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Some of the significant technological challenges to commercial-31 ization of polymer electrolyte membrane (PEM) fuel cells have been 32 addressed in the past two decades through extensive theoretical and ex-33 34 perimental research. As a result, the PEM fuel cell technology has advanced considerably. In particular, the amount of precious metal used 35 in the catalyst layers (CL) has been significantly reduced while achiev-36 ing remarkable performance improvements.<sup>1,2</sup> Nevertheless, impor-37 tant challenges related to cost and durability remain. While further 38 39 material development is indeed beneficial, some of the existing is-40 sues may be addressed through effective control and hybridization of these systems. This will require a good understanding of the pro-41 cesses that govern the fuel cell dynamics. Moreover, in-depth studies 42 43 of the transients can improve the current understanding of various electrochemical and transport phenomena. Therefore, there is a need 44 for better understanding of the transient response to further enhance 45 46 performance and lifetime of PEM fuel cells.

Arguably, the dynamic studies of PEM fuel cells have been over-47 shadowed by the significant efforts dedicated to steady state mea-48 surements and modeling. However, fuel cell transient response has 49 attracted some attention lately, as it can be used to elucidate and de-50 convolve complex transport phenomena.<sup>3-8</sup> Several transient models have also been proposed in the literature.<sup>9–15</sup> These models usually 51 52 use simplified reaction kinetics and do not account for the micro-53 structure of various cell layers and the anisotropic material properties. 54 Therefore, these models typically do not have the required fidelity to 55 allow detailed investigation of the transient phenomena affecting the 56 cell performance. Accordingly, it is the main objective of this work 57 to develop a transient model that captures the most salient features of 58 the cell's dynamics across its thickness. Furthermore, we execute the 59 model under a variety of operating conditions to delineate the criti-60 cal transient phenomena that determine the overall cell dynamics. It 61 should be noted that the model presented here is only helpful in un-62 derstanding transient phenomena through the thickness of a unit cell 63

\*Electrochemical Society Student Member. <sup>z</sup>E-mail: jchen186@ford.com; tersal@umich.edu with small active area. In other words, the compressor and channel flow dynamics, along the channel redistributions, and stack thermal dynamics are not discussed here. Nevertheless, the results of this work may be extended along the flow channel and across multiple cells to study the transients at those scales.

Specific to our objective is creating a model that, as much as possi-69 ble, directly translates the physically measurable parameters and op-70 erating conditions into the knowledge about spatio-temporal distribu-71 tions of critical variables such as temperature and water concentration 72 in different layers. To this end, it is imperative to effectively capture 73 the physical characteristics of the porous layers including the catalyst 74 layers and diffusion media (DM). It is worth pointing out that, as has re-75 cently been shown, a representative elementary volume (REV) cannot 76 be clearly defined in the through-plane direction for commercial DM<sup>16</sup> 77 and the REV for the in-plane direction is on par with the land-channel 78 sizes used in fuel cells.<sup>16,17</sup> Therefore, while the macroscopic models 79 can capture the aggregate behavior, their predictions may significantly 80 deviate from the local predictions by microscopic models.<sup>16,18</sup> This 81 result bears significance, as it points to the need for more elaborate 82 description of transport in the porous layers. Nevertheless, the exces-83 sively high cost of such simulations limits their application to very 84 few conditions and a limited material set. Therefore, the macroscopic 85 models remain the main tool to investigate the internal distributions 86 in a full cell model and including some level of description of the 87 microstructure is the approach adopted in this work to improve their 88 prediction capability. This is achieved here by using a recently devel-89 oped mixed wettability model for the porous layers.<sup>19,20</sup> To the best 90 of the authors' knowledge, this is the first time that a full implemen-91 tation of the mixed wettability model is being used in a 2D transient 92 model. In addition to the mixed wettability model for porous layers, 93 the presented model accounts for ionomer relaxation dynamics and 94 CL micro-structure, which have been neglected in most of the previ-95 ous models. Moreover, the effective material and transport properties 96 of the different layers are identified through an extensive literature 97 review of commercially available materials. Therefore, this model is 98 expected to offer higher fidelity than the state of the art models for 99

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Figure 1. Modeling domain.

 $_{100}$  the purpose of studying transient phenomena that impact performance and durability.<sup>21</sup>

The rest of the paper is organized as follows: First, the model formulation is presented along with a detailed review of the literature relevant to each sub-model to justify the choices made during model development. Simulation results and discussions are provided next, followed by a brief summary and concluding remarks. Model validation with experimental data from the literature is presented in the accompanying Supplementary Information.

### Model Formulation

The modeling domain of interest is shown in Fig. 1. The model draws from prior work by Balliet et al.,<sup>10</sup> Zenyuk et al.,<sup>22</sup> and Zhou et al.<sup>23</sup> with modifications to several sub-models. Therefore, the model is presented here in its entirety for completeness. A complete list of model parameters is provided in the accompanying Supplementary Information.

**Governing equations.**—The comprehensive 2D model solves the following governing equations, where the various source terms are given in Tables I and II:

$$\varepsilon_{g} \frac{\partial c_{i}}{\partial t} = \nabla \cdot (c_{g} D_{i}^{\text{eff}} \nabla x_{i}) - \nabla \cdot (c_{g} x_{i} \boldsymbol{u}_{g}) + S_{i}, \qquad [1]$$
$$\frac{\partial (\rho_{l} \varepsilon_{l})}{\partial t} = \nabla \cdot \left(\frac{\rho_{l} K_{l}^{\text{eff}}}{\mu_{l}} \nabla p_{l}\right) + S_{\text{liquid}}, \qquad [2]$$
$$\frac{\partial (\rho_{g} \varepsilon_{g})}{\partial t} = \nabla \cdot \left(\frac{\rho_{g} K_{g}^{\text{eff}}}{\mu_{g}} \nabla p_{g}\right) + S_{\text{gas}}, \qquad [3]$$

$$\varepsilon_{\rm ion} \frac{\rho_{\rm ion}}{EW} \frac{\partial \lambda}{\partial t} = \nabla \cdot (N_{\rm w,mb}) + S_{\lambda}, \qquad [4]$$

$$\sum_{\alpha} \varepsilon_{\alpha} \rho_{\alpha} c_{p,\alpha} \left( \frac{\partial T}{\partial t} + \boldsymbol{u}_{\alpha} \cdot \boldsymbol{\nabla} T \right) = \boldsymbol{\nabla} \cdot (k_T^{\text{eff}} \boldsymbol{\nabla} T) + S_T, \qquad [5]$$

$$\boldsymbol{\nabla} \cdot (\boldsymbol{\sigma}_1^{\text{eff}} \boldsymbol{\nabla} \boldsymbol{\phi}_1) = S_{e^-}, \qquad [6]$$

$$\nabla \cdot (\sigma_2^{\text{eff}} \nabla \phi_2) = S_{H^+}.$$
[7]

The first equation describes species transport in the microporous layers (MPLs), gas diffusion layers (GDLs), and CLs, where  $\varepsilon_g$  is the porosity 120 of the layer available for gas transport ( $\varepsilon_g = \varepsilon(1 - s)$ , with s the 121 liquid saturation and  $\varepsilon$  the compressed layer porosity),  $c_g$  is the total 122 gas concentration,  $\boldsymbol{u}_g = -\frac{K_g^{\text{eff}}}{\mu_g} \nabla p_g$  is the velocity of the gas phase, 123 and  $c_i$ ,  $D_i^{\text{eff}}$ , and  $x_i$  denote the concentration, the effective diffusivity, 124 and the molar fraction of species *i*, respectively. The first and second 125 terms on the right hand side model the diffusive and convective fluxes, 126 respectively, while the last term  $(S_i)$  is the relevant source term for 127 the specific gas species (see Table I). In the anode, the equation is 128 solved for water vapor molar fraction  $(x_{H_2O})$  and the hydrogen molar fraction  $(x_{H_2})$  is calculated by  $x_{H_2} = 1 - x_{H_2O}$ . On the cathode side, 130 this equation is solved for water vapor  $(x_{H_2O})$  and oxygen  $(x_{O_2})$  and 131 the nitrogen molar fraction is found from  $x_{N_2} = 1 - x_{O_2} - x_{H_2O}$ . 132

Equations 2 and 3 describe the mass conservation of the liquid and 133 gas phases, respectively. These equations model the pressure drop of 134 each phase in the CLs, MPLs, and GDLs according to Darcy's law. 135 Here,  $\rho_{\alpha}$ ,  $\varepsilon_{\alpha}$ ,  $K_{\alpha}^{\text{eff}}$ ,  $\mu_{\alpha}$ , and  $p_{\alpha}$  denote the density, volume fraction, effec-136 tive permeability (relative permeability times absolute permeability), 137 viscosity, and pressure of phase  $\alpha$ . Note that  $\varepsilon_{g} = \varepsilon(1-s)$  and  $\varepsilon_{l} = \varepsilon s$ . 138 Finally, Sliquid/gas denotes the source term for the corresponding phase 139 (see Table I). Note that liquid saturation that appears in these equations 140 through the volume fractions is a variable that depends on capillary 141 pressure. Therefore, closure equations that relate the saturation level 142 to the capillary pressure are required. In this work, the mixed wetta-143 bility model is used to derive water retention curves (liquid saturation 144 vs. capillary pressure) as well as effective property values such as gas 145 and liquid permeability for the different layers (see Mixed wettability 146 model for porous layers section). 147

Equation 4 governs water transport in the ionomer phase through-148 out the catalyst coated membrane (CCM). Therefore, its domain of 149 application is the anode and cathode catalyst layers and the mem-150 brane. In this equation,  $\varepsilon_{ion}$ ,  $\rho_{ion}$ , and EW denote the ionomer volume 151 fraction, density, and equivalent weight, respectively, while  $\lambda$  is the 152 dimensionless number that quantifies the water content in the ionomer, 153 i.e., the number of water molecules per sulfonic acid group. Finally, 154  $S_{\lambda}$  is the source term (see Table I) and  $N_{\rm w,mb}$  is the water flux in the 155 ionomer phase across the CCM, which includes the effects of electro-156 osmotic drag (EOD), diffusion, and thermo-osmosis and is calculated 157 as follows: 158

$$N_{\rm w,mb} = -n_d \frac{\sigma_2^{\rm eff}}{F} \nabla \phi_2 - \frac{\rho_{\rm ion}}{EW} D_{\rm w,mb}^{\rm eff} \nabla \lambda + D_{T,\rm mb} \nabla T, \qquad [8]$$

Domain	$S_{O_2}$	$S_{H_2O}$	$S_{ m liquid}$	$S_{ m gas}$	$S_\lambda$
Anode CL (ACL)		$S_{\rm pc} - S_{\rm ad}$	$-M_{H_2O}S_{\rm pc}$	$-M_{H_2} \frac{i_{\text{HOR}}}{2E} + M_{H_2O}(S_{\text{pc}} - S_{\text{ad}})$	S <sub>ad</sub>
Cathode CL (CCL)	$\frac{i_{ORR}}{4F}$	$S_{\rm pc} - S_{\rm ad}$	$-M_{H_2O}S_{\rm pc}$	$M_{O_2} \frac{i_{ORR}}{4F} + M_{H_2O}(S_{pc} - S_{ad})$	$S_{\rm ad} - \frac{i_{\rm ORR}}{2F}$
MPL and GDL	Ö	$S_{\rm pc}$	$-M_{H_2O}S_{pc}$	$M_{H_2O}S_{pc}$	

Table II. Energy and charge conservation source terms.

