

Three-Dimensional Imaging With Multiple Degrees of Freedom Using Data Fusion

This paper demonstrates that 3-D imaging using fusion provides multiple advantages including enhancement in visualization and reconstruction under different acquisition conditions.

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ABSTRACT | This paper presents an overview of research work and some novel strategies and results on using data fusion in 3-D imaging when using multiple information sources. We examine a variety of approaches and applications such as 3-D imaging integrated with polarimetric and multispectral imaging, low levels of photon flux for photon-counting 3-D imaging, and image fusion in both multiwavelength 3-D digital holography and 3-D integral imaging. Results demonstrate the benefits data fusion provides for different purposes, including visualization enhancement under different conditions, and 3-D reconstruction quality improvement.

KEYWORDS | Fusion; holography; integral imaging; multiresolution wavelet decomposition; multispectral imaging; photon counting; polarimetric imaging; 3-D imaging

I. INTRODUCTION

The definition given by the Joint Directors of Laboratories (JDL) about data fusion involves the "combination of data and information from several sources" [1]. This "require-

ment" was generalized in [2] when considering that the data could be provided either by a single source (sensor) or by multiple sources. In the particular case of image fusion methodologies, an intense research effort is being made in fields like remote sensing [3]–[7], surveillance [8]–[11], and medicine [12]–[15], where the current tendency is in the use of a combination of sensors to optimize information acquisition and extraction. In the case of remote sensing, the use of multiple sensors may help in rural and urban planning [3], species classification [4], [5], and prevention of disasters [6], [7].

On the other hand, surveillance systems may need to have all-weather and all-time acquisition capabilities. This capability might be given by fusing the information given by red–green–blue (RGB) and thermal sensors [8]–[10]. In the case of medicine there is a clear evidence that acquisition methodologies (magnetic resonance imaging, computed tomography, positron emission tomography, etc.) are complimentary and may be of great help in the prevention and detection of illnesses [11]–[15].

Other fields where image fusion from various data sources (sometimes referred as multimodal image fusion) is an active area of research include video processing [16], [17], biometric identification/classification [18]–[21], image fusion for visualization enhancement [22], industrial inspection [23], among others [24]–[27]. Image fusion methods might be also aimed at solving only one particular type of fusion problem, but current tendency is toward the creation of methodologies that may be able to solve image fusion problems in more than one area (fusion of medical images, or fusion of RGB and thermal images, using the same mathematical framework) [28]–[32].

Image fusion techniques can be classified taking into account the stage at which they are applied [33]. The most

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common strategy is to use the fusion strategy at feature level. However, they can also be designed to be used at the so-called decision level [34]. Fusion at the feature level means that the different features obtained are "combined" and later given to the stage where a final decision is taken. In the decision level case, different methods are simultaneously applied that provide different decisions on a local level, and the local decisions are combined using a decision function that creates the final decision.

In this paper, we present an overview of the work made by the authors on using fusion of different information sources in the particular framework of 3-D imaging. In our case, we consider fusion in the sense of using different degrees of freedom for light in order to improve information extraction. Besides, we can consider that the approaches explained here fall into the feature level fusion strategy [33].

To the best of our knowledge, a survey paper of different information sources (polarimetric, multispectral, different number of photons) and its combination in the framework of 3-D imaging has not been made to date. A general analysis of the state-of-the-art in multimodal image fusion is out of the scope of this paper, and the reader is referred to [33] about multimedia (including image and video) data fusion, as well as the different criteria that can be used to classify them, and [35] for multisensory data fusion. In particular, in this paper, we discuss multiperspective fusion under very low illumination conditions, 3-D imaging fusion with multispectral imaging, and multiwavelengths data fusion for digital holography and 3-D integral imaging. The paper is organized as follows. Section II presents an overview of integral imaging as an autostereoscopic technique that is currently being intensively researched. Section III presents multiperspective fusion results for very low illumination conditions. Section IV presents results on 3-D visualization at low light levels using multispectral photoncounting integral imaging. Section V presents new results on the fusion of 3-D information obtained from multiwavelengths integral images for robust depth extraction compared with a single-wavelength 3-D reconstructed image. Section VI presents an overview of multiwavelength data fusion for digital holography, and the fusion of polarimetric, multiwavelength and multispectral information for 3-D integral imaging.

In order to better understand the different concepts used in the paper, Table 1 presents a glossary of terms used throughout the paper, by order of appearance.

II. INTEGRAL IMAGING OVERVIEW

Three-dimensional optical image sensing and visualization technologies have been researched extensively for different applications in fields as diverse as TV broadcasting, entertainment, medical sciences, and robotics, to name a few [36]–[38]. As opposed to traditional 2-D imaging, 3-D sensing technologies can potentially capture the structural

device	acquisition.			
Stereo pair	System that allows to present slightly different images to each eye to create the sense of depth.			
Elemental image	Image generated by each one of the lenslets. In the case of a moving sensor in a Synthetic Aperture Integral Imaging (SAII) mode, it corresponds to each one of the images acquired by the sensor in each of its positions.			
Lenslet array	Array of small lenses (called lenslets) located in a grid which allow to obtain information from a scene from slightly different view-points.			
Points Spread Function (PSF)	Function that describes the response of an optical system to a light point source or object.			
Depth of Focus (DoF)	Distance the image plane can be displaced (plane where the image is seen) while being this image in acceptably sharp focus.			
Aberration	Deviation from "normal operating conditions" in an optical system.			
Field of View (FoV)	Spatial/angular extent of an observable scene that is seen by a sensor.			
Pickup aperture	Opening of an optical system that determines the light that arrives at the sensor.			
Pinhole	In optics, it refers to a small aperture the light can go through.			
Bayer filter array	It is a specific colour filter array to arrange Red, Green and Blue Sensors on a square grid.			
Holography	Recording and display technique that uses coherent light and generates images that change its appearance with the viewing angle.			
Optical path	Path that the light follows when propagates in a medium.			
Fresnel transformation method	Method to generate a discrete version of the Fresnel double integral propagation operator, used to assess its propagation			

Table 1 Glossary of Terms Used in This Paper

Definition

Group of techniques that "generate" 3-D

Device formed by a layer with vertical

images for visualization purposes

without the use of special glasses

slits that allows each eye to see a different set of pixels and creating a

Optical device that does not use an

illumination system for image

sense of depth.

