Three-dimensional wake transition for a circular cylinder near a moving wall

HONGYI JIANG^{1,2}, LIANG CHENG^{1,2†}, SCOTT DRAPER^{2,3} and HONGWEI AN²

¹DUT-UWA Joint Research Centre, State Key Laboratory of Coastal and Offshore Engineering, Dalian University of Technology, Dalian, 116024, China

²School of Civil, Environmental and Mining Engineering, The University of Western Australia, 35 Stirling Highway, Crawley, WA 6009, Australia

³Centre for Offshore Foundation Systems, The University of Western Australia, 35 Stirling Highway, Crawley, WA 6009, Australia

Abstract

Three-dimensional (3D) wake transition for a circular cylinder placed near to a moving wall is investigated using direct numerical simulation (DNS). The study covers a parameter space spanning a gap ratio $(G/D) \ge 0.3$ and Reynolds number (Re)up to 325. The wake transition regimes in the parameter space are mapped out. It is found that vortex dislocation associated with Mode A is completely suppressed at G/D smaller than approximately 1.0. The suppression of vortex dislocation is believed to be due to the confinement of the Mode A streamwise vortices by the plane wall, which suppresses the excess growth and local dislocation of any Mode A vortex loop. Detailed wake transition is examined at G/D = 0.4 where the wake transition sequence is "two-dimensional (2D) \rightarrow ordered Mode A \rightarrow mode swapping (without dislocations) \rightarrow Mode B". Relatively strong three-dimensionality is found at Re = 160- 220 as the wake is dominated by large-scale structure of ordered Mode A, and also at $Re \ge 285$ where Mode B becomes increasingly disordered. A local reduction in three-dimensionality is observed at Re = 225 - 275 where the wake is dominated by finer-scale structure of a mixture of ordered Modes A and B. Corresponding variations in the vortex shedding frequency and hydrodynamic forces are also investigated.

[†]Email address for correspondence: liang.cheng@uwa.edu.au

1. Introduction

Steady incoming flow past a circular cylinder in close proximity to a plane boundary has been studied extensively due to its fundamental and practical significance. For example, in practical scenarios the plane boundary may be representative of the "seabed" or "ground" involving bluff bodies such as pipelines. In this arrangement, the flow is governed by two dimensionless parameters, i.e. the Reynolds number and the gap-to-diameter ratio (referred to as the gap ratio hereafter). The Reynolds number Re = UD/v is defined based on the approaching flow velocity U, the cylinder diameter D and the kinematic viscosity of the fluid v. The gap ratio is defined as G/D, where G is the gap height between the cylinder and plane boundary.

In addition to the dependence on Re and G/D, the flow in the neighbourhood of the cylinder is complicated further by the development of the boundary layer near the plane boundary. For different boundary layer profiles, extensive experimental studies have revealed that vortex shedding is suppressed at $G/D < \sim 0.3$ for Re in the sub-critical regime ranging from 1.2×10³ to 2.5×10⁴ (e.g. Bearman and Zdravkovich, 1978; Grass et al., 1984; Lei et al., 1999; Price et al., 2002; Wang and Tan, 2008). Based on a two-dimensional (2D) direct numerical simulation (DNS) which employed the Blasius boundary layer profile at the inlet, Lei et al. (2000) found that at lower Re the critical G/D for vortex shedding suppression was 0.2 at $Re \ge 800$ (with a boundary layer thickness δ/D at the location of the cylinder of approximately 0.5), but increased to 0.6 at $Re = 200 \ (\delta/D = 0.9)$ and 1.0 at $Re = 100 \ (\delta/D = 1.2)$. In each of these scenarios the boundary layer varied with Re. Thapa et al. (2014) studied the three-dimensional (3D) flow structure at Re = 500 and both G/D = 0.4 and 0.8 by adopting the logarithmic law of wall for the inlet flow profile, and found that the streamwise vortices (a representation of the flow three-dimensionality) were much weaker than those for an isolated cylinder. However, it is worth noting that even by adopting the Blasius profile or logarithmic profile at the inlet, the boundary layer profile may still develop with distance from the inlet (even with the cylinder removed from the flow field). In other words, the boundary layer profile at the location of the cylinder is dependent on the streamwise location of the cylinder.

Since the above results of flow past a circular cylinder near a plane boundary are dependent on not only Re and G/D, but also the boundary layer profile at the location of the cylinder, the parameter space for numerical simulations is large. To isolate the "near-wall effect" (which is dependent on Re and G/D only) from the additional influence of the upstream boundary layer, the present study focuses on the case that the plane boundary moves at the same speed as the upstream flow (or equally that the body is moved in still fluid parallel to a stationary boundary).

Several past studies have focused on the flow past a circular cylinder near a moving wall (or equally that the cylinder is moved in still fluid near a stationary wall). For example, by towing a circular cylinder close to a stationary wall at Re = 170(Taneda, 1965) and Re = 3550 (Zdravkovich, 1985), Taneda (1965) and Zdravkovich (1985) observed alternate vortex shedding at G/D = 0.6, whereas only a single row of vortices was developed at G/D = 0.1. Huang and Sung (2007) performed 2D DNS for a circular cylinder near a moving wall for $G/D \ge 0.1$ and Re = 200 - 500, and reported variations of the pressure and force coefficients with G/D and Re. They also reported that at Re = 300 alternate vortex shedding was suppressed for $G/D \le 0.28$, and a single vortex row at the upper side of the cylinder dominated the flow for $G/D \le 0.28$. Yoon et al. (2010) carried out 2D DNS for $G/D \ge 0.1$ and Re = 60 - 200, and investigated variations of the pressure and force coefficients with G/D and Re. Rao et al. (2013) showed that while the 2D unsteady wake at larger G/D is characterised by the formation of the classical Kármán vortex streets, vortex shedding at smaller G/D (e.g. G/D = 0.1 or 0.01) is characterised by the pairing of the negatively signed separating shear layer from the top of the cylinder and the positively signed vortex from the boundary layer at the wall. It has been revealed from the above studies that without the boundary layer effect vortex shedding can be observed at a G/D of as low as 0.1. Rao et al. (2013, 2015) and Jiang et al. (2017) found that the onset point of vortex shedding (denoted as Re_{cr2D}) increases monotonically as G/D decreases from ∞ to 0.1. Jiang et al. (2017) also investigated the physical mechanisms responsible for the variations of the Re_{cr2D} and hydrodynamic forces, on the basis of the flow

characteristics at different G/D and Re.

The variation of the critical Re for 3D wake instability (denoted as Re_{cr3D}) with G/D has been predicted by Rao et al. (2013, 2015) and Jiang et al. (2017) through linear stability analysis and 3D DNS, respectively. For $G/D \le 0.22$, the flow undergoes a transition sequence of "2D steady \rightarrow 3D steady \rightarrow 3D unsteady" (Stewart et al., 2010; Rao et al., 2013, 2015; Jiang et al., 2017), and the 3D flow structures have been analysed by Stewart et al. (2010) and Rao et al. (2013) at G/D = 0.005 and by Jiang et al. (2017) at G/D = 0.2. Jiang et al. (2017) found that the 3D steady and 3D unsteady flows at G/D = 0.2 and Re up to at least 200 are triggered by Mode C instability due to a small gap ratio. However, the Mode C structure is not sustained indefinitely, since interference with the shear layer caused by the moving wall leads to other 3D flow structures (Jiang et al., 2017).

On the other hand, for $G/D \ge 0.3$, the flow undergoes a transition sequence of "2D steady \rightarrow 2D unsteady" (Rao et al., 2013, 2015), in line with the transition sequence for an isolated cylinder reported by Williamson (1996). Rao et al. (2015), through a linear stability analysis, found a Mode A instability at Re_{cr3D} , followed by a Mode B instability at a higher Re level. However, the unstable 3D modes discovered from linear stability analysis are based on a 2D base flow, without taking into account the non-linear interactions between the unstable modes (Henderson, 1997). For example, for the case of an isolated cylinder, the onset point for Mode B instability obtained by Barkley and Henderson (1996) through linear stability analysis was Re = 259, whereas the actual Mode B structure was observed in physical experiments at an Re of as low as 230 (Williamson, 1996).

In light of the previous works, the primary aim of the present study is to examine the 3D wake transition and interactions of the 3D wake modes for flow past a circular cylinder near a moving wall with $G/D \ge 0.3$. This is achieved using 3D DNS. The wake flow is compared with the wake transition process and the characteristics of the well-known Mode A and Mode B structures observed for an isolated cylinder.

The rest of this paper is organized in the following manner. In § 2, the governing equations and the numerical model are presented. The wake transition regimes in the

parameter space of $G/D \ge 0.3$ and $Re \le 300$ are presented in § 3.1. The flow structures and wake transition at G/D = 0.4 (where vortex dislocation is suppressed) with varying Re are examined in § 3.2, and the flow structures at Re = 200 with varying G/D are examined in § 3.3. Finally, major conclusions are drawn in § 4.

