 278 to 328 9.94 to 11.9 0.104 (al. ⁴⁸ 1974 10.005 13 240 to 360 7.89 to 12.9 0.078 (blosek and McKinley ⁹⁶ 1984 5 245 to 325 10.2 to 12 0.034 (al. ⁴⁸ 1984 1994 1994 10 2.20 to 289 11.5 to 13.5 to 16.4 0.035 (al. ⁴⁸ 1974 1981 6 20 to 289 11.5 to 13.5 0.055 (al. ⁴⁸ 1974 1981 6 20 to 289 11.5 to 13.5 0.055 (al. ⁴⁸ 1974 1981 1981 6 20 to 289 11.5 to 13.5 0.055 (al. ⁴⁸ 1974 1998 1994 4 31 to 361 7.7 to 14.1 0.31 (al. ⁴⁸ 1995 1996 4 31 to 361 7.7 to 14.1 0.31 (al. ⁴⁸ 1995 1996 4 31 to 361 7.7 to 10.7 0.038 (al. ⁴⁸ 1974 1975 1976 17 93.2 to 173 14.6 to 16.4 0.037 (al. ⁴⁸ 1995 1996 4 31 to 361 7.7 to 10.7 0.038 (al. ⁴⁸ 1995 1996 1998 1998 1998 1998 1998 1998 1998 | Tlegg and Powlincon ²⁸ | | | | | | |
| Deschner and Brown 1940 | Dana et al. 32 | | | | | | |
| | Daschner and Brown ³⁶ | | | | | | |
| Silos et al. | | | | | | | |
| laynes and Hiza ⁶¹ 1977 16 100 to 289 11.5 to 16.3 0.088 16.5 to 16.3 0.088 16.5 to 16.9 1967 16 278 to 361 7.76 to 11.9 0.251 16.0 to the tal. 10 1995 14 313 to 364 7.42 to 10.6 0.071 16.0 to mb and Outcalt 1 1998 4 290 to 350 8.66 to 11.5 0.266 11.5 to 16.5 0.266 11.5 to 16.4 0.042 16.0 to 18.2 1973 10 278 to 328 9.94 to 11.9 0.104 1983 1973 10 278 to 328 9.94 to 11.9 0.104 1984 1973 10 278 to 323 10.2 to 12 0.034 10.2 to 12 0.03 | The et al 48 | | | | | | |
| lelgeson and Sage ⁶³ 1967 16 278 to 361 7.76 to 11.9 0.251 folloomb et al. ¹⁰ 1995 14 313 to 364 7.42 to 10.6 0.071 folcomb and Outcalt ⁷¹ 1998 4 290 to 350 8.66 to 11.5 0.266 ensen and Kurata ⁷⁸ 1969 5 93.2 to 133 15.5 to 16.4 0.043 fashre ²¹ 1973 10 278 to 328 9.94 to 11.9 0.104 fashre ²¹ 1988 6 273 to 323 10.2 to 12 0.034 favukawa et al. ⁸⁷ 2005 13 240 to 360 7.89 to 12.9 0.078 folsek and McKinley ⁵⁰ 1968 4 94.8 to 130 15.6 to 16.4 0.035 fratzke and Miller ⁵¹ 1981 6 220 0.28 to 333 9.78 to 13.3 0.21 to 12 a.0 and Miller ⁵¹ 1981 6 220 to 289 11.5 to 13.5 0.055 flasses and Wright ¹¹⁴ 1921 13 195 to 249 12.7 to 14.1 0.31 deClune ¹¹⁸ 1976 17 93.2 to 173 14.6 to 16.4 0.035 fixes and Rainwater ¹⁵⁰ 1990 4 311 to 361 7.71 to 10.7 0.038 fixes and Rainwater ¹⁵⁰ 1990 4 311 to 361 7.71 to 10.7 0.038 fixes and Miller ¹⁷⁷ 1973 4 91 to 11.5 to 15.5 to 10.6 0.54 fashes and Miller ¹⁸⁷ 1976 17 93.2 to 173 14.6 to 16.4 0.037 fixes and Miller ¹⁹⁸ 1976 17 93.2 to 173 14.6 to 16.4 0.037 fixes and Miller ¹⁹⁹ 1990 4 311 to 361 7.71 to 10.7 0.038 fixes and Rainwater ¹⁵⁰ 1990 4 311 to 361 7.71 to 10.7 0.038 fixes and Miller ¹⁷⁷ 1974 1975 1975 1975 1975 1976 1977 1978 1978 1978 1978 1978 1978 1978 | JIOS et al. | | | | | | |
| tolcomb et al. 10 1995 14 313 to 364 7.42 to 10.6 0.071 10 10 10 10 10 10 10 10 10 10 10 10 10 | | | | | | | |
| folcomb and Outcalt ⁷¹ 1998 | | | | | | | |
| ensen and Kurata ⁷⁸ 1969 5 93.2 to 133 15.5 to 16.4 0.043 cahne ⁸¹ 1973 10 278 to 328 9.94 to 11.9 0.104 caminishi et al. ⁸² 1988 6 273 to 323 10.2 to 12 0.034 cayukawa et al. ⁸⁷ 2005 13 240 to 360 7.89 to 12.9 0.078 closek and McKinley ⁹⁶ 1988 4 9.48 to 130 15.6 to 16.4 0.033 cratzke and Müller ⁹⁹ 1984 5 245 to 325 10.1 to 12.8 0.043 cayakawa et al. ¹⁸⁸ 1942 20 228 to 333 9.78 to 13.3 0.21 cao and Miller ¹¹³ 1981 6 220 to 289 11.5 to 13.5 0.055 drass and Wright ¹⁴⁴ 1921 13 195 to 249 11.5 to 13.5 0.055 drass and Wright ¹⁴⁴ 1921 13 195 to 249 12.7 to 14.1 0.31 dreClune ¹⁴⁸ 1976 17 93.2 to 173 14.6 to 16.4 0.033 drivanto and Uematsu ¹²⁶ 2007 6 280 to 365 7.2 to 11.8 0.144 disease and Rainwater ¹³⁰ 1990 4 311 to 361 7.71 to 10.7 0.038 camer et al. ¹⁴⁴ 1949 10 313 to 370 5 to 10.6 0.54 codosevich and Miller ¹⁴⁷ 1973 4 91 to 115 15.9 to 16.5 to 10.6 0.54 codosevich and Miller ¹⁴⁷ 1973 4 91 to 115 15.9 to 16.5 to 11.4 2.42 combinson of 1990 14 283 to 372 5.67 to 11.7 0.342 from and Harrison 168 1982 22 258 to 369 6.08 to 12.4 0.12 combinson 170 1971 11 278 to 323 10.2 to 11.8 0.047 and er tel ¹⁷⁴ 1937 9 283 to 370 1.0 to 11.7 0.075 combinson 170 1973 5 327 to 370 0.981 to 3.67 0.342 chomas and Harrison 168 1982 9 329 to 370 0.981 to 3.67 3.9 Clags and Rowlinson 1895 1940 14 303 to 368 0.454 to 4.7 1.65 class 1.6 class | folcomb et al. | | | | | | |
| Calmers 1 1973 10 278 to 328 9.94 to 11.9 0.104 (Calmers 14 2 2 1988 6 273 to 323 10.2 to 12 0.034 (Calmers 14 18 2 1988 6 273 to 323 10.2 to 12 0.034 (Calmers 14 18 2 1984 5 245 to 325 10.1 to 12.8 0.044 (Calmers 14 18 2 1942 20 228 to 333 9.78 to 13.3 0.21 (Calmers 14 19 19 19 13 1981 6 220 to 289 11.5 to 13.5 0.055 (Calmers 18 19 19 19 1 13 1985 to 249 12.7 to 14.1 0.31 (Calmers 18 19 19 1 13 1985 to 249 12.7 to 14.1 0.31 (Calmers 18 19 19 19 1 13 19 1 19 1 13 19 1 19 1 13 19 1 1 13 19 1 1 13 19 1 1 1 1 | | | | | | | |
| Caminishi et al. S2 | ensen and Kurata | | | | | | |
| Cayukawa et al. **7 | | | | | | | |
| Closek and McKinley 96 | Kaminishi et al. 87 | | | | | | |
| Cratzke and Müller 99 1984 5 245 to 325 10.1 to 12.8 0.042 Legatski et al. 108 1992 20 228 to 333 9.78 to 13.3 0.21 2.0 co and Miller 13 1981 6 220 to 289 11.5 to 13.5 0.055 Mass and Wright 14 1921 13 195 to 249 12.7 to 14.1 0.31 McClune 118 1976 17 93.2 to 173 14.6 to 16.4 0.037 Miyamoto and Uematsu 126 2007 6 280 to 365 7.2 to 11.8 0.144 Niesen and Rainwater 10 1990 4 311 to 361 7.71 to 10.7 0.038 Reamer et al. 144 1949 10 313 to 370 5 to 10.6 0.54 Reamer and Lupretre 134 Seeman and Urban 157 1963 27 278 to 299 11.1 to 11.9 11.1 to 11.9 0.056 0.54 Nimishi 162 1996 14 283 to 372 5.67 to 11.7 0.342 10minson 170 1971 11 278 to 323 10.2 to 11.8 0.047 2007 2007 2007 2007 2007 2007 2007 2 | | | | | | | |
| Legatski et al. 108 1942 20 228 to 333 9.78 to 13.3 0.21 Lao and Miller 113 1981 6 220 to 289 11.5 to 13.5 0.055 Maass and Wright 114 1921 13 195 to 249 12.7 to 14.1 0.31 Micclune 118 1976 17 93.2 to 173 14.6 to 16.4 0.037 Micsen and Rainwater 130 1990 4 311 to 361 7.71 to 10.7 0.038 Viesen and Rainwater 130 1990 4 311 to 361 7.71 to 10.7 0.038 Drit and Laupretre 134 1978 31 86.7 to 244 12.8 to 16.6 0.026 Reamer et al. 144 1949 10 313 to 370 5 to 10.6 0.048 Rodosevich and Miller 147 1973 4 91 to 115 15.9 to 16.5 0.045 Rodemer et al. 144 1934 21 294 to 371 6.51 to 11.4 2.42 Reeman and Urban 157 1963 27 278 to 299 11.1 to 11.9 0.055 Silwinski 162 1969 | Closek and McKinley 90 | | | | | | |
| 200 and Miller 13 | Kratzke and Müller ⁹⁹ | | | | | | 0.043 |
| Mass and Wright 114 1921 13 195 to 249 12.7 to 14.1 0.31 McClune 118 1976 17 93.2 to 173 14.6 to 16.4 0.037 Miyamoto and Uematsu 126 2007 6 280 to 365 7.2 to 11.8 0.144 Niesen and Rainwater 130 1990 4 311 to 361 7.71 to 10.7 0.038 Trit and Lauprette 134 1978 31 86.7 to 244 12.8 to 16.6 0.026 Reamer et al. 144 1949 10 313 to 370 5 to 10.6 0.54 Rodosevich and Miller 147 1973 4 91 to 115 15.9 to 16.5 0.045 Raige et al. 151 1934 21 294 to 371 6.51 to 11.4 0.51 to 11.9 0.055 Riwinski 162 1969 14 283 to 372 5.67 to 11.7 0.342 Roman and Urban 157 1963 27 7878 to 299 11.1 to 11.9 0.055 Riwinski 162 1969 14 283 to 372 5.67 to 11.7 0.342 Roman and Harrison 168 1982 22 258 to 369 6.08 to 12.4 0.12 Comlinson 170 1971 11 278 to 323 10.2 to 11.8 0.047 Rain der Vet 174 1937 9 283 to 323 10.2 to 11.7 0.075 Rodulagatov et al. 3 195 11 342 to 370 1.4 to 4.7 1.65 Raismov et al. 10 1982 9 329 to 370 1.4 to 4.7 1.65 Raismov et al. 10 1982 1 368 3.61 0.833 Raismov et al. 10 1982 1 368 3.61 0.833 Raismov et al. 10 1982 1 368 3.61 0.833 Raismov et al. 10 1982 1 368 3.61 0.833 Raismov et al. 10 1982 1 368 3.61 0.833 Raismov et al. 10 1982 1 368 3.61 0.833 Raismov et al. 10 1982 1 368 3.61 0.833 Raismov et al. 10 1982 1 368 3.61 0.833 Raismov et al. 10 1982 1 368 3.61 0.833 Raismov et al. 10 1982 1 368 3.61 0.833 Raismov et al. 10 1982 1 368 3.61 0.833 Raismov et al. 10 1982 1 368 3.61 0.833 Raismov et al. 10 1982 1 368 3.61 0.833 Raismov et al. 10 1982 1 368 3.69 0.859 to 4.92 1.55 0.804 Raismov et al. 10 1982 1 368 0.859 0.967 0.968 Raismov et al. 10 1983 1 364 0.686 0.454 to 3.58 3.69 0.967 0.968 to 3.69 0.967 0.968 to 3.69 0.967 0.968 to 3.69 0.968 | Legatski et al. 108 | | | | | | |
| McClune ¹¹⁸ 1976 17 93.2 to 173 14.6 to 16.4 0.035 Migyamoto and Uematsu ¹²⁶ 2007 6 280 to 365 7.2 to 11.8 0.144 Niesen and Rainwater ¹³⁰ 1990 4 311 to 361 7.7 to 10.7 0.038 Orrit and Laupretre ¹³⁴ 1978 31 86.7 to 244 12.8 to 16.6 0.026 Reamer et al. ¹⁴⁴ 1949 10 313 to 370 5 to 10.6 0.54 Rodosevich and Miller ¹⁴⁷ 1973 4 91 to 115 15.9 to 16.5 0.045 Reamer and Urban ¹⁵⁷ 1963 27 278 to 299 11.1 to 11.9 0.056 Sliwinski ¹⁶² 1969 14 283 to 372 5.67 to 11.7 0.342 Romas and Harrison ¹⁶⁸ 1982 22 258 to 369 6.08 to 12.4 0.12 Formians and Harrison ¹⁶⁸ 1982 22 258 to 369 6.08 to 12.4 0.12 Formians and Harrison ¹⁶⁸ 1982 12 258 to 369 6.08 to 12.4 0.12 Formians and Urban ¹⁵⁷ 1937 9 283 to 323 10.2 to 11.8 0.047 ran der Vet ¹⁷⁴ 1937 9 283 to 323 10.2 to 11.8 0.047 ran der Vet ¹⁷⁴ 1937 9 283 to 320 10.2 to 11.7 0.075 Romas and Harrison ¹⁶⁸ 1982 1 368 3.61 0.2 to 11.7 0.075 Romas and Harrison ¹⁶⁸ 1982 1 368 3.61 0.2 to 11.7 0.075 Romas and Harrison ¹⁶⁸ 1982 1 368 3.61 0.2 to 11.7 0.075 Romas and Harrison ¹⁶⁸ 1982 1 368 3.61 0.2 to 11.7 0.075 Romas and Harrison ¹⁶⁸ 1982 1 368 3.61 0.2 to 11.7 0.075 Romas and Harrison ¹⁶⁸ 1982 1 368 3.61 0.2 to 11.7 0.075 Romas and Harrison ¹⁶⁸ 1982 1 368 3.61 0.2 to 11.7 0.075 Romas and Harrison ¹⁶⁸ 1982 1 368 3.61 0.2 to 11.7 0.075 Romas and Harrison ¹⁶⁸ 1982 1 368 3.61 0.2 to 11.7 0.075 Romas and Harrison ¹⁶⁸ 1982 1 368 3.61 0.2 to 11.7 0.7 0.7 0.7 0.2 to 11.7 0.7 0.7 | Luo and Miller ¹¹³ | 1981 | | | | 11.5 to 13.5 | 0.055 |
| Miyamoto and Uematsu ¹²⁶ 2007 6 280 to 365 7.2 to 11.8 0.144 Neisean and Rainwater ¹³⁰ 1990 4 311 to 361 7.71 to 10.7 0.038 Porit and Laupretre ¹³⁴ 1978 31 86.7 to 244 12.8 to 16.6 0.026 Reamer et al. ¹⁴⁴ 1949 10 313 to 370 5 to 10.6 0.54 Rodosevich and Miller ¹⁴⁷ 1973 4 91 to 115 15.9 to 16.5 0.049 Sage et al. ¹⁵¹ 1934 21 294 to 371 6.51 to 11.4 2.42 Seeman and Urban ¹⁵⁷ 1963 27 278 to 299 11.1 to 11.9 0.056 Silwinski ¹⁶² 1969 14 283 to 372 5.67 to 11.7 0.342 Tomilinson ¹⁷⁰ 1971 11 278 to 323 10.2 to 11.8 0.047 Abdulagatov et al. ³ 1997 17 11 278 to 323 10.2 to 11.8 0.047 Abdulagatov et al. ³ 1995 11 342 to 370 1.4 to 4.7 1.65 Anisimov et al. ⁶ 1982 1 368 3.61 0.833 Barber et al. ¹⁰ 1982 9 329 to 370 1.02 to 4.21 0.886 Barber et al. ¹⁰ 1982 9 329 to 370 0.981 to 3.67 3.9 Clark ²⁶ 1973 5 327 to 370 0.981 to 3.67 3.9 Clark ²⁶ 1973 5 327 to 370 0.981 to 3.67 3.9 Clark ²⁶ 1973 5 290 to 323 0.381 to 0.859 to 4.92 1.55 Dana et al. ³² 1926 5 290 to 323 0.381 to 0.859 0.967 Deschner and Brown ³⁶ 1940 14 303 to 368 0.454 to 3.58 3.69 Deschner and Brown ³⁶ 1940 14 303 to 368 0.454 to 3.58 3.69 Deschner and Brown ³⁶ 1940 14 303 to 368 0.454 to 3.58 3.69 Deschner and Brown ³⁶ 1995 14 313 to 364 0.669 to 2.4 0.597 Deschner and Alainwater ¹³⁰ 1995 14 313 to 364 0.669 to 2.4 0.597 Deschner and Alainwater ¹³⁰ 1995 14 313 to 364 0.669 to 2.42 1.36 Deschner and Alainwater ¹³⁰ 1995 14 313 to 364 0.669 to 2.42 1.36 Deschner and Alainwater ¹³⁰ 1995 14 313 to 360 0.669 to 2.40 0.597 Deschner and Alainwater ¹³⁰ 1995 14 313 to 364 0.669 to 2.42 1.36 Deschner and Alainwater ¹³⁰ 1995 14 313 to 360 0.669 to 2.42 1.36 Deschner and Alainwater ¹³⁰ 1995 14 313 to 360 0.669 to 2.40 0.597 Deschner and Alainwater ¹³⁰ 1995 14 313 to 360 0.669 to 2.40 0.595 Deschner and Alainwater ¹³⁰ 1995 14 313 to 360 0.669 to 2.40 0.595 Deschner and Alainwater ¹³⁰ 1995 14 313 to 370 0.695 to 5 1.89 Deschner and Alainwater ¹³⁰ 1995 15 | Maass and Wright ¹¹⁴ | 1921 | | 195 to 249 | | | 0.31 |
| Siesen and Rainwater 190 190 4 311 to 361 7.71 to 10.7 0.038 | AcClune ¹¹⁸ | 1976 | 17 | 93.2 to 173 | | 14.6 to 16.4 | 0.037 |
| 12.8 to 16.6 0.026 | Miyamoto and Uematsu ¹²⁶ | 2007 | 6 | 280 to 365 | | 7.2 to 11.8 | 0.144 |