Table I. Mass conservation source terms.

Domain	$S_T$	$S_{H^+}$	$S_{e^{-}}$
Anode CL (ACL)	$-M_{H_2O}S_{\rm pc}H_{\rm pc} + S_{\rm ad}H_{\rm ad} + H_{\rm HOR} + \frac{i_1\cdot i_1}{\sigma_{\rm q}^{\rm eff}} + \frac{i_2\cdot i_2}{\sigma_{\rm q}^{\rm eff}}$	i <sub>HOR</sub>	$-i_{\rm HOR}$
Cathode CL (CCL)	$-M_{H_2O}S_{\rm pc}H_{\rm pc} + S_{\rm ad}H_{\rm ad} + H_{\rm ORR} + \frac{i_1\cdot i_1}{\sigma_{\rm eff}^{\rm eff}} + \frac{i_2\cdot i_2}{\sigma_{\rm eff}^{\rm eff}}$	i <sub>ORR</sub>	$-i_{ORR}$
Membrane	$\frac{i_2 \cdot i_2}{\sigma_{\text{cff}}^{\text{eff}}}$	0	-
MPL and GDL	$-M_{H_2O}S_{\rm pc}H_{\rm pc}$	_	0

where  $n_d$  is the EOD coefficient,  $\phi_2$  is the ionic potential, F is the 159 Faraday's constant,  $\sigma_2^{\text{eff}}$  is the effective conductivity in the ionic phase, 160  $D_{\rm w \ mb}^{\rm eff}$  is the effective water diffusion coefficient in the membrane 161 and  $D_{T,mb}$  is the thermal water diffusivity in the membrane. Note 162 that thermo-osmosis is shown to drive water from the cold to the hot 163 side for a hydrophilic membrane.<sup>24</sup> As a convention, a positive flux 164 denotes water flux toward the cathode. The membrane water transport 165 properties are given in Table III. 166

Equation 5 is the energy conservation equation, which governs 167 the temperature distribution. In this equation,  $\rho_{\alpha}$ ,  $\varepsilon_{\alpha}$ ,  $c_{p,\alpha}$ , and  $\boldsymbol{u}_{\alpha}$  = 168  $\frac{K_{\alpha}^{\text{eff}}}{\omega} \nabla p_{\alpha}$  are the density, volume fraction, specific heat capacity, and 169 velocity of phase  $\alpha$ , where  $\alpha$  can be the gas, liquid, or solid phase. 170 In addition,  $k_T^{\text{eff}}$  is the effective thermal conductivity (see Calculation 171 of effective properties sec.) and  $S_T$  denotes the heat source term (see 172 Table II). Note that this equation captures heat transfer by conduction 173 (first term on the right hand side) as well as convection (second term 174 on the left hand side). 175

Equations 6 and 7 are the Ohm's law for electronic  $(\phi_1)$  and ionic 176  $(\varphi_2)$  potentials, respectively. Here,  $\sigma_1^{eff}$  and  $\sigma_2^{eff}$  denote the effective 177 conductivities of the respective phases and  $S_{H^+/e^-}$  is the relevant source 178 term (see Table II). 179

The source terms for mass conservation equations (Equations 1-4) 180 are given in Table I. Here,  $M_i$  is the molar mass of species *i*,  $i_{HOR/ORR}$ 181 is the volumetric HOR/ORR reaction current density, and  $S_{pc}$  is the 182 source term due to phase change and is given by:<sup>19</sup> 183

$$S_{\rm pc} = \begin{cases} k_{\rm evp} a_{\rm LG} \begin{bmatrix} \frac{p_{\nu} - p_{\rm sat}^{K}(p_c, T)}{p_{\rm sat}^{K}(p_c, T)} \\ k_{\rm cnd} a_{\rm LG} \begin{bmatrix} \frac{p_{\nu} - p_{\rm sat}^{K}(p_c, T)}{p_{\rm sat}^{K}(p_c, T)} \end{bmatrix} & \text{if } p_{\nu} > p_{\rm sat}^{K}(p_c, T) \\ \text{if } p_{\nu} \le p_{\rm sat}^{K}(p_c, T) \end{cases}$$
[9]

where  $k_{evp/cnd}$  denotes the rate of evaporation/condensation,  $a_{LG}$  is the 184 interfacial area between the liquid and gas phases (calculated by the 185 mixed wettability model),  $p_v$  is the vapor pressure, and  $p_{sat}^K(p_c, T)$ 186 is the corrected saturation pressure that takes the Kelvin effect into 187 account. The corrected saturation pressure is given by: 188

$$p_{\text{sat}}^{K}(p_{c},T) = p_{\text{sat}}(T) \exp\left(\frac{M_{H_{2}O}p_{c}}{R\rho_{v}T}\right).$$
 [10]

In the above equation,  $p_c$  is the capillary pressure  $(p_c = p_l - p_g)$ , R is 189 the universal gas constant,  $\rho_v$  is the density of water vapor, and  $p_{sat}(T)$ 190 is the saturation pressure as a function of temperature given by: 191

$$p_{\text{sat}}(T) = 0.61121 \exp\left[\left(18.678 - \frac{T}{234.5}\right)\frac{T}{257.14 + T}\right]$$
 [11]

where T is in Celsius and the calculated pressure is in kPa. 193 In Table I,  $S_{ad}$  denotes the source term due to water exchange (absorption/desorption) between the ionomer phase and the pore space 194

## Table III. Membrane water transport and uptake properties.



and is given by:

$$S_{\rm ad} = \frac{k_{\rm ad} \cdot \rho_{\rm ion}}{\delta_{\rm CL} \cdot EW} (\lambda^* - \lambda), \qquad [12]$$

where  $k_{ad}$  is the interfacial water transfer coefficient (see Table III),  $\delta_{CL}$  denotes the CL thickness, and  $\lambda^*$  is the dynamic variable for equi-197 librium water content in the ionomer (see Ionomer water uptake Sec.). 198 Note that water production with electrochemical reaction contributes 199 to  $S_{\lambda}$ . In other words, the produced water is assumed to be in absorbed 200 phase. This is in agreement with the assumed structure for the CL in 201 this work and has also been used by others.9 202

The source terms for energy and charge conservation (Equations 203 5–7) are given in Table II. In the table,  $i_1$  and  $i_2$  are the electronic and 204 ionic current densities, respectively: 205

$$\mathbf{i}_1 = -\sigma_1^{\text{eff}} \nabla \phi_1 \tag{13}$$

$$\mathbf{i}_2 = -\sigma_2^{\text{eff}} \nabla \phi_2 \qquad [14]$$

Moreover,  $H_{\text{HOR/ORR}}$  denotes the reversible and irreversible heat of 206 reaction given by:

$$H_{\text{HOR}} = i_{\text{HOR}}(\eta_{\text{HOR}} + \Pi_{\text{HOR}}) = i_{\text{HOR}} \left[ (\phi_1 - \phi_2 - E_{\text{rev}}^{\text{an}}) - 0.013 \frac{T}{298.15} \right]$$
[15]

$$H_{\text{ORR}} = i_{\text{ORR}}(\eta_{\text{ORR}} + \Pi_{\text{ORR}}) = i_{\text{ORR}} \left[ (\phi_1 - \phi_2 - E_{\text{rev}}^{\text{ca}}) - 0.24 \frac{T}{298.15} \right]_{[16]}$$

where  $\Pi_{\text{HOR/ORR}}$  is the Peltier coefficient for HOR/ORR,<sup>30</sup>  $E_{\text{rev}}^{\text{an}} = 0$ , 209 and  $E_{\text{rev}}^{\text{ca}} = 1.229 - 8.5 \times 10^{-4} \times (T - 298.15) + \frac{RT}{4F} \ln(p_{O_2})$  are the 210 reversible potentials in each electrode. 211 212

The enthalpy of phase change,  $H_{\rm pc}$ , is

$$H_{\rm pc} = -2.367 \times 10^{-5} T^4 + 1.882 \times 10^{-2} T^3 - 4.672 T^2 -2.098 \times 10^3 T + 3.178 \times 10^6 [\rm J/kg] , \qquad [17]$$

where T is in Kelvin. Finally,  $H_{ad}$  is the heat of sorption (due to water 213 exchange between the ionomer and the pore space, i.e., water vapor) 214 and is given by:<sup>31</sup> 215

$$H_{ad} = \begin{cases} M_{H_2O}H_{pc} - 28.28 \times 10^3 \left[ \text{erf} \left( \frac{18.68 M_{H_2O}}{EW} + 0.4016 \right) - 1 \right] & \text{sorption} \\ -M_{H_2O}H_{pc} + 55.65 \times 10^3 \left[ \text{erf} \left( \frac{10.39 M_{H_2O}}{EW} + 1.116 \right) - 1 \right] & \text{desorption} \end{cases}$$
[18]

Ionomer water uptake.—It is imperative for any transient model 216 of a PEM fuel cell to properly capture the dynamics of water sorp-217 tion, desorption, and transport across the membrane. Historically, 218 diffusive<sup>29</sup> and hydraulic<sup>32</sup> type models have been used for this purpose. However, there is abundant evidence in the literature suggest-220 ing that interfacial transport phenomena as well as swelling of the 221

Equation
$1.2 \tanh\left(\frac{\lambda}{2.5}\right)$
$0.0539 \times (1 + \frac{M_{H_2OP_{\rm ion}}}{EW}\lambda)^{-2} (1 + 0.0027\lambda^2) \left[1 + \tanh\left(\frac{\lambda - 2.6225}{0.8758}\right)\right] \exp\left(\frac{-3343}{T}\right)$
$\frac{1.04 \times 10^{-4}}{M_{\rm w}} \exp(-\frac{2362}{T})$
$1.14 \times 10^{-5} f_{\nu} \exp \left[ 2416 \left( \frac{1}{303} - \frac{1}{T} \right) \right]$ for absorption
$4.59 \times 10^{-5} f_v \exp \left[ 2416 \left( \frac{1}{303} - \frac{1}{T} \right) \right]$ for desorption
$f_v = \frac{18\lambda}{\frac{EW}{p_{\rm inn}} + 18\lambda}$ is the water volume fraction in ionomer
$(1-s)\left[\lambda_{303} + \frac{\lambda_{353} - \lambda_{303}}{50}(T-303)\right] + 22s$
$\lambda_{303} = 0.043 + 17.81a - 39.85a^2 + 36.0a^3$
$\lambda_{353} = 0.300 + 10.8a - 16.0a^2 + 14.1a^3$
a = RH, and s is the local liquid saturation