2. Numerical model

2.1. Numerical method

Numerical simulations have been carried out with OpenFOAM (www.openfoam.org) to solve the continuity and incompressible Navier-Stokes equations:

$$\frac{\partial u_i}{\partial x_i} = 0 \tag{2.1}$$

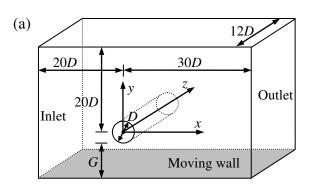
$$\frac{\partial u_i}{\partial t} + u_j \frac{\partial u_i}{\partial x_j} = -\frac{1}{\rho} \frac{\partial p}{\partial x_i} + v \frac{\partial^2 u_i}{\partial x_j \partial x_j}$$
(2.2)

where $(x_1, x_2, x_3) = (x, y, z)$ are Cartesian coordinates, u_i is the velocity component in the direction x_i , t is time, ρ is fluid density, and p is pressure. The same numerical approach used in Jiang et al. (2016, 2017) is adopted here. Specifically, the Finite Volume Method (FVM) and the Pressure Implicit with Splitting of Operators (PISO) algorithm (Issa, 1986) are used to solve the equations. The convection, diffusion and time derivative terms are discretized, respectively, using a fourth-order cubic scheme, a second-order linear scheme, and a blended scheme consisting of the second-order Crank-Nicolson scheme and a first-order Euler implicit scheme.

2.2. Computational domain and mesh

The computational domain and mesh are determined based on a domain size dependence study carried out in Jiang et al. (2016) and a mesh resolution dependence study carried out in Jiang et al. (2017). The standard 3D mesh reported in Jiang et al. (2017) is adopted in this study.

The details of the standard 3D mesh are as follows. As shown in Fig. 1(a), a hexahedral computational domain of $(L_x, L_y, L_z) = (50D, G + 20.5D, 12D)$, with L_x, L_y , and L_z being the domain sizes in the x-, y-, and z-directions, respectively, is constructed. The gap height G is varied in this study. In the x-y plane (the plane perpendicular to the cylinder axis), the cylinder perimeter is discretized with 132 nodes for $G/D \ge 1.5$ and 160 nodes for $G/D \le 1.5$ (due to the slight change of the mesh topology at smaller gap ratios). The height of the first layer of mesh next to the moving wall and next to the cylinder surface is approximately 0.001D. The cell expansion ratio in the whole domain is kept below 1.1. This results in at least 30 layers of mesh in the cylinder boundary layer for all of the cases considered in this study. To capture detailed wake flow structures, a relatively high mesh resolution is used in the cylinder wake by specifying a constant mesh size along the x-direction for x/D > 0.7. Fig. 1(b) shows a close-up view of the 2D mesh near the cylinder with a gap ratio of 0.4.



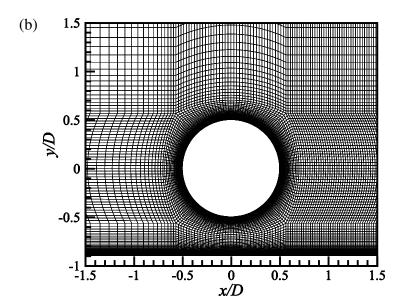


Fig. 1. (a) Schematic model of the computational domain, and (b) Close-up view of the 2D mesh near the cylinder for G/D = 0.4.

The 3D mesh is formed by replicating the 2D mesh along the z-axis, resulting in an identical mesh resolution in all planes perpendicular to the cylinder. Based on the 3D mesh dependence study for an isolated cylinder performed in Jiang et al. (2016), the spanwise cell and domain lengths are chosen as 0.1D and 12D, respectively. According to the linear stability analysis results by Rao et al. (2013) of flow past a circular cylinder near a moving wall with various gap ratios, the spanwise domain length of 12D is not always an integer multiple of the most unstable spanwise wavelength of the wake structure. This may restrict the development of 3D instability to some extent and result in an over-prediction of Re_{cr3D} . However, it has been demonstrated in Jiang et al. (2017) that the use of a spanwise domain length of 12D would only affect the accuracy of the predicted Re_{cr3D} value by less than 1%. Hence a uniform domain length of 12D is still adopted in the present study.

The boundary conditions for the 3D computational domain are listed in Table 1, where $\partial/\partial \mathbf{n} = 0$ denotes a zero normal gradient condition. In particular, a uniform flow velocity U is specified in the x-direction for the inlet and bottom boundaries. Symmetry boundary conditions are applied at the top boundary, while periodic boundary conditions are employed at the two lateral boundaries perpendicular to the

cylinder span.

Table 1. Boundary conditions for the 3D computational domain.

Boundary	Velocity components	Pressure
Inlet	$u_x = U, u_y = u_z = 0$	$\partial p/\partial \mathbf{n} = 0$
Outlet	$\partial u_i/\partial \mathbf{n} = 0$	p = 0
Тор	$\partial u_x/\partial \mathbf{n} = \partial u_z/\partial \mathbf{n} = 0, u_y = 0$	$\partial p/\partial \mathbf{n} = 0$
Bottom	$u_x = U, u_y = u_z = 0$	$\partial p/\partial \mathbf{n} = 0$
Front and back	$u_i(x, y, z = 0, t) = u_i(x, y, z = L_z, t),$	$p(x, y, z = 0, t) = p(x, y, z = L_z, t),$
	$\partial u_i/\partial \mathbf{n}(x, y, z = 0, t) = \partial u_i/\partial \mathbf{n}(x, y, t)$	$\partial p/\partial \mathbf{n}(x, y, z = 0, t) = \partial p/\partial \mathbf{n}(x, y, z)$
	$z = L_z, t)$	$=L_z,t)$
Cylinder surface	$u_i = 0$	$\partial p/\partial \mathbf{n} = 0$

The time step Δt adopted for each case is based on the criterion that the Courant number (Co) of all the cells in the computational domain is kept below 0.5, where Co is defined as:

$$Co = |u| \Delta t / \Delta l \tag{2.3}$$

where |u| is the magnitude of the velocity through a cell, and Δl is the cell size in the direction of the velocity.

2.3. Mesh convergence

For the case of flow past an isolated circular cylinder, Jiang et al. (2016) reported a mesh convergence study on the standard 3D mesh, and obtained DNS results of wake transition of flow past an isolated circular cylinder which are in good agreement with the experimental results reported by Williamson (1996).

For the case of flow past a circular cylinder near a moving wall, the Re_{cr2D} and Re_{cr3D} values under various gap ratios predicted with DNS by using the standard 3D mesh (Jiang et al., 2017) are in close agreement with the linear stability analysis results by Rao et al. (2015) (Fig. 2). The results by Rao et al. (2015) are believed to be

improved from those in Rao et al. (2013) (see Fig. 2) since it was noted in Rao et al. (2013) that the use of a relatively small computational domain size in that study could affect the accuracy of Re_{cr3D} by ~ 15%.

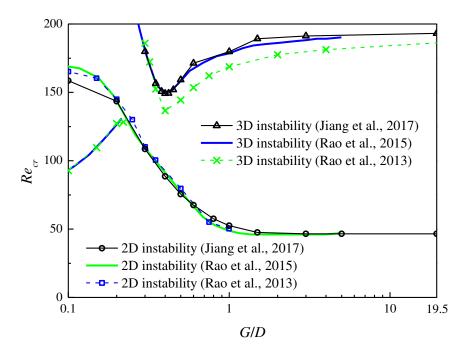


Fig. 2. Critical Re for 2D and 3D wake instabilities under various gap ratios.

In the present study, mesh convergence is further checked at G/D = 0.4 with Re = 325 (the largest Re adopted in this study). The resolution of the standard 3D mesh is examined by using a refined 3D mesh with the number of cells in both x- and y-directions 1.5 times that for the standard 3D mesh. In particular, the number of cells around the cylinder is increased by 1.5 times (from 160 to 240), the height of the first layer of mesh next to the moving wall and next to the cylinder surface is reduced by 1.5 times (from 0.001D to 0.00067D), and the number of mesh layers in the cylinder boundary layer is increased by 1.5 times (from 31 to 47). In addition, the influence of the time step on the numerical results is examined with a case which uses the standard 3D mesh but with a halved time step size (i.e. Co is kept below 0.25).

The mesh convergence is firstly checked via the drag and lift force coefficients $(C_D \text{ and } C_L)$ and Strouhal number (St) on the cylinder, which are defined as follows:

$$C_D = F_D / (\rho D U^2 L_z / 2) \tag{2.4}$$

$$C_L = F_L / (\rho D U^2 L_z / 2)$$
 (2.5)

$$St = f_L D / U (2.6)$$

where F_D and F_L are the integrated drag force and lift force on the cylinder, respectively, and f_L is the frequency of the fluctuating lift force. For the 3D cases where the time-history of C_L may not be regular periodic, St is determined using the peak frequency derived from the fast Fourier transform (FFT) of the time-history of C_L . The time-averaged drag and lift coefficients are denoted as $\overline{C_D}$ and $\overline{C_L}$, respectively. The root-mean-square lift coefficient C_L is defined as:

$$C_{L}' = \sqrt{\frac{1}{N} \sum_{i=1}^{N} \left(C_{L,i} - \overline{C_{L}} \right)^{2}}$$
 (2.7)

where N is the number of values in the time-history of C_L . At least 800 non-dimensional time units (defined as $t^* = Ut/D$) of the fully developed flow are used to calculate the statistical stationary hydrodynamic forces on the cylinder. As shown in Table 2, the hydrodynamic forces calculated with the two variation cases are quite close to those calculated with the standard mesh (relative differences are within 0.7% for St and $\overline{C_D}$, within 1.6% for $\overline{C_L}$, and within 4% for C_L').