| Reamer et al. 144 1949 10 313 to 370 5 to 10.6 0.54 Rodosevich and Miller 147 1973 4 91 to 115 15.9 to 16.5 0.049 age et al. 151 1934 21 294 to 371 6.51 to 11.4 2.42 195 to 16.5 10.14 2.42 195 to 16.5 10.14 195 195 195 195 195 195 195 195 195 195 | Niesen and Rainwater ¹³⁰ | 1990 | | | | 7.71 to 10.7 | 0.038 |
| teamer et al. 144 1949 10 313 to 370 5 to 10.6 0.54 todosevich and Miller 147 1973 4 91 to 115 15.9 to 16.5 0.049 (age et al. 151 1934 21 294 to 371 6.51 to 11.4 2.42 (aeeman and Urban 157 1963 27 278 to 299 11.1 to 11.9 0.056 (aliwinski 162 1969 14 283 to 372 5.67 to 11.7 0.342 (aeeman and Harrison 168 1982 22 258 to 369 6.08 to 12.4 0.12 (arminsmor 170 1971 11 278 to 323 10.2 to 11.8 0.047 (an der Vet 174 1937 9 283 to 323 10.2 to 11.8 0.047 (an der Vet 174 1937 9 283 to 323 10.2 to 11.7 0.075 (arminsmor et al. 10 1982 1 368 3.61 0.833 (arminsmor et al. 10 1982 9 329 to 370 1.02 to 4.21 0.886 (alika 167 3.9 arminsmor et al. 10 1982 9 329 to 370 0.981 to 3.67 3.9 (alika 168 20 492 1.55 20 and et al. 12 1926 5 290 to 323 0.381 to 0.859 to 4.92 1.55 20 and et al. 12 1926 5 290 to 323 0.381 to 0.859 0.967 (alika 168 20 42 110 to 340 0 to 1.34 2.11 (alika 20 42 1.10 to 340 0 to 1.34 2.11 (alika 20 42 1.10 to 340 0 to 1.34 2.11 (alika 20 42 1.36 42 | Orrit and Laupretre ¹³⁴ | 1978 | 31 | 86.7 to 244 | | 12.8 to 16.6 | 0.026 |
| Rodosevich and Miller ¹⁴⁷ 1973 4 91 to 115 15.9 to 16.5 0.048 size et al. 151 0.015 size et al. 151 0.056 size et al. 102 size et al. 102 size et al. 103 0.047 size et al. 102 size et al. 103 0.047 size et al. 103 size et al. 104 0.047 size et al. 104 0.048 size et al. 104 0.048 size et al. 104 | Reamer et al. 144 | | | | | | |
| Sage et al. 151 1934 21 294 to 371 6.51 to 11.4 2.42 Seeman and Urban 157 1963 27 278 to 299 11.1 to 11.9 0.056 Silwinski 162 1969 14 283 to 372 5.67 to 11.7 0.342 Thomas and Harrison 168 1982 22 258 to 369 6.08 to 12.4 0.12 Tomlinson 170 1971 11 278 to 323 10.2 to 11.8 0.047 Van der Vet 174 1937 9 283 to 323 10.2 to 11.7 0.075 Saturated Vapor Densities Saturated Vapor Densities Abdulagatov et al. 3 1995 11 342 to 370 1.4 to 4.7 1.65 Ansismov et al. 6 1982 1 368 3.61 0.833 Barber et al. 10 1982 9 329 to 370 1.02 to 4.21 0.886 Clark 26 1973 5 327 to 370 0.981 to 3.67 3.9 Clegg and Rowlinson 28 1955 9 323 to 370 0.859 to 4.92 | Rodosevich and Miller ¹⁴⁷ | 1973 | 4 | | | | 0.049 |
| Seeman and Urban 157 | Sage et al. 151 | | | 294 to 371 | | | |
| Stiminski 162 1969 14 283 to 372 5.67 to 11.7 0.342 | Seeman and Urban ¹⁵⁷ | | | | | | 0.056 |
| Chomas and Harrison 168 | Sliwinski ¹⁶² | | | | | | 0.342 |
| Complisson Tomple 1971 11 278 to 323 10.2 to 11.8 0.047 | Thomas and Harrison 168 | | | | | | |
| Saturated Vapor Densities Abdulagatov et al. ³ 1995 11 342 to 370 1.4 to 4.7 1.65 Anisimov et al. ⁶ 1982 1 368 3.61 0.833 Barber et al. ¹⁰ 1982 9 329 to 370 1.02 to 4.21 0.886 Clark ²⁶ 1973 5 327 to 370 0.981 to 3.67 3.9 Clegg and Rowlinson ²⁸ 1955 9 323 to 370 0.859 to 4.92 1.55 Obeschner and Brown ³⁶ 1940 14 303 to 368 0.454 to 3.58 3.69 Glos et al. ⁴⁸ 2004 24 110 to 340 0 to 1.34 2.11 Helgeson and Sage ⁶³ 1967 16 278 to 361 0.267 to 2.4 0.597 Holcomb and Outcalt ⁷¹ 1998 4 290 to 350 0.374 to 1.72 1.1 Holcomb et al. ⁷⁰ 1995 14 313 to 364 0.689 to 2.69 0.958 Reamer et al. ¹⁴⁴ 1949 10 313 to 370 0.695 to 5 1.89 Reamer et al. ¹⁵¹ 1934 21 294 to 371 0.433 to 4.05 2.42 Sliwinski ¹⁶² 1969 15 283 to 370 0.314 to 4.32 0.557 | Fomlinson ¹⁷⁰ | | | | | | 0.047 |
| Saturated Vapor Densities Abdulagatov et al. 3 1995 11 342 to 370 1.4 to 4.7 1.65 Anisimov et al. 6 1982 1 368 3.61 0.833 Barber et al. 10 1982 9 329 to 370 1.02 to 4.21 0.886 Clark 26 1973 5 327 to 370 0.981 to 3.67 3.9 Clegg and Rowlinson 28 1955 9 323 to 370 0.859 to 4.92 1.55 Dana et al. 32 1926 5 290 to 323 0.381 to 0.859 0.967 Deschner and Brown 36 1940 14 303 to 368 0.454 to 3.58 3.69 Cleges on and Sage 63 1967 16 278 to 361 0.267 to 2.4 0.597 Holcomb and Outcalt 71 1998 4 290 to 350 0.374 to 1.72 1.1 Cledicomb et al. 70 1995 14 313 to 364 0.689 to 2.69 0.958 Clear et al. 144 1949 10 313 to 370 0.695 to 5 1.89 Clear et al. 151 1934 21 294 to 371 0.433 to 4.05 2.42 Clivinski 162 1969 15 283 to 370 0.314 to 4.32 0.557 | an der Vet ¹⁷⁴ | | | | | | 0.079 |
| Abdulagatov et al. 3 1995 11 342 to 370 1.4 to 4.7 1.65 Anisimov et al. 6 1982 1 368 3.61 0.833 (arber et al. 10 1982 9 329 to 370 1.02 to 4.21 0.886 (ark 26 1982 1973 5 327 to 370 0.981 to 3.67 3.9 (ark 27 1926 5 290 to 323 0.381 to 0.859 to 4.92 1.55 (ara et al. 32 1926 5 290 to 323 0.381 to 0.859 to 4.92 1.55 (ara et al. 32 1926 5 290 to 323 0.381 to 0.859 0.967 (are al. 48 10 to 340 0 to 1.34 2.11 (are al. 48 10 to 340 0 to 1.34 2.11 (are al. 48 10 to 340 0 to 1.34 2.11 (are al. 48 10 to 340 0 to 1.34 2.11 (are al. 48 10 to 340 0 to 1.34 2.11 (are al. 48 10 to 340 0 to 1.34 2.11 (are al. 48 10 to 340 0 to 1.34 2.11 (are al. 48 10 to 340 0 to 1.34 2.11 (are al. 48 10 to 340 0 to 1.34 2.11 (are al. 48 10 to 340 0 to 350 0.374 to 1.72 1.1 (are al. 48 10 to 340 0 to 350 0.374 to 1.72 1.1 (are al. 48 10 to 340 0 to 350 0.374 to 1.72 1.1 (are al. 48 11 to 361 0.689 to 2.69 0.958 (are al. 48 11 to 361 0.646 to 2.42 1.36 (are al. 44 11 to 361 0.646 to 2.42 1.36 (are al. 44 11 10 to 340 0 to 371 0.433 to 4.05 2.42 (are al. 48 11 11 11 11 11 11 11 11 11 11 11 11 11 | | | 9 | Saturated Vapor Densities | | | |
| Anisimov et al. 6 1982 1 368 3.61 0.833 Barber et al. 10 1982 9 329 to 370 1.02 to 4.21 0.886 Clark 26 1973 5 327 to 370 0.981 to 3.67 3.9 Clarg and Rowlinson 28 1955 9 323 to 370 0.859 to 4.92 1.55 Dana et al. 32 1926 5 290 to 323 0.381 to 0.859 to 4.92 1.55 Deschner and Brown 36 1940 14 303 to 368 0.454 to 3.58 3.69 Glos et al. 48 2004 24 110 to 340 0 to 1.34 2.11 Clargeson and Sage 63 1967 16 278 to 361 0.267 to 2.4 0.597 Clargeson and Outcalt 71 1998 4 290 to 350 0.374 to 1.72 1.1 Clocomb and Outcalt 70 1995 14 313 to 364 0.689 to 2.69 0.958 Cles et al. 144 1949 10 313 to 370 0.695 to 5 1.89 Clark 26 1969 15 283 to 370 0.314 to 4.32 0.557 Clark 26 1969 15 283 to 370 0.314 to 4.32 0.557 | Abdulagatov et al.3 | 1995 | | | | 1.4 to 4.7 | 1.65 |
| Barber et al. 10 1982 9 329 to 370 1.02 to 4.21 0.886 Clark 26 1973 5 327 to 370 0.981 to 3.67 3.9 Clegg and Rowlinson 28 1955 9 323 to 370 0.859 to 4.92 1.55 Dana et al. 32 1926 5 290 to 323 0.381 to 0.859 0.967 Deschner and Brown 36 1940 14 303 to 368 0.454 to 3.58 3.69 Clegs and Sage 63 1967 16 278 to 361 0.267 to 2.4 0.597 Holcomb and Outcalt 71 1998 4 290 to 350 0.374 to 1.72 1.1 Holcomb et al. 70 1995 14 313 to 364 0.689 to 2.69 0.958 Niesen and Rainwater 130 1990 4 311 to 361 0.689 to 2.69 0.958 Reamer et al. 144 1949 10 313 to 370 0.695 to 5 1.89 age et al. 151 1934 21 294 to 371 0.433 to 4.05 2.42 Sliwinski 162 1969 15 283 to 370 0.314 to 4.32 0.557 | Anisimov et al ⁶ | | | | | | |
| Clark ²⁶ 1973 5 327 to 370 0.981 to 3.67 3.9 Clegg and Rowlinson ²⁸ 1955 9 323 to 370 0.859 to 4.92 1.55 Dana et al. ³² 1926 5 290 to 323 0.381 to 0.859 0.967 Deschner and Brown ³⁶ 1940 14 303 to 368 0.454 to 3.58 3.69 Bilos et al. ⁴⁸ 2004 24 110 to 340 0 to 1.34 2.11 Belgeson and Sage ⁶³ 1967 16 278 to 361 0.267 to 2.4 0.597 Bolcomb and Outcalt ⁷¹ 1998 4 290 to 350 0.374 to 1.72 1.1 Bolcomb et al. ⁷⁰ 1995 14 313 to 364 0.689 to 2.69 0.958 Biesen and Rainwater ¹³⁰ 1990 4 311 to 361 0.646 to 2.42 1.36 Reamer et al. ¹⁴⁴ 1949 10 313 to 370 0.695 to 5 1.89 Biage et al. ¹⁵¹ 1934 21 294 to 371 0.433 to 4.05 2.42 Biliwinski ¹⁶² 1969 15 283 to 370 0.314 to 4.32 0.557 | | | | | | | |
| Clegg and Rowlinson ²⁸ 1955 9 323 to 370 0.859 to 4.92 1.55 Dana et al. ³² 1926 5 290 to 323 0.381 to 0.859 0.967 Deschner and Brown ³⁶ 1940 14 303 to 368 0.454 to 3.58 3.69 Bilos et al. ⁴⁸ 2004 24 110 to 340 0 to 1.34 2.11 Belgeson and Sage ⁶³ 1967 16 278 to 361 0.267 to 2.4 0.597 Bolcomb and Outcalt ⁷¹ 1998 4 290 to 350 0.374 to 1.72 1.1 Bolcomb et al. ⁷⁰ 1995 14 313 to 364 0.689 to 2.69 0.958 Biesen and Rainwater ¹³⁰ 1990 4 311 to 361 0.646 to 2.42 1.36 Beamer et al. ¹⁴⁴ 1949 10 313 to 370 0.695 to 5 1.89 Biage et al. ¹⁵¹ 1934 21 294 to 371 0.433 to 4.05 2.42 Biliwinski ¹⁶² 1969 15 283 to 370 0.314 to 4.32 0.557 | | | | | | | |
| Dana et al. 32 1926 5 290 to 323 0.381 to 0.859 0.967 Deschner and Brown 36 1940 14 303 to 368 0.454 to 3.58 3.69 Deschner and Brown 36 1940 14 303 to 368 0.454 to 3.58 3.69 Deschner and Sage 63 1967 16 278 to 361 0.267 to 2.4 0.597 Descends and Outcalt 71 1998 4 290 to 350 0.374 to 1.72 1.1 Descends and Outcalt 70 1995 14 313 to 364 0.689 to 2.69 0.958 Descends and Rainwater 130 1990 4 311 to 361 0.646 to 2.42 1.36 Descends and Rainwater 130 1990 4 311 to 361 0.646 to 2.42 1.36 Descends and Rainwater 130 1949 10 313 to 370 0.695 to 5 1.89 Descends 151 1934 21 294 to 371 0.433 to 4.05 2.42 Descends 151 1934 21 294 to 371 0.433 to 4.05 2.42 Descends 151 1969 15 283 to 370 0.314 to 4.32 0.557 | | | | | | | |
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| Blos et al. 48 2004 24 110 to 340 0 to 1.34 2.11 delgeson and Sage 63 1967 16 278 to 361 0.267 to 2.4 0.597 dolcomb and Outcalt 71 1998 4 290 to 350 0.374 to 1.72 1.1 dolcomb et al. 70 1995 14 313 to 364 0.689 to 2.69 0.958 desamen and Rainwater 130 1990 4 311 to 361 0.646 to 2.42 1.36 decamer et al. 144 1949 10 313 to 370 0.695 to 5 1.89 age et al. 151 1934 21 294 to 371 0.433 to 4.05 2.42 liwinski 162 1969 15 283 to 370 0.314 to 4.32 0.557 | | | | | | | |
| Helgeson and Sage 63 1967 16 278 to 361 0.267 to 2.4 0.597 Holcomb and Outcalt 71 1998 4 290 to 350 0.374 to 1.72 1.1 Holcomb et al. 70 1995 14 313 to 364 0.689 to 2.69 0.958 Hiesen and Rainwater 130 1990 4 311 to 361 0.646 to 2.42 1.36 Reamer et al. 144 1949 10 313 to 370 0.695 to 5 1.89 Hage et al. 151 1934 21 294 to 371 0.433 to 4.05 2.42 Hiliwinski 162 1969 15 283 to 370 0.314 to 4.32 0.557 | Pescilici and Diown | | | | | | |
| Holcomb and Outcalt ⁷¹ 1998 4 290 to 350 0.374 to 1.72 1.1 Holcomb et al. ⁷⁰ 1995 14 313 to 364 0.689 to 2.69 0.958 Wiesen and Rainwater ¹³⁰ 1990 4 311 to 361 0.646 to 2.42 1.36 Reamer et al. ¹⁴⁴ 1949 10 313 to 370 0.695 to 5 1.89 Gage et al. ¹⁵¹ 1934 21 294 to 371 0.433 to 4.05 2.42 Sliwinski ¹⁶² 1969 15 283 to 370 0.314 to 4.32 0.557 | JIOS et al. | | | | | | |
| Holcomb et al. ⁷⁰ 1995 14 313 to 364 0.689 to 2.69 0.958 Viesen and Rainwater ¹³⁰ 1990 4 311 to 361 0.646 to 2.42 1.36 Reamer et al. ¹⁴⁴ 1949 10 313 to 370 0.695 to 5 1.89 Gage et al. ¹⁵¹ 1934 21 294 to 371 0.433 to 4.05 2.42 Sliwinski ¹⁶² 1969 15 283 to 370 0.314 to 4.32 0.557 | reigeson and Sage | | | | | | |
| Wiesen and Rainwater 130 1990 4 311 to 361 0.646 to 2.42 1.36 Reamer et al. 144 1949 10 313 to 370 0.695 to 5 1.89 Gage et al. 151 1934 21 294 to 371 0.433 to 4.05 2.42 Gliwinski 162 1969 15 283 to 370 0.314 to 4.32 0.557 | ioicomb and Outcalt' | | | | | | |
| Reamer et al. ¹⁴⁴ 1949 10 313 to 370 0.695 to 5 1.89 dage et al. ¹⁵¹ 1934 21 294 to 371 0.433 to 4.05 2.42 diwinski ¹⁶² 1969 15 283 to 370 0.314 to 4.32 0.557 | ioicomb et al. | | | | | | |
| Sage et al. ¹⁵¹ 1934 21 294 to 371 0.433 to 4.05 2.42 Sliwinski ¹⁶² 1969 15 283 to 370 0.314 to 4.32 0.557 | nesen and Rainwater 130 | | | | | | |
| Sliwinski ¹⁶² 1969 15 283 to 370 0.314 to 4.32 0.557 | Reamer et al. | | | | | | |
| Sliwinski ¹⁰² 1969 15 283 to 370 0.314 to 4.32 0.557 Thomas and Harrison ¹⁶⁸ 1982 11 323 to 369 0.876 to 3.92 0.115 | Sage et al. 151 | | | | | | |
| Γhomas and Harrison ¹⁰⁸ 1982 11 323 to 369 0.876 to 3.92 0.115 | Sliwinski 102 | | | | | | 0.557 |
| | Γhomas and Harrison ¹⁶⁸ | 1982 | 11 | 323 to 369 | | 0.876 to 3.92 | 0.115 |