6]

195

polymer backbone may play a significant role in water uptake and 222 transport dynamics.<sup>33,34</sup> In particular, the gravimetric water uptake 223 experiments conducted by Satterfield et al. have shown very long time 224 constants for membrane water sorption while the desorption time con-225 stants were found to be an order of magnitude smaller.<sup>34</sup> They sug-226 gested that the sorption behavior may be explained through the con-227 tributions of interfacial water transport and stress relaxation in the 228 polymer, whereas the desorption dynamics are dominated by the in-229 terfacial phenomena. Their experiments included a step in the hu-230 midity from fully dry to fully saturated conditions that resulted in 231 significant relaxation behavior. Other studies have found much less 232 pronounced impact of the relaxation dynamics when the membrane 233 was subjected to smaller changes in the humidity conditions.<sup>35</sup> Similar 234 results have been reported for ionomer thin films.<sup>36</sup> Dynamic vapor 235 sorption (DVS) experiments by Kusoglu et al. have also shown rela-236 tively long water uptake times with a time constant that increases with 237 membrane hydration.<sup>37,38</sup> Their results also indicate that the asym-238 metry between sorption and desorption is not as pronounced as that 239 observed in Satterfield et al.'s experiments. Such significant difference 240 was also challenged by Silverman et al. who found the desorption to 241 be only about twice faster than sorption.<sup>39</sup> In situ measurements of 242 membrane swelling and hydration by GM researchers have also found 243 the hydration and dehydration rates to be similar.<sup>40</sup> 244

Based on the preceding discussion, it stands to reason to incorporate the slow ionomer water uptake process into the model. Silverman et al. have developed a coupled transport and mechanical model that captures such phenomena.<sup>31,39</sup> However, adding the mechanical model will result in additional complexity that must be avoided for the purpose of performance modeling. Therefore, we simply use a dynamic variable to represent the quasi-equilibrium water content:<sup>15,41,42</sup>

$$\lambda^* = (1 - \varphi)\lambda_{\text{eq}} + s_{\text{relax}},$$
[19]

where  $\varphi$  determines the contribution of relaxation phenomena to the ionomer water uptake (a value of 0.15 is used for the simulations in this work), and  $s_{relax}$  is a variable accounting for the dynamics of stress relaxation. In particular, its dynamics are assumed to be first order:

$$\dot{s}_{\text{relax}} = -\frac{1}{\tau} (s_{\text{relax}} - \varphi \lambda_{\text{eq}}),$$
 [20]

where  $\lambda_{eq}$  is the equilibrium water content given in Table III and  $\tau$  is the relaxation time constant defined as:

$$\tau = \exp(2 + 0.2\lambda).$$
 [21

Note that the time constant was chosen to vary with the ionomer 258 water content in accordance with evidence in the literature for this 259 dependence.<sup>37</sup> Moreover, the stress relaxation is supposedly a ther-260 mally activated process.<sup>34,43</sup> Therefore, it would be reasonable to as-261 sume an Arrehnius type temperature dependence for the associated 262 263 time constant, which is not included here. Moreover, the effects of compressive stresses on membrane water uptake,<sup>40,44</sup> and the con-264 tentiously debated discrepancy between water uptake by ionomer thin 265 film and bulk ionomer<sup>36,37</sup> are not taken into account in the model. 266 Future parametric studies should aim at investigating these effects 267 along with the effects of changes to the relaxation model parameters 268 to understand their impact on the overall dynamic response of the cell. 269

Catalyst layer model.—Conventional catalyst layers of PEM fuel 270 cells consist of Pt catalyst particles dispersed on ionomer bound car-271 bon primary particles. The Pt particle size is in the range of 2-15 nm, 272 while the primary carbon particles may have sizes of up to 80 nm based 273 on the type of carbon support used. Early models of PEM fuel cells 274 regarded CLs as interfaces with no consideration of their structural 275 features. However, the significance of these structural features to the 276 cell performance has been established. A particularly important issue 277 that has resulted in significant efforts in CL modeling is the additional 278 transport resistance observed at lowered Pt loading or with high loaded 279 electrodes after degradation inducing cycles.45,46 The experimental ap-280 proach has utilized limiting current measurements with varying gas 281 composition and/or pressure to separate the pressure dependent and 282

pressure independent transport resistances.<sup>47</sup> The transport resistance 283 in the CL is almost entirely independent of pressure and can be esti-284 mated with such limiting current measurements. Using this approach, 285 it has been found that the CL transport resistance increases at lower Pt loadings<sup>48–53</sup> and this increase is strongly dependent on the available 287 Pt area for reaction. Therefore, the resistance appears to be due to 288 the increased flux near each active site at lower loadings.<sup>1</sup> Tempera-289 ture sensitivities were used to determine the contributions of Knudsen 290 diffusion and permeation through the ionomer thin film to the elec-291 trode transport resistance.<sup>54</sup> The ionomer thin film was found to be the 292 dominant cause of transport resistance in the CL. More recently, the 293 impact of carbon support and its porous structure on the local reactant 294 and bulk protonic transport resistances have been highlighted.<sup>2,55</sup> Par-295 ticularly, micro-pores with an opening smaller than 2 nm have been found to limit the reactant access to the Pt deposited inside the carbon pores. Despite such efforts, the root cause of the increased resistance 298 remains largely unknown.<sup>56</sup> Several hypotheses have been made, but 299 neither has been thoroughly validated. 300

Numerous models have been proposed to investigate the distri-301 bution of critical variables throughout the CLs and unveil the cause 302 of increased transport resistance at lower loadings. The agglomerate 303 model has been the most popular one for this purpose. In this model, 304 the Pt particles are assumed to be dispersed on the primary carbon 305 particles, many of which are assumed to aggregate during the fab-306 rication process to form larger agglomerates covered by an ionomer 307 thin film. The pore space in the CL is divided into two parts: the pri-308 mary pores between carbon particles in each agglomerate, and the 309 secondary pores formed between the agglomerates. Several variations 310 of this model have been proposed where the intra-agglomerate space is 311 either filled with water (i.e., water-filled agglomerates)<sup>57,58</sup> or ionomer 312 (i.e., ionomer-filled agglomerates).<sup>59,60</sup> 313

Initially, a wide range of agglomerate sizes (100-1000 nm) had 314 been used and significant variations of the ionomer film thickness 315 (10-100 nm) had been reported to match the experimental data.<sup>61,62</sup> 316 Cetinbas et al. have developed a hybrid method for reconstruction of 317 CL microstructure<sup>63,64</sup> and reported an agglomerate size distribution 318 between 25 to 300 nm with most agglomerates having a radius in the range of 75 to 200 nm.<sup>64</sup> Furthermore, the upper limit of the modeling 320 values for the agglomerate size and film thickness is not corroborated 321 by microscopy studies.<sup>65</sup> Therefore, the validity of this structural pic-322 ture has come under further scrutiny. In light of these experimental 323 observations, some have argued that the agglomerates probably do 324 not exist and have proposed homogeneous models for the electrode.62 325 Others have continued to use the agglomerate models with agglom-326 erate radii as small as 40 nm.<sup>22,66</sup> which is essentially the size of a 327 carbon primary particle. Of particular interest is the work by Nissan 328 researchers<sup>66</sup> who showed that the conventional flooded-agglomerate 329 model is not capable of reproducing experimental results with small 330 agglomerate size and partial ionomer coverage. They modified the 331 model to incorporate transport resistance near the electrochemical sur-332 face and showed that the modified model successfully predicted the 333 experimental trends. Generally, more recent models rely on interfacial 334 resistance at either the ionomer-gas or the Pt-ionomer interface or both to reproduce experimental transport resistance values. Jinnouchi et al. 336 used molecular dynamics simulations to associate such resistance with 337 a dense ionomer layer near the Pt surface.<sup>67</sup> Overall, attributing the ad-338 ditional resistance to interfacial phenomena has become increasingly 339 common in the literature. 340

Despite its commonality, the interfacial resistance has not been 341 experimentally verified. In fact, Liu et al. measured transport re-342 sistance in ionomer thin films and found no evidence of interfa-343 cial resistance when 3D diffusion was taken into account.<sup>68</sup> The un-344 certainty surrounding ionomer thin film properties, such as water 345 uptake,<sup>36,69–71</sup> ionic conduction,<sup>72</sup> and gas permeation,<sup>65</sup> which can 346 be significantly affected by confinement and substrate interactions,<sup>73</sup> 347 has further contributed to the ambiguity of the source of this increased 348 resistance. Some recent works have disputed the interfacial resistances 349 or downplayed its significance. Darling has proposed an agglomerate 350 model in which the increased resistance is mostly attributed to the

spherical diffusion through the agglomerate.<sup>74</sup> Others have investi-352 gated the inhomogeneity of mass fluxes near the Pt particles in ag-353 glomerates and the overlap between several agglomerates as possible 354 culprits.<sup>75,76</sup> Most recently, Muzaffar et al.<sup>77</sup> have investigated litera-355 ture data with a previously developed agglomerate model78 and found 356 that the reduction in Pt loading probably leads to higher levels of flood-357 ing in both the CL and GDL due to reduced vaporization capability of 358 the CL with decreased thickness. They also elevated the fact that both 359 experimental<sup>79</sup> and numerical studies<sup>80,81</sup> show only partial coverage 360 of catalyst particles with ionomer, leaving an alternative transport path 361 for oxygen to reach the active sites without facing the interfacial re-362 sistance at the Pt-ionomer interface. Therefore, they concluded that 363 the increased transport resistance may be attributable to reduced oxy-364 gen diffusivity due to pore blocking effects of liquid water and the 365 interfacial resistance does not play a significant role. The importance 366 of water management in successful use of low loaded electrodes was 367 also pointed out by Srouji et al.82 368

The preceding literature review shows that the structural picture of 369 the electrodes and the understanding of the factors that contribute to 370 the transport resistance are still incomplete. Therefore, further model 371 development and experimental investigations are required. Neverthe-372 less, it should be noted that for the purpose of a full cell simulation, 373 most of the proposed models can be parameterized to capture the lo-374 cal oxygen transport resistance, which is the most critical outcome 375 of such models. Moreover, Kulikovsky has demonstrated that under 376 certain conditions that are most relevant to typical fuel cell operation, 377 the agglomerate model is not required.<sup>83</sup> Therefore, unless the goal 378 of the model is to investigate different electrode designs at the nano-379 scale, a homogeneous model will be sufficient. Here, we use the model 380 proposed by Hao et al.,<sup>62</sup> which was shown to appropriately capture 381 382 the increased resistance at lower loadings. The model achieves this by assuming full ionomer coverage and introducing rather significant 383 interfacial resistances, which, in light of the above discussion, are dis-384 putable. Nevertheless, it is the general trend of the variations in the 385 transport resistance that is required for our purposes. The model is 386 briefly presented here and the reader is referred to the original publi-387 388 cation for further details.62