Table 2. Mesh convergence results for the case of (G/D, Re) = (0.4, 325).

Case	St	$\overline{C_{\scriptscriptstyle D}}$	$\overline{C_{\scriptscriptstyle L}}$	$C_{\scriptscriptstyle L}{}'$
Standard 3D mesh (reference case)	0.2073	1.5174	0.2233	0.6403
Refined 3D mesh	0.2069	1.5129	0.2268	0.6219
Time step reduced by half	0.2060	1.5069	0.2258	0.6153

In addition, Fig. 3 shows the time- and span-averaged streamwise and transverse velocity profiles at a few streamwise locations in the near wake (x/D = 0, 1, 1.5, and 5) for the three cases listed in Table 2. Very good agreements of the mean velocity profiles are observed in Fig. 3 for the three cases. The above results demonstrate that

the standard 3D mesh is sufficient for the numerical simulations of this study.

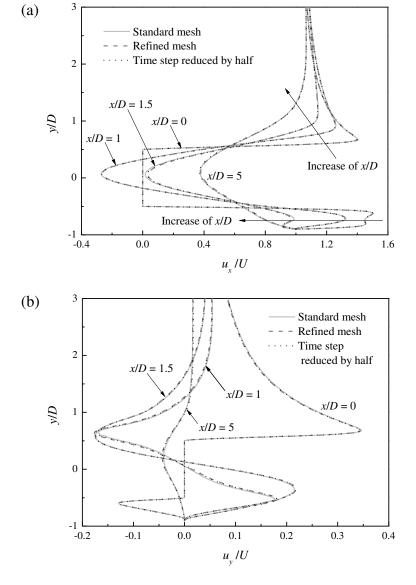


Fig. 3. Time- and span-averaged velocity profiles at a few streamwise locations (x/D = 0, 1, 1.5, and 5) for the three cases listed in Table 2: (a) streamwise velocity profiles, and (b) transverse velocity profiles.

3. Numerical results

For flow past a circular cylinder near a moving wall at $G/D \ge 0.3$, the wake transition sequence of "2D steady \rightarrow 2D unsteady \rightarrow 3D unsteady" has been observed by Rao et al. (2013, 2015) and Jiang et al. (2017) through linear stability analysis and 3D DNS, respectively. In the present study, flow past a circular cylinder near a

moving wall is investigated in the range of $G/D \ge 0.3$ with the focus on the 3D flow structures and wake transition beyond the onset of 3D instability, i.e. in the "3D unsteady" state.

3.1. Wake transition regimes

The 3D wake transition sequence for flow past a circular cylinder near a moving wall is studied in the parameter space of $G/D \ge 0.3$ and Re up to 300. Based on a number of cases with discrete combinations of G/D and Re, the approximate wake transition regimes are mapped out in Fig. 4. With increase of Re, the flow undergoes a transition sequence of "2D \rightarrow Mode A \rightarrow mode swapping \rightarrow Mode B" for all of the gap ratios considered. For $G/D \ge 1.5$, the critical Re values for the wake transition regimes are almost unchanged, which suggests that the effect of the plane boundary is still weak. With further decrease of G/D, the mode swapping and Mode B regimes are gradually delayed to slightly higher Re values.

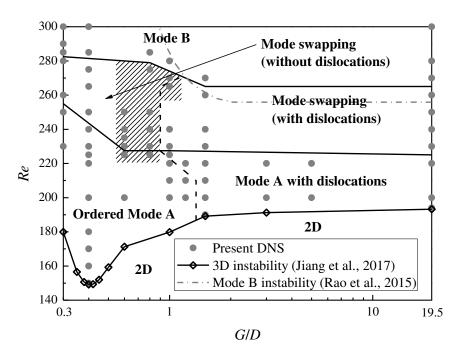


Fig. 4. Wake transition regimes for flow past a circular cylinder near a moving wall. The wake structures are initialized with 4 pairs of Mode A structure along the span width for the cases within the shadow area, and 3 pairs of Mode A for the rest of the cases within the Mode A and mode swapping regimes.

For the case of an isolated circular cylinder, the Mode A structure will evolve spontaneously into a more stable pattern with large-scale vortex dislocations (Williamson, 1996). Hence the transition sequence can be further specified as "2D \rightarrow Mode A with dislocations \rightarrow mode swapping (with dislocations) \rightarrow Mode B". The evolution of vortex dislocations (with the evolution of the non-dimensional flow time t^*) for the case of Re = 200 is illustrated in Fig. 5. The vortex structures are identified by the iso-surfaces of the streamwise vorticity ω_x , which is defined in a non-dimensional form of:

$$\omega_{x} = \left(\frac{\partial u_{z}}{\partial y} - \frac{\partial u_{y}}{\partial z}\right) \frac{D}{U} \tag{3.1}$$

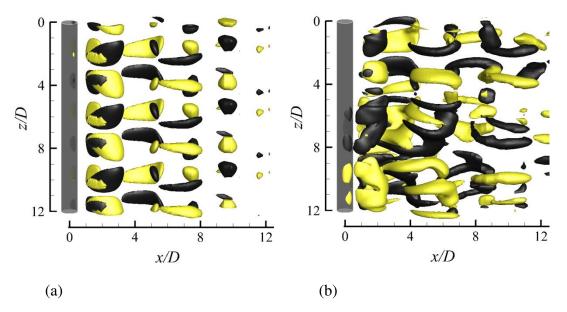


Fig. 5. Iso-surfaces of $\omega_x = \pm 0.5$ for flow past an isolated circular cylinder at Re = 200: (a) ordered Mode A structure at $t^* = 400$, and (b) Mode A with large-scale vortex dislocations at $t^* = 1000$. Dark grey and light yellow denote positive and negative values, respectively. The flow is from the left to the right past the cylinder on the left.

However, it is found that for flow past a circular cylinder near a moving wall, vortex dislocation is suppressed at small gap ratios, and consequently the flow undergoes a transition sequence of "2D \rightarrow ordered Mode A \rightarrow mode swapping

(without dislocations) \rightarrow Mode B". According to the occurrence or suppression of vortex dislocations associated with Mode A, the Mode A and mode swapping regimes shown in Fig. 4 are further separated by the dashed line at $G/D \sim 1.0$. The dashed separation line ends at the lower boundary of the Mode B regime, since beyond which point Mode A disappears and Mode B is naturally free of dislocation.

It is seen in Fig. 4 that the ordered Mode A regime occupies a considerable area in the parameter space. To further validate the suppression of vortex dislocation in the ordered Mode A regime, another DNS case with (G/D, Re) = (1.0, 210) is calculated with a doubled spanwise domain length of 24D. In this case, vortex dislocation is still completely suppressed. For the fully developed flow, six Mode A vortex pairs are observed along the span width, and their spanwise locations do not vary along the span in time (although the Mode A vortex pairs have slightly varied wavelengths).

It is also found that for the cases within the shadow area shown in Fig. 4, the wake structures are initialized with four pairs of Mode A structure along the span width. In contrast, for the rest of the cases within the Mode A and mode swapping regimes, three pairs of Mode A structure are observed at the beginning of the simulations. This is due to the variation of the most unstable spanwise wavelength of the Mode A structure. As reported by Rao et al. (2013) with linear stability analysis, the most unstable spanwise wavelength at Re_{cr3D} for G/D = 0.4 and 1.0 are 3.85D and 3.73D, respectively, but reduces to ~ 3.65D at G/D = 0.5 - 0.75. In addition, it is expected that the most unstable wavelength decreases with increase of Re, similar to the case of an isolated cylinder as reported in Williamson (1996) and Barkley and Henderson (1996). Hence it is expected that smallest most unstable wavelengths may be observed for the cases within the shadow area, and for these cases the wavelength of 3D (i.e. four pairs of Mode A) is more unstable than 4D (i.e. three pairs of Mode A).

