

Three-octave-spanning supercontinuum generation and sub-two-cycle self-compression of mid-infrared filaments in dielectrics

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We experimentally and numerically investigate the spectral and temporal structure of mid-infrared (mid-IR) filaments in bulk dielectrics with normal and anomalous group-velocity dispersion (GVD) pumped by a 2.1- μm optical parametric chirped-pulse amplifier (OPCPA). Formation of stable and robust filaments with several μJ of pulse energy is observed. We demonstrate more than 3-octave-spanning supercontinuum from ZnS in the normal GVD regime and self-compression of the mid-IR pulse to sub-2-cycle duration in CaF₂ in the anomalous GVD regime. The experimental observations quantitatively agree well with the numerical simulations based on a 3D nonlinear wave equation which reveals detailed spatio-temporal dynamics of mid-IR filaments in dielectrics.

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Supercontinuum generation (SCG) has attracted extensive attention owing to its broad applications in sensing, spectroscopy, optical coherence tomography, and so on [1]. Extending SCG to the mid-IR range is highly desired for detecting biomedical materials and air pollutants with the resonant fingerprints of the common molecules, such as H₂O, CO₂, CO, and NH₄. Moreover, coherent broadband mid-IR SC is a good candidate as the seed of mid-IR optical parametric amplifiers (OPAs) and OPCPAs for strong-field physics and attosecond science. In general, high-energy, few-cycle mid-IR pulses are extremely useful for the time-resolved studies of the fundamental processes in physics and chemistry.

The research work on SCG [2-5] and pulse compression [6] in the mid-IR range has been mostly explored in fibers in the past decade. SCG covering the whole mid-IR ‘fingerprint region’ has been demonstrated very recently in a chalcogenide step-index fiber pumped by 4.5 μm and 6.3 μm lasers [7]. However, there are intrinsic peak power limitations and alignment sensitivity issue with the method of fiber-based SCG. Recently, filamentation in bulk dielectrics started to show new opportunities with its advantages such as flexible materials available in normal and anomalous GVD regimes, no limitation of confinement loss at long wavelengths, high adaptable pump power, and high throughput. Multi-octave spanning SCG and the feasibility of few-cycle self-compression have been studied in a YAG crystal, pumped by femtosecond pulses at 3.1 μm [8, 9].

In this Letter, we use a pump wavelength at 2.1 μm , generated from an OPCPA, for laser filamentation [10] in the Mid-IR regime. This wavelength is compatible to

recently developed ultrafast laser amplifiers based on Tm- or Ho-doped material [11]. We systematically investigate mid-IR SCG from filaments in different dielectrics in both normal and anomalous GVD regimes. More than 3-octave broadband spectrum is demonstrated for the first time in ZnS in the normal GVD regime. Moreover, mid-IR pulse self-compression down to sub-2 cycle duration is demonstrated in CaF₂ in the anomalous GVD regime. Up to 9 μJ of pulse energy from the SC has been generated.

For a systematic study of the SCG in the mid-IR, CaF₂ (5-mm thick), BaF₂ (6-mm thick), and ZnS (8-mm thick), which have relatively flat dispersion around 2 μm were chosen as bulk dielectric materials. The zero-dispersion wavelength (ZDW) of the three materials is 1.67 μm , 1.92 μm , and 3.6 μm , respectively, as shown in Fig. 1(a). The bulk dielectrics were pumped by a 2.1 μm , 34 fs, 1 kHz OPCPA with passive carrier-envelope phase stabilization [12]. The pump pulse energy was varied in the range from 0.1 to 11 μJ for optimization of the SCG process towards ultrabroad bandwidth and stable single filamentation. The pump beam was focused using an f = 100 mm CaF₂ lens to a $1/e^2$ diameter of 200 μm . We placed the input surface of dielectrics 4–7 mm before the focal spot to 1) enable the end of the filament to be just at the output surface of the dielectrics; and 2) avoid focusing at the dielectric surface to cause damage. Three different spectrometers based on Si, InGaAs, and PbSe detectors, respectively, were employed to cover the spectra spanning from the visible to \sim 5 μm of wavelength.