Table 3. Continued

| | | | temperature range | pressure range | density range | |
|---|--------------|---------------|---------------------------------|--------------------------------|--|----------------|
| author | year | no. of points | (T/K) | (p/MPa) | $(\rho/\text{mol}\cdot\text{dm}^{-3})$ | $AARD^a$ (%) |
| | | Enthalpie | s of Vaporization | | | |
| Dana et al. ³² | 1926 | 14 | 234 to 293 | | | 1.12 |
| Guigo et al. ⁵⁴ | 1978 | 12 | 186 to 363 | | | 0.49 |
| Helgeson and Sage ⁶³ | 1967 | 14 | 311 to 330 | | | 0.931 |
| Kemp and Egan ⁸⁹ | 1938 | 1 | 231 | | | 0.046 |
| Sage et al. 149 | 1939 | 16 | 313 to 348 | | | 2.21 |
| | 1006 | | Densities | 200 | 5.50 | 0.000 |
| Aalto and Liukkonen ¹ | 1996 | 55 | 343 to 373 | 3.99 to 6.99 | 5.58 to 9.97 | 0.988 |
| Babb and Robertson ⁷ Beattie et al. ¹² | 1970 | 63 82 | 308 to 473 | 63.8 to 1070 4.25 to 4.29 | 13 to 18.5 | 0.368 |
| Burgoyne ¹⁷ | 1935 1940 | 62 41 | 370 243 to 294 | 0.507 to 6.08 | 4.2 to 5.92 11.4 to 13.2 | 9.12 1.26 |
| Cherney et al. ²³ | 1940 | 25 | 323 to 398 | 1.08 to 4.98 | 0.383 to 2.58 | 0.1 |
| Claus et al. ²⁷ | 2002 | 130 | 340 to 520 | 1.99 to 30.2 | 0.543 to 11.5 | 0.015 |
| Dawson and McKetta ³³ | 1960 | 18 | 243 to 348 | 0.049 to 0.184 | 0.021 to 0.071 | 0.034 |
| Defibaugh and Moldover ³⁴ | 1997 | 945 | 245 to 372 | 1.2 to 6.51 | 6.23 to 13 | 0.094 |
| Deschner and Brown ³⁶ | 1940 | 275 | 303 to 609 | 0.101 to 14.8 | 0.023 to 11.7 | 0.667 |
| Dittmar et al. ³⁷ | 1962 | 335 | 273 to 413 | 0.981 to 103 | 7.26 to 13.4 | 0.218 |
| Ely and Kobayashi ⁴¹ | 1978 | 222 | 166 to 324 | 0.096 to 42.8 | 11.5 to 14.8 | 0.09 |
| Galicia-Luna et al. ⁴⁶ | 1994 | 60 | 323 to 398 | 2.5 to 39.5 | 6.34 to 12.1 | 0.075 |
| Glos et al. ⁴⁸ | 2004 | 72 | 95 to 340 | 0.201 to 12.1 | 0.078 to 16.5 | 0.003 |
| Golovskoi et al. ⁵⁰ | 1991 | 155 | 88.2 to 272 | 1.54 to 61 | 13.5 to 16.7 | 0.204 |
| Haynes ⁶⁰ | 1983 | 196 | 90 to 300 | 0.614 to 37.5 | 11.2 to 16.8 | 0.123 |
| Huang et al. ⁷⁴ Jepson et al. ⁷⁹ | 1966 1957 | 36 8 | 173 to 273 | 0 to 34.5 0.993 to 3.29 | 12 to 15.2 | 0.386 |
| Kayukawa et al. ⁸⁷ | 2005 | 192 | 457 to 529 240 to 380 | 0.993 to 3.29 0.148 to 7.07 | 0.273 to 0.815 0.27 to 13.1 | 0.521 0.104 |
| Kayukawa et al. Kayukawa and Watanabe ⁸⁸ | 2003 | 26 | 305 to 380 | 0.583 to 3.81 | 0.27 to 13.1 0.253 to 1.93 | 0.169 |
| Kitajima et al. 94 | 2005 | 38 | 270 to 425 | 3.66 to 28.7 | 6.81 to 12.2 | 0.171 |
| Kratzke and Müller ⁹⁹ | 1984 | 60 | 247 to 491 | 2.24 to 60.9 | 10 to 12.8 | 0.035 |
| Manley and Swift ¹¹⁵ | 1971 | 19 | 244 to 333 | 2.07 to 11 | 10 to 13.1 | 0.111 |
| McLinden ¹²⁰ (excluding critical region) | 2009 | 261 | 265 to 500 | 0.262 to 35.9 | 0.101 to 13.2 | 0.021 |
| McLinden ¹²⁰ (critical region) | 2009 | 33 | 369 to 372 | 4.24 to 4.42 | 4.0 to 5.56 | 0.750 |
| Miyamoto and Uematsu ¹²⁵ | 2006 | 63 | 340 to 400 | 3 to 200 | 7.59 to 14.3 | 0.099 |
| Miyamoto and Uematsu ¹²⁶ | 2007 | 59 | 280 to 365 | 0.581 to 4.03 | 7.21 to 11.8 | 0.153 |
| Miyamoto et al. 124 | 2007 | 147 | 280 to 440 | 1 to 200 | 7.59 to 15 | 0.094 |
| Perkins et al. 139 | 2009 | 253 | 99.7 to 346 | 1.61 to 34.7 | 10.4 to 16.3 | 0.012 |
| Prasad ¹⁴¹ | 1982 | 111 | 373 to 423 | 0.177 to 4.66 | 0.052 to 2.5 | 0.634 |
| Reamer et al. ¹⁴⁴ Richter et al. ¹⁴⁶ | 1949 | 306 1 | 311 to 511 273 | 0.101 to 68.9 0.101 | 0.024 to 13.1 0.046 | 0.145 |
| Rodosevich and Miller ¹⁴⁷ | 2009 1973 | 4 | 91 to 115 | 0.013 to 0.05 | 15.9 to 16.5 | 0.009 0.048 |
| Sage et al. 151 | 1934 | 154 | 294 to 378 | 0.013 to 0.03 0.172 to 20.7 | 0.056 to 12.3 | 1.15 |
| Seeman and Urban ¹⁵⁷ | 1963 | 28 | 203 to 230 | 0.101 | 13.2 to 13.9 | 0.038 |
| Seibt ¹⁵⁸ | 2008 | 108 | 373 | 0.07 to 29.8 | 0.023 to 10.7 | 0.568 |
| Starling et al. 163 | 1984 | 25 | 273 to 323 | 0.05 to 1.4 | 0.021 to 0.657 | 0.027 |
| Straty and Palavra ¹⁶⁴ | 1984 | 144 | 363 to 598 | 0.221 to 34.6 | 0.051 to 7.88 | 0.179 |
| Teichmann ¹⁶⁶ | 1978 | 148 | 323 to 573 | 2.77 to 60.9 | 2.44 to 10.5 | 0.075 |
| Thomas and Harrison ¹⁶⁸ | 1982 | 834 | 258 to 623 | 0.511 to 40 | 0.8 to 12.5 | 2.73 |
| Tomlinson ¹⁷⁰ | 1971 | 40 | 278 to 328 | 1.06 to 13.8 | 10.3 to 12 | 0.123 |
| Warowny et al. 176 | 1978 | 51 | 373 to 423 | 0.319 to 6.31 | 0.105 to 3.85 | 0.332 |
| | | Second V | irial Coefficients ^a | | | |
| TRC (Frenkel et al.) ¹⁹⁴ | | 27 | 244 to 523 | | | 5.11 |
| Barber et al. ¹⁰ | 1982 | 8 | 329 to 398 | | | 4.55 |
| Barkan ¹¹ | 1983 | 18 | 220 to 560 | | | 1.36 |
| Chun ²⁴ | 1964 | 7 | 370 to 493 | | | 20.1 |
| Dawson and McKetta ³³ | 1960 | 6 | 243 to 348 | | | 11 |
| Esper et al. 43 | 1995 | 13 | 230 to 350 | | | 10 |
| Eubank et al. ⁴⁴ Glos et al. ⁴⁸ | 1973 | 13 | 260 to 550 | | | 15.4 |
| Gios et al Gunn ⁵⁵ | 2004 1958 | 5 11 | 260 to 340 311 to 511 | | | 0.852 6.69 |
| Hahn et al. ⁵⁶ | 1938 | 10 | 211 to 493 | | | 2.49 |
| Hirschfelder et al. ⁶⁸ | 1942 | 17 | 303 to 570 | | | 6.83 |
| Huff et al. 75 | 1963 | 5 | 311 to 511 | | | 4.99 |
| Kretschmer and Wiebe ¹⁰¹ | 1951 | 3 | 273 to 323 | | | 16.2 |
| Lichtenthaler and Schäfer ¹⁰⁹ | 1969 | 5 | 288 to 323 | | | 8.18 |
| McGlashan and Potter ¹¹⁹ | 1962 | 12 | 295 to 413 | | | 4.2 |
| Patel et al. 138 | 1988 | 4 | 373 to 423 | | | 2.39 |
| Pompe and Spurling ¹⁴⁰ | 1974 | 34 | 294 to 609 | | | 8.49 |
| Prasad ¹⁴¹ | 1982 | 6 | 373 to 423 | | | 2.15 |
| Schäfer et al. 153 | 1974 | 5 | 353 to 512 | | | 9.2 |
| Strein et al. 165 | 1971 | 11 | 296 to 493 | | | 1.15 |
| Thomas and Harrison ¹⁶⁸ | 1982 | 23 | 323 to 623 | | | 0.71 |
| Thomas and Harrison | 100 - | _ | 227 277 | | | |
| Trusler et al. ¹⁷¹ Warowny et al. ¹⁷⁶ | 1996 1978 | 7 6 | 225 to 375 373 to 423 | | | 0.695 2.02 |

Table 3. Continued

| | | | temperature range | pressure range | density range | |
|--|-------|---------------|--|----------------|--|-------------|
| author | year | no. of points | (T/K) | (p/MPa) | $(\rho/\text{mol} \cdot \text{dm}^{-3})$ | $AARD^a$ (% |
| | | Second A | coustic Virial Coefficients | 1 | | |
| Esper et al. ⁴³ | 1995 | 26 | 230 to 350 | | | 11.4 |
| Goodwin and Lemmon ⁵² | 1995 | 14 | 265 to 355 | | | 7.03 |
| He et al. ⁶² | 2002 | 4 | 293 to 323 | | | 12.4 |
| Trusler and Zarari ¹⁷² | 1996 | 7 | 225 to 375 | | | 4.85 |
| Truster and Zaran | 1,,,0 | , | | | | 1.05 |
| | | | d Virial Coefficients ^a | | | |
| Chun ²⁴ | 1964 | 7 | 370 to 493 | | | 21.5 |
| Glos et al. ⁴⁸ | 2004 | 5 | 260 to 340 | | | 3.71 |
| Patel et al. 138 | 1988 | 4 | 373 to 423 | | | 4.89 |
| Pompe and Spurling ¹⁴⁰ | 1974 | 37 | 294 to 609 | | | 10.2 |
| Thomas and Harrison ¹⁶⁸ | 1982 | 19 | 343 to 623 | | | 1.31 |
| Trusler et al. 171 | 1996 | 7 | 225 to 375 | | | 16.2 |
| Warowny et al. ¹⁷⁶ | 1978 | 6 | 373 to 423 | | | 1.66 |
| | | Third Ac | coustic Virial Coefficients ^a | | | |
| Trusler and Zarari ¹⁷² | 1996 | 7 | 225 to 375 | | | 31.3 |
| | | | Enthalpias | | | |
| V V | 1070 | 17 | Enthalpies | 5.07 | | 0.001 |
| Van Kasteren and Zeldenrust ¹⁷⁵ | 1979 | 17 | 110 to 270 | 5.07 | | 0.091 |
| | | | Speeds of Sound | | | |
| Goodwin and Lemmon ⁵² | 1995 | 80 | 265 to 355 | 0.008 to 1.76 | | 0.077 |
| He et al. ⁶² | 2002 | 24 | 293 to 323 | 0.203 to 0.669 | | 0.086 |
| Hurly et al. ⁷⁶ | 2003 | 11 | 298 | 0.099 to 0.831 | | 0.006 |
| Lacam ¹⁰³ | 1956 | 200 | 298 to 498 | 1.01 to 101 | | 1.48 |
| Meier ¹²¹ | 2009 | 298 | 240 to 420 | 1.3 to 100 | | 0.012 |
| Niepmann ¹²⁹ | 1984 | 227 | 200 to 340 | 0.02 to 60.6 | | 0.323 |
| Rao ¹⁴³ | 1971 | 10 | 143 to 228 | < 0.9 | | 16.4 |
| Terres et al. 167 | 1957 | 95 | 293 to 448 | <11.8 | | 1.99 |
| Trusler and Zarari ¹⁷² | 1996 | 68 | 225 to 375 | 0.01 to 0.851 | | 0.004 |
| Younglove ¹⁸³ | 1981 | 180 | 90 to 300 | <35 | | 0.05 |
| | | Isol | baric Heat Capacities | | | |
| Beeck ¹³ | 1936 | 4 | 273 to 573 | 0.101 | | 4.35 |
| Dobratz ³⁹ | 1941 | 4 | 294 to 444 | 0.101 | | 5.22 |
| Ernst and Büsser ⁴² | 1970 | 36 | 293 to 353 | 0.049 to 1.37 | | 0.141 |
| Kistiakowsky and Rice ⁹³ | 1940 | 5 | 294 to 361 | 0.101 | | 0.405 |
| Lammers et al. ¹⁰⁴ | 1978 | 16 | 120 to 260 | 2.53 to 5.07 | | 1.21 |
| Sage et al. ¹⁵² | 1937 | 10 | 294 to 444 | 0.101 | | 4.84 |
| Van Kasteren and Zeldenrust ¹⁷⁵ | 1979 | 24 | 110 to 270 | 2.53 to 5.07 | | 1.68 |
| Yesavage et al. ¹⁸¹ | 1969 | 199 | 116 to 422 | 1.72 to 13.8 | | 2.38 |
| | | C-4 | | | | |
| G d 134 : 30 | 1065 | | ration Heat Capacities | | | 0.760 |
| Cutler and Morrison ³⁰ | 1965 | 7 | 91.1 to 105 | | | 0.768 |
| Dana et al. ³² Goodwin ⁵³ | 1926 | 12 | 242 to 292 | | | 3.15 |
| | 1978 | 78 | 81.1 to 289 | | | 0.277 |
| Guigo et al. ⁵⁴ | 1978 | 22 | 163 to 363 | | | 0.354 |
| Kemp and Egan ⁸⁹ | 1938 | 22 | 89.7 to 230 | | | 0.349 |
| Perkins et al. 139 | 2009 | 223 | 88.9 to 344 | | | 0.321 |
| | | | horic Heat Capacities | | | |
| Abdulagatov et al. ² | 1996 | 88 | 370 to 472 | | 5.04 | 7.3 |
| Abdulagatov et al.3 | 1995 | 37 | 305 to 370 | | 1.4 to 10.9 | 12.2 |
| Anisimov et al.6 | 1982 | 52 | 271 to 374 | | 3.61 to 12 | 10.3 |
| Goodwin ⁵³ | 1978 | 128 | 85.6 to 337 | | 11.2 to 16.3 | 1.23 |
| Kitajima et al. ⁹⁴ | 2005 | 38 | 270 to 425 | | 6.81 to 12.2 | 6.05 |
| Perkins et al. ¹³⁹ | 2009 | 231 | 101 to 345 | | 10.4 to 16.3 | 0.843 |
| | | Two-Phas | e Isochoric Heat Capacitie | s | | |
| Abdulagatov et al. ² | 1996 | 70 | 292 to 370 | 9 | 5.04 | 1.4 |
| Abdulagatov et al. Abdulagatov et al. 4 | 1990 | 1582 | 288 to 370 | | 1.4 to 10.9 | 1.88 |
| Anisimov et al. ⁶ | 1997 | 95 | 85.7 to 370 | | 3.61 to 12 | 1.00 |
| Guigo et al. ⁵⁴ | 1982 | 22 | 163 to 363 | | 7.32 | 0.348 |
| Perkins et al. 139 | 2009 | 223 | 88.9 to 344 | | 9.08 to 16.5 | 1.0 |
| i Cikilis Ci di. | 2009 | 443 | 00.7 W 344 | | 7.00 to 10.J | 1.0 |

^a Values are given as average absolute differences in cm³⋅mol⁻¹ for the second virial coefficients and in cm⁶⋅mol⁻² for the third virial coefficients.

the vapor phase and the $\exp(-\delta^l)$ part in the liquid phase. Thus, at temperatures approaching the triple point temperature in the vapor phase, where the density is very small, higher values of d in the δ^d part of each term result in a smaller influence of the exponential increase in temperature. Likewise, in the liquid region at similar temperatures, a higher value of l dampens out the effect of the τ^t part in the term. At densities near the critical density, δ^d $\exp(-\delta^l)$ approaches a constant of around 0.4, and the shape of the τ^t contribution can greatly affect the critical region behavior of the model. Additional graphs and descriptions of these effects from different terms are explained below and in the work of Tillner-Roth.²⁰⁰ Equations of state should use the smallest possible value for t in the polynomial terms; in the new equation for propane developed here, the highest value of t is 4.62.

Fitting Procedures. The development of an equation of state is a process of correlating selected experimental data by leastsquares fitting methods with a model that is generally empirical in nature but is designed to exhibit proper limiting behavior in the ideal gas and low density regions and to extrapolate to temperatures and pressures higher than those defined by experiment. In all cases, experimental data are considered paramount, and the validity of any equation of state is established by its ability to represent the thermodynamic properties of the fluid within the uncertainty of the experimental values. The selected data are usually a subset of the available database determined by the correlator to be representative of the most accurate values measured. The type of fitting procedure (e.g., nonlinear versus linear fitting of the parameters) determines how the experimental data will be used. In this work, a small subset of data was used in nonlinear fitting due to the extensive calculations required to develop the equation. The resulting equation was then compared to all experimental data to verify that the data selection was sufficient to accurately represent the available data.

One of the biggest advantages in nonlinear fitting is the ability to fit experimental data using all of the properties that were measured. For example, in linear fitting of the speed of sound, a preliminary equation of state is required to transform measured values of pressure and temperature to the independent variables of density and temperature required by the equation of state. Additionally, the ratio c_p/c_v is required (also from a preliminary equation) to fit sound speed with linear methods. Nonlinear fitting can use pressure, temperature, and sound speed directly without any transformation of the input variables. Shock wave measurements of the Hugoniot curve are another example where nonlinear fitting can directly use pressure-density-enthalpy measurements even when the temperature for any given point is unknown. Another advantage in nonlinear fitting is the ability to use "greater than" or "less than" operators for controlling the extrapolation behavior of properties such as heat capacities or pressures at low or high temperatures. In linear fitting, only equalities can be used; thus curves are often extrapolated by hand, and data points are manually taken from the curves at various temperatures to give the fit the proper shape. With successive fitting, the curves are updated until the correlator is satisfied with the final qualitative behavior. In nonlinear fitting, curves can be controlled by ensuring that a calculated value along a constant property path is always greater (or less) than a previous value; thus, only the shape is specified, not the magnitude. The nonlinear fitter then determines the best value for the properties based on other information in a specific region.

Equations have been developed with linear regression techniques for several decades by fitting comprehensive wideranging sets of $p\rho T$ data, isochoric heat capacity data, linearized sound speed data (as a function of density and temperature), second virial coefficients, and vapor pressures calculated from an ancillary equation. This process typically results in final equations with 25 to 40 terms. A cyclic process is sometimes used consisting of linear optimization, nonlinear fitting, and repeated linearization. Ideally this process is repeated until differences between the linear and nonlinear solutions are negligible. In certain cases, this convergence could not be reached—this led to the development of the "quasi-nonlinear" optimization algorithm. However, since this algorithm still involves linear steps, it could not be used in combination with "less than" or "greater than" relations. Details about the quasinonlinear regression algorithm can be found elsewhere (Wagner, 195 Wagner and Pruss 199).

In the case of propane, only nonlinear methods were used here to arrive at the final equation. A good preliminary equation is required as a starting point in the nonlinear fitting process; in this work, the equation of Bücker and Wagner¹⁸⁷ for ethane was employed. Nonlinear fitting techniques were used to shorten and improve upon this equation. The exponents for density and temperature, given in eq 18 as t_k , d_k , and l_k , along with the coefficients and exponents in the Gaussian bell-shaped terms, were determined simultaneously with the coefficients of the equation. In addition, the terms in the ideal gas heat capacity equation and the reducing parameters (critical point) of the equation of state were fitted. Thus, with an 18 term equation, there were at times up to 90 values being fitted simultaneously to derive the equation presented here. The end result has very little similarity to the functional form for ethane with which it began.

The nonlinear algorithm adjusted the parameters of the equation of state to minimize the overall sum of squares of the deviations of calculated properties from the input data, where the residual sum of squares was represented as

$$S = \sum W_{\rho} F_{\rho}^2 + \sum W_{p} F_{p}^2 + \sum W_{c_{p}} F_{c_{p}}^2 + \dots$$
 (19)

where W is the weight assigned to each data point and F is the function used to minimize the deviations. The equation of state was fitted to $p\rho T$ data with either deviations in pressure, $F_p = (p_{\text{data}} - p_{\text{calc}})/p_{\text{data}}$, for vapor phase and critical region data, or deviations in density, $F_\rho = (\rho_{\text{data}} - \rho_{\text{calc}})/\rho_{\text{data}}$, for liquid phase data. Since the calculation of density as a function of temperature and pressure requires an iterative solution that greatly increases calculation time during the fitting process, the nearly equivalent, noniterative form

$$F_{\rho} = \frac{(p_{\text{data}} - p_{\text{calc}})}{\rho_{\text{data}}} \left(\frac{\partial \rho}{\partial p}\right)_{T} \tag{20}$$

was used instead, where $p_{\rm calc}$ and the derivative of density with respect to pressure were calculated at the ρ and T of the data point. Other experimental data were fitted in a like manner, e.g., $F_w = (w_{\rm data} - w_{\rm calc})/w_{\rm data}$ for the speed of sound. The weight for each selected data point was individually adjusted according to type, region, and uncertainty. Typical values of W are 1 for $p\rho T$ and vapor pressure values, 0.05 for heat capacities, and 10 to 100 for vapor sound speeds. The equation of state was constrained to the critical parameters by adding the values of the first and second derivatives of pressure with respect to density at the critical point, multiplied by some arbitrary weight, to the sum of squares. In this manner, the calculated values of these derivatives would be zero at the selected critical point given in eqs 1 to 3.