It is worth noting that while the onset points for 3D instability obtained by Rao et al. (2015) and Jiang et al. (2017) agree well with each other (Fig. 2), it is apparent that the regime for Mode B instability obtained by Rao et al. (2015) through linear stability analysis does not coincide with either the mode swapping regime or the

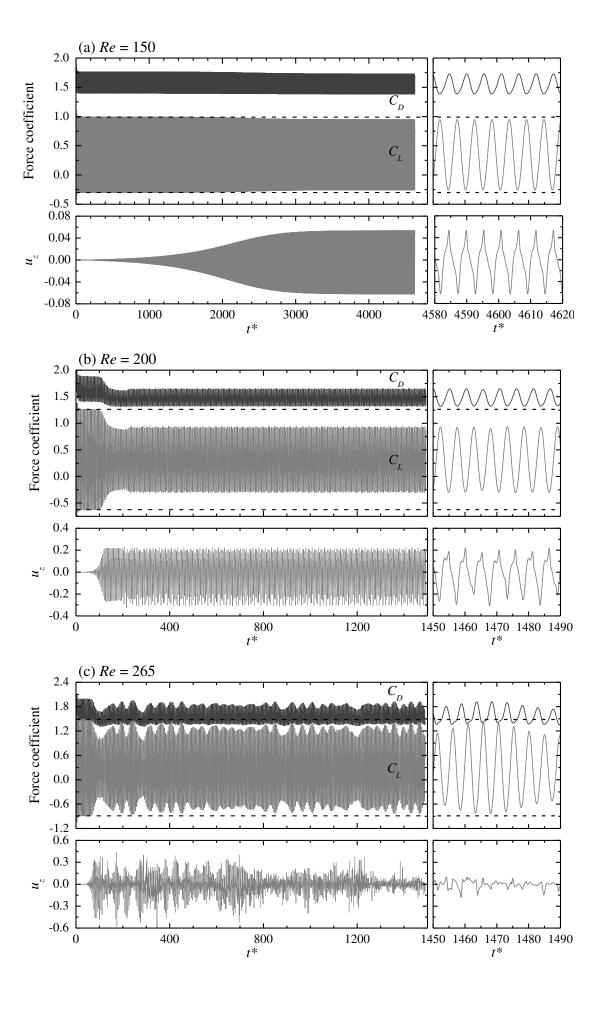
Mode B regime determined by the present DNS (Fig. 4), since the existence of Mode A instability would destabilize Mode B in the non-linear interaction between the two modes (Henderson, 1997). Hence a non-linear DNS study is required for the simulation of the actual wake transition process at $Re > Re_{cr3D}$.

3.2. Results at G/D = 0.4 with varying Re

Based on the standard 3D mesh, a series of 3D cases is simulated at a fixed gap ratio of G/D = 0.4 where vortex dislocation is suppressed (Fig. 4). As shown in Fig. 2, the 2D and 3D wake instabilities occur at $Re_{cr2D} = 88.5$ (± 0.5) and $Re_{cr3D} = 149.2$, respectively. In this section, the wake structures and transition for G/D = 0.4 are examined with Re ranging from 80 to 325, covering the laminar and 3D wake transition regimes. The general conclusions drawn through G/D = 0.4 are expected to be applicable to a range of gap ratios from 0.3 to 0.8 where the flow undergoes a transition sequence of "2D \rightarrow ordered Mode A \rightarrow mode swapping (without dislocations) \rightarrow Mode B" (Fig. 4). On the other hand, the transition sequence of "2D \rightarrow Mode A with dislocations \rightarrow mode swapping (with dislocations) \rightarrow Mode B" for $G/D \ge 1.5$ (Fig. 4) is expected to be similar to that of an isolated cylinder and therefore will not be elaborated in this study.

3.2.1. 3D wake transition

Fig. 6 shows the time-histories of the span-averaged drag and lift coefficients, as well as the point spanwise velocity sampled at (x/D, y/D, z/D) = (3.0, 0.5, 6.0) for G/D = 0.4 with various Re. In Fig. 6, the left column shows the entire ranges of the time-histories, while the right column shows the time-histories of 40 non-dimensional time units of the fully developed flow close to the end of each simulation.



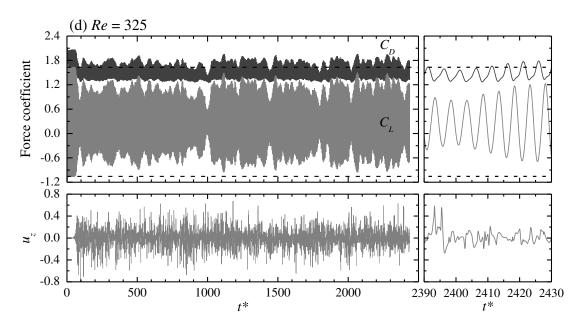


Fig. 6. Time-histories of the span-averaged drag and lift coefficients, as well as the point spanwise velocity sampled at (x/D, y/D, z/D) = (3.0, 0.5, 6.0) for G/D = 0.4 with various Re. The horizontal dashed lines mark the fluctuation range of the corresponding 2D lift coefficient.

For $Re > Re_{cr3D}$ (= 149.2), an exponential growth of the spanwise velocity amplitude is observed at the very beginning of each time-history shown in Fig. 6, marking the development of 3D wake instability. As illustrated in Jiang et al. (2017), the Re_{cr3D} value can be obtained from the linear relationship between the exponential growth rate and Re, through interpolation at the zero growth rate point. For $Re > Re_{cr3D}$, the growth rate of the spanwise velocity amplitude increases with increasing Re, and therefore the growing period becomes shorter and the flow saturates more quickly (Fig. 6).

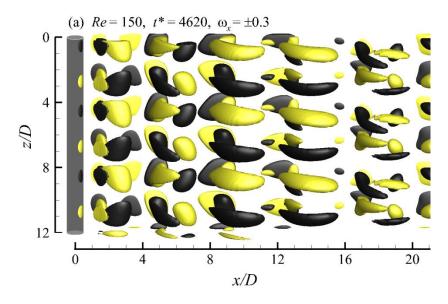
At the beginning of each simulation, the flow three-dimensionality in the computational domain is zero. Hence the time-history of the spanwise velocity shown in Fig. 6 grows from $u_z = 0$, and the fluctuation ranges of the drag and lift coefficients calculated by 3D DNS are identical to their 2D counterparts (the fluctuation ranges of the 2D lift coefficient are marked by the horizontal dashed lines in Fig. 6). With growth of the flow three-dimensionality, the spanwise velocity amplitude increases, and the 3D drag coefficient and fluctuation amplitude of the 3D lift coefficient drop

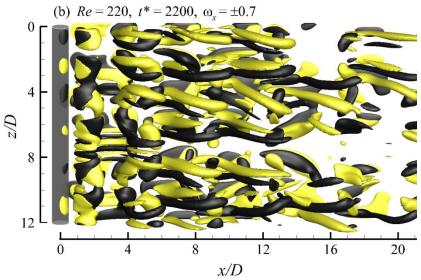
from their 2D counterparts. The drops in the drag coefficient and fluctuation amplitude of lift coefficient are barely visible when the spanwise velocity amplitude is within an order of magnitude of 0.01U, but become apparent when the spanwise velocity amplitude grows beyond $\sim 0.1U$ (Fig. 6).

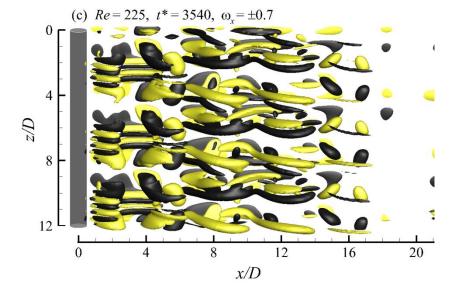
The vortex structures during the 3D wake transition process are examined through numerical flow visualization. At a small gap ratio of 0.4, a major difference compared with the case of an isolated cylinder is that vortex dislocation is completely suppressed. This also results in relatively regular time-histories of the force coefficients and point velocity signals (whereas irregular and large-amplitude fluctuations of the time-histories are observed when vortex dislocations are present). Table 3 summarizes the observed patterns of the time-histories of the force coefficients and point velocity signals (some are shown in Fig. 6) and fully developed vortex structures represented by the iso-surfaces of the streamwise vorticity ω_x (some are shown in Fig. 7).

Table 3. Patterns of the time-histories and fully developed vortex structures for G/D = 0.4 with $Re > Re_{cr3D}$.

Re	Time-histories	Fully developed vortex structure	
150 – 180	extremely regular	Three pairs of ordered Mode A (without Mode B)	
200		Three pairs of	loops occasionally occupied by Mode B
220	relatively regular	ordered Mode <	one particular loop filled with Mode B
225 - 240		A with	all of the three loops filled with Mode B
250 – 275	irregular	Swapping between ordered Mode A and Mode B	
285 - 325	more irregular	Mostly disordered Mode B	







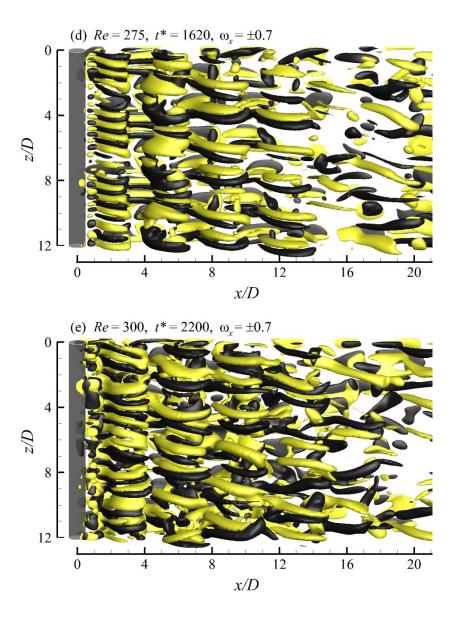


Fig. 7. Iso-surfaces of ω_x for the cases with G/D = 0.4 and $Re > Re_{cr3D}$. Dark grey and light yellow denote positive and negative values, respectively. The flow is from the left to the right past the cylinder on the left. The moving wall is at the back of the structure.