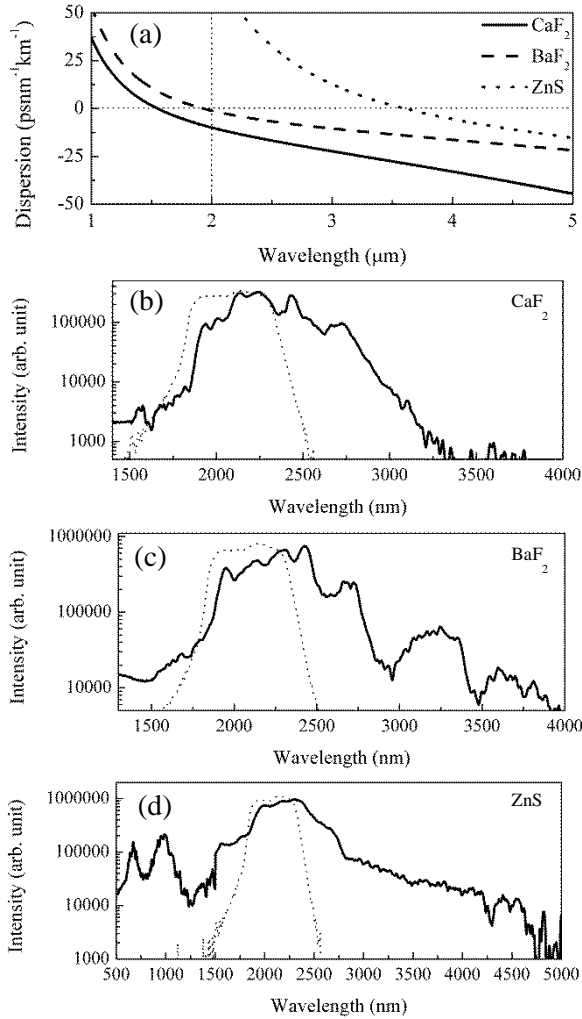


Fig. 1. (a) Material dispersion of CaF₂ (solid), BaF₂ (dash), and ZnS (dot). The generated SC from (b) 5-mm-thick CaF₂ at 9 μJ, (c) 6-mm-thick BaF₂ at 7 μJ (c), and (d) 8-mm-thick ZnS at 5 μJ. The dotted curves in (b), (c), and (d) are the spectra of the 2.1 μm pump laser.

As shown in Figs. 1(b) and (c), with the pump wavelength at 2.1 μm, the continuum spectrum is extended to wavelengths up to ~3.4 μm and ~4 μm in CaF₂ and BaF₂, respectively. The deeper extension into the mid-IR in BaF₂ is due to its flatter and lower dispersion, and thus broader conversion bandwidth with less temporal walk-off. Moreover, we performed SCG in a ZnS crystal with normal GVD, for the first time. As shown in Fig. 1(d), the generated SC spans from 500 nm to 4.5 μm, corresponding to 3.1 octave. The peaks at ~980 nm and ~670 nm are observed, where the 670-nm component is possibly the third harmonic of the 2.1 μm pump pulse. It is interesting that ZnS has a nonlinear refractive index (n_2) as high as 90×10^{-16} cm²/W, which is ~50 times larger than that of CaF₂. Surprisingly, we were still able to maintain a very stable filament with an input energy of 11 μJ, which corresponds to ~1000 times the critical power for self-focusing. The normal GVD seems to help the stable filamentation at over-critical power by rapidly

broadening the pulse, but further investigation is needed to understand the detailed mechanism.

The visible images of the far-field pattern and the filaments inside CaF₂, BaF₂, and ZnS are captured. Stable conical far-field profiles were observed for SC from CaF₂ and BaF₂ as shown in Fig. 2(a) and (b), while ZnS has a more uniform far-field pattern shown in Fig. 2(c). The filaments from all the three dielectrics manifest a robust single filament as shown in Fig. 2 (d), (e), and (f). However, it is possible that multiple micro-filaments are generated in ZnS due to the highly over-critical power.