Concept

Auto-stereoscopy

Parallax barriers

Passive optical

device

information of the scene. In many instances, the capabilities of 3-D imaging and display systems have revolutionized the progress of these disciplines, enabling new detection/display abilities that would not have been otherwise possible. There are different methods to create and

in any media.

A Spatial Light Modulator (SLM) is a

system that allows the generation of a

spatially varying modulation on a light

through it. It is called LC-SLM when the element that creates the modulation is a Liquid Crystal Device (LCD).

beam when the light beam passes

Liquid Crystal

Spatial Light

Modulator

(LCSLM)

visualize 3-D images. Some of them make use of special glasses, which may create adverse effects like sickness, etc. Other methods use parallax barriers in order to avoid using glasses, adapting their parameters to the viewer position [39]. Content-adaptive parallax barriers for which display elements are optimized for the multiview content are also being developed [40]. Alternative methods use multiple cameras located at several positions.

As one of the promising methods in the area of 3-D sensing and display, integral imaging is an autostereoscopic 3-D imaging method that offers a passive and relatively inexpensive way to capture 3-D information and to optically or computationally visualize it [41]-[46]. The integral imaging technique belongs to the broader class of multiview imaging techniques. Recently, it has been shown that the spatial 3-D resolution obtained with the integral imaging method is better than the resolution obtained when using a stereo pair [45]. Integral imaging provides 3-D information through a collection of 2-D projections of realworld objects. There are two separate procedures for acquisition and visualization of 3-D objects which are referred to as: 1) pickup and 2) reconstruction stages, respectively. In the pickup stage (see Fig. 1), multiple 2-D images (hereafter called elemental images) are captured through an array of small lenses (lenslet array). Each lenslet carries out a unique projective transformation that maps the 3-D object space onto a 2-D elemental image and is a function of the lenslet position and the focal length. Since each projective transform uniquely defines a perspective view, both direction and intensity of rays emanating from the 3-D object can be recorded on the image sensor. As a result, an array of inverted real images is



Fig. 1. Integral imaging pickup procedure.



Fig. 2. Integral imaging display procedure.

formed on the image sensor. For optical reconstruction of the scene, a 2-D liquid-crystal display (LCD) may project the recorded integral image onto the focal plane of the display lenslet array with homogeneous (matched) pixel arrangement as that of pickup lenslet array. Each elemental image is then optically taken by its corresponding lenslet back into 3-D space. The overlap of all elemental images creates light distributions similar to the original object of interest. As a result, an observer can see a real 3-D image, with inverted depth (see Fig. 2).

In lenslet-based integral imaging systems, the resolution of each elemental image is constrained by three parameters: 1) the lenslet point spread function (PSF); 2) the lenslet depth of focus (DoF); and 3) the pixel size [47]–[49]. Aberrations and diffraction effects must also be considered because of the relatively small size of each lenslet.

As an alternative methodology to that based on lensletbased systems, integral imaging can be performed either using an array of high-resolution imaging sensors, or in a synthetic aperture mode, hereafter called synthetic aperture integral imaging mode (SAII; see Fig. 3). When a single sensor translates on a 2-D plane to capture multiple 2-D images, this enables one to obtain larger field-of-view (FOV) 2-D images. In addition, SAII potentially creates larger pickup apertures than the lenslet-array-based approach. Pickup aperture is useful for long-distance objects. Fig. 3 illustrates the pickup stage by using a sensor array.

Three-dimensional reconstruction of images can be achieved by computationally simulating the optical backprojection of the elemental images. In particular, a



Fig. 3. Synthetic aperture integral imaging acquisition.

computer-synthesized virtual pinhole array is used to inversely map the elemental images into the object space, as illustrated in Fig. 4. Superposition of properly shifted elemental images provides the 3-D reconstructed images [50]

$$I(x,y,z) = \frac{1}{O(x,y)} \sum_{k=0}^{K-1} \sum_{l=0}^{L-1} E_{kl} \left(x - k \frac{N_x p}{c_x M}, y - l \frac{N_y p}{c_y M} \right)$$
(1)

where I(x, y, z) represents the intensity of the reconstructed 3-D image at depth z, x and y are the indexes of the pixel, E_{kl} represents the intensity of the kth row and lth column elemental image, $N_x \times N_y$ is the total number of pixels for each elemental image, M = z/f is the magnification factor, $c_x \times c_y$ is the physical size of the camera sensor, p is the camera pitch, and O(x, y) is the overlapping number matrix.

The use of integral imaging techniques may be useful to recognize and classify objects under adverse conditions (in noisy or photon starved conditions), and under occlusions [51], [52], and recent results show the potential



Fig. 4. Computational reconstruction method in integral imaging.

of this technique in new application and research avenues [53]–[56].

III. MULTIPERSPECTIVES FUSION TO IMAGE 3-D SCENES UNDER EXTREMELY LOW ILLUMINATION CONDITIONS

Capturing images from multiple perspectives, as done with the integral imaging technique described in Section II, may be viewed as a multichannel image acquisition process. Since the data captured through the multiple channels (i.e., the perspective images) is typically redundant, it is possible by proper digital process, to overcome signal-to-noise ratio (SNR) limitations that are considered prohibitive with single-channel imaging. Fusion of multichannel images to overcome SNR limitation in 2-D imaging was explored in many fields as in astronomy, medical imaging, and microscopy. Here we describe the possibility to use the elemental images captured with the integral imaging technique to reconstruct 3-D objects in extremely starved imaging conditions. Photon starving imaging conditions may occur in scenarios of low light illumination, as in night vision, or when imaging with short exposure time, as for instance in high frame rate video acquisition.