For Re between 150 and 180, three ordered Mode A streamwise vortex pairs (e.g. Fig. 7(a)) are observed along the cylinder span for the entire simulations. The basic features of the Mode A structure for the near wall case, e.g. the waviness of the primary vortex cores, an out-of-phase pattern for the streamwise vortices, and a spanwise wavelength of approximately 4D, are similar to those for an isolated

cylinder, which suggests that the physical mechanism for the formation of Mode A instability for the near wall case is similar to that for an isolated cylinder, i.e. an elliptic instability of the primary vortex cores and the formation of streamwise vortex pairs through the Biot-Savart induction (Williamson, 1996; Leweke and Williamson, 1998; Thompson et al., 2001). In this *Re* range, even the time-history of the point spanwise velocity (e.g. Fig. 6(a)) is extremely regular, which suggests that the wake structure is highly repeatable in time. In particular, with the absence of vortex dislocation, the Mode A vortices do not vary along the cylinder span in time, since the formation of Mode A is self-sustaining through the Biot-Savart induction (Williamson, 1996).

As Re exceeds 200, the ordered Mode A structure remains unchanged while ordered Mode B structure starts to develop within the Mode A vortex loops. For Re = 220, one of the three loops (the loop at $z/D \sim 7.5$ in Fig. 7(b)) is persistently filled with the ordered Mode B structure. For Re = 225 – 240, all of the three Mode A vortex loops are filled with ordered Mode B structure throughout (e.g. Fig. 7(c)). Since all of the Mode A structures are still persistent with the evolution in time, they still do not vary along the span width. The persistent existence of three ordered Mode A streamwise vortex pairs for Re = 200 – 240 is responsible for the relatively regular periodic time-histories of the force coefficients and spanwise velocity (e.g. Fig. 6(b)), while the additional co-existed Mode B structure may add some irregularities to the time-histories.

Due to the existence of Mode A instability which destabilizes Mode B in the non-linear interaction between the two modes (Henderson, 1997), the present DNS results show that the Mode B structure starts to emerge at *Re* of as low as 200, much lower than the lower boundary of the Mode B regime obtained by Rao et al. (2015) through linear stability analysis (Fig. 4). Through numerical flow visualization of the evolution of the wake structure, it is found that the Mode B structure is always initialized within the Mode A vortex loops. Since the physical mechanism for Mode B instability is a hyperbolic instability of the braid shear layer region (Williamson, 1996; Leweke and Williamson, 1998; Thompson et al., 2001), the streamwise vortices of

Mode A that develop in the braid shear layer region are believed to be the reason for the destabilization of Mode B.

A gradual transition from the ordered Mode A structure to relatively ordered Mode B structure is observed at Re = 250 - 275. It should be noted that vortex dislocation is still suppressed, and only ordered Mode A and Mode B structures are observed. In this regime, the Mode B structure fills up not only the areas within the Mode A vortex loops, but can sometimes also replace some or all of the ordered Mode A vortex pairs (e.g. Fig. 7(d)). In Fig. 7(d), 15 pairs of the Mode B structure are observed along the span width at Re = 275, which indicates a spanwise wavelength of Mode B of approximately 0.8D, similar to the wavelength of Mode B for an isolated cylinder of 0.82D (Barkley and Henderson, 1996). It is also worth noting that as the self-sustaining formation of Mode A is interrupted by the replacement of Mode B, the Mode A vortices in the mode swapping regime are no longer fixed at their respective initial spanwise locations. As the mode swapping process sets in, the time-histories of the force coefficients and spanwise velocity become much more irregular (e.g. Fig. 6(c)).

Fig. 8 shows the time-histories of the mode swapping process focusing on the intermittent appearance of the pattern of "all of the three Mode A vortex pairs appear along the span width" (the shadow periods in Fig. 8). The statistics starts after the flow is fully developed and lasts for 1000 to 1150 non-dimensional time units (with an output interval of 10) to ensure that the statistical results are not strongly influenced by the sampling range. For each case, more than 100 snapshots of the wake structure are visually examined. It is seen in Fig. 8 that with increase of *Re*, the durations of the shadow periods become shorter while the durations of the clear periods become longer. Therefore, as can be seen in Fig. 8 and more clearly in Fig. 9, the probability of occurrence of "all of the three Mode A vortex pairs appear along the span width" reduces with increase of *Re*. The probability of occurrence is defined as the ratio of the accumulated time of appearance of the mode being examined to the total sampling time. Assuming that this probability reduces linearly with increase of *Re*, the range of *Re* for the mode swapping process is between 246 and 281 (Fig. 9),

which is slightly higher than the mode swapping regime of Re = 230 - 260 for an isolated cylinder obtained by Jiang et al. (2016) based on the same numerical formulation.

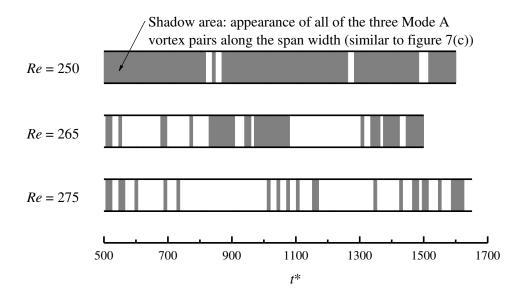


Fig. 8. Time-histories for the appearance of all of the three Mode A vortex pairs along the span width for *Re* in the mode swapping regime.

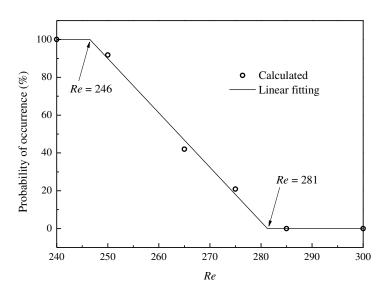


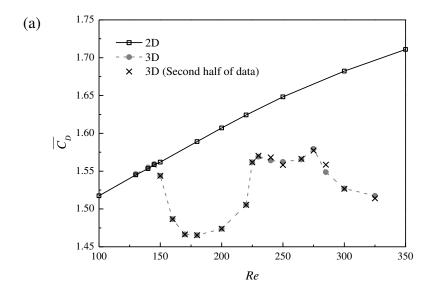
Fig. 9. Variation of the probability of occurrence of "all of the three Mode A vortex pairs appear along the span width" with *Re*.

For $Re \ge 285$, the Mode B structure occupies the entire cylinder span width for

most of the time. Mode A may sometimes be observed in the form of scattered pairs but can no longer occupy the entire span width. With increase of *Re*, the Mode B structure becomes increasingly disordered (e.g. Fig. 7(e)), which is consistent with the even more irregular time-histories of the force coefficients shown in Fig. 6(d).

3.2.2. Hydrodynamic forces and flow three-dimensionality

Fig. 10 shows the variations of the statistically stationary force coefficients with Re. For the cases of $Re \le 220$ with relatively regular time-histories of spanwise velocity and force coefficients, at least 500 non-dimensional time units are used for the statistics. As the time-histories become less regular for $Re \ge 225$, the statistical range is increased to at least 1000 non-dimensional time units. Further confirmation is carried out by calculating the 3D force coefficients using only the second half of the statistical data. It is seen in Fig. 10 that the 3D results calculated using the full length and second half of the data are quite close to each other, which suggests that the statistical data range is sufficient.



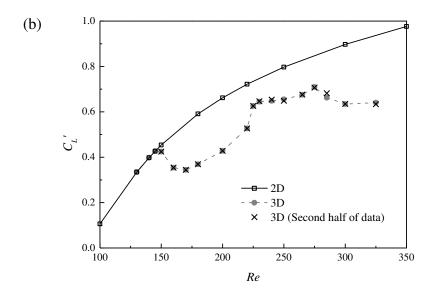


Fig. 10. Variations of the statistically stationary force coefficients with Re: (a) time-averaged drag coefficient $\overline{C_D}$, and (b) root-mean-square lift coefficient C_L .

As shown in Fig. 10, the force coefficient quantities start to deviate from their 2D counterparts at $Re = Re_{cr3D}$. The 3D results are all to the right of the 2D curves, i.e. the 2D simulations can achieve the same mean values and fluctuation amplitudes of the force coefficients at a lower Re compared with the 3D simulations. This suggests that in 3D simulations, part of the energy is transferred to the spanwise direction. The magnitude of the flow three-dimensionality is represented by the degree of deviation between the 2D and 3D results and will be discussed later on. It should be noted that although only the time-averaged drag coefficient and root-mean-square lift coefficient are shown in Fig. 10, the above findings also apply to the time-averaged lift coefficient and root-mean-square drag coefficient (omitted for simplicity).