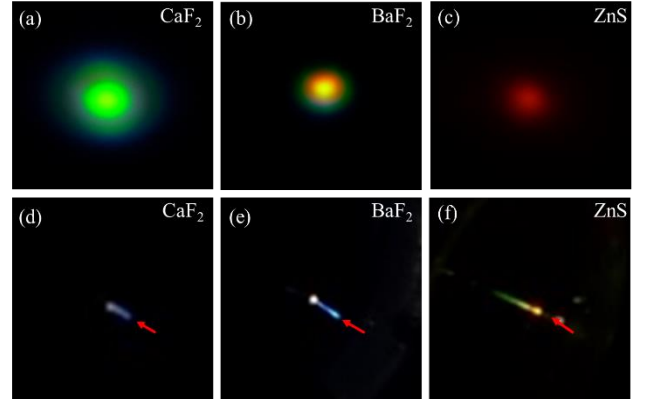


Fig. 2. The far field of the SC from (a) CaF₂, (b) BaF₂, and (c) ZnS. (d), (e), and (f) are the visible images of their corresponding filaments inside the material, respectively. The red arrows indicate the incident direction of the pump pulses. (Color online)

The temporal profiles of the generated mid-IR SC were characterized using a second-harmonic generation (SHG) interferometric autocorrelator. A 100-μm thick β -Barium Borate and a 400-μm thick AgGaS₂ is used for the SHG of the 2.1 μm pump pulse and the mid-IR filaments, respectively. A 900 nm long-pass filter and a 1500 nm short-pass filter were employed after SHG to ensure background free measurements, so that the mid-IR SC from 1800 to 3000 nm was characterized. As shown in Figs. 3(a) and 3(b), with the ~34 fs pump pulse in full width at half maximum (FWHM), the SC from BaF₂ was broadened to ~49 fs in FWHM. This is due to the self-phase-modulation (SPM) induced chirp that has not been well compensated by the weak anomalous GVD. In contrast, as shown in Fig. 3(c), from CaF₂, which has stronger anomalous GVD, the generated SC was self-compressed to <14 fs in FWHM, corresponding to sub-two optical cycles, close to the transform-limited pulse duration for 1800–3000 nm of measurement window. This implies the SPM and strong anomalous GVD are almost perfectly balanced. The interferometric autocorrelation trace of SC in CaF₂ shown in the inset of Fig. 3(c) was calculated from the 1800–3000 nm components of the measured SC spectrum with a flat-phase assumption. The calculated autocorrelation trace matches well with the measurement, except there are some side lobes in the measured trace which is attributed to the high-order dispersion and temporal splitting. On the other hand, the measured duration of pulses from ZnS filaments are longer than 200 fs because the SC forms the dispersive wave.