The model assumes Pt particles are deposited on primary carbon 389 particles that are covered by an ionomer thin film. Liquid water in the 390 pores of the electrode forms a thin film on top of the ionomer. This 391 structural picture is used to derive the volume fraction of each phase 392 393 (Pt, carbon, ionomer, and pore space) in both the anode and cathode 394 CLs. However, the local transport resistance to hydrogen in the anode CL is assumed negligible and the calculations are only carried out for 395 oxygen transport resistance. The oxygen in the pore space has to (1) 396 dissolve in water, (2) diffuse through the water film, (3) dissolve in 397 ionomer, (4) diffuse through the ionomer film, and (5) be adsorbed 398 on the Pt surface. The model does not account for spherical diffusion, 399 400 but uses instead a 1D diffusion equation to calculate the local flux of 401 oxygen:

$$N_{O_2} = \frac{c_{O_2}^{\text{pore}} - c_{O_2}^{\text{Pt}}}{R_{\text{T}}},$$
[22]

where  $N_{O_2}$ ,  $c_{O_2}^{\text{pore}}$ , and  $c_{O_2}^{\text{Pot}}$  are the oxygen flux near the Pt surface, oxygen concentration in the CL pore space, and its concentration at the Pt surface, respectively.  $R_{\text{T}}$  is the total local transport resistance:

$$R_{\rm T} = R_{\rm w,int} + \frac{\delta_{\rm w}}{D_{O_2,\rm w}} + R_{\rm ion,int} + \frac{\delta_{\rm ion}^{\rm eff}}{D_{O_2,\rm ion}} + R_{\rm Pt,int}^{\rm eff}, \qquad [23]$$

where the first, third, and last terms describe the interfacial resistances 405 at the liquid film, ionomer film, and Pt surfaces, respectively. The 406 fractional terms denote diffusional resistance through the water and 407 ionomer thin films. A key argument made in developing the model 408 is a geometrical one, where an effective diffusion length through the 409 410 ionomer is calculated based on the effective surface area of a single Pt particle and the effective ionomer surface area available for that 411 particle: 412

$$A_{\rm Pt}^{\rm eff} = 4\pi r_{\rm Pt}^2 \theta_{\rm Pt}, \qquad [24]$$

$$A_{\rm ion}^{\rm eff} = \frac{4\pi (r_{\rm c} + \delta_{\rm ion})}{n_{\rm Pt}},$$
 [25]

where  $r_{\rm Pt}$  and  $r_{\rm c}$  are the Pt and carbon primary particle radii, respectively,  $\theta_{\rm Pt}$  denotes the fraction of Pt surface not covered with oxide species (see Reaction kinetics Sec.),  $\delta_{\rm ion}$  is the ionomer film thickness, and  $n_{\rm Pt}$  is the number of Pt particles deposited on a single carbon particle. The effective ionomer film thickness is then calculated by: 413

$$\delta_{\rm ion}^{\rm eff} = \frac{A_{\rm ion}^{\rm eff}}{A_{\rm Pt}^{\rm eff}} \delta_{\rm ion}.$$
 [26]

The same scaling factor is used to scale the interfacial resistance at 418 the Pt surface: 419

$$R_{\rm Pt,int}^{\rm eff} = \frac{A_{\rm ion}^{\rm eff}}{A_{\rm Pt}^{\rm eff}} R_{\rm Pt,int}.$$
 [27]

This scaling is one of the most important features of the model as it 420 compensates for the fact that 3D spherical diffusion is neglected, and 421 allows for the effects of high fluxes near sparsely deposited Pt particles 422 to be captured by the model. It is imperative, however, to be cautious 423 and not put too much emphasis on the source of the local transport 424 resistance in this model. As mentioned earlier, the electrode structure 425 assumed in this model is contentious. Nevertheless, on a macro-level, 426 the predictions match the experimental observations, which is the most 427 important aspect for full cell simulations. 428

Finally, another important assumption made in the model is that the interfacial resistances are proportional to the diffusional resistances. This is done due the lack of measured data for the interfacial resistances at various interfaces. In particular, three fitting parameters  $k_1$ ,  $k_2$ , and  $k_3$  are introduced:

$$R_{\text{ion,int}} = k_1 \frac{\delta_{\text{ion}}}{D_{O_2,\text{ion}}}, R_{\text{Pt,int}} = k_2 \frac{\delta_{\text{ion}}}{D_{O_2,\text{ion}}}, R_{\text{w,int}} = k_3 \frac{\delta_{\text{w}}}{D_{O_2,\text{w}}}$$
 [28]

Therefore, the various terms contributing to the transport resistance 434 are identified. Noting that:

$$N_{O_2} = -\frac{i_{\text{ORR}}}{4Fa_c x},$$
[29]

where  $i_{ORR}$  is the volumetric ORR current density,  $a_c$  is the volumetric surface area of the ionomer, and x is the number fraction of carbon supported Pt particles (used to model the effects of catalyst dilution by bare carbon), Equation 22 can be written as:

$$R_{\rm T} = \frac{4Fa_c x (c_{O_2}^{\rm pore} - c_{O_2}^{\rm Pt})}{i_{\rm ORR}}.$$
 [30]

This algebraic equation can be solved numerically to find the oxygen 440 concentration at the Pt surface. It is worth pointing out that an ana-441 lytical solution is possible in the case that reaction order is assumed 442 to be unity for ORR.<sup>62</sup> Nevertheless, such an assumption may be un-443 realistic and in some cases inconsistent with the ORR kinetics model 444 (see Reaction kinetics sec.). Therefore, we use the numerical solu-445 tion with no assumption on the reaction order for ORR to avoid such 446 inconsistencies. 447

It is also important to have a consistent set of structural parameters for the CLs. In particular, volume fraction of different phases ought to be known. These volume fractions can be calculated as follows:<sup>60,63</sup>

$$\varepsilon_{\rm c} = \frac{1}{\rho_{\rm c}} \frac{L_{\rm c}}{\delta_{\rm CL}},\tag{31}$$

$$\varepsilon_{\rm Pt} = \frac{1}{\rho_{\rm Pt}} \frac{L_{\rm Pt}}{\delta_{\rm CL}},$$
[32]

$$\varepsilon_{\rm ion} = (I/C)\varepsilon_{\rm c} \frac{\rho_{\rm c}}{\rho_{\rm ion}} \left(1 + \frac{M_{H_2O}\rho_{\rm ion}}{\rho_l EW}\lambda\right),$$
[33]

where  $\varepsilon_i$  is the volume fraction of *i*,  $L_{c/PT}$  is the carbon/Pt loading, 451  $\rho_i$  is the density of *i*,  $\delta_{CL}$  is the CL thickness, and (I/C) denotes the 452 ionomer to carbon ratio. The remaining CL volume constitutes its pore 453 space ( $\varepsilon_{CL} = 1 - \varepsilon_c - \varepsilon_{Pt} - \varepsilon_{ion}$ ). Finally, the ionomer and liquid water film thicknesses are given by:

$$\delta_{\rm ion} = r_{\rm c} \left[ \left( \frac{\varepsilon_{\rm ion}}{\varepsilon_{\rm c}} + 1 \right)^{(1/3)} - 1 \right], \qquad [34]$$

$$\delta_{\rm w} = \left[ s \varepsilon_{\rm CL} \left( \frac{r_{\rm c}^3}{\varepsilon_{\rm c}} \right) + (r_{\rm c} + \delta_{\rm ion})^3 \right]^{(1/3)} - (r_{\rm c} + \delta_{\rm ion}).$$
 [35]

<sup>456</sup> This completes the CL model used in this work. The reader is referred to<sup>62</sup> for further details about this model. As for the parameter values, an *I/C* ratio of 1.1 and an electrochemically active area (ECSA) of 65  $m_{Pt}^2/gr_{Pt}$  are assumed for both anode and cathode CLs. The anode Pt loading is assumed to be 0.1 mg/cm<sup>2</sup> with a Pt/C weight percentage of 30%, while the cathode Pt loading is changed between 0.4 and 0.05 mg/cm<sup>2</sup>, considering a Pt/C weight percentage of 40% in all cases.

**Reaction kinetics.**—Accurate models for the HOR and ORR half reactions are required for the model. HOR is known to have facile kinetics and does not result in significant performance loss under most typical conditions. Therefore, it is typically described using a simplified Butler-Volmer kinetics model. Here, we use the dual-pathway kinetics model proposed by Wang et al.,<sup>84</sup> where the volumetric current density is found by:

$$i_{\text{HOR}} = a_{\text{Pt}} \frac{c_{H_2}}{c_{H_2}^{\text{ref}}} \bigg[ i_{0T} \left( 1 - \exp(-\frac{2F\eta_{\text{HOR}}}{\vartheta RT}) \right) + i_{0H} \left( \exp\left(\frac{F\eta_{\text{HOR}}}{\vartheta RT}\right) - \exp(-\frac{F\eta_{\text{HOR}}}{\vartheta RT} - \frac{F\eta_{\text{HOR}}}{2RT}) \right) \bigg], \quad [36]$$

<sup>470</sup> where  $a_{\text{Pt}}$  is the active volumetric surface area of Pt,  $i_{0T}$  and  $i_{0H}$  are <sup>471</sup> the exchange current densities for the Tafel and Heyrovsky pathways, <sup>472</sup> respectively,  $\vartheta$  is a potential constant, and  $\eta_{\text{HOR}}$  is the anode overpo-<sup>473</sup> tential.

The ORR kinetics are more complicated than the HOR and require further attention. Again, various forms of the Butler-Volmer model have been used to describe the ORR kinetics. More recently, the effects of surface coverage have been considered to derive a modified Tafel expression:<sup>85</sup>

$$i_{\text{ORR}} = -i_{0,\text{ca}} a_{\text{Pt}} (1 - \theta_{\text{PtO}}) \left( \frac{c_{O_2}^{\text{Pt}}}{c_{O_2}^{\text{ref}}} \right)^{\gamma_{\text{ca}}} \exp\left[ -\frac{\alpha_{\text{ca}}}{RT} F \eta_{\text{ORR}} - \frac{\omega \theta_{\text{PtO}}}{RT} \right],$$
[37]

where  $i_{0,ca}$ ,  $\alpha_{ca}$ ,  $\eta_{ORR}$ ,  $\gamma_{ca}$ , are the cathode exchange current density, 479 transfer coefficient, ORR overpotential and reaction order, respec-480 tively, and  $\omega$  denotes the energy parameter for the Temkin isotherm. 481 The model results in a potential dependent Tafel slope. The oxide 482 coverage is potential and time dependent as cyclic voltammograms 483 (CV) show considerable difference between the anodic and cathodic 484 sweeps.<sup>85</sup> A simple sigmoidal curve can be fitted to steady-state 485 measurements:62 486

$$\Theta_{\rm PtO} = \frac{1}{1 + \exp\left[22.4(0.818 - E)\right]},$$
 [38]

<sup>487</sup> where *E* is the cathode potential vs. reference hydrogen electrode <sup>488</sup> (RHE).