The ability to visualize 3-D data from photon starved integral images was demonstrated in [57]. By applying the penalized maximum likelihood expectation-maximization (PMLEM) algorithm, 3-D images were reconstructed from integral images captured with SNR significantly lower than 1. For the description of the PMLEM reconstruction process, we will first formulate the integral imaging acquisition process using an operator formalism

$$\mathbf{E} = \mathbf{H}\mathbf{f} + \mathbf{n} \tag{2}$$

where the 3-D object data are represented by the (lexicographically ordered) vector **f**, **E** is a lexicographic vector representing the set of elemental images forming the integral image, H is the forward operator and n is the acquisition noise. Technically, the operator H can be implemented as a matrix or as a function handle (procedure) that maps each pixel from the object plane to the image plane. In the geometrical optics limits, H can be evaluated by simply tracing the ray from the object to the image plane (Fig. 1). If necessary, diffraction and other nongeometrical optical distortions can be included as well. In regular imaging conditions the image flux from the object is much higher than the noise (i.e., $\|\mathbf{f}\| > \|\mathbf{n}\|$) and a 3-D reconstruction can be obtained simply by a backprojection process. In an operator formalism this process is described as the application of the adjoint operator \mathbf{H}^{T} on the captured elemental images $\mathbf{E}, \mathbf{I} = \mathbf{H}^{\mathrm{T}} \cdot \mathbf{E}$. Technically, the backprojection process can be evaluated via (1). For photon starved conditions, an iterative reconstruction algorithm implementing a PMLEM estimator is much more efficient. The PMLEM iteration step is given by

$$\hat{\mathbf{f}}^{k+1} = \frac{\hat{\mathbf{f}}^{(k)}}{\mathbf{s} + \beta \cdot \mathbf{P} \hat{\mathbf{f}}^{(k)}} \mathbf{H}^{\mathrm{T}} \frac{\mathbf{E}}{\mathbf{H} \cdot \hat{\mathbf{f}}^{(k)}}$$
(3)

where $\mathbf{\hat{f}}^{(k)}$ is the reconstructed image vector at the kth iteration, s is referred to as the "sensitivity vector" accounting for the number of elemental images contributing to reconstruction of each object point. P is the penalty operator and β is a constant controlling the amount of regularization. The division in (3) should be taken as Hadamard (component-wise) division. The penalty operator P works as a regularizer to improve the robustness in case of large noise values. Various penalty operators can be defined, each reflecting a specific assumption on the local behavior of the object. In [58], penalties reflecting quadratic, median root, and total variation (TV) priors were investigated for photon-counting integral imaging. Among these priors the TV penalty was found to give the best results. The ability to overcome the noise limitation by fusing the elemental images captured with the integral imaging technique is demonstrated in Fig. 5. Fig. 5(a) shows an array of 7×7 elemental images captured with regular illumination conditions. Each elemental image captures from slightly different direction the 3-D scene which comprised two toys: a truck and an airplane located at distances of 50 and 70 cm from the camera, respectively. Fig. 5(b) and (c) shows the reconstruction of the 3-D scene by focusing at two depth planes of the two toys. The reconstruction is implemented by backprojection [see (1)]. Fig. 5(d) shows the array of elemental images taken with the same geometrical setup as that used for capturing Fig. 5(a), but with a shorter exposure time so that the SNR (defined as ||E||/||n||) is approximately 0.16. With such a low SNR the signal is buried much below the noise level, therefore the objects are absolutely indistinguishable. However, by fusing the elemental images using the PMLEM algorithm with a TV prior the two objects, at the two different depth planes, can be readily reconstructed, as demonstrated in Fig. 5(e) and (f).

IV. THREE-DIMENSIONAL VISUALIZATION AT LOW LIGHT LEVEL USING MULTISPECTRAL PHOTON-COUNTING INTEGRAL IMAGING

Photon-counting imaging technique which is suitable to photon-limited situations such as night vision has been successfully applied in 3-D object imaging and recognition [59]–[62]. On the other hand, 3-D objects can be computationally reconstructed and recognized in a photoncounting integral imaging (PCII) system with grayscale elemental images under low-light levels [59]. However,



Fig. 5. (a) 7×7 elemental images, and reconstruction of object planes at (b) a distance of 50 cm and (c) a distance of 70 cm. (d) 7×7 elemental images captured in photon starved conditions (SNR = 0.16, average flux of 3.8 photons/pixels) and reconstructed object planes at distance 50 cm (e) and 70 cm. (f) All the results are from [57].

the elemental images in this PCII system are captured with monochrome sensors and the object boundaries might be easily degraded when they are imaged under low light levels. Similarly, the reconstructed object in a PCII system may also suffer from degraded shape cues. As a consequence, object recognition based on these degraded images is a challenging problem. Nevertheless, color image



Fig. 6. Schematic setup of multispectral PCII system shown in [63].

information can provide informative patterns to help us visualize 3-D objects. In addition, color information may improve recognition performance when other features are not significant such as degraded shape cues in a photoncounting integral imaging system. Therefore, multispectral photon-counting integral imaging system may ameliorate the deficiency that exists in conventional PCII with grayscale elemental images since these images may lose an important amount of information of detail of the object. In [63], we have demonstrated that a 3-D scene can be visualized at a low light levels with our proposed multispectral PCII technique.

The diagram of multispectral PCII system is given in Fig. 6. A Bayer color filter array which is a widely adopted color image sensor is used to capture the color information of 3-D objects. However, a demosaicing or interpolation algorithm has to be introduced to estimate the missing two colors in a Bayer image in order to get a full RGB color image. Our numerical simulation results showed that the gradient corrected linear interpolation method proposed by Malvar *et al.* [64] may achieve better results for demosaicing Bayer image into full RGB color image when compared with some of the state-of-the-art demosaicing schemes [63]. The Malvar *et al.*'s interpolation method uses the interpolated current pixel value and the gradient information in the Bayer image to estimate the two missing values at the current pixel location.