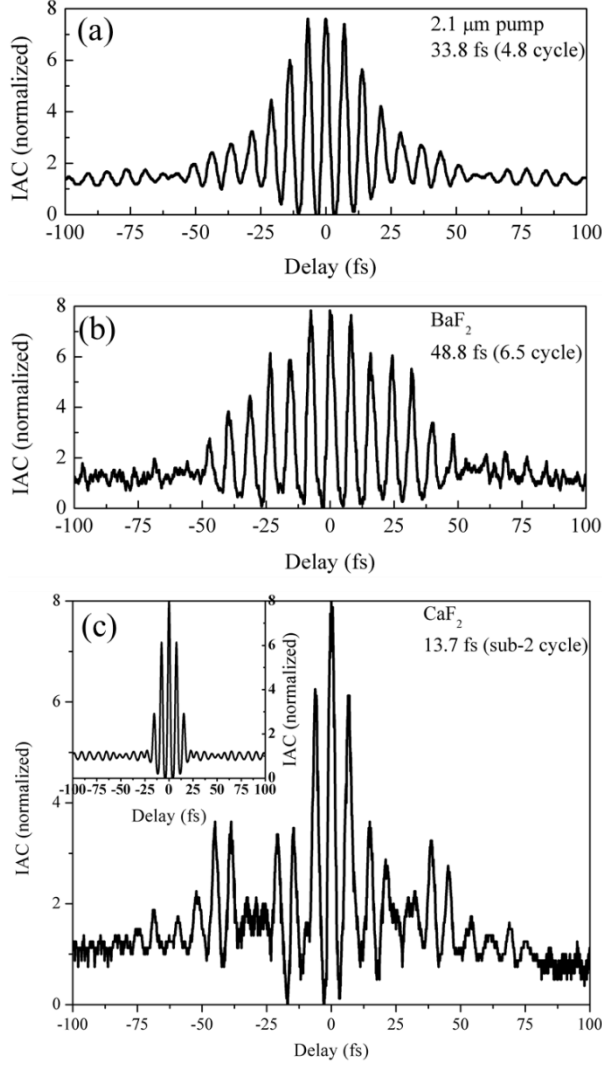


Fig. 3. The measured interferometric autocorrelation traces of the SC generated in (a) 2.1 μm pump pulse, (b) BaF_2 , and (c) CaF_2 . The pulse energy of 6 μJ was used for both CaF_2 and BaF_2 . The inset of (c) is the calculated autocorrelation trace from the 1800-3000 nm components of the measured spectrum.

To have more quantitative understanding about the experiments, we carried out numerical simulations using the nonlinear envelope equation (NEE) in normalized units which is given by [13,14]

$$\begin{aligned} \frac{\partial A}{\partial \xi} = & \frac{i}{4} \left(1 + \frac{i\partial}{\omega\tau_p\partial\tau} \right)^{-1} \nabla^2 A + iL_{df} \sum_{n=2}^6 \frac{\beta_n}{n!} \left(\frac{i\partial}{\tau_p\partial\tau} \right)^n A \\ & + i \left(1 + \frac{i\partial}{\omega\tau_p\partial\tau} \right) \frac{L_{df}}{L_{nl}} |A|^2 A - \frac{L_{df}}{2L_{mp}} \frac{A}{|A|^2} \frac{\partial \eta}{\partial \tau} \\ & - \frac{L_{df}}{L_{pl}} \left(i + \frac{1}{\omega\tau_c} \right) \eta \left[A + \frac{\tau_c \partial A}{\tau_p \partial \tau} \right], \end{aligned} \quad (1)$$

where A is the electric field normalized by the input electric field amplitude, ξ is the propagation distance normalized by the input beam diffraction length L_{df} , ω is

the central frequency of the laser pulse, τ is the retarded time normalized by the pulse duration τ_p , ω is the angular frequency of the central wavelength, β_n is the dispersion parameter (e.g., β_2 is GVD), L_{nl} is the nonlinear length, L_{mp} is the multi-photon absorption length, L_{pl} is the plasma length, η is the normalized electron density, and τ_c is the collision time. Each term on the right side of the equation represents diffraction, dispersion, self-focusing via Kerr-nonlinearity, multi-photon absorption, and plasma terms (defocusing and collisional absorption), respectively. Multi-photon ionization and avalanche ionization generate free electrons, which is described by

$$\frac{\partial \eta}{\partial \tau} = |A|^{2m} + \alpha \eta |A|^2, \quad (2)$$

where m is the number of photons to ionize the medium, and α is the avalanche ionization coefficient.

The simulated SCG reproduces the experiment measurement with high accuracy as shown in Figs. 4(a) and (b). For BaF_2 , its calculated output spectrum has larger spectral components at 3-4 μm than that of CaF_2 , which is consistent with the experimental data. For ZnS , the calculation also quantitatively reproduces the measured spectrum that there is significant spectral extension up to >4.5 μm . Besides the SC spectra, temporal dynamics of the SCG in different dielectrics were also revealed by simulations. Pulses in the anomalous GVD regime *i.e.*, in BaF_2 and CaF_2 , shown in Figs. 4(c) and (d) are strongly localized near $t = 0$ even though there is short-time scale pulse splitting due to plasma generated by the high intensity pulses. To the contrary, pulse broadening and pulse splitting are clearly observed in the normal GVD regime in ZnS [15], shown in Fig. 4(e). The spatially-averaged autocorrelation traces over entire spectral bandwidth were simulated for comparison with the measurement results. For the SC in CaF_2 , the autocorrelation trace in Fig. 4(f) shows a 17 fs in FWHM, corresponding to a 12 fs pulse width. This tallies well with the measured self-compressed sub-two-cycle pulse from the SC in CaF_2 except that the measured pulse duration is longer because of the limited bandwidth. The imperfect self-compression in BaF_2 is also well reproduced by simulations shown in Fig. 4(g). On the other hand, ZnS broadens the autocorrelation to ~ 300 fs due to the normal GVD and pulse splitting, which is also consistent with the measurement.