The variation of the flow three-dimensionality with Re is further examined with the statistically stationary streamwise enstrophy ε_x and spanwise kinetic energy E_z integrated over the near wake region of x/D = 0 - 10 (Fig. 11), where ε_x and E_z are defined as:

$$\varepsilon_{x} = \frac{1}{2} \int_{V} \omega_{x}^{2} dV \tag{3.2}$$

$$E_z = \frac{1}{2} \int_V \left(u_z / U \right)^2 \mathrm{d}V \tag{3.3}$$

where V is the volume of the flow field of interest. The same statistical data ranges as used for obtaining the statistically stationary force coefficients are adopted here for calculating ε_x and E_z . It is seen in Fig. 11 and Fig. 10 that the variation trends of ε_x and E_z are consistent with the degree of deviation between the 2D and 3D force coefficients. At Re = 150 which is just beyond the Re_{cr3D} , the Mode A structure is strongly confined and extremely ordered (Fig. 7(a)), which results in a very weak flow three-dimensionality. A gradual growth of the flow three-dimensionality is observed as Re increases from 150 to 200. Within this range, the wake flow is dominated by the ordered Mode A structure. The growth rate of the flow three-dimensionality reduces at Re = 220 as the finer-scale ordered Mode B structure is observed within one of the Mode A vortex loops (Fig. 7(b)). A local reduction of the flow three-dimensionality is observed in Fig. 11 and Fig. 10 for Re = 225 - 275 as the finer-scale Mode B structure becomes dominant (Fig. 7(c,d)). The ordered Mode B structure is observed within all of the three Mode A vortex loops, and may even occupy the entire span width during the mode swapping process. For Re > 275, although the wake structure is almost fully occupied by Mode B, the Mode B structure becomes increasingly disordered (Fig. 7(e) versus Fig. 7(d)), which is the reason why the flow three-dimensionality experiences a sharp increase. The emergence of increasingly disordered Mode B structure and the corresponding sharp increase of flow three-dimensionality have also been observed for an isolated cylinder (Williamson, 1996; Jiang et al., 2016).

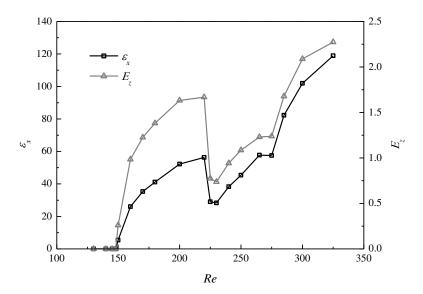


Fig. 11. Variations of the statistically stationary streamwise enstrophy and spanwise kinetic energy integrated over the near wake region of x/D = 0 - 10 with Re.

The hysteresis of the Mode A instability at Re_{cr3D} (= 149.2) is checked by adopting a case with the fully developed Mode A flow at Re = 150 as the initial condition and a slightly reduced Re of 148.5 for the simulation. Based on the examination of the flow three-dimensionality (through ε_x and E_z) in the fully developed flow, hysteresis effect is not detected. In comparison with the case of an isolated circular cylinder which shows a hysteresis effect (Williamson, 1996), the suppression of vortex structures with large three-dimensionality and the absence of convective instability of such large disturbances may be the reasons why a hysteresis effect is not observed in the present case.

Fig. 12 shows the St–Re relationship for G/D = 0.4, together with the results for an isolated cylinder. The sampling data sets are identical to those for obtaining the force coefficients. It is seen in Fig. 12 that while the deviations between the 2D and 3D results for the near wall case are consistent with the deviation trends of the force coefficients (Fig. 10) as well as the streamwise enstrophy and spanwise disturbance energy (Fig. 11), they are quite different from the characteristics for an isolated cylinder. At the onset of 3D wake instability, a gradual deviation of the St values predicted from 2D and 3D simulations is observed for the near wall case, whereas a

sudden drop of St is observed for an isolated cylinder. The gradual and continuous drop of St for the near wall case is consistent with the very weak flow three-dimensionality and very close 2D and 3D results of the force coefficients for Re just above Re_{cr3D} , and is attributed to the extremely ordered (strongly confined) Mode A structure. In contrast, the sudden drop of St for an isolated cylinder is due to the well-developed Mode A structure with large-scale vortex dislocations (Williamson, 1996).

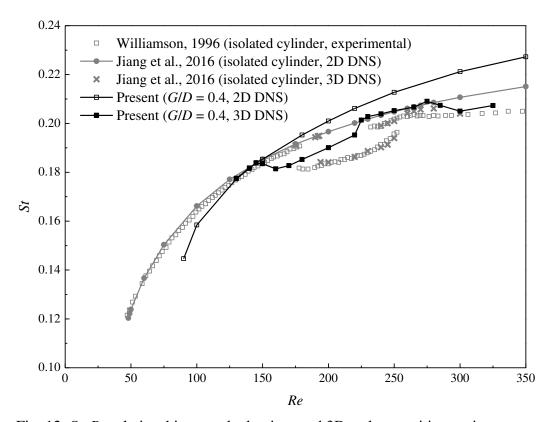


Fig. 12. *St–Re* relationship over the laminar and 3D wake transition regimes.

Another difference in the St–Re relationship shown in Fig. 12 is that for the near wall case only one single vortex shedding frequency peak is observed at each Re for the entire St–Re curve, whereas for the isolated cylinder case two different frequency peaks are observed in the mode swapping regime of approximately Re = 230 - 260. The lower and higher frequency peaks for the isolated cylinder case correspond to Mode A with large-scale dislocations and Mode B, respectively (Williamson, 1996). It is speculated in Williamson (1996) that for an isolated cylinder, if vortex dislocations

do not occur, the St–Re curve would be a single and continuous curve, with each Re corresponding to a single St. However, Henderson (1997) suggested that the lower frequency peak for the isolated cylinder case is due to the Mode A instability only, irrespective of the dislocations. For the present case of a circular cylinder near a moving wall, the mode swapping process does not contain relatively large scale vortex structures of dislocations or even pure Mode A. The finer-scale structure of a mixture of ordered Modes A and B share a single frequency peak. It should be noted that for the 3D DNS study of an isolated cylinder by Jiang et al. (2016) at Re = 270 (just beyond the mode swapping regime), the flow structure is also characterized by a mixture of ordered Modes A and B, and only a single frequency peak is present.

Prior to the mode swapping regime of the near wall case, an obvious increase of St is observed when Re increases from 220 to 225, as the wake structure changes from large-scale-dominant (mainly pure Mode A) to small-scale-dominant (Mode B occupies all of the Mode A loops and may even occupy the entire span width). This seems to support the argument by Henderson (1997) that a lower frequency peak is due to the Mode A structure (large scale structure), whereas vortex dislocation is not a necessity. For the near wall case, large scale structures are observed for the entire simulations of Re = 150 - 220 and finer-scale structures are observed for the entire simulations of Re = 225 - 275. Hence a sudden increase of St is observed at Re = 220 - 225 but only one frequency peak is observed for each case. In contrast, for the mode swapping process of the isolated cylinder case, large scale structure (Mode A with dislocations) and finer-scale structure (a mixture of ordered Modes A and B) occur alternately in the same simulation case (see Jiang et al., 2016). As a result, two different frequency peaks are observed.

While it is demonstrated above that the relatively large scale Mode A structure may be responsible for a lower frequency peak, further support will be given in § 3.3 to show that vortex dislocation may not be the reason for a lower frequency peak.

Fig. 13 shows some of the frequency spectra of C_L which are used to determine St. The amplitude of C_L shown in Fig. 13 is normalized with $1/(\sqrt{2}C_L')$ which is calculated from the same sampling data set. In this way, the normalized amplitude of C_L becomes 1 if the time-history of C_L is sinusoidal with an arbitrary amplitude. Each vertical line under the frequency spectrum shown in Fig. 13 represents a discrete point on the spectrum curve. The spacing between the discrete vertical lines is due to the use of a finite data range of the time-history of C_L for the FFT.

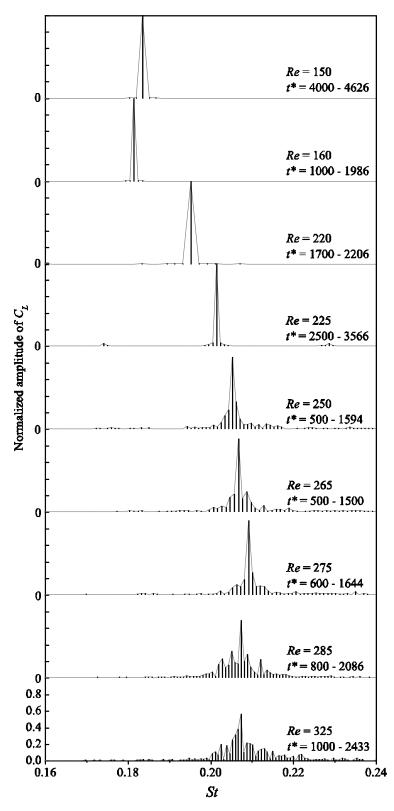


Fig. 13. Frequency spectra of C_L for G/D = 0.4 and Re in the range of 150 to 325.