In Fig. 6, multiple Bayer color filter arrays are used to capture Bayer elemental images in the integral imaging sys tem. However, when all of the Bayer elemental images are generated under low light level conditions, the photon-counted Bayer elemental images would be recorded in Bayer color filter arrays in this multispectral PCII system. This process can be simulated by controlling the expected number of photons in a multispectral scene. It is assumed that each pixel separately follows a Poisson distribution for each channel (R, G, and B) of the Bayer image. Assume that $\tilde{B}_w(x, y)$ is the normalized irradiance of each color channel on the Bayer image and n_p , the expected number of photons for each elemental image, then the Poisson parameter λ_w for each pixel on the three color channels

can be written as $\tilde{B}_w(x, y) \times n_p$. Thus, the Poisson random number of counts for arbitrary pixel positions on each elemental image is modeled as follows [63]:

$$C_w(x,y) \approx \text{Poisson}(\lambda_w = \tilde{B}_w(x,y) \times n_p)$$
 (4)

where the subscript *w* represents the three RGB color channels. On the other hand, the 3-D point is computationally reconstructed with the photon-counted Bayer elemental images by using parametric maximum likelihood estimator (MLE) [58]. That is, the 3-D point can be achieved with MLE by using a series of 2-D points on the photon-counted Bayer elemental images. This process can be modeled as follows [63]:

$$PS_{w}(v) = \text{MLE}(\lambda_{w}(v))$$

$$= \arg \max_{\lambda_{w}(v)} \left(\log \prod_{k=1}^{N} \exp(-\lambda_{w}(v))(\lambda_{w}(v))^{C_{k,w}(v)} \right)$$

$$= \frac{1}{N} \sum_{k=1}^{N} C_{k,w}(v)$$
(5)

where $C_{k,w}(v)$ is the pixel point value of the k_{th} photoncounted elemental image. $PS_w(v)$ represents the 3-D scene, v defines one voxel position, $\lambda_w(v)$ denotes the mean parameter of the w(Red, Green, or Blue) spectral channel, and N denotes the total number of elemental images. Finally, the reconstructed Bayer slice image is demosaiced with the gradient corrected linear interpolation technique.

Experiments were conducted to show the feasibility of the multispectral PCII system for 3-D visualization at low light level conditions. Two different objects (three colored balls and a toy bird) were used as the 3-D scene. With these Bayer elemental images, the two 3-D objects with Bayer format can be computationally reconstructed at two different distances. Then, the true color RGB reconstructed images can be achieved by applying Malvar's demosaicing algorithm to these reconstructed Bayer images. Fig. 7 shows the reconstructed Bayer images and their corresponding true color RGB images after Malvar's demosaicing method is applied.

In the case of low light levels, the photon-counted Bayer elemental images can be simulated based on Bayer elemental images using (4) and controlling the expected number of photons. With these photon-counted Bayer elemental images simulated under different number of photons, we show in Fig. 8 that the multispectral 3-D objects can be correctly visualized. The images in Fig. 8 were demosaiced from the reconstructed Bayer images that are derived with (5) by using these photon-counted Bayer elemental images at two different distances where one is with the color balls in focus, while the other one is with toy bird in focus.



Fig. 7. Reconstructed images at two different depths. (a) and (b) Reconstructed Bayer images with different object focused. (c) and (d) True color RGB images of (a) and (b) with Malvar's interpolation method applied [63].

Fig. 8 also shows that this multispectral PCII method can be used for multispectral visualization of 3-D objects when the number of photons is limited. In addition, the following PSNR metric was applied to measure the quality of multispectral 3-D reconstructed images under low light levels:

$$PSNR = 10 \log_{10} \left(\frac{I_{\max}^2}{MSE} \right)$$
(6)



Fig. 8. Multispectral 3-D visualization under low light levels. (a), (c), and (e) are reconstructed RGB images with tricolored balls focused under $n_p = 10, 10^3$, and 10^5 respectively. (b), (d), and (f) are reconstructed RGB images with toy bird focused under $n_p = 10, 10^3$, and 10^5 , respectively [63].



Fig. 9. PSNR [as defined in (6)] for green, red, and blue channels between intensities of multispectral II (I_{MII}) in Fig. 7 and multispectral photon-counting II (I_{MPCII}) in Fig. 8 versus the expected number of photons. (a) PSNR between Fig. 7(c) and I_{MPCII} in Fig. 8 (focused ball images). (b) PSNR between Fig. 7(d) and I_{MPCII} in Fig. 8 (focused bird images) [63].

where I_{max} is the maximum possible pixel value of the multispectral integral imaging as ground truth or reference (I_{MII}) and MSE is mean squared error between multispectral photon-counting integral imaging (I_{MPCII}) and I_{MII} . It quantitatively verified that the multispectral 3-D scene can be reconstructed from photon-counted Bayer elemental images with MLE and gradient corrected linear interpolation algorithm at low light levels (see Fig. 9 and [63]).

V. MULTISPECTRAL DATA FUSION FOR DEPTH ESTIMATION IMPROVEMENT IN 3-D INTEGRAL IMAGING

Introduction of spectral information may help in object recognition and/or classification in 3-D imaging: 1) in underwater 3-D visualization [51], since water absorption is wavelength dependent; 2) in dermatology [65], in particular in skin cancer detection, because melanoma pigmented skin lesion is wavelength dependent and its structure is directly related to its evolution and degree of severity; 3) in remote sensing applications, in the case of sensors onboard airplanes or satellites which may be able to create 3-D models with the inclusion of multispectral information; 4) in remote sensing pattern recognition (i.e., identification of the 3-D structure and the spectral response of an object from the distance); and 5) in photon starved or "hard to visualize" conditions (at night, under "foggy" conditions, etc.) [60]. Multispectral 3-D reconstruction has already been applied in microscopy [66]. Other 3-D acquisition and visualization techniques have already incorporated multispectral information [67]–[69].