In conclusion, we systematically investigated the mid-IR SCG from filaments in bulk dielectrics with normal and anomalous GVD. 3-octave-spanning SC spectrum in ZnS with normal GVD was generated with robust and stable output power. In the anomalous GVD regime, sub-two-cycle self-compression of mid-IR filaments from CaF_2 was experimentally observed. Filaments have several μJ of pulse energy. Such a coherent broadband source with few-cycle duration in the mid-IR range is a promising seed source for seeding mid-IR OPA and OPCPA as well as a good candidate for time-resolved tools for molecular motion study.

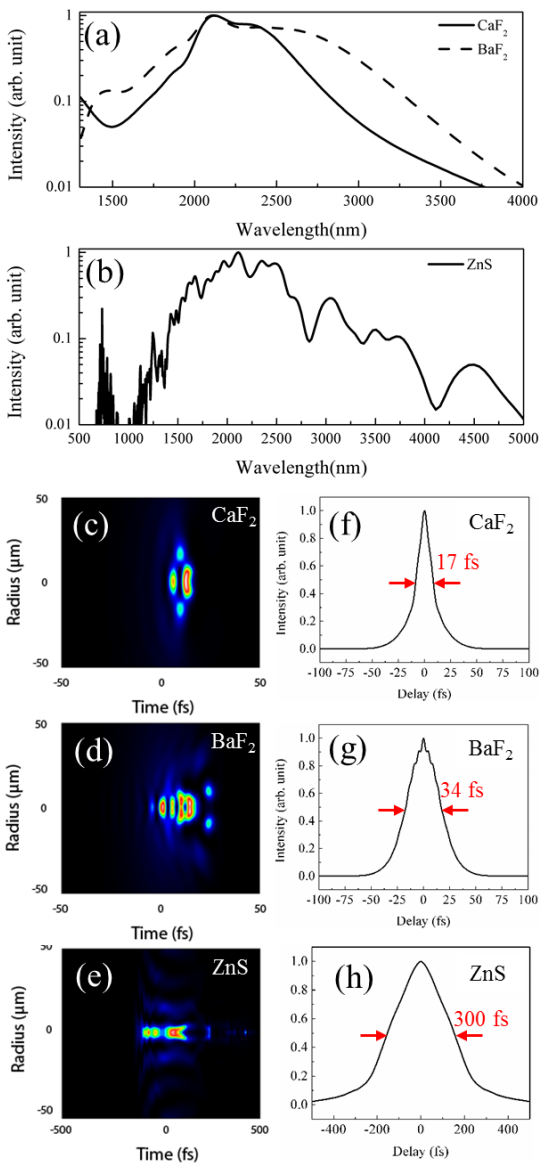


Fig. 4. Simulated spatially-averaged spectra in (a) CaF_2 and BaF_2 , and (b) ZnS . Simulated spatio-temporal profiles when $2.1 \mu\text{m}$, 30 fs pulses pass through (c) CaF_2 , (d) BaF_2 , and (e) ZnS . Ten-time larger time scale is used in (e). Simulated spatially-averaged autocorrelation traces of SC in (f) CaF_2 , (g) BaF_2 , and (h) ZnS . The pulse energies used for simulation are $6 \mu\text{J}$ for CaF_2 and BaF_2 , and $5 \mu\text{J}$ for ZnS .

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