To reduce the number of terms in the equation, terms were eliminated in successive fits by either deleting the term that contributed least to the overall sum of squares in a previous fit or by combining two terms that had similar values of the exponents (resulting in similar contributions to the equation of state). After a term was eliminated, the fit was repeated until the sum of squares for the resulting new equation was of the same order of magnitude as the previous equation. The final functional form for propane included 18 terms, 11 of which were extended polynomials and 7 were Gaussian bell-shaped terms.

The exponents on density in the equation of state must be positive integers so that the derivatives of the Helmholtz energy with respect to density have the correct theoretical expansion around the ideal gas limit. Since noninteger values for the

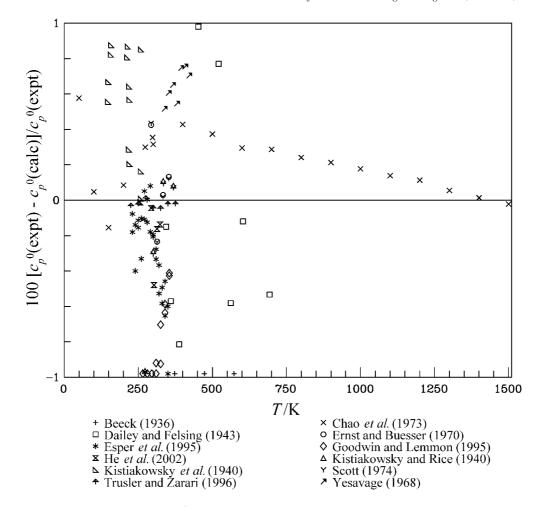


Figure 5. Comparisons of ideal gas heat capacities c_p^0 calculated with the equation of state to experimental and theoretical data as a function of temperature T.

density exponents resulted from the nonlinear fitting methods, a sequential process of rounding each density exponent to the nearest integer, followed by refitting the other parameters to minimize the overall sum of squares, was implemented until all of the density exponents in the final form were positive integers. A similar process was used for the temperature exponents to reduce the number of significant figures to one or two past the decimal point.

In addition to reducing the number of individual terms in the equation compared to that produced by conventional linear least-squares methods, the extrapolation behavior of the shorter equations is generally more accurate, partially because there are fewer degrees of freedom in the final equation. In the longer equations, two or more correlated terms are often needed to match the accuracy of a single term in the nonlinear fit. The values of these correlated terms can be large in magnitude and can lead to unreasonable behavior outside the range of validity. Span and Wagner¹⁹⁷ discuss the effects at high temperatures and pressures from intercorrelated terms.

The new fitting techniques and criteria that were created for the development of the R-125 equation of state (Lemmon and Jacobsen¹⁸⁹) were also used in the development of the propane equation of state. The details, which will not be repeated here, included proper handling of the second and third virial coefficients, elimination of the curvature of low-temperature isotherms in the vapor phase, control of the two-phase loops and the number of false two-phase solutions, convergence of the extremely high temperature isotherms to a single line (resulting from the term with t = 1 and d = 4), and proper control of the ideal curves (e.g., the Joule inversion curve). The R-125 paper describes what properties were added to the sum of squares so that the equation of state would behave properly and meet these criteria. As was done with R-125, a minimum number of simple polynomial terms (five) were used: three to represent the second virial coefficients (d = 1), one for the third virial coefficients (d=2), and one for the term for the extreme conditions (d=4). This final term is described in detail by Lemmon and Jacobsen. 189

Upon completion of the equation of state for propane, we began fitting an equation for propylene and have since found even better constraints and methods to control the derivatives of the equation of state and to force the extrapolation of the equation to near 0 K without any adverse behavior. This new work was not applied to propane since the equation had been completed and released in version 8 of the REFPROP software (Lemmon et al.²⁰¹). These new techniques will be described in the forthcoming publication of Lemmon et al.²⁰²

Equation of State of Propane

Previous Equations of State. Researchers worldwide have developed many equations of state for propane. Although a preliminary equation of state was presented in the work on the butanes by Bücker and Wagner¹⁸⁸ in 2006, it was intended only as an interim equation of state until the one presented here was finished, and it will not be referred to hereafter. A short equation

Table 4. Parameters and Coefficients of the Equation of State

| k | N_k | t_k | d_k | l_k | η_k | β_k | γ_k | ε_k |
|----|--------------|-------|-------|-------|----------|-----------|------------|-----------------|
| 1 | 0.042910051 | 1.00 | 4 | - | | | | |
| 2 | 1.7313671 | 0.33 | 1 | - | | | | |
| 3 | -2.4516524 | 0.80 | 1 | - | | | | |
| 4 | 0.34157466 | 0.43 | 2 | - | | | | |
| 5 | -0.46047898 | 0.90 | 2 | - | | | | |
| 6 | -0.66847295 | 2.46 | 1 | 1 | | | | |
| 7 | 0.20889705 | 2.09 | 3 | 1 | | | | |
| 8 | 0.19421381 | 0.88 | 6 | 1 | | | | |
| 9 | -0.22917851 | 1.09 | 6 | 1 | | | | |
| 10 | -0.60405866 | 3.25 | 2 | 2 | | | | |
| 11 | 0.066680654 | 4.62 | 3 | 2 | | | | |
| 12 | 0.017534618 | 0.76 | 1 | - | 0.963 | 2.33 | 0.684 | 1.283 |
| 13 | 0.33874242 | 2.50 | 1 | - | 1.977 | 3.47 | 0.829 | 0.6936 |
| 14 | 0.22228777 | 2.75 | 1 | - | 1.917 | 3.15 | 1.419 | 0.788 |
| 15 | -0.23219062 | 3.05 | 2 | - | 2.307 | 3.19 | 0.817 | 0.473 |
| 16 | -0.092206940 | 2.55 | 2 | - | 2.546 | 0.92 | 1.500 | 0.8577 |
| 17 | -0.47575718 | 8.40 | 4 | - | 3.28 | 18.8 | 1.426 | 0.271 |
| 18 | -0.017486824 | 6.75 | 1 | - | 14.6 | 547.8 | 1.093 | 0.948 |

of state was presented for propane in the work of Span and Wagner²⁰³ in 2003 to demonstrate the applicability of one functional form with fixed exponents to represent the properties of a broad range of nonpolar fluids. This form was not aimed at reaching the highest accuracy possible but to establish a new class of equations with a stable functional form that could be applied to fluids for which only limited experimental data were available. Their equations were designed for technical applications and do not compete with high-accuracy equations of state dedicated to a particular fluid. The Span and Wagner equation²⁰³ was used by Kunz et al.²⁰⁴ during the development of the GERG-2004 equation of state for natural gas mixtures. Miyamoto and Watanabe²⁰⁵ presented a 19-term equation in 2000 that is explicit in the Helmholtz energy with only simple and extended polynomial terms of the type described earlier. The 1987 equation of Younglove and Ely²⁰⁶ is a 32-term modified Benedict-Webb-Rubin equation. Sychev et al. 207 published an equation of state in 1991 in terms of the compressibility factor with 50 terms with only simple polynomials (without the exponential part).

One of the earlier equations of state that covered the full fluid range was that of Goodwin and Haynes²⁰⁸ from 1982; however, this equation used a unique functional form that cannot be easily implemented in computer algorithms, and it has seen little use since its publication. Their work extensively documents the available measurements prior to 1982. Even earlier equations include those of Bühner et al.²⁰⁹ in 1981 and Teja and Singh²¹⁰ in 1977 that were based on the Bender type of equation, which, although able to compute properties for both liquid and vapor states, lacked the higher accuracies obtained with the more recent equations.

These equations suffer from one or more shortcomings that have been removed in the current equation. These shortcomings include:

- (1) State-of-the-art thermodynamic data for propane are not represented to within their experimental uncertainties. These new data were described in the Introduction and were not available when the other equations were developed.
- (2) Some of the equations show unacceptable behavior in regions where experimental data were not available at the time of fitting. These regions represent accessible valid states of the fluid surface.
- (3) The magnitudes of pressure and other properties within the two-phase region reached enormous values (e.g., some

equations of state can reach up to pressures of $\pm~10^{50}$ MPa) caused by large exponents on the temperature term.

- (4) The extrapolation behavior outside the range of validity of the equations is poor or incorrect, especially at high pressures (densities) or at low temperatures.
- (5) Data in the extended critical region are not represented within their uncertainty.
 - (6) The ITS-90 temperature scale was not used.

The new equation presented here is an 18-term fundamental equation explicit in the reduced Helmholtz energy that overcomes all of these shortcomings. New optimization techniques, extrapolation criteria, and experimental data all contribute to make the equation state of the art. The range of validity of the equation of state for propane is from the triple point temperature (85.525 K) to 625 K at pressures to 1000 MPa, but it can be extended in all directions (higher temperatures, pressures, and densities, and lower temperatures) while maintaining physically reasonable behavior. In addition to the equation of state, ancillary functions were developed for the vapor pressure and for the densities of the saturated liquid and saturated vapor. These ancillary equations can be used as initial estimates in computer programs for defining the saturation boundaries but are not required to calculate properties from the equation of state.

The units adopted for this work were in kelvin (ITS-90) for temperature, megapascals for pressure, and moles per cubic decimeter for density. Units of the experimental data were converted as necessary from those of the original publications to these units. Where necessary, temperatures reported on IPTS-48 and IPTS-68 scales were converted to the International Temperature Scale of 1990 (ITS-90) (Preston-Thomas²¹¹). The $p\rho T$ and other data selected for the determination of the coefficients of the equation of state are described later along with comparisons of calculated properties to experimental values to verify the accuracy of the model developed in this research. Data used in fitting the equation of state for propane were selected to avoid redundancy in various regions of the surface.

New Equation of State. The critical temperature and density required in the reducing parameters for the equation of state given in eq 10 are 369.89 K and 5.00 mol·dm⁻³. The ideal gas reference state points are $T_0 = 273.15$ K, $p_0 = 0.001$ MPa, $h_0^0 = 26148.48$ J·mol⁻¹, and $s_0^0 = 157.9105$ J·mol⁻¹·K⁻¹. The values for h_0^0 and s_0^0 were chosen so that the enthalpy and entropy of the saturated liquid state at 0 °C are 200 kJ·kg⁻¹ and 1 kJ·kg⁻¹·K⁻¹, respectively, corresponding to the common convention in the refrigeration industry. Other values for h_0^0 and s_0^0 can be used, depending on the user's interest.

In the calculation of the thermodynamic properties of propane with an equation of state explicit in the Helmholtz energy, an equation for the ideal gas heat capacity, c_p^0 , is needed to calculate the Helmholtz energy for the ideal gas, α^0 . Values of the ideal gas heat capacity derived from low-pressure experimental heat capacity or speed of sound data are given in Table 3 along with theoretical values from statistical mechanics based on spectroscopic data (fundamental frequencies). Differences between the different sets of theoretical values arise from the use of different fundamental frequencies and from the models used to calculate the various couplings between the vibrational modes of the molecule. The equation for the ideal gas heat capacity for propane, used throughout the remainder of this work, was developed in part by fitting values reported by Trusler and Zarari¹⁷² and is given by

$$\frac{c_p^0}{R} = 4 + \sum_{k=3}^6 v_k \frac{u_k^2 \exp(u_k)}{\left[\exp(u_k) - 1\right]^2}$$
 (21)

where $v_3 = 3.043$, $v_4 = 5.874$, $v_5 = 9.337$, $v_6 = 7.922$, $u_3 = 393$ K/T, $u_4 = 1237$ K/T, $u_5 = 1984$ K/T, $u_6 = 4351$ K/T, and the gas constant, R, is $8.314472 \text{ J} \cdot \text{mol}^{-1} \cdot \text{K}^{-1}$ (Mohr et al. 212). The Einstein functions containing the terms u_3 , u_4 , u_5 , and u_6 were used so that the shape of the ideal gas heat capacity versus temperature would be similar to that derived from statistical mechanical models. However, these are empirical coefficients and should not be confused with the fundamental frequencies.

Comparisons of values calculated with eq 21 to the ideal gas heat capacity data are given in Figure 5. The sound speeds reported by Goodwin and Lemmon⁵² are greater than those determined by Trusler and Zarari¹⁷² and Hurly et al.⁷⁶ with differences that increase with decreasing temperature. All of the heat capacities derived from sound speed measurements are lower than values obtained from spectroscopic data, for example, as reported by Chao et al.²² A higher sound speed

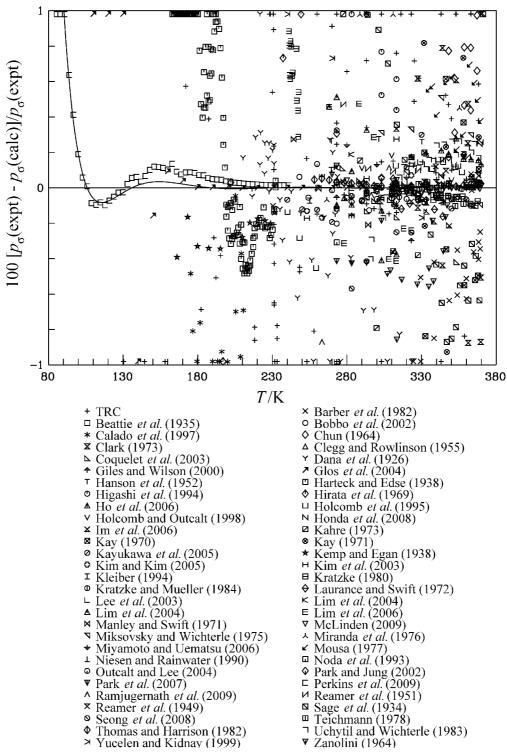


Figure 6. Comparisons of vapor pressures p_{σ} calculated with the equation of state to experimental data as a function of temperature T. The line corresponds to values calculated from the ancillary equation, eq 5.

implies a lower heat capacity—one plausible source of this difference is an impurity that has a speed of sound greater than propane, which is about 250 m·s⁻¹. The possible impurities include both air and argon that both have sound speeds of about 300 m·s⁻¹. It is possible to estimate the quantity of air required to give rise to the differences shown. However, no measurements have been performed to verify this conjecture, and neither Trusler and Zarari¹⁷² nor Esper et al.⁴³ give information about this discrepancy. This observation may be resolved by further experiments that are outside the realm of this work.

The ideal gas Helmholtz energy equation, derived from eqs 15 and 21, is

$$\alpha^{0} = \ln \delta + 3 \ln \tau + a_{1} + a_{2}\tau + \sum_{i=3}^{6} \nu_{i} \ln[1 - \exp(-b_{i}\tau)]$$
(22)

where $a_1 = -4.970583$, $a_2 = 4.29352$, $b_3 = 1.062478$, $b_4 = 3.344237$, $b_5 = 5.363757$, $b_6 = 11.762957$, and the values of v_k are the same as those used in eq 21. The values of b_k are equal to u_k divided by the critical temperature.

The coefficients N_k and other parameters of the residual part of the equation of state [given in eq 18 and repeated below] are given in Table 4.

$$\alpha^{r}(\delta, \tau) = \sum_{k=1}^{5} N_{k} \delta^{d_{k}} \tau^{l_{k}} + \sum_{k=6}^{11} N_{k} \delta^{d_{k}} \tau^{l_{k}} \exp(-\delta^{l_{k}}) + \sum_{k=12}^{18} N_{k} \delta^{d_{k}} \tau^{l_{k}} \exp(-\eta_{k} (\delta - \varepsilon_{k})^{2} - \beta_{k} (\tau - \gamma_{k})^{2})$$
 (23)

Experimental Data and Comparisons to the Equation of State

Since the identification of propane in 1910 by Dr. Walter O. Snelling at the U.S. Bureau of Mines, many experimental studies of the thermodynamic properties of propane have been reported, e.g., $p\rho T$ properties, saturation properties, critical parameters, heat capacities, speeds of sound, second virial coefficients, and ideal gas heat capacities (see refs 1–186). Goodwin and Haynes²⁰⁸ summarized most of the experimental data published for propane prior to 1982. Selected data were used for the development of the new thermodynamic property formulation reported here. Comparisons were made to all available experi-

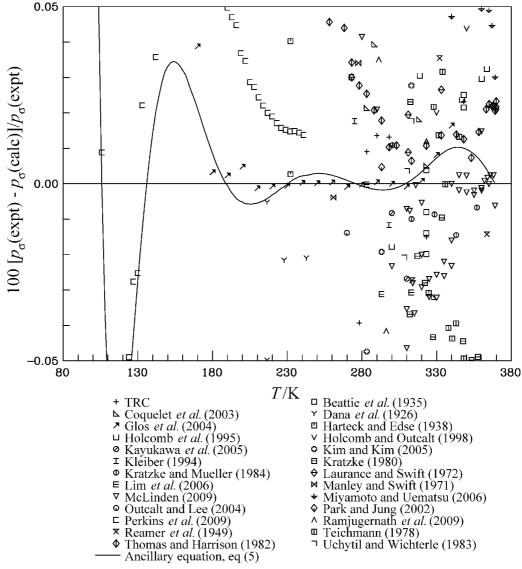


Figure 7. Comparisons of vapor pressures p_{σ} calculated with the equation of state to high-accuracy experimental data as a function of temperature T. The line corresponds to values calculated from the ancillary equation, eq 5.

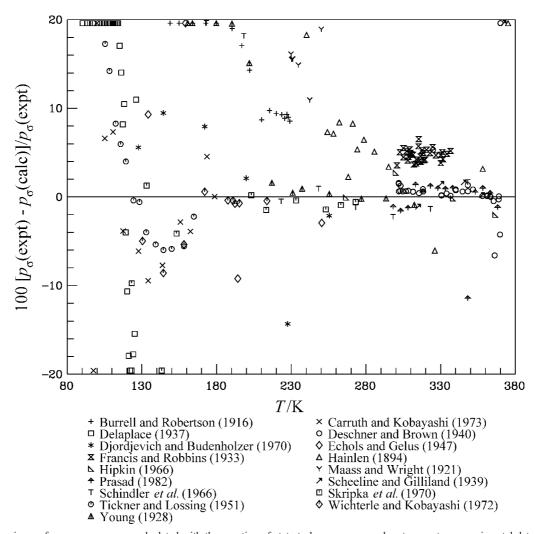


Figure 8. Comparisons of vapor pressures p_q calculated with the equation of state to low-accuracy or low-temperature experimental data as a function of temperature T.

mental data, including those not used in the development of the equation of state. Much of the data reported here was obtained from the Thermodynamic Data Engine (TDE) program (Frenkel et al. 194) available from the Thermodynamic Research Center (TRC) of NIST. Data sets with only one to three data points were not included in this work unless the data points were important to the development of the equation of state. Approximately 50 literature sources contained only one to three data points, and they are not identified here. However, these extra measurements are shown in the figures and are labeled as "TRC".

The accuracy of the equation of state was determined by statistical comparisons of calculated property values to experimental data. These statistics are based on the percent deviation in any property, X, defined as

$$\Delta X = 100 \left(\frac{X_{\text{data}} - X_{\text{calc}}}{X_{\text{data}}} \right) \tag{24}$$

With this definition, the average absolute relative deviation is defined as

$$AARD = \frac{1}{n} \sum_{i=1}^{n} |\Delta X_i|$$
 (25)

where n is the number of data points. The average absolute relative deviations between experimental data and calculated values from the equation of state are given in Table 3. In this table, measured saturation properties are compared with the equation of state, not with the ancillary equations. The comparisons given in the sections below for the various data sets compare values calculated from the equation of state to the experimental data with the average absolute relative deviations given by eq 25 unless otherwise stated (such as the maximum value). Discussions of maximum errors or of systematic offsets use the absolute values of the deviations. Data points with excessive deviations are shown at the outer limits of the plots to indicate where these outliers were measured.