In this section, we will show novel results in the fusion of integral images extracted from different spectral channels, combining the depth information of each multispectral channel to make more accurate and robust depth estimation in scenes acquired with a multispectral sensor.

Three-dimensional image reconstruction in integral imaging has been traditionally performed in orthogonal



Fig. 10. Variance minimization principle (adapted from [71]).

planes to the optical axis. A certain spatial point on the reconstruction plane is set to the average of the collected samples of the corresponding 3-D space point. Based on the pinhole projection model, the relationship between the coordinate of 3-D space point (x, y, z) and its projected image pixel coordinate (ξ, η) on the *i*th column and *j*th row image sensor is given by [70]

$$(\xi,\eta) = \left(\frac{Kg(x+C_x^{ij})}{s_x z}, \frac{Lg(y+C_y^{ij})}{s_y z}\right)$$
(7)

where superscript *ij* means the *i*th column and the *j*th row, (C_x^{ij}, C_y^{ij}) is the center position of the *ij*th image sensor, (S_x, S_y) is the image size, and g represents the distance between the pinhole and the image sensor (see Fig. 10).

From this information, depth of each point in the scene can be estimated using the method explained in [71] and summarized here. Let us define the statistical mean and variance for a 3-D point P(x, y, z) as follows:

$$E(x, y, z) = \frac{\sum_{i=1}^{N} \sum_{j=1}^{M} I^{ij}(\xi, \eta)}{NM}$$
(8)

$$V(x, y, z) = \frac{\sum_{i=1}^{N} \sum_{j=1}^{M} (I^{ij}(\xi, \eta) - E(x, y, z))^2}{NM}$$
(9)

where $I^{ij}(\xi, \eta)$ represents the intensity of pixel (ξ, η) on the *ij*th elemental image, and *N* and *M* represent the number of elemental images in each (*x* and *y*) direction. E(x, y, z) and V(x, y, z) represent the intensity mean and variance of 3-D point, respectively. Therefore, if a point belongs to an object, V(x, y, z) is expected to reach a local minimum

(Fig. 10). Therefore, the depth of each 3-D object point can be estimated by considering

$$\hat{z}(x,y) = \arg\min V(x,y,z) \tag{10}$$

with $z \in z = [z_{\min}, z_{\max}]$. This method, however, suffers from one main drawback. The variance does not "behave" correctly for parts of objects in the scene that present specular reflection or surface sharp discontinuities. The method proposed here to overcome this drawback is to take advantage of the focusing capability in synthetic aperture integral imaging and therefore also use a "focus measure" criterion. The "Tenengrad" focus measure method [72] consists of assessing the following function per pixel position:

$$\phi(x,y) = \sum_{(i,j)\in\Omega(x,y)} \left(G_x(i,j)^2 + G_y(i,j)^2 \right)$$
(11)

where $\Omega(x, y)$ represents the group of pixels in a neighborhood of pixel (x, y), and $G_x = I \bigotimes S_x$ and $G_y = I \bigotimes S_y$ are the "x" and "y" image gradients obtained by convolving an image (I) with a Sobel filter in the "x" and "y" directions $\{S_x, S_y\}$.

In practice, depth estimation varies if the scene is acquired with spectral filters. When combining multispectral and integral imaging, a straightforward way to perform 3-D reconstruction is to apply the process to each multispectral band independently. However, we can take advantage of the 3-D information each band may acquire and combine them to improve the scene depth measurements obtained from each spectral band independently.

A. Depth Estimation Using a Combination of Variance and Focus Measure

A series of 121 elemental images were acquired using a Marlin F080B monochrome camera and a liquid crystal tunable filter (LCTF) applying the SAII technique, for a 11×11 grid [73]. Acquisition wavelengths were: {480, 510, 550, 570, 600, 650, 680}. Fig. 11(a) shows the experimental setup used for the acquisition. Fig. 11(b) shows the grayscale image corresponding to the elemental image in position (6, 5) of the 11×11 grid, for $\lambda = 650$ nm. The proposed multispectral fusion strategy consists of the following steps.

 Infer the depth corresponding to the minimum variance and the depth of the maximum Tenengrad function measure for each pixel and wavelength band

$$z_1^*(x, y, \lambda_i) = \arg\min_z V(x, y, z, \lambda_i)$$
(12)
$$z_2^*(x, y, \lambda_i) = \arg\max_z \phi(x, y, z, \lambda_i).$$
(13)

2) Select for each pixel the depth corresponding to the minimum variance among bands, and the





Fig. 11. (a) Experimental setup for the multispectral integral imaging system shown in [73]. Elemental image in position (6, 5) of the camera array for $\lambda = 650$ nm.

depth corresponding to the maximum focus measure among bands as well

$$z_1^{*'}(x,y) = \arg\min_{\lambda_i} \left[V(x,y,z_1^*(x,y,\lambda_i),\lambda_i) \right]$$
(14)

$$z_{2}^{*'}(x,y) = \arg \max_{\lambda_{j}} \left[\phi\left(x, y, z_{2}^{*}(x, y, \lambda_{j}), \lambda_{j}\right) \right].$$
(15)

 Infer the variance histogram corresponding to the minimum variance distribution among bands of step 2) and generate a variance threshold (θ) corresponding to 99.5% of the accumulated variance in this histogram

$$\theta \Big[H \Big(V \Big(z_1^{*'}(x, y) \Big) \Big) \Big] = \tilde{v}$$



Fig. 12. Accumulated histogram for the variance for the depths obtained using (14). The line corresponding to the threshold used in (17) is plotted as well.

such that

$$\frac{\sum_{b=1}^{\widetilde{V}} H(V)}{V_{T}} = 0.995$$
(16)

where $V_T = \sum_D H(V)$ is the total accumulated variance for the whole variance range.