A more elaborate model for ORR kinetics is the double trap (DT) 489 model originally proposed by Wang et al.<sup>86,87</sup> The model includes 490 two pathways for oxygen adsorption: a reductive adsorption (RA) and 491 a dissociative adsorption (DA) pathway. The latter is followed by a 492 reductive transition (RT) to adsorbed OH. In either case, the adsorbed 493 OH is desorbed through a reductive step (RD) to form water. The 494 original formulation neglected the reverse RD step and concluded that 495 ORR activity is limited by the desorption of strongly adsorbed O and 496 OH. Moore et al.<sup>88</sup> modified the model by including the backward 497 reactions and refitting the parameters and found ORR to be adsorption 498 limited. Moreover, the coverage of adsorbed species predicted by the 499 modified model tends to zero at high overpotentials, whereas a constant 500

nonzero value was predicted with the original model.<sup>86</sup> The modified model is in better agreement with the experimental coverage values reported by Subramanian et al.<sup>85</sup> 503

Other modifications to the DT model have been proposed as well. 504 Markiewicz et al.<sup>89</sup> added two elementary reactions to the model: a 505 reductive addition of a proton to oxygen molecule, producing an ad-506 sorbed protonated superoxide, and another reductive addition of proton 507 followed by dissociation into adsorbed OH. Through these modifica-508 tions, they reported a significant coverage of Pt sites by adsorbed HO<sub>2</sub> 509 species at high overpotentials. More recently, Jayasankar et al.90 re-510 placed the DA step with an associative adsorption (AA) into adsorbed 511 HO<sub>2</sub>, which is followed by dissociative transition steps into adsorbed 512 O and OH. They have also extended the model to include oxide growth 513 mechanisms. Their results corroborate those of Markiewicz et al., as 514 they also find an increase in  $HO_2$  coverage at high overpotentials. 515 This can have significance for studies with low loaded catalysts, as 516 it provides another possible explanation for the reduced performance 517 observed experimentally. 518

In this work, we use the modified DT model proposed by Moore,<sup>88</sup> as it has been parameterized for fuel cell polarization curves and used by others in full cell simulation.<sup>19,22</sup> In this model, the ORR current can be described as the current from a single RD step: 522

$$i_{\text{ORR}} = a_{\text{Pt}} i^* \left[ \exp(-\frac{\Delta G_{\text{RD}}^*}{kT}) \theta_{\text{OH}} - \exp(-\frac{\Delta G_{-\text{RD}}^*}{kT}) (1 - \theta_{\text{O}} - \theta_{\text{OH}}) \right],$$
[39]

where  $i^*$  is a reference prefactor (similar to the exchange current density in the Butler-Volmer model), k is the Boltzmann constant,  $\Delta G^*_{\text{RD}}$ and  $\Delta G^*_{-\text{RD}}$  are the potential dependent activation energies of the forward and backward RD step, respectively, and  $\theta_i$  denotes the coverage of species *i*. The expressions for the activation energies and species coverage can be found in Ref. 88

The DT model is used for simulation case studies. However, when comparing with experimental data, we have chosen to work with the Tafel model in Equation 37 as its parameters are more intuitive and allow for easier parameterization of the model and can also reproduce the kinetic current predicted by the DT model with a varying reaction order.<sup>91</sup>

It should be noted that several effects have been neglected to sim-535 plify the model and avoid ambiguity in the results. First, the steady-536 state coverage profiles are used in the kinetic equations and the dy-537 namics of oxide growth are ignored. These dynamics can be very slow 538 as observed in low frequency impedance spectra<sup>92,93</sup> and coulometric 539 measurements.94 Such dynamics can result in a hysteresis loop in the 540 Tafel plot obtained through CVs even when a low potential prehold 541 is used to reduce the oxide layer.<sup>95</sup> Therefore, oxide growth dynamics 542 can have a profound impact on current transients, especially at higher 543 potentials. However, including these dynamics adds to the complex-544 ity of a model, whose main focus is on mass transport and hydration 545 effects. Hence, the oxide growth dynamics are neglected in this work. 546 It should also be pointed out that the ORR activity is shown to be af-547 fected by presence of ionomer.<sup>96–98</sup> This effect is not explicitly taken 548 into account in the current model, since doing so will add to the uncer-549 tainty in the parameter set. Nevertheless, the exchange current density 550 values (or the reference prefactor in the case of the DT model) used 551 are supposed to capture this reduced activity. 552

Finally, the dependence of ORR kinetics on the relative humidity 553 (RH) is also neglected in this work. This effect was reported by Xu 554 et al.<sup>99</sup> to be significant, resulting in up to 100 mV difference at dry 555 condition, even when protonic resistance in the CL was taken into 556 account.<sup>100</sup> However, work by GM shows much less pronounced effects of RH on ORR kinetics.<sup>101,102</sup> This discrepancy in the reported 557 558 values could also be partly due to the effects of RH on water oxidiza-559 tion and subsequent catalyst poisoning.<sup>103</sup> The accessibility of Pt in the 560 inner pores of porous carbon support is also shown to decrease at low 561 RH values, which can result in loss of electrochemically active area.<sup>104</sup> 562 Regardless, the RH effects on ORR kinetics may be included in the 563 model by scaling the exchange current density in the BV model  $(i_0)$  or 564

the reference prefactor in the DT model  $(i^*)$ . A scaling factor varying 565 linearly with ionomer water content has been used for this purpose 566 by Gerteisen et al.9 More recently, a scaling factor that changes with 567 ionomer water content in a sigmoidal fashion has been proposed,<sup>42</sup> 568 which is in a better agreement with the experimental trends. Such 569 scaling factors may be treated as fitting parameters in performance 570 models to enhance the predictive capabilities. Nevertheless, we have 571 chosen to leave this factor out, in order to simplify the model and allow 572 for a clearer understanding of the transport phenomena. 573

Mixed wettability model for porous layers .- The main goal of 574 a model for the porous layers is to define a mapping from operat-575 ing conditions and material properties to effective charge, heat, and 576 mass transport properties. This problem has been studied on a variety 577 of length scales ranging from microscopic lattice Boltzmann<sup>16</sup> and 578 pore network modeling studies<sup>105</sup> to macroscopic models with empir-579 ical relationships.<sup>106</sup> The microscopic models, along with significant 580 advances in experimental techniques to characterize porous layers at 581 higher resolutions, can be used to develop a fundamental understand-582 ing of various transport phenomena in such layers. Even though such 583 models cannot be used in full cell simulations due to significant com-584 putational requirements, they can be utilized to refine the macroscopic 585 models of lower complexity. 586

Understanding the water phase change process and its transport 587 through the porous layers is also of crucial importance. To this end, 588 one particular model for porous layers that has gained more popularity 589 in recent years is the mixed wettability pore size distribution (PSD) 590 model that was proposed by Weber et al.<sup>107</sup> The model represents the 591 pores as bundles of cylindrical capillaries that are randomly joined 592 together using log-normal distributions. The key feature of the model 593 is that it accounts for mixed wettability of the layers, which is ignored 594 for the most part in many of the macroscopic models. Therefore, both 595 hydrophilic (HI) and hydrophobic (HO) pores are considered to de-596 597 rive PSDs and contact angles. The original implementation by Weber et al.<sup>107</sup> assumed the HI and HO PSDs to be identical. Furthermore, a 598 two-point discrete contact angle distribution was assumed. A similar 599 600 model was used by Eikerling for transport studies in the cathode CL, although he did not consider mixed wettability, choosing to investigate 601 the PSDs due to primary and secondary pores in the CL.<sup>108</sup> More re-602 cently, Villanueva studied effects of different PSDs for the HI and HO 603 pores.<sup>20</sup> However, recent implementation of the model in a full cell 604 simulation by the same group seems to be using similar PSDs for both 605 HI and HO pores.<sup>19</sup> It is worth mentioning that this model was further 606 extended by Weber to include a continuous contact angle distribution 607 (CAD).<sup>109</sup> This extension was shown to improve the predictive capa-608 bilities as well as the numerical robustness of the model for use in full 609 cell simulations. A continuous CAD with a discrete PSD was used by 610



Figure 2. Water retention curves used in this work for the different porous layers.

Cheung et al.<sup>110</sup> Nevertheless, adoption of the continuous CAD has remained minimal in the literature due to unavailability of CAD for most of the porous layers of interest.

This work utilizes the mixed wettability model with an implementation that allows for different PSDs to be used for HI and HO pores and also includes the continuous CAD. However, we obtain PSDs and contact angles from the literature, and therefore our implementation coincides with the original implementation by Weber et al.<sup>107</sup> when continuous CAD is not available.

The model equations can be found in the literature<sup>20,109</sup> and are 620 omitted here for space considerations. The inputs to the model include 621 the PSDs, the fraction of HI pores, and CADs (currently two-point 622 discrete CADs are used). The model is used to obtain water retention 623 curves (liquid saturation vs. capillary pressure), relative permeabilities 624 of the gas and liquid phases, Knudsen radii, and liquid-gas interfacial 625 area available for phase change in the CLs, MPLs, and GDLs. The 626 model calculations are conducted off-line and the resulting curves 627 are used in the full cell simulations using cubic-spline fitting. The 628 model parameters used for the simulation case studies in this work 629 are presented in Table IV and the resulting water retention curves 630 are shown in Fig. 2. The CL parameters used in this study are those 631 reported by Mashio et al.<sup>111</sup> who obtained experimental PSDs through 632 nitrogen adsorption. In particular, the PSD for a CL with graphitized 633 Ketien Black carbon support and an ionomer to carbon ratio of 0.9 634 is used here. The MPL and GDL PSDs are those reported by Zhou 635

•		Value			
Parameter		CL (GKB) <sup>111</sup>	MPL (SGL 24) <sup>23</sup>	GDL (SGL 24) <sup>19</sup>	
Characteristic pore radii [µm]	$r_1$	0.002	0.072	14.2	
	$r_2$	0.006	0.125	34	
	$r_3$	0.025	2	-	
	$r_4$	0.080	_	-	
Characteristic pore widths	<i>s</i> <sub>1</sub>	0.60	0.35	1.00	
-	<i>s</i> <sub>2</sub>	0.60	0.50	0.35	
	\$3	0.45	0.90	-	
	<i>S</i> 4	0.80	_	-	
Characteristic pore fractions	$f_1$	0.05	0.45	0.28	
-	$f_2$	0.12	0.10	0.72	
	f3	0.73	0.45	-	
	$f_4$	0.10	_	-	
Hydrophilic volume fraction	$F_{\rm HI}$	0.30	0.05	0.08	
Hydrophilic contact angle	$\theta_{\rm HI}$	55	84	70	
Hydrophobic contact angle	$\theta_{HO}$	91	110	122	

# Table IV. Mixed wettability model parameters.

636 et al.<sup>19,23</sup> for SGL 34 series that are also applicable for the SGL 24 637 series used in this work.