Comparisons with Saturation Thermal Data. Figures 6 through 8 compare vapor pressures calculated from the equation of state with experimental data. Figure 6 gives an overview of deviations of the equation from most of the data; Figure 7 provides an expanded view of the highest accuracy data (those that were used to test the equation of state); and Figure 8 shows data of low accuracy or at low temperature where the pressures are extremely small (less than 1 Pa) and percentage deviations can be high. The lines in these figures represent the ancillary equation, eq 5. Most of the experimental vapor pressures for propane fall within 1 % of the equation of state above 300 K. Below this, the number of experimental data decreases, and the data that are available fall within 0.5 %. All of these data are scattered evenly around the equation. Of all the data measured

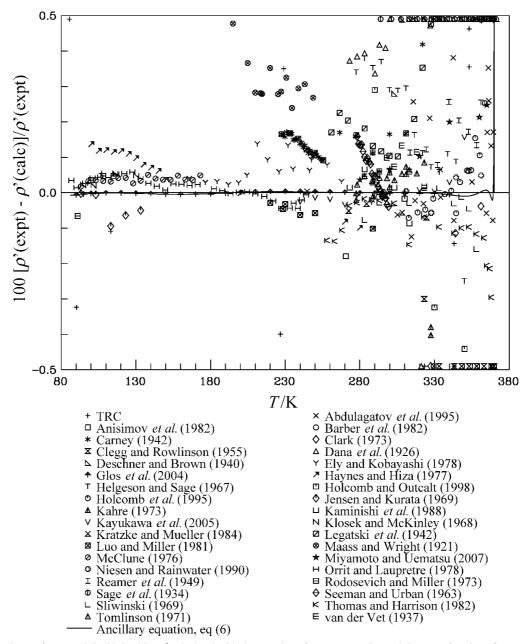


Figure 9. Comparisons of saturated liquid densities ρ' calculated with the equation of state to experimental data as a function of temperature T. The line corresponds to values calculated from the ancillary equation, eq 6.

before 1990, only 5 fall within the 0.1 % range: the data of Beattie et al., 12 Kratzke, 98 Kratzke and Müller, 99 Teichmann, 166 and Thomas and Harrison. 168 Of these, only the data of Beattie et al. were measured before 1970. Thus, unlike the data for the critical point, experimentalists have been able to greatly reduce the uncertainty in vapor pressure measurements with time. This is especially evident with the data measured after 2000 and which were used in the development of the equation of state. The data of Glos et al.⁴⁸ from the Ruhr Universität have an uncertainty in pressure ranging from 0.007 % at the highest temperature to 0.02 % at 230 K, and the equation shows deviations of less than 0.005 % (50 ppm) in the temperature range between (180 and 320) K. Below 150 K, the deviations increase to above 1 %, but the pressure at these low temperatures is extremely low, less than 300 Pa, and it becomes very difficult to make high accuracy measurements, even with very pure samples. The deviations between the data of Glos et al. and the equation are all less than the uncertainties in the measurements, even at the lowest temperatures. Above 300 K, there is a slight difference between the data of Glos et al. and the data measured at NIST by McLinden¹²⁰ on the order of 0.03 %. Since the data of Glos et al. extend only to 340 K, the equation was fitted to the data of McLinden above this, resulting in a deviation of 0.015~% in the highest temperature measurement of Glos et al. Above 340 K, the data of McLinden are fitted within 0.005 %. These data extend to the critical point. The data of Outcalt and Lee, 135 also measured at NIST with a different apparatus, are fitted to within 0.06 %.

At low temperatures, there is a data set available that used heat capacities in the two-phase region to determine the vapor pressure. These heat capacities are derived from internal energy measurements. This technique is often better than vapor pressure measurements at extremely low pressures, due to the difficulty inherit in experimental techniques. The data of Perkins et al. 139 show deviations of +0.19 % at 100 K and a maximum deviation of +2.2% at the triple point temperature, where their derived vapor pressure is about 0.17 mPa. The derived values given by Perkins et al. were obtained while the equation presented here

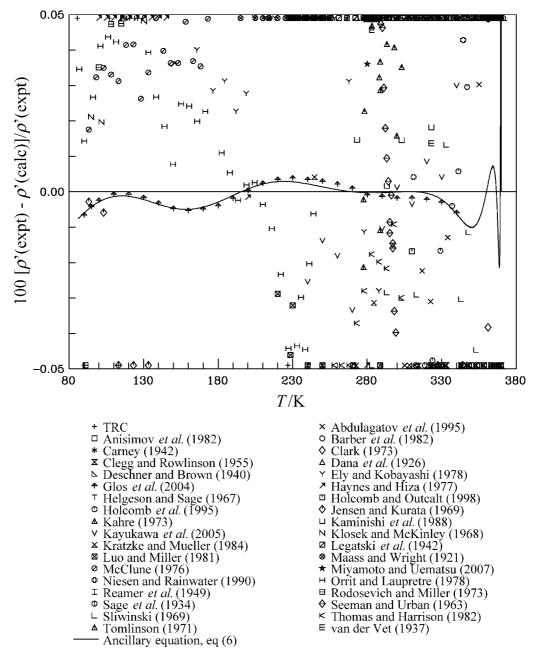


Figure 10. Comparisons of saturated liquid densities ρ' calculated with the equation of state to high-accuracy experimental data as a function of temperature T. The line corresponds to values calculated from the ancillary equation, eq 6.

was being developed, and the measurements and the equation benefitted from an iterative process in which each was influenced by the other's modifications. In the region where the data of Perkins et al. and Glos et al. overlap, the data of Perkins et al. closely follow (generally within 0.01 %) the data of Glos et al. Above 105 K, differences between the equation of state and the data of Perkins et al. are generally less than 0.1 %.

The consistency between saturated liquid densities below 273 K is quite remarkable; for the most part, the data are all within 0.2 %, as shown in Figures 9 and 10. Figure 9 shows all of the data, and Figure 10 provides an expanded view of the highest-accuracy data. The lines in these figures represent the ancillary equations reported in eq 6. The data sets that fall within 0.05 % include those of Haynes and Hiza,⁶¹ Jensen and Kurata,⁷⁸ Klosek and McKinley,⁹⁶ Luo and Miller,¹¹³ McClune,¹¹⁸ Orrit and Laupretre, 134 and Rodosevich and Miller. 147 The data of Haynes and Hiza exceed 0.05 % below 150 K. The data measured by Glos et al.⁴⁸ have uncertainties of 0.015 % and are represented by the equation of state to within 0.005 % (50 ppm). Above 273 K, the data of Glos et al. are still represented to within 0.005 % up to their maximum temperature of 340 K. Although McLinden 120 did not measure saturated liquid densities, his $p\rho T$ measurements are concentrated around the critical region and close to the saturation boundaries. Other data above 273 K show higher scatter, especially toward the critical point. Most of the data are within 0.5 %, with many inconsistent data sets showing scatter of up to 0.2 %. Aside from the data of Glos et al., none of the data sets stand out as exceptional.

The scatter in saturated vapor phase measurements is substantially higher, up to 2 % for a number of data sets, as shown in Figure 11. The data sets showing the highest degree of consistency are those of Clark,²⁶ Clegg and Rowlinson,²⁸ Sliwinski, 162 and Thomas and Harrison, 168 although these data are still 0.5 % or more from the equation of state, except for the data of Thomas and Harrison, which are generally within

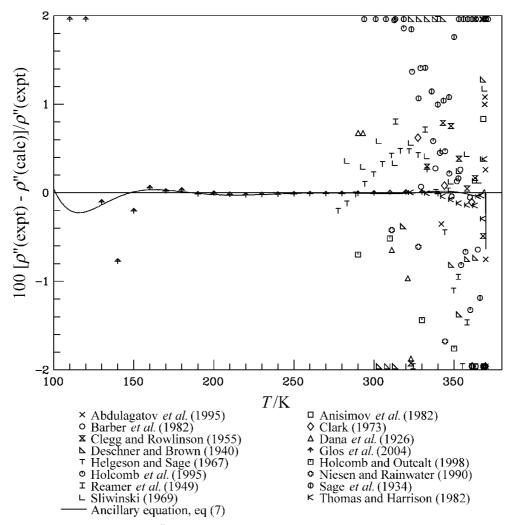


Figure 11. Comparisons of saturated vapor densities ρ'' calculated with the equation of state to experimental data as a function of temperature T. The line corresponds to values calculated from the ancillary equation, eq 7.

0.1 %. The data of Thomas and Harrison have been one of the most accurate sets published for propane before 2000 and have been the foundation for many previous equations of state. The new data of Glos et al.⁴⁸ are a combination of measurements down to 230 K and a truncated virial equation of state at lower temperatures where measurements of density become impossible due to their extremely low values. These data are represented by the equation of state to within 0.02 % for temperatures between (150 and 280) K and within 0.01 % up to their maximum temperature of 340 K.

 $p \rho T$ Data and Virial Coefficients. The experimental $p \rho T$ data for propane are summarized in Table 3 and shown graphically in Figure 12. For clarity, data in the extended critical region are also shown on temperature-density coordinates in Figure 13. As can be seen in this figure, there is a substantial number of high-quality data in the extended critical region, which is unusual for most fluids. Figure 14 compares densities calculated from the equation of state with experimental data; Figure 15 shows comparisons with only high-accuracy measurements in a similar manner; and Figure 16 compares pressures calculated from the equation of state with the experimental data in the extended critical region of propane. In the figures, the deviations are shown in groups containing data generally within a 10 K interval. The temperature listed at the top of each small plot is the lower bound of the data in the plot.

Three key sets of pressure—density—temperature data are now available to characterize the properties of propane with very high accuracy. These are the data of Glos et al., 48 Claus et al., 27 and McLinden, 120 and these data are compared in Figure 15 to the equation of state. The first two data sets were available when the fitting of the equation of state began. The third set was measured during the fitting process and was used as both a check on how the equation was progressing and an aid to determine how much more, and in what regions, new data should be measured. Careful attention was given in the critical region so that sufficient data were measured such that the critical parameters could be determined simultaneously with the coefficients and exponents of the equation of state, as described earlier. The apparatuses of McLinden and of Glos et al. are both two-sinker densimeters and use the most accurate measuring technique for density currently available. The high-temperature measurements of Claus et al.,²⁷ which are reported in the work of Glos et al., were performed in a single-sinker apparatus. In the low-temperature region, where only the data of Glos et al. are available (up to 260 K), the equation represents these data with an AARD of 0.002 % (20 ppm). In the liquid region where the data of Glos et al. overlap the data of McLinden [(260 to 340) K], this trend continues, while the equation represents the data of McLinden with an AARD of 0.004 %. Glos et al. measured 13 points in the vapor phase below 340 K and the equation represents these to within 0.005 %. The data of Claus et al. extend the measurements from (340 to 520) K, and the equation shows an AARD of 0.015 % with respect to these data. This data set contains only a few critical region values. The

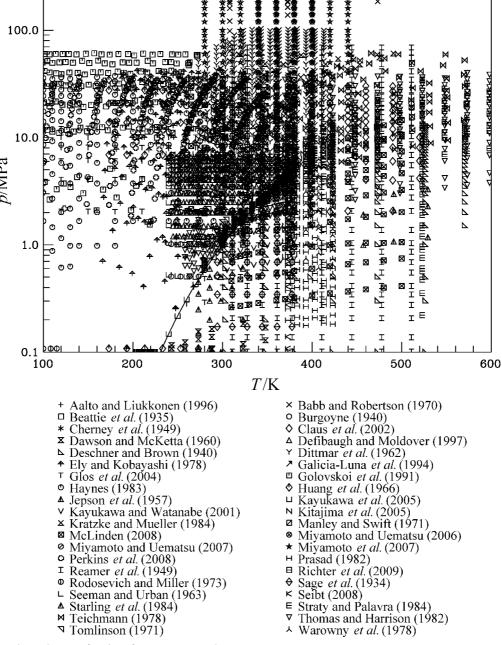


Figure 12. Experimental $p\rho T$ data as a function of temperature T and pressure p.

work of McLinden also studied the critical region and has to be divided into several areas to give informative statistics that help understand how the equation behaves. Since the slope of pressure with respect to density approaches zero near the critical point, density variations can become large with small changes in temperature or pressure. Thus it is more meaningful instead to report deviations in pressure, which will be done here for the points close to the critical point. The following statistics for the data of McLinden apply to those points above 340 K. At densities greater than 8 mol·dm⁻³, the equation represents the data on average to within 0.004 % in density. Between (6 and 8) mol·dm⁻³, the average deviations in density are 0.03 %. In the vapor region with densities less than 4 mol·dm⁻³, the average deviations in density are 0.02 %. In the critical region between (4 and 6) mol·dm⁻³, the average deviations in pressure are 0.009 %. The deviations are much higher for density (0.7 %) but are less meaningful for reasons described above. All of the data of McLinden above 380 K are represented on average to within 0.017 % in density.

Aside from the data of Glos et al., 48 Claus et al., 27 and McLinden, 120 there are several other data sets for $p\rho T$ that have low uncertainties and help validate the equation of state. Although the data of Perkins et al. 139 show average deviations of 0.012 %, these data were based on an experimental volume calibrated with the present propane equation and thus cannot be used for validation. The calibration was performed so that measurements with other fluids could be made with lower uncertainties. Richter et al. 146 measured one experimental data point with an uncertainty of 0.02 % at 273 K and 1 atm in the vapor phase with a special two-sinker densimeter designed to very accurately measure densities of gases under standard conditions at very low densities. The deviation of the equation from this point is 0.009 %. Other data that are well represented in the vapor phase include those of Starling et al. 163 and Dawson and McKetta, 33 both with average deviations of 0.03 %. In the liquid phase, the data of Kratzke and Müller⁹⁹ span the temperature range from (250 to 490) K and are represented to within 0.035 %. The deviations for the four data points of

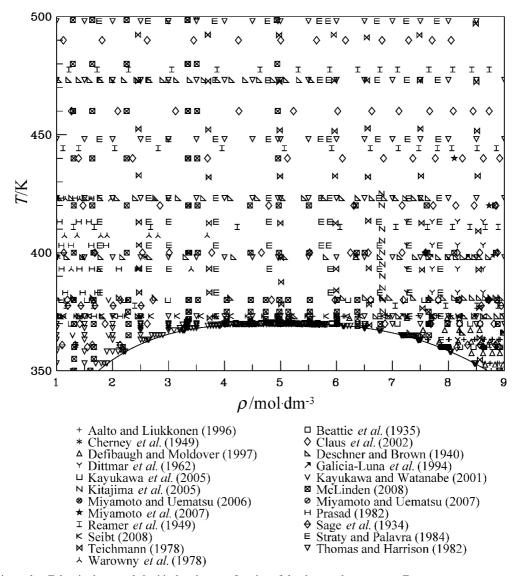


Figure 13. Experimental $p\rho T$ data in the extended critical region as a function of density ρ and temperature T.

Rodosevich and Miller¹⁴⁷ between (90 and 115) K are about 0.04 %. Teichmann¹⁶⁶ measured data at temperatures from (322 to 573) K, and the equation shows average deviations of 0.07 %. Similar deviations are visible with the data of Galicia-Luna et al. 46 Differences of around 0.09 % are seen in the data sets of Defibaugh and Moldover, 34 Ely and Kobayashi 41 (which extend down to 166 K), and Miyamoto and Uematsu. 125 The latter measured densities up to 200 MPa. The equation of state represents the data of Miyamoto and Uematsu best at 200 MPa, where the deviations are about 0.03 %. The only data set that extends to higher pressures is that of Babb and Robertson,⁷ which extends to nearly 1000 MPa. These data show deviations of around 0.4 % and appear to be systematically high when compared to the data of Miyamoto and Uematsu. However, this conclusion is subjective and needs further experimental work to ascertain the true thermodynamic properties of propane at very high pressures. The data of Thomas and Harrison¹⁶⁸ extend up to 623 K, and the deviations range from less than 0.1 % below 18 MPa to generally less than 0.2 % below 40 MPa (the upper pressure limit of the data).

In the critical region, the data of Thomas and Harrison¹⁶⁸ have been used for decades in fitting because they were the most accurate data in the critical region. With the new measurements of McLinden, this situation has now changed,

and the data of Thomas and Harrison appear to be systematically higher by $0.03\,\%$ in pressure. Although this is a small amount, such small changes have large impacts on the calculation of density in the critical region. The data still serve a vital purpose in making it possible to extrapolate between the limited measurements made by McLinden. As seen in Figure 16, Thomas and Harrison report about 10 times as many measurements, and these measurements show that the equation is smooth in between the data points where McLinden measured. The data of Beattie et al. 12 serve a similar purpose; these data differ in pressure by about $0.05\,\%$ from the equation of state.

Table 3 summarizes the sources for the second virial coefficients of propane. Deviations from the equation of state are shown in Figure 17. Many of the data are scattered within $5 \, \mathrm{cm}^3 \cdot \mathrm{mol}^{-1}$ above 300 K. Additional information about the high uncertainties in the second virial coefficients at low temperatures was reported by Wagner and Pruss. ¹⁹⁹ The data of Glos et al. ⁴⁸ (which extend from (260 to 340) K) are represented to within a maximum of 1.8 cm³·mol⁻¹ (0.3 %). Comparisons of third virial coefficients calculated with the equation of state with those presented in the literature are shown in Figure 18. Figure 19 shows a plot of (Z - 1)/ ρ vs ρ and demonstrates the behavior of the second and third virial coefficients as well as the shape of the equation of state in the two-phase region. The lines show isotherms calculated from

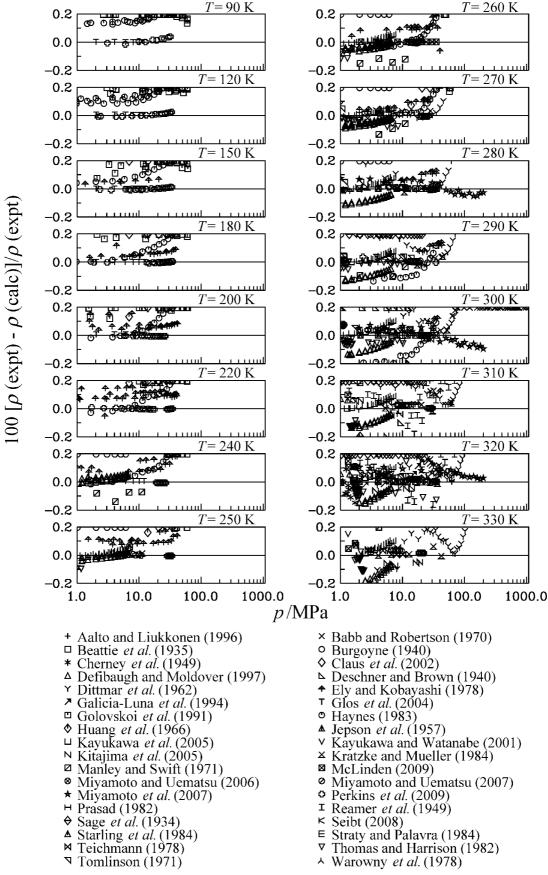


Figure 14. Comparisons of densities ρ calculated with the equation of state to experimental data as a function of pressure p.

the equation of state presented here, and the curve represents the saturated vapor density. The y-intercept (zero density) represents the second virial coefficients at a given temperature, and the third virial coefficients are the slope of each line at zero density. Many equations of state show curvature in the lines at low temperatures caused by high values of the exponent t on temperature. As can

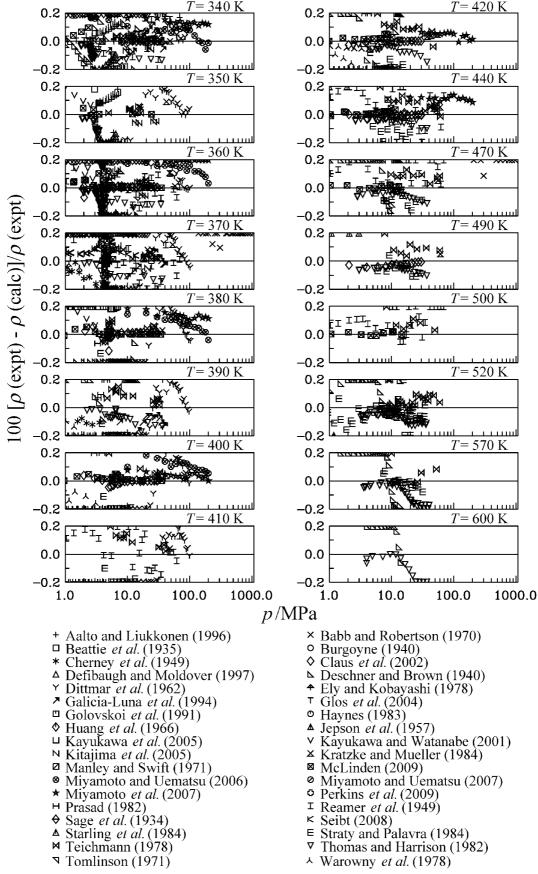


Figure 14. Continued.

be seen in this plot, there is no curvature in the lines, and the equation is extremely smooth and linear at low densities, as it should be. The paper describing the R-125 equation by Lemmon and Jacobsen¹⁸⁹ discusses this point in more detail.