If the variance of a pixel [in the histogram of step 3)] is higher than θ, the distance associated to the pixel is the one given by the "focus measure" criterion in step 2). Otherwise, the minimum variance in 2) is associated to this pixel

$$z_F(x,y) = \begin{cases} z_2^{*'}, & \text{if } V(x,y,z_1^{*'}) \ge \theta \\ z_1^{*'}, & \text{otherwise.} \end{cases}$$
(17)

Fig. 12 shows the accumulated histogram distribution of $H(V(z_1^{*'}(x,y)))$. The threshold θ corresponding to the 99.5% of the accumulated variance is represented as a dotted red line. Table 2 shows the measured distance from each one of the dice to the Canon TV zoom lens. Table 3 shows the depth estimation results obtained using: a) one wavelength ($\lambda = 650$ nm); and b) the procedure explained in steps 1)–4).

We considered that the best depth reconstruction for a single wavelength was that at $\lambda=650$ nm, which is the

Table 2 Distance From Each Die to the Acquisition System

Blue die (mm)	Red die (mm)	Green die (mm)
220	240	262

the Different Fusion Methods

Table 3 Distance Estimation Results for the Best Wavelength Case and for

	Blue die (mm)	Red die (mm)	Green die (mm)
$\lambda = 650$ nm	237.8 ± 18.7	254.7 ± 13.3	265.1 ± 20.8
Fusion	238.1 ± 7.7	249.6 ± 10.6	262.4 ± 6.1

one with the lowest total RMSE error defined as

$$\text{RMSE} = \sqrt{\frac{1}{N} \cdot \sum_{i=1}^{N} (d_i - d_{GT,i})^2}.$$
 (18)

Here d_i refers to the distance between pixel "*i*" and the acquisition system, as assessed by a method and $d_{GT,i}$ refers to the ground-truth distance measured by a rule.

Table 4 shows the total RMSE as well as RMSE error per die.

Fig. 13(a) shows a 3-D plot with the depth reconstruction results for $\lambda = 650$ nm obtained using the minimum variance criterion in (9). Fig. 13(b) shows the corresponding depth results after the application of the formulas given in (12)–(17). As we can see, the problems that appear for the depth reconstruction using the minimum variance principle are not so evident. Fig. 13(c) shows the application of steps 1 and 3 of this strategy, for $\lambda = 650$ nm. In the three cases, the grayscale image of elemental image (6, 5) for $\lambda = 650$ nm has been used for visualization purposes.

VI. IMAGE FUSION IN MULTIWAVELENGTH DIGITAL HOLOGRAPHY AND INTEGRAL IMAGING

This section shows the results obtained by the authors in the application of the multiresolution wavelet decomposition (MWD) technique for image fusion in two different fields: 1) multiwavelength digital holography (MWDH); and 2) multidimensional optical data fusion, showing its capability to improve visualization results in both cases.

A. Multiwavelength Digital Holography

Digital holography (DH) [74]–[91] has been applied in different fields such as microscopy [74]–[75], imaging and display technology [76]–[77], data storage [78], 3-D object recognition and 3-D optical encryption [79], [80], to cite a few. Current research efforts also focus on including color and multispectral information in DH [92]–[100]. The

Table 4 Total Root Mean Square Error (RMSE_T) and RMSE Error Per Die

	RMSET	RMSE _B	RMSE _R	RMSEG
$\lambda = 650$ nm	21.6	24.5	19.9	20.8
Fusion	14.0	19.8	14.3	7.1



Depth reconstruction for the combination of the minimum variance and focus measure principles



Fig. 13. (a) Depth reconstruction result using the minimum variance principle. (b) Depth reconstruction for the combination of the minimum variance and the focus measure strategy in steps 1–4 in Section V. (c) Depth reconstruction when using criteria in (b) for $\lambda = 650$ nm only.

interested reviewer is referred to [101] for a comprehensive review for current fields of application.

In this section, a summary of the fusion results shown in [102] will be presented. Multiwavelength digital holography (MWDH) has been extensively researched during the last few years. It has shown superior object phase recovery capability in relation to other techniques [101], natural color holographic cameras have already been proposed [90], [91], and a great effort has been made to infer the spectral information of objects simultaneously to capture 3-D information using DH [91].

Image fusion methods aim at creating a composite image of the same scene acquired at different wavelengths. Gaussian pyramids and multiresolution wavelet decomposition (MWD) techniques have received attention during the last decade.

MWD may be combined with MWDH in order to generate better quality color 3-D images. Direct RGB creation of reconstructed images acquired at different wavelengths has contrast and resolution limitations, due to the speckle noise, which appears when using coherent light illumination. MWD techniques are based on the decomposition of the lowfrequency component of the previous resolution level and its assignment into the higher resolution level. Let us consider P_0 a grayscale image. The first level decomposition will be

$$P_0 \longrightarrow P_{a1}, P_{\nu 1}, P_{h1}, P_{d1}. \tag{19}$$

 P_{a1} is the so-called approximation term, and P_{v1} , P_{h1} , and P_{d1} are the vertical, horizontal, and diagonal details of the next

(first in this case) level decomposition, respectively. The details and the approximation contain the high-frequency and low-frequency features of the image, respectively. The approximation of each level may be recursively decomposed into the next-level components as follows:

$$P_{a(n-1)} \longrightarrow P_{an}, P_{\nu n}, P_{hn}, P_{dn}, \quad \text{for } n = 1, 2, \dots$$
 (20)

Once the multiresolution wavelet coefficients of each image acquired by each sensor are obtained, high- and lowfrequency components can be postprocessed using specific fusion rules, such as addition, or weighted averaging. Fig. 14 shows a two-level MWD fusion method for multiwavelength images. These images need to be registered. After registration, their multiresolution wavelet decomposition is obtained. Fusion rules are applied to their high- and low-frequency components afterwards. These transformed (fused) wavelet coefficients are inverse wavelet transformed into a final fused image.