It should be noted that, as has been shown by Zenyuk et al.,<sup>17</sup> 638 the GDL PSD changes with compression. Therefore, it seems rea-639 sonable to use a PSD corresponding to higher compression under the 640 land compared to the one used under the channel. However, using the 641 PSDs that were reported for SGL series by Zenyuk et al. under various 642 compressions,<sup>17</sup> we found that the effective transport properties of in-643 terest show little change with the PSD variations at the compression 644 levels of interest (1 to 1.5 MPa). Therefore, the changes in the PSD 645 with compression under the land are ignored in this work. Finally, as 646 it has been alluded to by Weber,<sup>109</sup> the bundle of capillaries model 647 breaks down for wide PSDs, which in turn results in very low relative 648 permeabilities predicted by the model. We have found this to be es-649 pecially problematic for the MPL. Therefore, a 5-th order power law 650 is used to estimate the liquid and gas phase relative permeabilities for 651 the MPL. 652

Calculation of effective properties .--- To complete the model for-653 mulation, effective properties, such as gas diffusivity and thermal con-654 ductivity values are needed. Some of the layers demonstrate rather 655 considerable anisotropy due to their heterogeneous structure, which 656 should be taken into account. Furthermore, the effects of nonuniform 657 compression under the channel and lands should be considered to ob-658 tain an accurate in-plane distribution of the variables of interest.<sup>40,112</sup> 659 Accordingly, we have carefully examined the literature for the reported 660 values of such transport properties. When applicable, the land-channel 661 variations in parameter values are applied in a continuous fashion us-662 ing sigmoid functions. This is in better agreement with the observed 663 pressure distribution and also simplifies numerical convergence. 664

In this work, we use SGL 24BC and Nafion 211 as the diffusion 665 media and membrane, respectively. These materials are chosen due to 666 their standard application in the fuel cell literature and an abundance 667 of experimental characterization data available for them. The layer 668 thickness and porosities are listed in Table V. Note that a compressed 669 GDL thickness is assumed based on a compressive load of 1 MPa, 670 which is expected to result in a strain of about 0.2.<sup>115</sup> While a uniform 671 thickness is used for both the channel and land locations, the collapse 672 of pore space is applied to the land area, where a reduced porosity 673 of 0.69 is used for the GDL. The CL, and MPL are assumed to be 674 incompressible. Furthermore, note that Nafion 211 has no reinforce-675 ment, yielding  $\varepsilon_{ion} = 1$  in the membrane region. Finally, it should 676 be pointed out that an intermediate composite region is believed to 677 exist between the MPL and GDL with transport properties that are 678 considerably different from those of either layers. Since the proper-679 ties of this intermediate region are not well known, it is not explicitly 680 modeled in this work. The material property variations between adja-681 cent layers are taken into account using smooth sigmoid functions to 682 improve convergence. A detailed discussion of the effective transport 683 properties used in the simulation studies follows. 684

• Effective diffusivity - In calculating the diffusivity of species *i*, contributions from both molecular and Knudsen diffusion are taken into account:

$$D_{i} = \left(\frac{1}{D_{\mathrm{Kn},i}} + \frac{1}{D_{\mathrm{mix},i}}\right)^{-1},$$
 [40]

where  $D_{\mathrm{Kn},i}$  is the Knudsen diffusivity and  $D_{\mathrm{mix},i}$  is the molecular diffusion coefficient. Knudsen diffusivity is given by:

$$D_{\mathrm{Kn},i} = \frac{2r_{\mathrm{Kn}}}{3} \sqrt{\frac{8RT}{\pi M_i}},$$
[41]

where  $r_{\text{Kn},i}$  is the Knudsen radius of the porous layer, which is obtained from the mixed wettability model in this work, and  $M_i$  is the molecular mass of species *i*. The molecular diffusion coefficient is given by:<sup>116</sup>

$$D_{\min,i} = \left(\sum_{j=1,\,j\neq i}^{N_{s}} \frac{x_{j}}{D_{i,j}}\right)^{-1},$$
[42]

where  $x_j$  is the molar fraction of species j and  $D_{i,j}$  denotes the binary diffusion coefficient of species i in j.<sup>117</sup> With  $D_i$  available, the effective diffusivity is calculated as

$$D_i^{\text{eff}} = f(\varepsilon)g(s)D_i, \qquad [43]$$

which accounts for the tortuous pathway for gas transport inside the porous layers as well as the pore blocking effects of liquid water accumulation. Several microstructure-property functional relationships have been proposed for both  $f(\varepsilon)$  and g(s) in the literature, most of which take the form of a power law.<sup>118,119</sup> Zamel et al. provide a good review of the relevant literature on this topic.<sup>120</sup> In this work, since we consider SGL 24BC as the diffusion medium, we have used the following relationship for  $f(\varepsilon)$  recently suggested by Holzer et al.:<sup>121</sup> 703

$$f(\varepsilon)_{\rm IP} = 1.074\varepsilon - 0.335,$$
[44]  
$$f(\varepsilon)_{\rm TP} = 0.906\varepsilon - 0.252,$$
[45]

where the subscripts IP and TP stand for the in-plane and through-704 plane directions, respectively. These relationships were suggested for 705 SGL 25BA series, which do not have the MPL coating. Due to lack of 706 data, the same relationships are used for the MPL. The reader should 707 be cautious in applying these relationships to other types of diffusion 708 layers, as they are explicitly derived for SGL carbon papers. Typi-709 cal power laws are better applicable in general and are suggested for 710 different types of diffusion layers. 711

As for g(s), the following relationships are used:<sup>118</sup>

$$g(s)_{\rm IP} = (1-s)^{2.25},$$
 [46]

712

$$g(s)_{\rm TP} = (1-s)^{2.15}.$$
 [47]

These relationships were determined for Toray carbon papers and are 713 used here due to lack of data for SGL series. It should be noted that 714 the nearly isotropic relationships were developed for local conditions, 715 i.e., domains with flat saturation distributions.<sup>122</sup> In contrast, Niu et al. 716 found a more significant difference between the liquid saturation ef-717 fects on the in-plane and through-plane diffusion coefficients, fitting 718 the results with cubic and quadratic power laws, respectively.<sup>119</sup> There-719 fore, such functional relationships should not be taken for granted. 720 Rather, we believe that it is a better practice to leave the order of de-721 pendence as a fitting parameter when experimental performance data 722 are available. 723

Finally, the correction factor for effective diffusivity calculations 724 in the CL is calculated as follows:<sup>19,108</sup> 725

$$f(\varepsilon)g(s) = (1-s)^2 \left(\frac{\varepsilon - \varepsilon_p}{1 - \varepsilon_p}\right)^2 H(\varepsilon(1-s) - \varepsilon_p), \qquad [48]$$

Table V. Thickness and porosity of cell layers.

Layer	Thickness [µm]	Volume Fraction/Porosity [-]
MB	25.4	1
ACL	5 (Pt loading of $0.1 \text{ mg/cm}^2$ )	0.431
CCL	15/7.5/3.75/1.875 (Pt loading of 0.4/0.2/0.1/0.05 mg/cm <sup>2</sup> )	0.479
MPL	60 <sup>113</sup>	$0.6^{114}$
GDL	140	0.8 (Channel) and 0.69 (Land)

<sup>726</sup> where  $\varepsilon_p$  is the percolation threshold, which is assumed to be 0.25 in <sup>727</sup> this work, and *H* is the Heaviside function.

· Absolute permeability - A range of values for absolute gas and 728 liquid permeabilities are reported in the literature. In most of the cases, 729 the absolute permeability of the GDL is found to be on the order of 730 10<sup>-11</sup> m<sup>2</sup>.<sup>123</sup> The MPL permeability values are typically one to two 731 orders of magnitude smaller than those for the GDL.<sup>124</sup> In spite of 732 such measurements, it has been shown that these permeability val-733 ues will result in a negligible pressure drop across the porous layers 734 due to oversimplification of the capillary dominated transport through 735 the use of Darcy's law.<sup>22,125</sup> Therefore, it has been suggested that the 736 experimentally reported values should be reduced by several orders 737 of magnitude to obtain a realistic pressure drop.<sup>22</sup> In addition to these 738 considerations, Holzer et al. recently found that the through-plane per-739 meability values are slightly higher than the in-plane values for SGL 740 25BA GDLs.<sup>123</sup> Taking these into account, the absolute permeabilities 741 assumed in the model are given in Table VI. 742

• Thermal conductivity and heat capacity - There is an exten-743 sive literature on the thermal conductivity of the PEM fuel cell layers 744 through both modeling and experimental means with somewhat scat-745 tered results. In selecting the thermal transport parameters, one has to 746 pay attention to the changes in thermal conductivity with liquid satu-747 ration, in addition to the anisotropy and compression effects. Another 748 difficulty is in distinguishing between the thermal properties of the 749 MPL and the GDL from the data obtained from a composite layer. 750 Here we briefly review the existing literature for SGL papers. 751

One of the earliest works in this area was by Khandelwal et al. 752 who measured the TP thermal conductivities of various cell layers.<sup>126</sup> 753 They reported a value of 0.31 W/( $m \cdot K$ ) for SGL BA series (with no 754 MPL). Unfortunately, they did not report the number specification of 755 756 the GDL. This can bear some significance as the SGL 24 series have more binder that can improve the fiber to fiber contact and increase 757 the thermal conductivity.<sup>127</sup> Nevertheless, this value is well within 758 the range of 0.26-0.37 W/(m  $\cdot$  K) reported by others for the same 759 type of GDL.<sup>127-130</sup> Accordingly, the base value of GDL TP thermal 760 conductivity is set to 0.3 W/( $m \cdot K$ ) under the channel and to 0.45 761 762  $W/(m \cdot K)$  under the land due to the inhomogeneous compression.<sup>130</sup> As for the IP thermal conductivity, a base value of  $12 \text{ W}/(\text{m} \cdot \text{K})$ 763 is used<sup>131,132</sup> for both the channel and land locations as the effect of 764 compression on IP conductivity is assumed to be minimal. 765