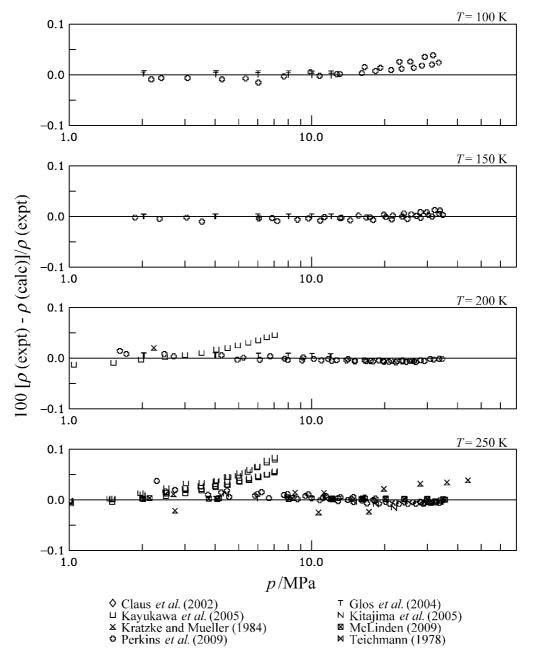


Figure 15. Comparisons of densities ρ calculated with the equation of state to high-accuracy experimental data as a function of pressure p.

Caloric Data. The sources of experimental data for the caloric properties of propane are summarized in Table 3. Comparisons of values calculated from the equation of state for the enthalpy of vaporization are shown in Figure 20. There have been no new measurements on the enthalpy of vaporization of propane over the last 30 years, and many of the data that are available are generally fitted within 1 %. Comparisons of values calculated from the equation of state for the speed of sound are shown in Figure 21 for the liquid phase and in Figure 22 for the vapor phase. As part of the new work on propane, speed of sound measurements were made by Meier. 121 These data have an uncertainty of 0.03 % and are among the most accurate of any liquid phase speed of sound data available. The equation of state represents these data generally to within 0.03 % with an AARD of 0.012 %. The data of Younglove¹⁸³ measured in 1981 at NIST overlap the data of Meier from (240 to 310) K and then extend down to temperatures near the triple point. These data show an offset of about 0.03 % from the data of Meier, and this offset was left as such over all temperatures during the fitting of the equation of state. By so doing, the scatter in the data of Younglove near the triple point lies between (0 and -0.1) %, but the uncertainty in the equation is most likely 0.05 % at the lowest temperatures. Figure 21 shows how the comparisons would appear if the data of Younglove were modified based on the differences with the new data of Meier (the data are indicated as "adjusted Younglove" in the figure). There is an unexplainable dip in the data of Younglove between (160 and 180) K, and it is unclear why these data are inconsistent with his other data. There are other data sets in the liquid phase that overlap these two data sets, but their uncertainties are much higher (1 % or more) and do not contribute to the development of the equation or in its evaluation.

Several data sets are also available for vapor phase speeds of sound, as shown in Figure 22. The data of He et al.⁶² deviate by 0.2 % from the equation, and the data of Trusler and Zarari¹⁷² and Hurly et al. 76 are represented to within 0.01 % (and an AARD of 0.006 %). The data of Hurly were measured at 298 K, and the data of Trusler and Zarari were taken over the range from (225 to 375) K. This latter set was of extreme

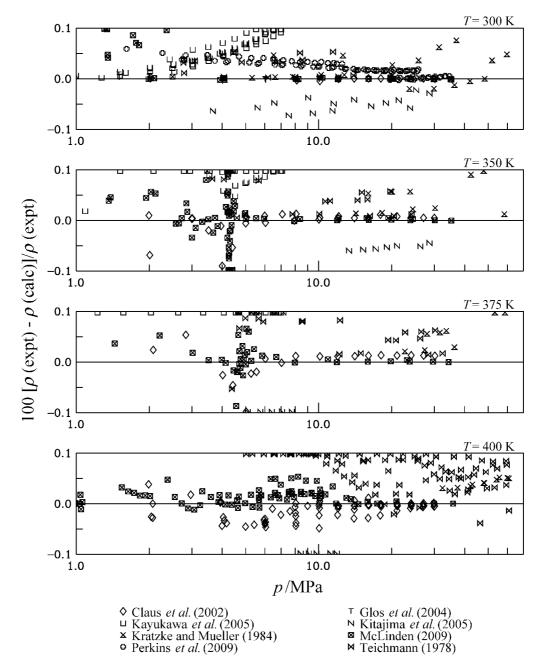


Figure 15. Continued.

importance in the development of the equation because of its low uncertainty and its position on the surface of state of propane, i.e., in the gas phase at very low pressures, where it is difficult to make $p\rho T$ measurements. Additionally, these measurements contributed to the ideal gas heat capacity equation, which was fitted simultaneously with the equation of state.

The reported measurements of the isochoric heat capacity, saturation liquid heat capacity, and isobaric heat capacity for propane are summarized in Table 3. Comparisons of values calculated from the equation of state are shown for the saturation liquid heat capacities in Figure 23, the isobaric heat capacities in Figure 24, and isochoric heat capacities in Figure 25. There are a number of good measurements for the saturation heat capacity of propane (c_{σ}) and for the isobaric heat capacity at saturation (c_{n}) . At low temperatures, these two properties are nearly identical. They start to diverge near 270 K, and by 350 K, they differ by about 15 %. Up to 320 K, the equation of state evenly splits the data sets into two groups: the data of Perkins et al. 139 and of Guigo et al.⁵⁴ show positive deviations, and the data of Cutler and Morrison, 30 Dana et al., 32 Goodwin, 53 and Kemp and Egan 89 show negative deviations as shown in Figure 23. Between (90 and 220) K, the data are fitted to within 0.5 %, which is the uncertainty of these data sets. There is somewhat higher scatter above 220 K in the data of Perkins et al. up to 315 K (the data have higher uncertainties as they approach the critical point). Above this temperature, there is a sharp downward shift as the data approach the critical region. Because of the analytical nature of the equation of state, these data are not as well represented as could be done with a scaling equation developed solely for the critical region.

The data available for the isobaric heat capacity show quite high scatter and were not used in developing the equation of state. In the vapor phase, only the data of Ernst and $B\ddot{u}ser^{42}$ and Kistiakowsky and $Rice^{93}$ show deviations less than 0.5 %. Generally, speed of sound data are a much better choice for fitting the vapor phase than are isobaric heat capacities, and the latter are rarely used, except for the correlation of the ideal gas heat capacity.



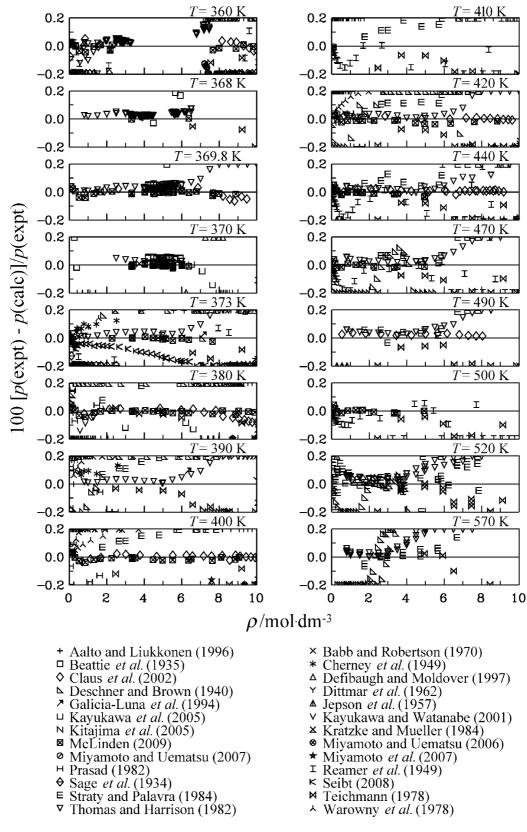


Figure 16. Comparisons of pressures p calculated with the equation of state to experimental data in the extended critical region as a function of density ρ .

The situation in the liquid phase is not much better. The data of Kemp and Egan⁸⁹ show deviations of 0.5 %, and the rest of the available data are scattered by 2 % or more. Fortunately, the extremely accurate speed of sound data of Meier¹²¹ and of Younglove, 183 along with the saturation heat capacities, are

available, and their use in fitting was sufficient to fully define the liquid phase of propane without the need for heat capacity data at higher pressures. This is possible because an equation of state requires consistency among all of its various properties. For example, fitting very accurate vapor pressures will result in good

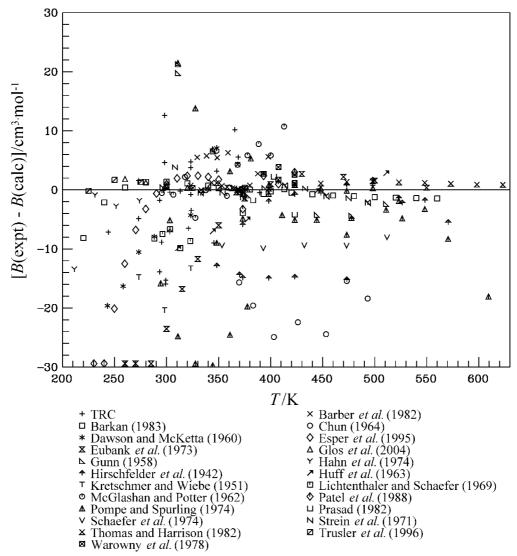


Figure 17. Comparisons of second virial coefficients B calculated with the equation of state to experimental data as a function of temperature T.

values of the enthalpies of vaporization. Likewise, fitting extremely accurate density, speeds of sound, and saturation heat capacity data will result in accurate calculations of the isobaric and isochoric heat capacities. It is not possible to force the equation to fit isobaric heat capacities having deviations of 2 % or more when these other accurate data are available.

There are a number of measurements for the isochoric heat capacity in the liquid phase of propane. These include the data of Perkins et al., 139 Goodwin, 53 Abdulagatov et al., 2,3 and Anisimov et al.6 The data of Abdulagatov et al. and Anisimov et al. were measured in the critical region and at high temperatures. The equation shows substantial deviations from these data sets, and it is unclear whether this is due to deficiencies in the data or in the equation of state. The data of Perkins et al. and of Goodwin show deviations of 0.5 % above 290 K and deviations of 1 % below this, except near 100 K for the data of Perkins et al., where the deviations are again around 0.5 %. This is discussed further in the work of Perkins et al. 139

Extrapolation Behavior. Because the equation of state for propane can be used as a reference formulation in corresponding states applications due to its extremely long saturation line and high-quality data, extreme attention was given to the lowtemperature regime below the triple point. Although it is possible to cool a liquid below its triple point and maintain its liquid state, these property measurements are difficult and rare, and thus such data are generally not available. However, it is possible to easily extrapolate the equation to lower temperatures. This extrapolation is important for a number of reasons: (1) if the extrapolation is correct, then state points in normal regions should be more accurate (since bad extrapolations outside the normal range result from incorrect slopes in normal regions, and properties such as heat capacities are highly slope dependent); (2) there are some fluids such as 1-butene that have an even longer saturation line (i.e., a lower reduced triple point temperature); and (3) mixture models can access regions outside the range of validity of the equation of state, depending on what it is mixed with and how nonideal the mixture is.

New fitting techniques developed in the R-125 equation of state (Lemmon and Jacobsen¹⁸⁹) allowed good extrapolation to well below the triple point. One of the best techniques for determining how low an equation can be used is to find the point at which the speed of sound is no longer linear with respect to temperature along the saturated liquid line (ignoring the critical region). For R-125, the speed of sound calculated from the equation started to diverge from a linear trend at about 150 K. This is below its triple point temperature of 172.52 K and represents an approximate reduced temperature of 0.44. For propane, the reduced triple point is 0.23, and thus the functional form for R-125 would have to be modified to allow a proper representation to this lower reduced temperature.

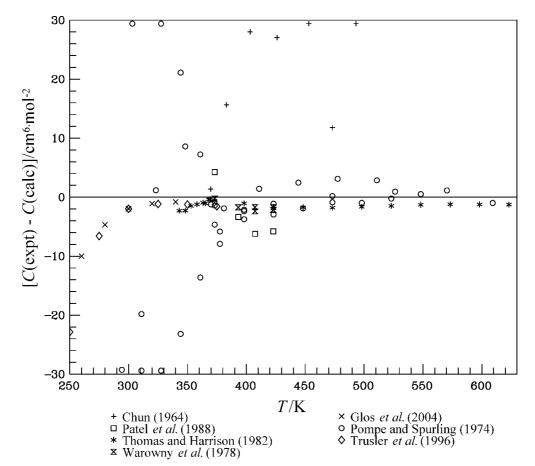


Figure 18. Comparisons of third virial coefficients C calculated with the equation of state to experimental data as a function of temperature T.

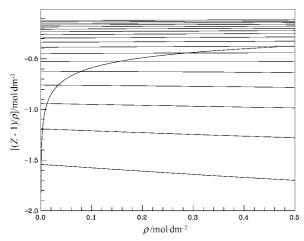


Figure 19. Calculations of $(Z-1)/\rho$ along isotherms versus density ρ in the vapor phase region and two-phase region. Isotherms are shown from temperatures of (160 to 500) K in steps of 20 K.

The improved fitting techniques developed in this work achieved this goal and further decreased the lowest point at which the speed of sound remained linear. Figure 26 shows the speed of sound versus temperature along the saturation lines and along isobars. The melting line is shown on this plot as the curve that starts at the saturated liquid state at the triple point temperature and then intersects the liquid phase isobars. This figure shows that the saturation line for the liquid remains straight down to about 40 K, a reduced temperature of 0.11. We are currently developing an equation of state for propylene, and the new preliminary equation shows excellent extrapolation down to a reduced temperature of 0.005, which will be very useful in future plans to develop an equation for helium-3.

Additional plots of constant property lines on various thermodynamic coordinates were made to assess other behaviors of the equation of state. Figures 27 and 28 show plots of temperature versus isochoric heat capacity and isobaric heat capacity. These plots indicate that the equation of state exhibits reasonable behavior over all temperatures and pressures within the range of validity and that the extrapolation behavior is reasonable at higher temperatures and pressures. The plot of isochoric heat capacities shows an upward trend in the liquid phase at low temperatures. This is quite common among many fluids and has been validated experimentally for these fluids.

Figure 29 shows a plot of temperature vs density to extremely high conditions that are far beyond the limits of propane as a stable molecule (where dissociation has occurred). The purpose of this plot is to demonstrate that the equation continues to extrapolate extremely well to extremely high pressures, densities, and temperatures and that there are no hidden irregularities beyond normal applications. Most often these regions are overlooked, and most equations of state show adverse behavior at extreme values. Similar to the arguments given above for extrapolation to low temperatures, it is important that the curvature of the equation remains correct in regions of validity. Small changes in these regions have large effects on heat capacities and speeds of sound. One test to determine whether the curvature is correct is to look at extreme values where the curvature becomes apparent. If these regions are bad, then small changes in the curvature are most likely present within the range of validity

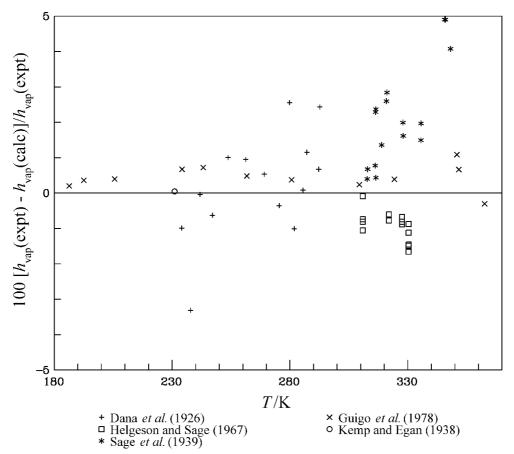


Figure 20. Comparisons of enthalpies of vaporization h_{vap} calculated with the equation of state to experimental data as a function of temperature T.

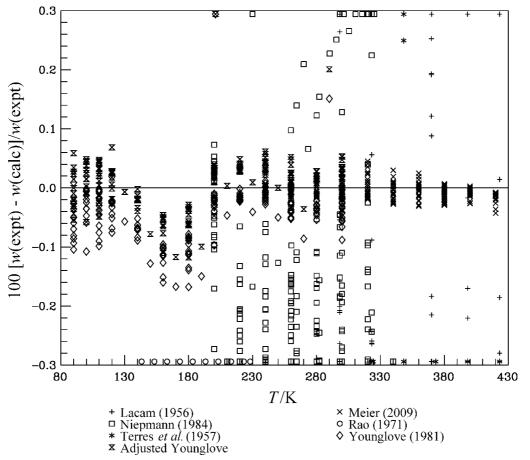


Figure 21. Comparisons of speeds of sound w in the liquid phase calculated with the equation of state to experimental data as a function of temperature Т.



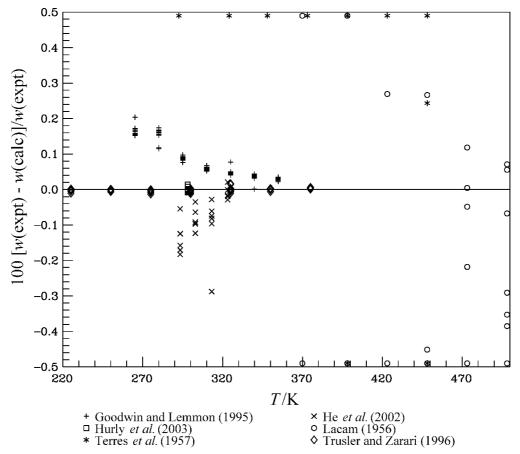


Figure 22. Comparisons of speeds of sound w in the vapor phase calculated with the equation of state to experimental data as a function of temperature T.

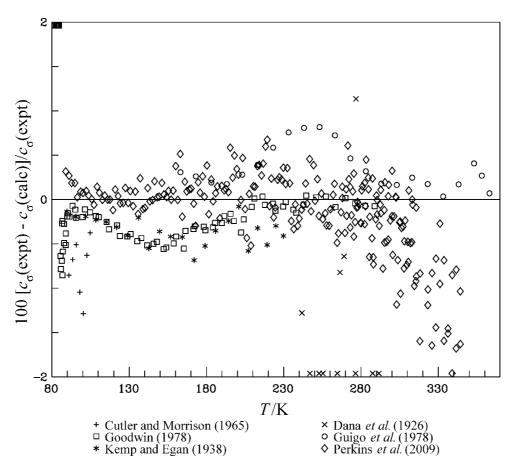


Figure 23. Comparisons of saturation heat capacities c_{σ} calculated with the equation of state to experimental data as a function of temperature T.