The experimental setup used to record MWDH holograms is illustrated in Fig. 15. Two light sources consisting of two lasers emitting at $\lambda_1 = 632.8$ nm and $\lambda_2 = 532.0$ nm were used. The two lasers were allowed to propagate along the same path for either the reference or the object beams. The reflecting prism located in the path of the red laser beam allows matching the optical paths of the two interfering beams inside the optical coherence length of the laser. The object beam was at a distance of 850 mm in



Fig. 14. Image fusion of multiwavelength holographic images by use of MWD (adapted from [102]).



Fig. 15. Optical recording setup for digital holograms with two wavelengths. M: mirror; BE: beam expander; O: object; BS: beam splitter; RP: reflecting prism (adapted from [102]).

front of the CCD array. The CCD sensor size is 1024×1024 square pixels, $6.7 - \mu m$ length.

Two holograms corresponding to the two wavelengths used were reconstructed separately applying the Fresnel transformation method. Reconstruction was obtained considering the pixel size $(\Delta \xi, \Delta \eta)$ of the CCD array, being this size different from the pixel size $(\Delta x', \Delta y')$ in the image plane. They are, however, related by the following expressions: $\Delta x' = d \cdot \lambda / N \cdot \Delta \xi$ and $\Delta y' = d \cdot \lambda / N \cdot \Delta \eta$, where N^2 defines the total number of pixels in the CCD array and d is the reconstruction distance. On the other hand, the size of the image in MWDH can be controlled and made independent of the wavelength used to record it, in order to permit a perfect superposition. In particular, N was increased by padding zeros, taking into account that the following relationship is assumed to hold:

$$N_2 \approx N_1 \left(\frac{\lambda_2}{\lambda_1}\right).$$
 (21)

A group of images were obtained with the two wavelengths shown in Fig. 16. They were converted into the same size using (21) and fused afterwards using a six-level decomposition scheme and Haar wavelets.

Fig. 16(a) shows an RGB image of a matrioshka doll used in the experiments. Fig. 16(b) shows the fused holographic image observed when only the red or green image is considered. Fig. 16(c) shows the reconstructed color holographic image of the matrioshka doll obtained when summing the two reconstructed images. Fig. 16(c) shows low contrast quality due to the speckle contrast. A second group of images was obtained by applying a 1-pixel vertical and horizontal shift to the previous group. These two groups were subsequently fused separately and finally combined into one image, using weighted averaging. A twofold weight was given to the high-frequency components, in order to obtain



(a)







Fig. 16. Experimental holographic fusion results. (a) Original RGB image of a matrioshka doll. (b) Holographic image of red and green images fused using the MWD procedure. (c) Color holographic reconstruction obtained by summing RGB composed images with λ_1 = 632.8 nm and λ_2 = 532.0 nm. (d) Fused image reconstruction. (e) Fused reconstruction after the application of the mean filter. (f) Mean-filtering result of (c) (originally from [102]).

speckle-free images. Fig. 16(d) shows the results of the weighted average fusion. The contrast improves in this case. Fig. 16(e) shows the result of the application of a 3×3 mean filter, before the fusion step. This strategy shows better results than simply summing the filtered images, taking into account that no fusion operation was applied [Fig. 16(f)].

B. Multidimensional Optical Sensor and **Imaging System**

Three-dimensional imaging systems allow us to obtain 3-D information about a scene. On the other hand, the use (integration) of information such as spectral and polarization features may also be useful for object recognition, image fusion, etc. In this section, we briefly summarize some of the fusion results obtained with the multidimensional optical sensor and imaging system (MOSIS) presented in [103]. Fig. 17 shows a scheme of the proposed MOSIS system. This system uses the moving array lenslet technique (MALT) to increase the reconstructed image resolution [104]. This technique allows to increase the spatial sampling rate of the acquired scene by moving the lenslet within one pitch of the lenslet. In particular,



Fig. 17. Scheme of the MOSIS system with three multispectral, polarimetric, and MALT resolution capabilities (adapted from [103]).

the pickup lenslet array and the display lenslet array move synchronously with a predetermined speed in a plane that is perpendicular to the optical axis. A group of elemental image sets are recorded. These sets are integrated in the time domain afterwards, by displaying them on the spatial light modulator (SLM) or LCD at the same sampling speed of the elemental images in the pickup procedure. In computational MALT [105], the 3-D scene is reconstructed computationally with a synthesized virtual pinhole array taking into account the assessed position and intensity of the inversely mapped elemental images.

Fusion of integral images is made using wavelet decomposition. The registered images are transformed into a six-level decomposition. In the same way, as described in Section VI-A, the weighted sum fusion rule is used to fuse the high-frequency and low-frequency parts of the multiresolution wavelet coefficients. Afterwards, the corresponding fused multiresolution wavelet coefficients are inverse wavelet transformed to generate the final fused image. The MOSIS system also allows to do 3-D polarimetric imaging. A 3-D object is illuminated by linearly polarized light and the reflected light propagates through a lenslet array, and a rotating linear analyzer forms the elemental images, which are acquired afterwards by an image sensor. The Jones vector of elliptically polarized light was subsequently obtained using a rotating linear polarizer–analyzer. On the other hand, multiwavelength information in the visible and near-infrared (NIR) range was obtained using light sources and pass-band filters (at sensor level) in the visible and NIR ranges. The visible and NIR images were finally fused/combined simultaneously to the 3-D reconstruction.