For the MPL thermal conductivity, the reported values are far more 766 767 inconsistent than those for the GDL. Such discrepancies stem mostly 768 from unknown contact resistances, uncertainties about the MPL thickness in a combined layer, assumed compressibility or incompressibil-769 ity of the MPL with applied pressure, and the nature of the transi-770 tion region between the MPL and GDL. These have resulted in re-771 ported values for the TP thermal conductivity ranging from 0.035133 772 to  $0.6 \text{ W}/(\text{m} \cdot \text{K})$ .<sup>130</sup> An interesting observation was made by Burheim 773 et al.,<sup>134</sup> who argued that the MPL has a lower thermal conductivity 774 than the GDL (0.08 W/( $m \cdot K$ )), with an intermediate composite re-775 gion between the two layers that has the highest thermal conductivity 776 with an essentially flat temperature distribution. Here we use a value 777 of 0.15 W/( $m \cdot K$ ) for both the channel and land locations. This is 778 based on the assumption of incompressibility of the MPL, which has 779

Table VI. Transport parameters used in the model.

been questioned recently.  $^{134,135}$  Nevertheless, this value is in the range of reported values in the literature. The base value for the IP thermal conductivity of the MPL is chosen to be 3 W/(m  $\cdot$  K) based on the literature.  $^{131}$  783

The reported TP thermal conductivities for the CL range from  $^{764}$  0.04<sup>136</sup> to 0.34 W/(m  $\cdot$  K).<sup>137</sup> In this work, we use the base value of 0.27 W/(m  $\cdot$  K) reported by Khandelwal et al.<sup>126</sup> for both the IP and TP thermal conductivities assuming no anisotropy for the CL.<sup>137</sup>

Liquid accumulation in the pores can alter the thermal conductivity 788 of the porous layers. In this work, we use the following approximation 789 to capture this effect for the TP thermal conductivity of the GDL:<sup>115</sup> 790

$$k_T^{\text{eff}} = k_{T,\text{base}} + 1.44s,$$
 [49]

where  $k_{T,\text{base}}$  is the base value reported in Table VI. For the TP thermal 791 conductivity of other layers (CL and MPL) and the IP conductivity of 792 all porous layers, volume averaging is employed: 793

$$k_T^{\text{eff}} = k_{T,\text{base}} + \varepsilon s k_{T,l}, \qquad [50]$$

where  $k_{T,l} = 0.569 \text{W}/(\text{m} \cdot \text{K})$  is the thermal conductivity of liquid 794 water.

Finally, the thermal conductivity of the membrane in both the IP 796 and TP directions is given by:<sup>138</sup> 797

$$k_{T,\text{mb}}^{\text{eff}} = 0.177 + 3.7 \times 10^{-3} \lambda \quad [W/(m \cdot K)].$$
 [51]

The volumetric specific heat capacities ( $\rho c_p$ ) used in the model are: 798 1.9, 1.562, <sup>10</sup> 1.98, <sup>10,139</sup> and 1.5827<sup>139,140</sup> J/(cm<sup>3</sup>·K) for the membrane, 799 CL, MPL, and GDL, respectively. 800

• Electronic and ionic conductivity - The electronic conductivity of the porous layers should be subject to similar considerations as the thermal conductivity. The values used for the various layers in this work are obtained from the work of Sadeghifar et al.<sup>141</sup> and are listed in Table VI. As for the ionic conductivity of the membrane and the CLs, the conductivity is calculated as:<sup>107</sup>

$$\sigma_2^{\text{eff}} = \varepsilon_{\text{ion}}^{1.5} \cdot 0.35 (f_v - 0.045)^{1.5} \exp\left[\frac{15000}{R} \left(\frac{1}{303.15} - \frac{1}{T}\right)\right].$$
[52]

The debated suppression of ionic conductivity in thin ionomer films <sup>807</sup> is not taken into account in this work.<sup>142</sup> Future work should aim at <sup>808</sup> investigating such effects through parametric studies. <sup>809</sup>

• Evaporation and condensation rates -A value of  $2 \times 10^{-2}$ 810  $mol/(cm^2 \cdot s)$  is used for the condensation rate to avoid the non-811 physical case of oversaturated gas phase.<sup>19</sup> The evaporation rate is 812 set to  $2 \times 10^{-3}$  mol/(cm<sup>2</sup> · s). Even though this value is lower than 813 the condensation rate, it yields rather fast evaporation kinetics, which 814 agrees with the experimental findings of Zenyuk et al.<sup>143</sup> that showed 815 the evaporation to be transport-limited. The discrepancy between the 816 evaporation and condensation rates is corroborated by experimental 817 findings in the literature.<sup>144</sup> Furthermore, the rate of phase change is 818 expected to decline with temperature,<sup>144</sup> which is not taken into ac-819 count in this work. It should be noted that the evaporation rate is a 820 critical parameter and may have a significant impact on water balance 821 in the cell depending on the operating conditions. Future work should 822

		>	Through-Plane			In-Plane	
		CL	MPL	GDL	CL	MPL	GDL
Channel	$K_l^{\rm abs}[\rm cm^2]$	$2 \times 10^{-13}$	$3 \times 10^{-11}$	$4 \times 10^{-9}$	$2 \times 10^{-13}$	$3 \times 10^{-11}$	$3 \times 10^{-9}$
	$K_{\rho}^{abs}[cm^2]$	$2 \times 10^{-12}$	$3 \times 10^{-11}$	$4 \times 10^{-9}$	$2 \times 10^{-12}$	$3 \times 10^{-11}$	$3 \times 10^{-9}$
	$\vec{k_T} \left[ \frac{W}{m \cdot K} \right]$	0.27	0.15	0.3	0.27	3	12
	$\sigma_1[\frac{S}{cm}]$	2	2	6	2	50	51
Land	$K_l^{\rm abs}[\rm cm^2]$	$2 \times 10^{-13}$	$3 \times 10^{-11}$	$4 \times 10^{-9}$	$2 \times 10^{-13}$	$3 \times 10^{-11}$	$3 \times 10^{-9}$
	$K_{\rho}^{abs}[cm^2]$	$2 \times 10^{-12}$	$3 \times 10^{-11}$	$4 \times 10^{-9}$	$2 \times 10^{-12}$	$3 \times 10^{-11}$	$3 \times 10^{-9}$
	$\vec{k_T} \left[ \frac{W}{m \cdot K} \right]$	0.27	0.15	0.45	0.27	3	12
	$\sigma_1[\frac{S}{cm}]$	2	2.5	9	2	50	51

aim at a sensitivity analysis for this parameter to better understand its impact on the performance in the two phase regime.

Boundary conditions.—The model boundary conditions (BCs) 825 are given in Table VII, where *n* denotes the unit normal vector. Sym-826 metry boundary conditions (i.e., zero flux) are applied at the top and 827 bottom boundaries of the modeling domain shown in Fig. 1. The tem-828 perature BCs include two heat flux BCs at the channel and land loca-829 tions. The channel heat flux corresponds to convective heat transport with the gas stream ( $h_{\text{conv}} = 0.2 \frac{\text{W}}{\text{cm}^2 \cdot \text{K}}$ ), while the land BC accounts for 830 831 the thermal contact resistance  $(R_{T,\text{cont}} = 2 \frac{\text{cm}^2 \cdot \text{K}}{\text{W}})$  between the plate 832 and the GDL. The molar fractions of gas species are also modeled 833 with mass flux BCs at the channel location to account for the con-834 vective mass transport resistance. In the corresponding equation,  $D_{i,i}^{\text{free}}$ 835 denotes the bulk diffusivity of species i in species j, Sh is the dimen-836 sionless Sherwood number (=2.7), and  $D_h$  is the hydraulic diameter 837 of the channel. Dirichlet BCs are used for gas pressures at the channel 838 boundaries. The liquid pressure BC requires further attention. Various 839 types of BCs have been used for this purpose, including Dirichlet BC 840 for liquid saturation or capillary pressure,<sup>145</sup> as well as Neumann type 841 BC.<sup>9</sup> In this work, we use the following BC: 842

$$-\boldsymbol{n} \cdot \left(-\frac{\rho_l K_l^{\text{eff}}}{\mu_l} \nabla p_l\right) = N_l = -k_{l,\text{flux}} s \left[ 0.5 \left( 1 + \tanh\left(\frac{s - s_0}{\sigma_s}\right) \right) \right],$$
[53]

where  $k_{l,\text{flux}}$  is a parameter determining rate of water outflow,  $s_0$  con-843 trols the liquid saturation at which water outflow begins, and  $\sigma_s$  is 844 а dimensionless parameter used to smooth the transition between no 845 flux BC and the outflow BC. Note that the parameter  $s_0$  essentially ac-846 counts for the break-through pressure, which is the capillary pressure 847 required for liquid water to flow out of the porous GDL. The values 848 of the three parameters used in this work are:  $k_{l,\text{flux}} = 8 \times 10^{-4} \frac{\text{g}}{\text{cm}^2 \cdot \text{s}}$ 849  $s_0 = 0.1$ , and  $\sigma_s = 0.01$ . It should be pointed out that this BC can be 850 parameterized to be identical to the BC used by Zhou et al.<sup>19</sup> However, 851 852 it has the advantage that the parameters are more intuitive, which can simplify the parameterization process. 853

Numerical implementation and model validation.—The model 854 is implemented in the commercial finite element software COMSOL 855 Multiphysics 5.3a. A mapped mesh consisting of 5080 quadrilateral 856 857 elements is used throughout the domain with increased mesh density 858 in the membrane and catalyst layers. Furthermore, the mesh density is exponentially increased near the boundaries between adjacent layers to 859 accommodate the different material properties. The backward differ-860 entiation formula (BDF) method is used for time stepping and the max-861 imum time step size is limited to 200 milliseconds. The resulting linear 862 system is solved using the MUMPS direct solver provided in COM-863 864 SOL. To improve the computational efficiency, an under-relaxation scheme is employed, where the value of liquid saturation at the pre-865 vious time step is used to calculate effective properties such as the 866 diffusion coefficients at the current time step. This was achieved us-867 ing the Previous Solution operator in COMSOL 5.3a. In a preliminary 868 study, it was found that the under-relaxation scheme can result in up to 869

five times faster solutions in the two-phase regime. The results for the 340 seconds long simulation case studies in this paper were computed in 5 to 12 hours depending on the condition, with the most difficult cases being the ones where the transition from dry to wet conditions takes a long time. The simulations were run on a desktop computer with a 3.5 GHz processor and 16 GB of RAM.

The model is validated with experimental data by Gerteisen et al.<sup>9</sup> The results can be found in the Supplementary Information accompanying this paper.