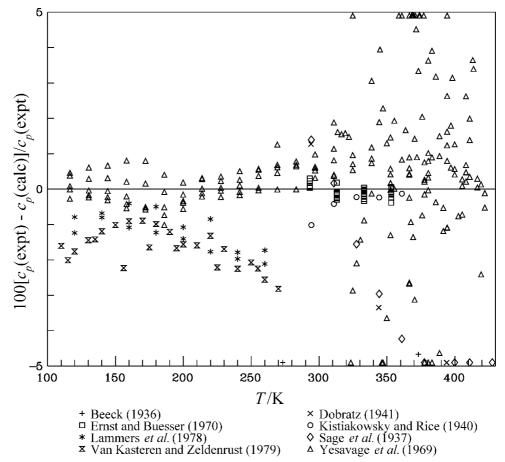


Figure 24. Comparisons of isobaric heat capacities c_p calculated with the equation of state to experimental data as a function of temperature T.

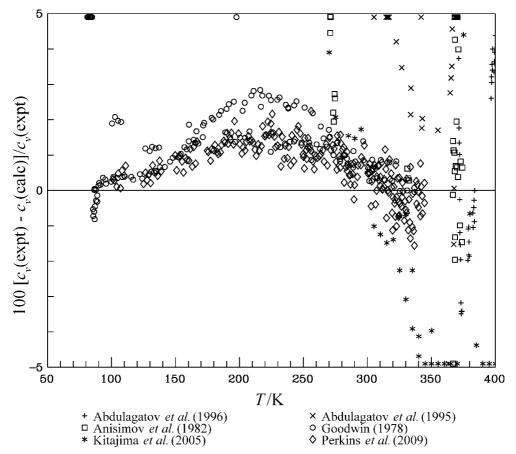


Figure 25. Comparisons of isochoric heat capacities c_n calculated with the equation of state to experimental data as a function of temperature T.

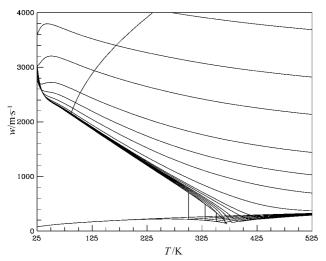


Figure 26. Speed of sound w versus temperature T diagram. Isobars are shown at pressures of (0, 1, 2, 3, 4, 5, 6, 8, 10, 20, 50, 100, 200, 500, 1000, and 2000) MPa. The melting line is shown intersecting the liquid phase isotherms. State points below the melting line are extrapolations of the liquid phase to very low temperatures.

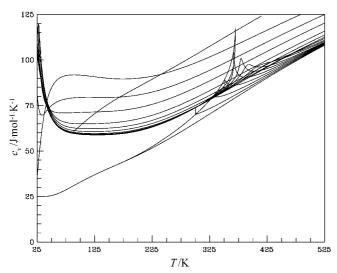


Figure 27. Isochoric heat capacity c_v versus temperature T diagram. Isobars are shown at pressures of (0, 1, 2, 3, 4, 5, 6, 8, 10, 20, 50, 100, 200, 500, 1000, and 2000) MPa. The melting line is shown intersecting the liquid phase isotherms. State points below the melting line are extrapolations of the liquid phase to very low temperatures.

of the equation. Figure 29 shows that the extrapolation is smooth to extremely high temperatures, pressures, and densities. This smooth behavior comes from the term with t = 1 and d = 4, as explained by Lemmon and Jacobsen. ¹⁸⁹

Plots of certain characteristic curves are useful in assessing the behavior of an equation of state in regions away from the available data (Deiters and de Reuck, ²¹³ Span and Wagner, ¹⁹⁷ Span²¹⁴). The characteristic curves are the Boyle curve, given by the equation

$$\left(\frac{\partial Z}{\partial \nu}\right)_T = 0\tag{26}$$

the Joule-Thomson inversion curve

$$\left(\frac{\partial Z}{\partial T}\right)_{p} = 0 \tag{27}$$

the Joule inversion curve

$$\left(\frac{\partial Z}{\partial T}\right)_{\nu} = 0 \tag{28}$$

and the ideal curve

$$\frac{p}{\rho RT} = 1 \tag{29}$$

The temperature at which the Boyle and ideal curves begin (at zero pressure) is also known as the Boyle temperature, or the temperature at which the second virial coefficient is zero. The point at which the Joule inversion curve begins (at zero pressure) corresponds to the temperature at which the second virial coefficient is at a maximum. (Thus, for the Joule inversion curve to extend to zero pressure, the second virial coefficient must pass through a maximum value, a criterion that is not followed by all equations of state.) Although the curves do not provide numerical information, reasonable shapes of the curves, as shown for propane in Figure 30, indicate qualitatively correct extrapolation behavior of the equation of state extending to high pressures and temperatures far in excess of the likely thermal stability of the fluid. The behavior of properties on the ideal curves should always be analyzed during the development of an equation.

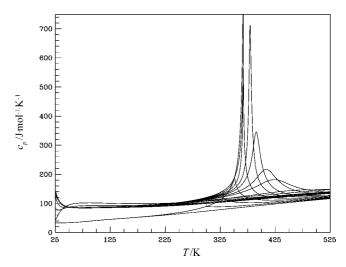


Figure 28. Isobaric heat capacity c_p versus temperature T diagram. Isobars are shown at pressures of (0, 1, 2, 3, 4, 5, 6, 8, 10, 20, 50, 100, 200, 500, 1000, and 2000) MPa. State points below the melting line are extrapolations of the liquid phase to very low temperatures.

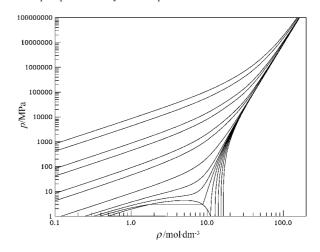


Figure 29. Isothermal behavior of the propane equation of state at extreme conditions of temperature T and pressure p. Isotherms are shown at temperatures of (100, 150, 200, 250, 300, 350, 400, 500, 1000, 5000, 10 000, ..., 1 000 000) K.

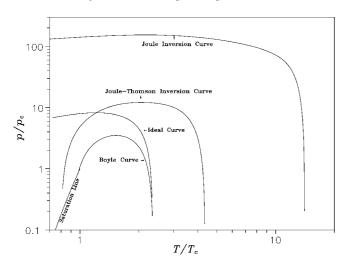


Figure 30. Characteristic (ideal) curves of the equation of state for propane as a function of temperature T and pressure p.

Table 5. Calculated Values of Properties for Algorithm Verification

| T | ho | p | c_v | c_p | w |
|-------|--|------------|--|---------------------------------|-------------------|
| K | $\overline{\text{mol} \cdot \text{dm}^{-3}}$ | MPa | $\overline{J\boldsymbol{\cdot} mol^{-1}\boldsymbol{\cdot} K^{-1}}$ | $J \cdot mol^{-1} \cdot K^{-1}$ | m•s ⁻¹ |
| 200.0 | 14.0 | 2.3795138 | 61.078424 | 93.475362 | 1381.9552 |
| 300.0 | 12.0 | 19.053797 | 73.972542 | 108.61529 | 958.40520 |
| 300.0 | 0.4 | 0.84694991 | 69.021875 | 85.753997 | 221.88959 |
| 400.0 | 5.0 | 6.6462840 | 97.017439 | 271.07044 | 194.65847 |
| 369.9 | 5.0 | 4.2519399 | 117.71621 | 753625.00 | 130.89800 |

Equation of state terms with values of t < 0 have a detrimental effect on the shapes of the ideal curves. The effects of all terms should be dampened at high temperatures, but with t < 0, the contribution to the equation increases as the temperature rises. Negative temperature exponents should never be allowed in an equation of state of the form presented in this work.

Estimated Uncertainties of Calculated Properties

Below 350 K, the uncertainties (k=2) in the new reference equation of state for propane for density are 0.01 % in the liquid phase and 0.03 % in the vapor phase (including saturated states for both phases). The liquid phase value also applies at temperatures greater than 350 K (to about 500 K) at pressures greater than 10 MPa. In the extended critical region, the uncertainties increase to 0.1 % in density, except very near the critical point, where the uncertainties in density increase rapidly as the critical point is approached. However, in this same region, the uncertainty in pressure calculated from density and temperature is 0.04 %, even at the critical point.

The uncertainties in the speed of sound are 0.01 % in the vapor phase at pressures up to 1 MPa, 0.03 % in the liquid phase between (260 and 420) K, and 0.1 % in the liquid phase at temperatures below 260 K. The uncertainties in vapor pressure are 0.02 % above 180 K and 0.1 % between (120 and 180) K and increase steadily below 120 K. Below 115 K, vapor pressures are less than 1 Pa, and uncertainty values increase to 3 % at the triple point. Uncertainties in heat capacities are 0.5 % in the liquid phase, 0.2 % in the vapor phase, and higher in the supercritical region.

As an aid for computer implementation, calculated values of properties from the equation of state for propane are given in Table 5. The number of digits displayed does not indicate the accuracy in the values but are given for validation of computer code.

Acknowledgment

We thank Mostafa Salehi and Marc Smith for their assistance with data entry and literature searching. We thank Dr. Roland Span whose insights and collaborations have inspired us in various projects, including this one, over many years.

Appendix A: Thermodynamic Equations

The functional form of the Helmholtz energy equation of state is explicit in the dimensionless Helmholtz energy, α , with independent variables of dimensionless density and temperature

$$\alpha(\delta, \tau) = \alpha^{0}(\delta, \tau) + \alpha^{r}(\delta, \tau) \tag{30}$$

where $\delta = \rho/\rho_c$ and $\tau = T_c/T$. The critical parameters are 369.89 K and 5 mol·dm⁻³. The ideal gas Helmholtz energy is

$$\alpha^{0} = \ln \delta + 3 \ln \tau + a_{1} + a_{2}\tau + \sum_{i=3}^{6} a_{i} \ln[1 - \exp(-b_{i}\tau)]$$
(31)

where $a_1 = -4.970583$, $a_2 = 4.29352$, $a_3 = 3.043$, $b_3 = 1.062478$, $a_4 = 5.874$, $b_4 = 3.344237$, $a_5 = 9.337$, $b_5 = 5.363757$, $a_6 = 7.922$, and $b_6 = 11.762957$.

The residual fluid Helmholtz energy is

$$\alpha^{r}(\delta, \tau) = \sum_{k=1}^{5} N_{k} \delta^{d_{k}} \tau^{t_{k}} + \sum_{k=6}^{11} N_{k} \delta^{d_{k}} \tau^{t_{k}} \exp(-\delta^{l_{k}}) + \sum_{k=12}^{18} N_{k} \delta^{d_{k}} \tau^{t_{k}} \exp(-\eta_{k} (\delta - \varepsilon_{k})^{2} - \beta_{k} (\tau - \gamma_{k})^{2})$$
(32)

The coefficients and parameters of this equation are given in Table 4. The functions used for calculating pressure (p), compressibility factor (Z), internal energy (u), enthalpy (h), entropy (s), Gibbs energy (g), isochoric heat capacity (c_v) , isobaric heat capacity (c_p) , and the speed of sound (w) from eq 30 are given below.

$$p = \rho^2 \left(\frac{\partial a}{\partial \rho}\right)_T = \rho RT \left[1 + \delta \left(\frac{\partial \alpha^r}{\partial \delta}\right)_\tau\right]$$
 (33)

$$Z = \frac{p}{\rho RT} = 1 + \delta \left(\frac{\partial \alpha^{r}}{\partial \delta}\right)_{\tau}$$
 (34)

$$\frac{u}{RT} = \frac{a + Ts}{RT} = \tau \left[\left(\frac{\partial \alpha^0}{\partial \tau} \right)_{\delta} + \left(\frac{\partial \alpha^{\mathrm{r}}}{\partial \tau} \right)_{\delta} \right]$$
(35)

$$\frac{h}{RT} = \frac{u + pv}{RT} = \tau \left[\left(\frac{\partial \alpha^0}{\partial \tau} \right)_{\delta} + \left(\frac{\partial \alpha^r}{\partial \tau} \right)_{\delta} \right] + \delta \left(\frac{\partial \alpha^r}{\partial \delta} \right)_{\tau} + 1$$
(36)

$$\frac{s}{R} = -\frac{1}{R} \left(\frac{\partial a}{\partial T} \right)_{\rho} = \tau \left[\left(\frac{\partial \alpha^{0}}{\partial \tau} \right)_{\delta} + \left(\frac{\partial \alpha^{r}}{\partial \tau} \right)_{\delta} \right] - \alpha^{0} - \alpha^{r} \quad (37)$$

$$\frac{g}{RT} = \frac{h - Ts}{RT} = 1 + \alpha^0 + \alpha^r + \delta \left(\frac{\partial \alpha^r}{\partial \delta}\right)_{\tau}$$
(38)

$$\frac{c_v}{R} = \frac{1}{R} \left(\frac{\partial u}{\partial T} \right)_{\rho} = -\tau^2 \left[\left(\frac{\partial^2 \alpha^0}{\partial \tau^2} \right)_{\delta} + \left(\frac{\partial^2 \alpha^r}{\partial \tau^2} \right)_{\delta} \right]$$
(39)

$$\frac{c_p}{R} = \frac{1}{R} \left(\frac{\partial h}{\partial T} \right)_p = \frac{c_v}{R} + \frac{\left[1 + \delta \left(\frac{\partial \alpha^{r}}{\partial \delta} \right)_{\tau} - \delta \tau \left(\frac{\partial^{2} \alpha^{r}}{\partial \delta \partial \tau} \right) \right]^{2}}{\left[1 + 2\delta \left(\frac{\partial \alpha^{r}}{\partial \delta} \right)_{\tau} + \delta^{2} \left(\frac{\partial^{2} \alpha^{r}}{\partial \delta^{2}} \right)_{\tau} \right]}$$
(40)

Table A1. Table of Thermodynamic Properties of Propane at Saturation^a

| T | p | ρ | h | S | c_v | c_p | w |
|----------------|-------------------------|------------------------------------|---------------------|--|---|--|---|
| °C | MPa | kg•m ⁻³ | kJ•kg ⁻¹ | $\overline{\mathrm{kJ} \cdot \mathrm{kg}^{-1} \cdot \mathrm{K}^{-}}$ | $\overline{\mathrm{k}\mathrm{J}\!\cdot\!\mathrm{k}\mathrm{g}^{-1}\!\cdot\!\mathrm{K}^{-1}}$ | $\overline{kJ \cdot kg^{-1} \cdot K^{-1}}$ | $\overline{\text{m}\cdot\text{s}^{-1}}$ |
| -187.625^{b} | $0.17203 \cdot 10^{-9}$ | 733.13 | -196.64 | -1.396 | 1.355 | 1.916 | 2136.4 |
| | | $0.107 \cdot 10^{-7}$ | 366.26 | 5.186 | 0.6907 | 0.8792 | 143.3 |
| -185. | $0.48526 \cdot 10^{-9}$ | 730.39 | -191.61 | -1.338 | 1.352 | 1.918 | 2118.6 |
| | | $0.292 \cdot 10^{-7}$ | 368.58 | 5.017 | 0.7010 | 0.8896 | 145.2 |
| -180. | $0.29386 \cdot 10^{-8}$ | 725.20 | -182.01 | -1.232 | 1.346 | 1.923 | 2084.6 |
| −175 . | $0.14596 \cdot 10^{-7}$ | 0.167 • 10 ⁻⁶ 720.05 | 373.08 -172.38 | 4.727 -1.131 | 0.7208 1.343 | 0.9093 1.928 | 148.9 |
| -175. | 0.14390*10 | $0.789 \cdot 10^{-6}$ | 377.67 | 4.473 | 0.7404 | 0.9289 | 2050.4 152.4 |
| -170. | $0.61256 \cdot 10^{-7}$ | 714.92 | -162.73 | -1.035 | 1.340 | 1.934 | 2016.2 |
| | | $0.315 \cdot 10^{-5}$ | 382.36 | 4.249 | 0.7596 | 0.9481 | 155.8 |
| -165. | $0.22252 \cdot 10^{-6}$ | 709.82 | -153.04 | -0.9437 | 1.338 | 1.941 | 1982.0 |
| | | 0.0000109 | 387.15 | 4.051 | 0.7784 | 0.9669 | 159.2 |
| -160. | $0.71368 \cdot 10^{-6}$ | 704.73 | -143.32 | -0.8558 | 1.336 | 1.947 | 1947.9 |
| | | 0.0000335 | 392.03 | 3.876 | 0.7967 | 0.9852 | 162.4 |
| -155. | $0.20542 \cdot 10^{-5}$ | 699.67 | -133.57 | -0.7715 | 1.335 | 1.954 | 1913.9 |
| 150 | 0.52705 . 10=5 | 0.0000922 | 397.00 | 3.719 | 0.8145 | 1.003 | 165.6 |
| -150. | $0.53795 \cdot 10^{-5}$ | 694.61 0.000232 | -123.78 402.06 | -0.6903 3.580 | 1.334 0.8319 | 1.962 1.020 | 1880.0 168.8 |
| -145. | $0.12965 \cdot 10^{-4}$ | 689.56 | -113.95 | -0.6121 | 1.334 | 1.969 | 1846.2 |
| 143. | 0.12)03 10 | 0.000537 | 407.21 | 3.455 | 0.8489 | 1.037 | 171.8 |
| -140. | $0.29040 \cdot 10^{-4}$ | 684.51 | -104.09 | -0.5366 | 1.334 | 1.977 | 1812.5 |
| | | 0.00116 | 412.43 | 3.343 | 0.8655 | 1.054 | 174.9 |
| -135. | $0.60950 \cdot 10^{-4}$ | 679.46 | -94.181 | -0.4636 | 1.335 | 1.985 | 1779.0 |
| | | 0.00234 | 417.74 | 3.242 | 0.8818 | 1.070 | 177.8 |
| -130. | 0.00012073 | 674.40 | -84.234 | -0.3929 | 1.336 | 1.994 | 1745.5 |
| | | 0.00447 | 423.12 | 3.151 | 0.8979 | 1.087 | 180.7 |
| -125. | 0.00022708 | 669.33 | -74.243 | -0.3243 | 1.337 | 2.003 | 1712.0 |
| − 120. | 0.00040774 | 0.00813 | 428.58 -64.207 | 3.070 -0.2576 | 0.9138 | 1.103 | 183.5 1678.6 |
| -120. | 0.00040774 | 664.26 0.01413 | 434.11 | 2.996 | 1.339 0.9297 | 2.012 1.119 | 186.3 |
| −115 . | 0.00070215 | 659.16 | -54.122 | -0.1928 | 1.341 | 2.022 | 1645.2 |
| 113. | 0.00070215 | 0.02357 | 439.71 | 2.930 | 0.9455 | 1.135 | 189.0 |
| -110. | 0.0011644 | 654.05 | -43.988 | -0.1298 | 1.343 | 2.032 | 1611.8 |
| | | 0.03790 | 445.38 | 2.870 | 0.9614 | 1.151 | 191.7 |
| -105. | 0.0018661 | 648.91 | -33.802 | -0.06827 | 1.346 | 2.043 | 1578.4 |
| | | 0.05897 | 451.10 | 2.815 | 0.9775 | 1.168 | 194.2 |
| -100. | 0.0028994 | 643.74 | -23.560 | -0.00826 | 1.350 | 2.054 | 1544.9 |
| 05 | 0.0042705 | 0.08904 | 456.88 | 2.766 | 0.9937 | 1.184 | 196.8 |
| −95 . | 0.0043795 | 638.55 0.13085 | -13.260 462.71 | 0.05038 2.722 | 1.355 1.010 | 2.066 1.202 | 1511.5 199.2 |
| −90 . | 0.0064475 | 633.32 | -2.8974 | 0.1077 | 1.360 | 2.078 | 1478.0 |
| <i>7</i> 0. | 0.0004473 | 0.18762 | 468.58 | 2.682 | 1.027 | 1.220 | 201.5 |
| −85 . | 0.0092716 | 628.06 | 7.5304 | 0.1639 | 1.366 | 2.092 | 1444.6 |
| | | 0.26304 | 474.49 | 2.646 | 1.045 | 1.239 | 203.8 |
| -80. | 0.013049 | 622.76 | 18.028 | 0.2189 | 1.372 | 2.106 | 1411.2 |
| | | 0.36132 | 480.44 | 2.613 | 1.063 | 1.258 | 205.9 |
| −75. | 0.018008 | 617.41 | 28.600 | 0.2729 | 1.380 | 2.121 | 1377.8 |
| 70 | 0.024404 | 0.48715 | 486.41 | 2.583 | 1.081 | 1.279 | 208.0 |
| −70. | 0.024404 | 612.02 0.64570 | 39.251 492.41 | 0.3259 2.557 | 1.388 1.100 | 2.137 1.300 | 1344.6 209.9 |
| −65 . | 0.032527 | 606.57 | 49.986 | 0.3781 | 1.397 | 2.154 | 1311.4 |
| 03. | 0.032327 | 0.84261 | 498.42 | 2.532 | 1.120 | 1.323 | 211.8 |
| -60. | 0.042693 | 601.08 | 60.811 | 0.4294 | 1.406 | 2.172 | 1278.4 |
| | | 1.0840 | 504.44 | 2.511 | 1.140 | 1.346 | 213.5 |
| −55 . | 0.055249 | 595.52 | 71.731 | 0.4799 | 1.417 | 2.191 | 1245.4 |
| | | 1.3764 | 510.46 | 2.491 | 1.161 | 1.371 | 215.0 |
| −50 . | 0.070569 | 589.90 | 82.753 | 0.5298 | 1.428 | 2.212 | 1212.5 |
| 4.7 | 0.000071 | 1.7270 | 516.48 | 2.473 | 1.182 | 1.397 | 216.5 |
| −45 . | 0.089051 | 584.20 | 93.881 | 0.5789 | 1.439 | 2.233 | 1179.7 |
| -42.114^{c} | 0.101225 | 2.1430 580.88 | 522.49 | 2.458 0.6070 | 1.204 | 1.424 2.246 | 217.7 1160.8 |
| 72.114 | 0.101325 | 2.4161 | 100.36 525.95 | 2.449 | 1.446 1.217 | 1.440 | 218.4 |
| -40 . | 0.11112 | 578.43 | 105.12 | 0.6275 | 1.452 | 2.256 | 1147.0 |
| | | 2.6326 | 528.48 | 2.443 | 1.227 | 1.453 | 218.9 |
| | | | | | | | |