It is seen in Fig. 13 that for $Re \le 225$, since the time-history of the lift coefficient is relatively regular (Fig. 6), the frequency spectrum is represented by a single

frequency value with the normalized amplitude very close to 1. In the mode swapping regime of Re = 250 - 275, as the time-history of the lift coefficient becomes relatively irregular, the frequency spectrum is represented by a sharp peak together with small-scale fluctuations, and the peak amplitude reduces to around 0.9. As the Mode B structure becomes increasingly disordered at $Re \ge 285$, the frequency spectrum becomes increasingly broad-band and the peak amplitude further drops to approximately 0.6.

3.3. Results at Re = 200 with varying G/D

A series of cases with Re = 200 and G/D ranging between 0.4 and 19.5 is studied. As shown in Fig. 4, the wake transition regime changes from "ordered Mode A (without dislocations)" to "Mode A with dislocations" when G/D increases from 1.2 to 1.5. Consequently, the time-histories of the force coefficients and point spanwise velocity change from a relatively regular pattern which is similar to the case of (G/D, Re) = (0.4, 200) (Fig. 6(b)) into a chaotic irregular pattern which is similar to the case of an isolated cylinder. Similar to Fig. 13, Fig. 14 shows the frequency spectra of C_L for Re = 200 with the amplitude normalized with $1/(\sqrt{2}C_L)$. For $G/D \le 1.2$ (without dislocations), a single frequency value is observed in the frequency spectrum and the normalized amplitude is very close to 1. For $G/D \ge 1.5$ (with dislocations), however, the frequency spectrum is broad-band and the peak amplitude reduces to approximately 0.6.

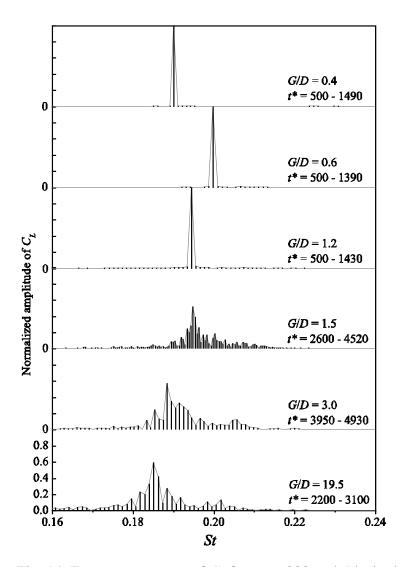


Fig. 14. Frequency spectra of C_L for Re = 200 and G/D in the range of 0.4 to 19.5.

Fig. 15 shows the variations of the statistically stationary Strouhal number and force coefficients with G/D. It is seen that the 3D results of the Strouhal number and force coefficients are decreased from their 2D counterparts to a similar degree for all of the gap ratios considered. Particularly, there is no abrupt variation of the quantities shown in Fig. 15 when G/D increases from 1.2 (without dislocations) to 1.5 (with dislocations). This suggests that the Strouhal number and force coefficients are not strongly influenced by the occurrence or suppression of vortex dislocation. This seems to support the argument by Henderson (1997) that the particular shedding frequency is due to the Mode A instability only, rather than the occurrence of dislocation, whereas the occurrence of dislocation accounts for a broad-band

frequency spectrum (see Fig. 14).

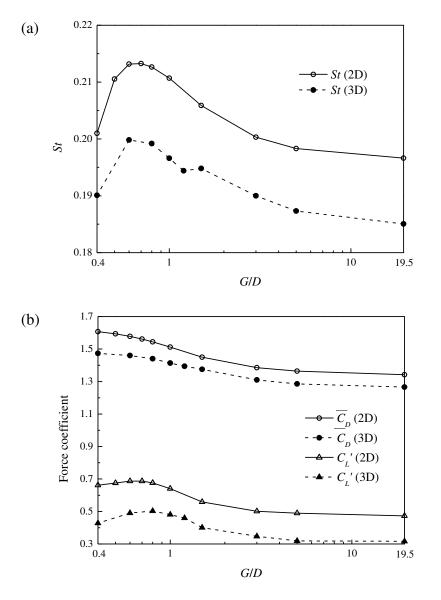
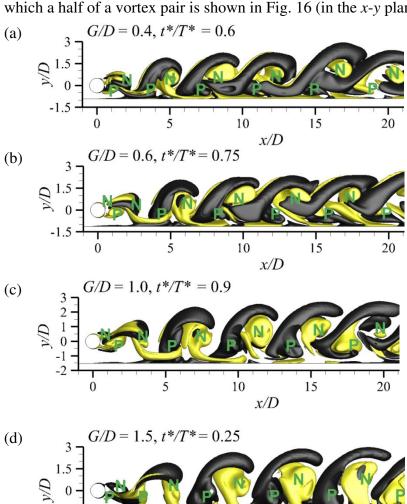
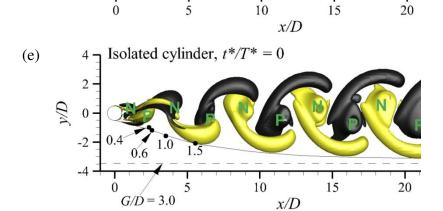


Fig. 15. Variations of the statistically stationary quantities with G/D: (a) Strouhal number, and (b) time-averaged drag coefficient and root-mean-square lift coefficient.

The confinement of the wake structures at different gap ratios is examined through numerical flow visualization. Fig. 16 shows the iso-surfaces of ω_x for various G/D with Re = 200, overlaid with the locations of the positive (P) and negative (N) primary vortex cores determined from the iso-surfaces of the second negative eigenvalue λ_2 of the tensor $\Psi^2 + \Omega^2$, where Ψ and Ω are the symmetric and antisymmetric parts of the velocity gradient tensor, respectively (Jeong and Hussain,

1995). For $0.4 \le G/D \le 1.0$ where vortex dislocation is suppressed, the fully developed wake structure is presented. For $G/D \ge 1.5$ where vortex dislocation will evolve spontaneously, the pure Mode A structure at the time just before the occurrence of dislocation is shown. For each case, three relatively ordered Mode A streamwise vortex pairs are observed along the cylinder span width (in the x-z plane), among which a half of a vortex pair is shown in Fig. 16 (in the x-y plane).





-3

Fig. 16. Iso-surfaces of $\omega_x = \pm 0.2$ for Re = 200 with various gap ratios, overlaid with the locations of the positive (P) and negative (N) primary vortex cores. Dark grey and light yellow denote positive and negative values, respectively. The flow is from the left to the right past the cylinder on the left.

The time evolution of the vortex structure has been examined in a full vortex shedding cycle (with a shedding period of T). The non-dimensional flow time t^* (= Ut/D) is normalized with the non-dimensional shedding period T^* (= UT/D) so that t^*/T^* ranges from 0 to 1 in this shedding cycle (discarding the previous flow time). The shedding cycle starts at the time instant $t^*/T^* = 0$ where the lift coefficient on the cylinder reaches its maximum, and a negative primary vortex core develops at the upper side of the cylinder. Each case in Fig. 16 is shown at the phase of its earliest confinement (in terms of the streamwise location x/D) of the negative streamwise vortices by the plane wall in the shedding cycle. As expected, the earliest confinement point moves downstream as the gap ratio increases.

Fig. 16(e) shows the lower envelope of the streamwise vortices for the case of an isolated cylinder at Re = 200. It is seen that the earliest confinement points for $0.4 \le G/D \le 1.5$ all fall onto this envelope, which suggests that the confinement of the negative streamwise vortices is largely due to the interference of the plane wall with the natural development of the streamwise vortices in the cylinder wake. For G/D = 3.0, there is no intersection point between the envelope of the streamwise vortices and the plane wall (Fig. 16(e)), and consequently the wake structure is not noticeably affected (omitted for simplicity).

For each case shown in Fig. 16, alternate vortex shedding is observed, which is represented by a row of negative primary vortex cores shed from the upper side of the cylinder and a row of positive primary vortex cores shed from the lower side of the cylinder. For the case of an isolated cylinder (Fig. 16(e)), the primary vortex cores and streamwise vortices with opposite signs developed on the two sides of the cylinder possess a Z_2 spatiotemporal symmetry (spatial reflection of the flow about the wake centreline after every T/2 time evolution) as they propagate downstream. With

decrease of the gap ratio, both rows of primary vortex cores are deflected upwards. The negative streamwise vortices downstream of the earliest confinement point are squeezed by the plane wall and the neighbouring positive streamwise vortex. The positive streamwise vortices downstream of the earliest confinement point are also slightly confined by the plane wall at their lower ends, each displaying a wedge-shaped lower end extending towards the upstream side. The distortions of the streamwise vortices become stronger as they propagate downstream (Fig. 16(a–d)), since for an isolated cylinder the lower envelope of the streamwise vortices reaches further lower positions (Fig. 16(e)). At small gap ratios, the extended lower ends of the positive streamwise vortices may even be strong enough to merge with the subsequent positive streamwise vortices (e.g. Fig. 16(a)).

For $G/D \ge 1.5$, it is found that any large-scale vortex dislocation is always initialized with the local dislocation of a particular Mode A vortex loop after it grows to be stronger than other Mode A vortex loops along the span width. Hence the suppression of vortex dislocation for $G/D \le 1.2$ is believed to be due to the confinement of the Mode A streamwise vortices by the plane wall, which suppresses the excess growth and local dislocation of any Mode A vortex loop.