1) Polarimetric 3-D Image Sensing and Reconstruction: Fig. 18(a)–(c) shows a die illuminated with a halogen lamp, with two orthogonally polarized sheets attached on each face. The arrows give information about the orientation of the linear analyzer–polarizer. The reflected light from the die impinged on a lenslet array. A liquid-crystal spatial light modulator (LC–SLM) in between orthogonal linear polarizers was used to change the visual characteristics of the elemental images. Additionally, the elemental images were changed to reconstruct the 3-D scene with different polarization states. In order to reconstruct the 3-D image, a polarizer and a lenslet array are placed in front of the LCD. Fig. 18(d)-(f) shows the reconstructed 3-D object with three polarization states: $\{0^{\circ}, 90^{\circ}, 45^{\circ}\}$.

2) Multidimensional Image Sensing: A scene formed by a heart-shaped object and two dice is used in the experiments.



Fig. 18. Die with orthogonally polarized sheets attached to each side. Images were acquired when changing the polarization direction of the linear analyzer-polarizer: (a) vertically, (b) horizontally, and (c) diagonally. The reconstructed 3-D object for the case when the polarization direction of the linear analyzer-polarizer was (d) vertical and viewed from left, (e) horizontal and viewed from the right, and (f) diagonal and viewed from the center (adapted from [103]).

The pickup microlens array is located in front of the objects in order to form the elemental images. The distance between the front face of the die and the pickup microlens array is 19 mm, and the distance between the heart-shaped object and the pickup microlens array is 31 mm. A 4-megapixels 10-b CCD camera acquires the scene. The microlens array is composed of 53 \times 53 square refractive microlenses (each one with a focal length of 3.3 mm) in a 55-mm square area. The size of each captured elemental image is 54 \times 54 pixels. A 0° oriented polarizing sheet is used to cover the left face of the large die and a 90° oriented polarizing sheet is



Fig. 19. Elemental images with different combinations of illumination: (a) a die illuminated by NIR light and captured by a CCD camera with an NIR pass filter; (b) a heart-shaped object illuminated by visible light and captured by a CCD camera with a visible band pass filter; (c) the left face of a die with a 0° polarized sheet and acquired by a CCD camera with a 0° polarizer; (d) the right face of a die with a 90° polarized sheet and captured by a CCD camera with a 90° polarizer (adapted from [103]).

used to cover the right face. A visible pass and an IR pass filter with their corresponding visible and IR light sources are used to record the scene. Another polarizer was used in front of the CCD sensor. When the larger die is sensed, the small die and the heart-shaped object are covered with a polarizing sheet accordingly so that they are not detected.

3) Three-Dimensional Image Fusion of Multidimensional Data: The filters in front of the objects and the CCD camera make the objects to be sensed or not depending on the coupling between their spectrum-polarization states. Fig. 19 shows sections of the NIR-light and visible-light illuminated heart-shaped object. The scene also contains a die whose left face has a 0° polarization state and the right face has a 90° polarization state. The number of elemental images is 46 × 19 in this case. Because the heart-shaped object is illuminated by visible light, it is not seen in Fig. 19(a), and because the die is illuminated by NIR light, it is not seen in Fig. 19(b). The left and right faces can be



Fig. 20. Reconstructed die considering the elemental images of Fig. 19(a) at a distance of (a) z = 19 mm and (b) z = 31 mm. Reconstructed heart-shaped object image considering the elemental images that appear in Fig. 19(b) at a distance of (c) z = 19 mm and (d) z = 31 mm. Reconstructed left face of a dice from the elemental images in Fig. 19(c) at a distance of (e) z = 19 mm and (f) z = 31 mm. Reconstructed right face of a dice from the elemental images in Fig. 19(d) at distance of (g) z = 19 mm and (h) z = 31 mm. Reconstructed image from the fused elemental images at a distance of (i) z = 19 mm and (j) z = 31 mm (adapted from [103]). seen in Fig. 19(c) and (d), respectively. The reconstructions at a depth of 19 and 31 mm from the elemental image in Fig. 19(a) are shown in Fig. 20(a) and (b), respectively. We can see that the die in Fig. 20(a) is in focus, whereas it is out of focus in Fig. 20(b). The reconstructions of the heart-shaped object images at 19 and 31 mm from the elemental image in Fig. 19(b) are shown in Fig. 20(c) and (d), respectively. The reconstructed left faces (where a 0° polarized sheet has been attached to it) of the larger die at 19 and 31 mm from the elemental image in Fig. 20(e) and (f), respectively.

The reconstructed right faces at 19 and 31 mm, for the larger die, when a 90° polarized sheet has been attached to it [from the elemental image in Fig. 19(d)] are shown in Fig. 20(g) and (h), respectively. Images shown in Fig. 20 were normalized for visualization purposes.

Six levels of wavelet decomposition with the Haar wavelet were used, and a weighted averaging operation was applied to the decomposed high- and low-frequency components as the fusion rule. The fusion process was performed on the 2-D elemental images, and the 3-D volume was reconstructed from them. Fig. 20(i) and (j) shows these reconstructed 3-D images. With the 3-D multidimensional fusion technique, we are able to improve the image details which are not visible in the output of other sensors.

VII. CONCLUSION

In this paper, we have presented an overview and some new results of fusion approaches applied to 3-D data obtained by 3-D imaging based on combining other sources of information, such as polarimetry and multispectral imaging, with integral imaging and digital holographic systems. In addition, the use of fusion algorithms for visualization improvement of 3-D data obtained under extremely low light illumination conditions was discussed. We have shown that fusion may result in visualization and reconstruction improvement under different acquisition conditions and visualization purposes. There is a wide variety of applications of these multiple degrees of freedom for 3-D systems ranging from healthcare, military, security, displays, entertainment, manufacturing, and night vision. The readers are referred to the references for some of these applications.

As is the case with any overview article of this nature, it has not been possible to present an exhaustive coverage of the entire fields of 3-D imaging, multimodal imaging, or fusion in this paper. Therefore, we may have inadvertently overlooked some relevant work or we did not have the scope to cover them all. We have included a number of references [35]–[105], some of which are overview articles [33], [35], [36], [38], [46], [54], to aid the readers with various aspects of these fields.

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