Table A1. Continued

| | <i>p</i> | ρ | h | S | C_v | c_p | w |
|--------------|----------|-------------------|--------------------|--------------------------------|---------------------------------|---------------------------------|-------------------|
| °C | MPa | $kg \cdot m^{-3}$ | $kJ \cdot kg^{-1}$ | $kJ \cdot kg^{-1} \cdot K^{-}$ | $kJ \cdot kg^{-1} \cdot K^{-1}$ | $kJ \cdot kg^{-1} \cdot K^{-1}$ | m•s ⁻¹ |
| -35. | 0.13723 | 572.58 | 116.49 | 0.6755 | 1.464 | 2.280 | 1114.4 |
| | 0.15725 | 3.2042 | 534.45 | 2.431 | 1.250 | 1.482 | 219.8 |
| -30. | 0.16783 | 566.64 | 127.97 | 0.7231 | 1.478 | 2.305 | 1081.7 |
| 50. | 0.10703 | 3.8669 | 540.38 | 2.419 | 1.274 | 1.513 | 220.6 |
| 25. | 0.20343 | 560.60 | 139.60 | 0.7701 | 1.492 | 2.332 | 1049.1 |
| 23. | 0.20343 | 4.6302 | 546.28 | 2.409 | 1.298 | 1.546 | 221.2 |
| -20. | 0.24452 | 554.45 | 151.36 | 0.8168 | 1.507 | 2.361 | 1016.: |
| 20. | 0.24432 | 5.5046 | 552.13 | 2.400 | 1.323 | 1.580 | 221. |
| -15. | 0.29162 | 548.19 | 163.28 | 0.8630 | 1.522 | 2.391 | 983. |
| 13. | 0.27102 | 6.5012 | 557.93 | 2.392 | 1.348 | 1.616 | 221. |
| -10. | 0.34528 | 541.80 | 175.35 | 0.9090 | 1.538 | 2.423 | 951. |
| 10. | 0.54326 | 7.6321 | 563.65 | 2.385 | 1.374 | 1.655 | 221. |
| - 5. | 0.40604 | 535.27 | 187.59 | 0.9546 | 1.555 | 2.457 | 918. |
| 5. | 0.40004 | 8.9103 | 569.30 | 2.378 | 1.400 | 1.695 | 221. |
| 0. | 0.47446 | 528.59 | 200.00 | 1.000 | 1.572 | 2.493 | 885 |
| 0. | 0.47440 | 10.351 | 574.87 | 2.372 | 1.427 | 1.739 | 221. |
| 5. | 0.55112 | 521.75 | 212.60 | 1.045 | 1.590 | 2.532 | 852. |
| 3. | 0.33112 | 11.969 | | 2.367 | | 1.785 | 220. |
| 10. | 0.63660 | | 580.33 | 1.090 | 1.455 1.608 | | 819. |
| 10. | 0.03000 | 514.73 | 225.40 | | | 2.573 | |
| 1.5 | 0.72151 | 13.783 | 585.67 | 2.363 | 1.484 | 1.835 | 219. |
| 15. | 0.73151 | 507.50 | 238.40 | 1.135 | 1.627 | 2.618 | 786. |
| 20 | 0.02646 | 15.813 | 590.89 | 2.358 | 1.514 | 1.890 | 218. |
| 20. | 0.83646 | 500.06 | 251.64 | 1.180 | 1.647 | 2.666 | 752. |
| 2.5 | 0.05005 | 18.082 | 595.95 | 2.354 | 1.544 | 1.949 | 217. |
| 25. | 0.95207 | 492.36 | 265.11 | 1.225 | 1.667 | 2.719 | 719. |
| | | 20.618 | 600.84 | 2.351 | 1.576 | 2.015 | 215. |
| 30. | 1.0790 | 484.39 | 278.83 | 1.269 | 1.688 | 2.777 | 685. |
| | | 23.451 | 605.54 | 2.347 | 1.609 | 2.088 | 213. |
| 35. | 1.2179 | 476.10 | 292.84 | 1.314 | 1.710 | 2.841 | 651. |
| | | 26.618 | 610.01 | 2.344 | 1.643 | 2.170 | 211. |
| 40. | 1.3694 | 467.46 | 307.15 | 1.359 | 1.732 | 2.913 | 617. |
| | | 30.165 | 614.21 | 2.340 | 1.678 | 2.263 | 208. |
| 45. | 1.5343 | 458.40 | 321.79 | 1.405 | 1.756 | 2.995 | 582. |
| | | 34.146 | 618.12 | 2.336 | 1.715 | 2.371 | 205. |
| 50. | 1.7133 | 448.87 | 336.80 | 1.450 | 1.780 | 3.089 | 546. |
| | | 38.630 | 621.66 | 2.332 | 1.753 | 2.499 | 202. |
| 55. | 1.9072 | 438.76 | 352.23 | 1.496 | 1.805 | 3.201 | 510. |
| | | 43.706 | 624.77 | 2.327 | 1.794 | 2.652 | 198. |
| 60. | 2.1168 | 427.97 | 368.14 | 1.543 | 1.832 | 3.337 | 474. |
| | | 49.493 | 627.36 | 2.321 | 1.836 | 2.841 | 194. |
| 65. | 2.3430 | 416.34 | 384.60 | 1.590 | 1.861 | 3.509 | 436. |
| | | 56.152 | 629.29 | 2.314 | 1.880 | 3.086 | 189. |
| 70. | 2.5868 | 403.62 | 401.75 | 1.639 | 1.892 | 3.735 | 397. |
| | | 63.916 | 630.37 | 2.305 | 1.930 | 3.421 | 184. |
| 75. | 2.8493 | 389.47 | 419.76 | 1.689 | 1.927 | 4.053 | 357. |
| | | 73.140 | 630.33 | 2.294 | 1.987 | 3.914 | 178. |
| 80. | 3.1319 | 373.29 | 438.93 | 1.742 | 1.969 | 4.545 | 314. |
| | | 84.406 | 628.73 | 2.279 | 2.057 | 4.707 | 171. |
| 85. | 3.4361 | 353.96 | 459.81 | 1.798 | 2.023 | 5.433 | 269. |
| | | 98.818 | 624.75 | 2.259 | 2.144 | 6.182 | 164. |
| 90. | 3.7641 | 328.83 | 483.71 | 1.862 | 2.107 | 7.623 | 218. |
| | | 119.00 | 616.47 | 2.227 | 2.260 | 9.888 | 155. |
| 95. | 4.1195 | 286.51 | 516.33 | 1.948 | 2.302 | 23.59 | 158. |
| | | 156.31 | 595.81 | 2.164 | 2.467 | 36.07 | 144. |
| 96.740^{d} | 4.2512 | 220.48 | 555.24 | 2.052 | 2.70/ | 50.07 | 177. |

^a The first line at each temperature gives saturated liquid properties, and the second line gives saturated vapor properties. ^b Triple point. ^c Normal boiling point. ^d Critical point.

$$\frac{w^{2}M}{RT} = \frac{M}{RT} \left(\frac{\partial p}{\partial \rho}\right)_{s}$$

$$= 1 + 2\delta \left(\frac{\partial \alpha^{r}}{\partial \delta}\right)_{\tau} + \delta^{2} \left(\frac{\partial^{2}\alpha^{r}}{\partial \delta^{2}}\right)_{\tau} - \frac{\left[1 + \delta \left(\frac{\partial \alpha^{r}}{\partial \delta}\right)_{\tau} - \delta \tau \left(\frac{\partial^{2}\alpha^{r}}{\partial \delta \partial \tau}\right)\right]^{2}}{\tau^{2} \left[\left(\frac{\partial^{2}\alpha^{0}}{\partial \tau^{2}}\right)_{\delta} + \left(\frac{\partial^{2}\alpha^{r}}{\partial \tau^{2}}\right)_{\delta}\right]} \tag{41}$$

The fugacity coefficient and second and third virial coefficients are given in the following equations.

$$\phi = \exp[Z - 1 - \ln(Z) + \alpha^{\mathrm{r}}] \tag{42}$$

$$B(T) = \lim_{\delta \to 0} \left[\frac{1}{\rho_{\rm c}} \left(\frac{\partial \alpha^{\rm r}}{\partial \delta} \right)_{\rm r} \right] \tag{43}$$

$$C(T) = \lim_{\delta \to 0} \left[\frac{1}{\rho_{c}^{2}} \left(\frac{\partial^{2} \alpha^{r}}{\partial \delta^{2}} \right)_{\tau} \right]$$
 (44)

Other derived properties, given below, include the first derivative of pressure with respect to density at constant temperature $(\partial p/\partial \rho)_T$, the second derivative of pressure with respect to density at constant temperature $(\partial^2 p/\partial \rho^2)_T$, and the first derivative of pressure with respect to temperature at constant density $(\partial p/\partial T)_{o}$.

$$\left(\frac{\partial p}{\partial \rho}\right)_{T} = RT \left[1 + 2\delta \left(\frac{\partial \alpha^{r}}{\partial \delta}\right)_{\tau} + \delta^{2} \left(\frac{\partial^{2} \alpha^{r}}{\partial \delta^{2}}\right)_{\tau}\right]$$

$$\left(\frac{\partial^{2} p}{\partial \rho^{2}}\right)_{T} = \frac{RT}{\rho} \left[2\delta \left(\frac{\partial \alpha^{r}}{\partial \delta}\right)_{\tau} + 4\delta^{2} \left(\frac{\partial^{2} \alpha^{r}}{\partial \delta^{2}}\right)_{\tau} + \delta^{3} \left(\frac{\partial^{3} \alpha^{r}}{\partial \delta^{3}}\right)_{\tau}\right]$$
(46)

$$\left(\frac{\partial p}{\partial T}\right)_{\rho} = R\rho \left[1 + \delta \left(\frac{\partial \alpha^{r}}{\partial \delta}\right)_{\tau} - \delta \tau \left(\frac{\partial^{2} \alpha^{r}}{\partial \delta \partial \tau}\right)\right] \tag{47}$$

Equations for additional thermodynamic properties such as the isothermal compressibility and the Joule-Thomson coefficient are given in Lemmon et al.²¹⁵

The derivatives of the ideal gas Helmholtz energy required by the equations for the thermodynamic properties are

$$\tau \frac{\partial \alpha^{0}}{\partial \tau} = 3 + a_{2}\tau + \tau \sum_{k=2}^{6} a_{k} b_{k} \left[\frac{1}{\exp(b_{k}\tau) - 1} \right]$$
 (48)

and

$$\tau^2 \frac{\partial^2 \alpha^0}{\partial \tau^2} = -3 - \tau^2 \sum_{k=3}^{6} a_k b_k^2 \frac{\exp(b_k \tau)}{\left[\exp(b_k \tau) - 1\right]^2}$$
 (49)

The derivatives of the residual Helmholtz energy are given in the following equations.

$$\delta \frac{\partial \alpha^{r}}{\partial \delta} = \sum_{k=1}^{3} N_{k} \delta^{d_{k}} \tau^{l_{k}} d_{k} + \sum_{k=6}^{11} N_{k} \delta^{d_{k}} \tau^{l_{k}} \exp(-\delta^{l_{k}}) \times \\ [d_{k} - l_{k} \delta^{l_{k}}] + \sum_{k=12}^{18} N_{k} \delta^{d_{k}} \tau^{l_{k}} \exp(-\eta_{k} (\delta - \varepsilon_{k})^{2} - \beta_{k} (\tau - \gamma_{k})^{2}) \cdot [d_{k} - 2\eta_{k} \delta(\delta - \varepsilon_{k})]$$

$$\delta^{2} \frac{\partial^{2} \alpha^{r}}{\partial \delta^{2}} = \sum_{k=1}^{5} N_{k} \delta^{d_{k}} \tau^{l_{k}} [d_{k} (d_{k} - 1)] + \sum_{k=6}^{11} N_{k} \delta^{d_{k}} \tau^{l_{k}} \times \\ \exp(-\delta^{l_{k}}) [(d_{k} - l_{k} \delta^{l_{k}}) (d_{k} - 1 - l_{k} \delta^{l_{k}}) - l_{k}^{2} \delta^{l_{k}}] + \\ \sum_{k=12}^{18} N_{k} \delta^{d_{k}} \tau^{l_{k}} \exp(-\eta_{k} (\delta - \varepsilon_{k})^{2} - \beta_{k} (\tau - \gamma_{k})^{2}) \cdot \\ \{[d_{k} - 2\eta_{k} \delta(\delta - \varepsilon_{k})]^{2} - d_{k} - 2\eta_{k} \delta^{2}\}$$
(51)

$$\delta^{3} \frac{\partial^{3} \alpha^{r}}{\partial \delta^{3}} = \sum_{k=1}^{5} N_{k} \delta^{d_{k}} \tau^{l_{k}} [d_{k}(d_{k} - 1)(d_{k} - 2)] +$$

$$\sum_{k=6}^{11} N_{k} \delta^{d_{k}} \tau^{l_{k}} \exp(-\delta^{l_{k}}) \{d_{k}(d_{k} - 1)(d_{k} - 2) +$$

$$l_{k} \delta^{l_{k}} [-2 + 6d_{k} - 3d_{k}^{2} - 3d_{k}l_{k} + 3l_{k} - l_{k}^{2}] +$$

$$3l_{k}^{2} \delta^{2l_{k}} [d_{k} - 1 + l_{k}] - l_{k}^{3} \delta^{3l_{k}} \} +$$

$$\sum_{k=12}^{18} N_{k} \delta^{d_{k}} \tau^{l_{k}} \exp(-\eta_{k}(\delta - \varepsilon_{k})^{2} - \beta_{k}(\tau - \gamma_{k})^{2}) \cdot$$

$$\{ [d_{k} - 2\eta_{k} \delta(\delta - \varepsilon_{k})]^{3} - 3d_{k}^{2} + 2d_{k} -$$

$$6d_{k} \eta_{k} \delta^{2} + 6\eta_{k} \delta(\delta - \varepsilon_{k})(d_{k} + 2\eta_{k} \delta^{2}) \}$$

$$(52)$$

$$\tau^{\frac{\partial \alpha^{r}}{\partial \tau}} = \sum_{k=1}^{5} N_{k} \delta^{d_{k}} \tau^{l_{k}} \exp(-\eta_{k}(\delta - \varepsilon_{k})^{2} - \beta_{k}(\tau - \gamma_{k})^{2}) \times$$

$$[t_{k} - 2\beta_{k} \tau(\tau - \gamma_{k})]$$

$$[t_{k} - 2\beta_{k} \tau(\tau - \gamma_{k})] + \sum_{k=6}^{11} N_{k} \delta^{d_{k}} \tau^{l_{k}} \exp(-\delta^{l_{k}})$$

$$[t_{k}(t_{k} - 1)] + \sum_{k=12}^{18} N_{k} \delta^{d_{k}} \tau^{l_{k}} \exp(-\eta_{k}(\delta - \varepsilon_{k})^{2} - \beta_{k}(\tau - \gamma_{k})^{2}) \cdot$$

$$[t_{k}(t_{k} - 1)] + \sum_{k=12}^{18} N_{k} \delta^{d_{k}} \tau^{l_{k}} \exp(-\eta_{k}(\delta - \varepsilon_{k})^{2} - \beta_{k}(\tau - \gamma_{k})^{2}) \cdot$$

$$[t_{k}(d_{k} - l_{k} \delta^{l_{k}})] + \sum_{k=12}^{18} N_{k} \delta^{d_{k}} \tau^{l_{k}} \exp(-\eta_{k}(\delta - \varepsilon_{k})^{2} - \beta_{k}(\tau - \gamma_{k})^{2}) \cdot$$

$$[t_{k}(d_{k} - l_{k} \delta^{l_{k}})] + \sum_{k=12}^{18} N_{k} \delta^{d_{k}} \tau^{l_{k}} \exp(-\eta_{k}(\delta - \varepsilon_{k})^{2} - \beta_{k}(\tau - \gamma_{k})^{2}) \cdot$$

$$\delta^{2} \frac{\partial^{2} \alpha^{r}}{\partial \tau \partial \delta} = \sum_{k=1}^{5} N_{k} \delta^{d_{k}} \tau^{l_{k}} [d_{k} l_{k}] + \sum_{k=6}^{18} N_{k} \delta^{d_{k}} \tau^{l_{k}} \exp(-\eta_{k}(\delta - \varepsilon_{k})^{2} - \beta_{k}(\tau - \gamma_{k})^{2}) \cdot$$

$$\delta^{2} \frac{\partial^{3} \alpha^{r}}{\partial \delta \partial \tau^{2}} = \sum_{k=1}^{5} N_{k} \delta^{d_{k}} \tau^{l_{k}} [d_{k} l_{k}(t_{k} - 1)] + \sum_{k=6}^{11} N_{k} \delta^{d_{k}} \tau^{l_{k}} \exp(-\eta_{k}(\delta - \varepsilon_{k})^{2} - \beta_{k}(\tau - \gamma_{k})^{2}) \cdot$$

$$\delta^{2} \frac{\partial^{3} \alpha^{r}}{\partial \delta \partial \tau^{2}} = \sum_{k=1}^{5} N_{k} \delta^{d_{k}} \tau^{l_{k}} [d_{k} l_{k}(t_{k} - 1)] + \sum_{k=6}^{11} N_{k} \delta^{d_{k}} \tau^{l_{k}} \exp(-\delta^{l_{k}})$$

$$\delta^{2} \frac{\partial^{3} \alpha^{r}}{\partial \delta \partial \tau^{2}} = \sum_{k=1}^{5} N_{k} \delta^{d_{k}} \tau^{l_{k}} [d_{k} l_{k}(t_{k} - 1)] + \sum_{k=6}^{11} N_{k} \delta^{d_{k}} \tau^{l_{k}} \exp(-\delta^{l_{k}})$$

$$\delta^{2} \frac{\partial^{3} \alpha^{r}}{\partial \delta \partial \tau^{2}} = \sum_{k=1}^{5} N_{k} \delta^{d_{k}}$$

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