It is found that vortex dislocation is also suppressed for the case of flow past a circular cylinder in proximity to a symmetry boundary (rather than a moving wall) with (G/D, Re) = (1.2, 200). This case suggests that the suppression of vortex dislocation is not due to the shear layers developed on the plane wall.

It is worth mentioning that similar suppression of vortex dislocation of the Mode A flow is also observed for flow past a circular cylinder with two near-wake wires (of an equal diameter of 0.05D) placed at $(x/D, y/D) = (0.75, \pm 0.75)$. In this case, the near-wake wires are the reasons for the confinement of the streamwise vortices (Fig. 17) and consequently the suppression of local dislocation of Mode A vortex loops.

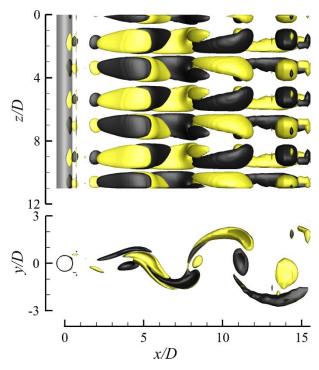


Fig. 17. Iso-surfaces of $\omega_x = \pm 0.1$ for flow past a circular cylinder with two near-wake wires at Re = 220. Dark grey and light yellow denote positive and negative values, respectively. The flow is from the left to the right past the cylinder on the left.

4. Conclusions

This paper presents 3D DNS of flow past a circular cylinder near a moving wall, covering a parameter space spanning a gap ratio $(G/D) \ge 0.3$ and Reynolds number (Re) up to 325. For $G/D \ge 0.3$, the flow undergoes a transition sequence of "2D \rightarrow Mode A \rightarrow mode swapping \rightarrow Mode B" with increasing Re. The Mode A and mode swapping regimes are further separated at $G/D \sim 1.0$, based on the occurrence or suppression of vortex dislocation associated with Mode A. The suppression of vortex dislocation is believed to be due to the confinement of the Mode A streamwise vortices by the plane wall, which suppresses the excess growth and local dislocation of any Mode A vortex loop.

A series of cases at G/D = 0.4 with varying Re is examined, where vortex dislocation is suppressed in the wake transition process. For $Re_{cr3D} < Re \le 180$, the fully developed flow is represented by ordered Mode A structure only. For $200 \le Re < 225$, the ordered Mode A structure remains unchanged while ordered Mode B

structure starts to develop within the Mode A vortex loops. For $225 \le Re \le 240$, all of the Mode A vortex loops are filled with ordered Mode B structure throughout the simulations. The mode swapping process with a gradual transition from the ordered Mode A structure to relatively ordered Mode B structure occurs at Re = 246 - 281. For $Re \ge 285$, the wake is dominated by increasingly disordered Mode B structure. Relatively strong flow three-dimensionality is observed at Re = 160 - 220 as the wake is dominated by large scale structure of ordered Mode A, and also at $Re \ge 285$ where Mode B becomes increasingly disordered. A local reduction of the flow three-dimensionality is observed at Re = 225 - 275 where the wake is dominated by finer-scale structure of a mixture of ordered Modes A and B. This leads to a reduction of the deviation of the 3D results (Strouhal number and force coefficients) from their 2D counterparts. Together with the results at Re = 200 with varying G/D, the results obtained from the present study support the argument by Henderson (1997) that the particular vortex shedding frequency for Mode A is due to the Mode A instability only, rather than the occurrence of vortex dislocations, while the occurrence of dislocations accounts for a broad-band frequency spectrum.

Acknowledgments

This work was supported by resources provided by the Pawsey Supercomputing Centre with funding from the Australian Government and the Government of Western Australia. The first author would like to acknowledge the support from the Australian Government and The University of Western Australia by providing IPRS and APA scholarships for a doctoral degree, as well as the Australia-China Natural Gas Technology Postgraduate Research Scholarships from the Australian and Western Australian Governments, the North West Shelf Joint Venture Partners, and the Western Australian Energy Research Alliance. The fourth author would like to acknowledge the support from the Australian Research Council through Discovery Early Career Research Award (DE150100428).

References

- Barkley, D., Henderson, R.D., 1996. Three-dimensional Floquet stability analysis of the wake of a circular cylinder. Journal of Fluid Mechanics 322, 215–241.
- Bearman, P.W., Zdravkovich, M.M., 1978. Flow around a circular cylinder near a plane boundary. Journal of Fluid Mechanics 89, 33–47.
- Braza, M., Faghani, D., Persillon, H., 2001. Successive stages and the role of natural vortex dislocations in three-dimensional wake transition. Journal of Fluid Mechanics 439, 1–41.
- Grass, A.J., Raven, P.W.J., Stuart, R.J., Bray, J.A., 1984. The influence of boundary layer velocity gradients and bed proximity on vortex shedding from free spanning pipelines. Journal of Energy Resources Technology 106, 70–78.
- Henderson, R.D., 1997. Nonlinear dynamics and pattern formation in turbulent wake transition. Journal of Fluid Mechanics 352, 65–112.
- Huang, W.X., Sung, H.J., 2007. Vortex shedding from a circular cylinder near a moving wall. Journal of Fluids and Structures 23, 1064–1076.
- Issa, R.I., 1986. Solution of implicitly discretized fluid flow equations by operator-splitting. Journal of Computational Physics 62, 40–65.
- Jeong, J., Hussain, F., 1995. On the identification of a vortex. Journal of Fluid Mechanics 285, 69–94.
- Jiang, H., Cheng, L., Draper, S., An, H., Tong, F., 2016. Three-dimensional direct numerical simulation of wake transitions of a circular cylinder. Journal of Fluid Mechanics 801, 353–391.
- Jiang, H., Cheng, L., Draper, S., An, H., 2017. Two- and three-dimensional instabilities in the wake of a circular cylinder near a moving wall. Journal of Fluid Mechanics 812, 435–462.
- Lei, C., Cheng, L., Kavanagh, K., 1999. Re-examination of the effect of a plane boundary on force and vortex shedding of a circular cylinder. Journal of Wind Engineering and Industrial Aerodynamics 80, 263–286.
- Lei, C., Cheng, L., Armfield, S.W., Kavanagh, K., 2000. Vortex shedding suppression for flow over a circular cylinder near a plane boundary. Ocean Engineering 27, 1109–1127.
- Leweke, T., Williamson, C.H.K., 1998. Three-dimensional instabilities in wake transition.

- European Journal of Mechanics B/Fluids 17, 571–586.
- OpenFOAM. Available from www.openfoam.org.
- Posdziech, O., Grundmann, R., 2001. Numerical simulation of the flow around an infinitely long circular cylinder in the transition regime. Theoretical and Computational Fluid Dynamics 15, 121–141.
- Price, S.J., Sumner, D., Smith, J.G., Leong, K., Païdoussis, M.P., 2002. Flow visualization around a circular cylinder near to a plane wall. Journal of Fluids and Structures 16, 175–191.
- Rao, A., Thompson, M.C., Leweke, T., Hourigan, K., 2013. The flow past a circular cylinder translating at different heights above a wall. Journal of Fluids and Structures 41, 9–21.
- Rao, A., Thompson, M.C., Leweke, T., Hourigan, K., 2015. Flow past a rotating cylinder translating at different gap heights along a wall. Journal of Fluids and Structures 57, 314–330.
- Stewart, B.E., Thompson, M.C., Leweke, T., Hourigan, K., 2010. The wake behind a cylinder rolling on a wall at varying rotation rates. Journal of Fluid Mechanics 648, 225–256.
- Taneda, S., 1965. Experimental investigation of vortex streets. Journal of the Physical Society of Japan 20, 1714–1721.
- Thapa, J., Zhao, M., Zhou, T., Cheng, L., 2014. Three-dimensional simulation of vortex shedding flow in the wake of a yawed circular cylinder near a plane boundary at a Reynolds number of 500. Ocean Engineering 87, 25–39.
- Thompson, M.C., Leweke, T., Williamson, C.H.K., 2001. The physical mechanism of transition in bluff body wakes. Journal of Fluids and Structures 15, 607–616.
- Wang, X.K., Tan, S.K., 2008. Near-wake flow characteristics of a circular cylinder close to a wall. Journal of Fluids and Structures 24, 605–627.
- Williamson, C.H.K., 1996. Three-dimensional wake transition. Journal of Fluid Mechanics 328, 345–407.
- Yoon, H.S., Lee, J.B., Seo, J.H., Park, H.S., 2010. Characteristics for flow and heat transfer around a circular cylinder near a moving wall in wide range of low Reynolds number. International Journal of Heat and Mass Transfer 53, 5111–5120.
- Zdravkovich, M.M., 1985. Observation of vortex shedding behind a towed circular cylinder near a wall. Proceedings of the 3rd International Symposium on Flow Visualization, Ann Arbor,

Michigan. Hemisphere Publishing Corp., Washington, D.C., 423–427.