### Simulation Case Studies

879

To better understand the transient behavior of the cell, several sim-880 ulations are conducted using the model developed in this work. In 881 particular, the transient performance under a variety of temperature 882 and humidity conditions as well as different Pt loadings in the cath-883 ode CL is investigated. Furthermore, we investigate the cell dynamics 884 under both potential and current control operating modes. The former 885 constitutes running the model with voltage as an input, while the lat-886 ter takes the cell current density as the input. As will be shown, the 887 dynamics of the cell response can be dramatically different depending 888 on the operating condition. All of the simulations in this work were 889 conducted at a pressure of 1.5 bar for both sides. The gas feeds are 890 assumed to be pure hydrogen and air for the anode and cathode sides, 891 respectively. Finally, same RH values are used for both the anode and 892 cathode sides and initial conditions for all simulations are identical. 893

**Potentio-dynamic simulations.** The first set of simulations are those under voltage control or potentio-dynamic mode of operation. Here a voltage profile is applied and the current density is allowed to vary with time. The time varying current density also means that the rate of water production changes with time, which complicates the analysis of the dynamics to some extent. Nevertheless, useful insights can be obtained from these simulations.

The voltage profile for these simulations is shown in Fig. 3. The 901 profile is made up of the following voltage steps: 0.8-0.6 V, 0.6-0.4 V, 902 0.4-0.6 V, and 0.6-0.8 V. Note that the step changes are smooth and 903 happen over a period of 1 second for numerical convergence. This 904 profile allows us to inspect the transients during both load increments 905 and decrements. The 100 second hold time used at 0.6 and 0.4 V 906 does not allow the system to fully reach its steady state conditions. 907 Nevertheless, this hold time is limited due to computational reasons 908 and is long enough for the model to settle to a quasi steady state before 909 another change in the load. 910

Overall, 36 simulations are conducted under the potentio-dynamic 911 mode based on a full factorial design for variations in RH (30, 60, 912 and 90%), operating temperature (40, 60, and 80°C), and cathode Pt 913 loading  $(0.4, 0.2, 0.1, \text{ and } 0.05 \text{ mg/cm}^2)$ . Note that the CL thickness 914 is assumed to scale linearly with the Pt loading. The resulting current 915 density dynamics for all 36 simulations are shown in Fig. 4. The cor-916 responding average water contents in the membrane for all the cases 917 are shown in Fig. 5. Furthermore, for the conditions that result in liq-918 uid buildup in the GDL, the average liquid saturations in the cathode 919

Table VII. Model boundary conditions (\*denotes zero flux BC for the corresponding variable).

Variable	СН	LAND	MPL   CL	CL  MB
φ1	*	an:0, ca: $E_{cell}/i_{cell}$	_	*
φ <sub>2</sub>	_	—	*	_
Т	$-\boldsymbol{n} \cdot (-k_T^{\text{eff}} \boldsymbol{\nabla} T) = h_{\text{conv}}(T_{\text{cell}} - T)$	$-\boldsymbol{n} \cdot (-k_T^{\text{eff}} \boldsymbol{\nabla} T) = \frac{1}{R_{T,\text{cont}}} (T_{\text{cell}} - T)$	—	-
$x_i$	$-\boldsymbol{n} \cdot (-c_g D_{i,j}^{\text{free}} \nabla x_i) = \frac{Sh}{D_h} (c_{g,\text{CH}} x_{i,\text{CH}} - c_g x_i)$	*	-	-
$p_l$	$-\boldsymbol{n}\cdot(-\tfrac{\rho_lK_l^{\mathrm{eff}}}{\mu_l}\boldsymbol{\nabla}\boldsymbol{p}_l)=N_l$	*	—	*
$p_g$	<i>Р</i> СН	*	_	*
λ	_	—	*	—



Figure 3. Voltage and current profiles used for potentio- and galvano-dynamic simulations, respectively.

<sup>920</sup> GDL are shown in Fig. 6 (the cases with  $T = 60^{\circ}$ C, RH = 60% and Pt <sup>921</sup> loadings of 0.4 and 0.2 mg/cm<sup>2</sup> also result in some liquid saturation <sup>922</sup> during the voltage hold at 0.4 V, but are not shown in the figure). The <sup>923</sup> anode side remains dry for the simulated conditions, which is mostly <sup>924</sup> due to the high EOD.

Based on these results, several conclusions can be made about the through-the-membrane phenomena affecting the transient response of the cell. The following analysis of the average response is organized based on the step change in the load. Discussions on the distribution 928 of the critical variables are provided later in the paper. 929

Voltage step from 0.8 to 0.6 V.-During this step change, the 930 current responds monotonically with varying settling times that de-931 crease with channel RH, i.e., a faster response for more humidified 932 conditions, which can be attributed to sufficient membrane humidifi-933 cation. This can be observed in Fig. 5, which shows the membrane 934 water content dynamics, where the transient response is found to sig-935 nificantly depend on the operating conditions. In particular, under dry 936 conditions that dry out the membrane prior to the voltage step down, 937 the membrane water content increases monotonically with the step 938 change in voltage. This increase is less pronounced at higher temper-939 atures, where further increase in temperature at higher loads results in 940 lower water uptake by the membrane. As the humidity increases and 941 the membrane holds enough water in its initial state prior to the step 942 change, we observe some cases with reverse response, i.e., an initial 943 decrease in the membrane water content followed by an increasing 944 trend (see, for example, the case with  $T = 40^{\circ}$ C, RH = 60% and a Pt 945 loading of  $0.4 \text{ mg/cm}^2$  in Fig. 5). This reverse response is due to EOD 946 that tends to dry out the anode side of the membrane and is only seen 947 at higher current densities. Another observation is that the changes in 948 the membrane hydration are much more pronounced at lower temper-949 ature, where slight variations in water production rate can significantly 950 alter the membrane water content. The slow relaxation dynamics dis-951 cussed in the Model Formulation section are also evident in Fig. 5. 952 In particular, we note that the relaxation dynamics become slower at 953 higher water contents. These relaxation effects are not observable in 954 the current dynamics, since the ohmic drop at this relatively low load 955



Figure 4. Average current dynamics for the potentio-dynamic simulations.



Figure 5. Average membrane water content dynamics for the potentio-dynamic simulations.

is insignificant. Finally, as shown in Fig. 6, some liquid water builds 956 up in the cathode GDL after the voltage step down for three condi-957 tions with low temperature and high humidity. As expected, the build 958 up of liquid is faster under cooler and wetter conditions, while for 959 some conditions the dynamics are slow and the liquid saturation does 960 not reach a steady state within the 100 second hold at 0.6 V (see, for 961 example, the case with  $T = 40^{\circ}$ C, RH = 60% and a Pt loading of 0.4 962  $mg/cm^2$  in Fig. 6). 963

The figures also demonstrate that the cathode Pt loading has an im-964 pact on the transient response by influencing the current generation, 965 membrane hydration, and liquid saturation dynamics. More specif-966 ically, Fig. 4 shows that higher current densities are achieved with 967 higher loadings, which in turn affect the membrane humidification 968 process, especially under drier conditions, where the membrane is 969 humidified with the electrochemically generated water. This can be 970 clearly seen in Fig. 5 for  $T = 40^{\circ}$ C and RH = 30%. It is observed that 971 with higher loadings, the water generation is high enough to humidify 972 the membrane, whereas with a loading of  $0.05 \text{ mg/cm}^2$ , the membrane 973 remains dry after the step change in the voltage. Additionally, Fig. 5 974 shows that the membrane water content is indeed influenced by the 975 Pt loading, which can be associated with different levels of current 976 and heat generation as well as a change in the overall water balance in 977 978 the cell with the CL thickness. It can also be observed that the cases with higher cathode Pt loading show higher levels of liquid saturation 979 in the GDL (Fig. 6). This can be attributed to the fact that higher Pt 980 loading results in higher current density and therefore higher rate of 981 water generation. In addition, the resulting variations in the CL thick-982 ness with changes in Pt loading mean that lower loaded CLs generate 983 984 more heat on a volumetric basis, which creates a stronger drive for water evaporation. The impact of Pt loading on the overall water balance in the cell is discussed in further detail below as well as in the discussion of the galvano-dynamic simulations, where the results are not convoluted by varying levels of water generation.

*Voltage step from 0.6 to 0.4 V.*—The second voltage step results 989 in more involved dynamics in some cases, but the current response 990 can be categorically identified as being monotonically increasing or 991 displaying an overshoot. In particular, the drier conditions tend to re-992 sult in a monotonic increase in the current density (see the first row 993 of Fig. 4). Similar to the previous step, this monotonic response is 994 associated with a hydrating membrane. This is mostly evident, for in-995 stance, at  $T = 60^{\circ}C$  and RH = 30%, where the relaxation dynamics 996 for the membrane water uptake also play a role in the slow increase in current density. Under wetter conditions, however, the gas phase 998 in the cathode CL is saturated with vapor and the membrane protonic 999 resistance is low enough prior to the step change. This low protonic re- 1000 sistance can support high current generation immediately after the step 1001 change. The high current density dries out the anode side of the mem- 1002 brane with EOD and increases the protonic resistance, which results 1003 in a performance drop as seen in Fig. 4. The overshoot response due to 1004 EOD is relatively fast and settles within 5 seconds of the step change, 1005 when the generated water on the cathode side diffuses back toward the 1006 anode and rehydrates the dry portion of the membrane.<sup>146</sup> It is also ob- 1007 served that the overshoot becomes progressively less significant as the 1008 temperature increases. The large overshoots at low temperatures can 1009 be attributed to the high sensitivity of the membrane hydration state 1010 to changes in the current density. This high sensitivity stems from 1011 more rapid changes in the environmental conditions (T and RH) in the 1012



Figure 6. Average liquid saturation dynamics in the cathode GDL for the potentio-dynamic simulations.

1013 CL and the increased protonic resistance at these lower temperatures. It should be noted that flooding of the porous layers, discharging of 1014 the electrochemical double layer, and mass transport limitations are 1015 also believed to lead to this type of behavior.<sup>4</sup> However, the over-1016 shoot in the presented results is due to membrane dry out with EOD, 1017 which is in agreement with other experimental results.<sup>146</sup> Following 1018 this overshoot, the wetter conditions display a relatively slow drop in 1019 performance during the hold at 0.4 V (e.g., see the case with  $T = 60^{\circ}C$ 1020 and RH = 90% in Fig. 4). This slow drop in performance is attributable 1021 to liquid build up in the GDL that incurs a mass transport resistance 1022 and is most significant for the cases where the current density goes 1023 above 1.5 A/cm<sup>2</sup>. 1024

The case with  $T = 60^{\circ}$ C, RH = 60%, and a Pt loading of 0.4 1025  $mg/cm^2$  displays interesting dynamics after the voltage step. An ini-1026 tial overshoot due to EOD is observed that causes the current density 1027 to drop by about 0.1 A/cm<sup>2</sup> within 2 seconds of the step change. 1028 This drop is then followed by an increase of about  $0.06 \text{ A/cm}^2$  during 1029 the next 15 seconds. This increase is due to liquid accumulation in 1030 the CL that helps the membrane humidification without causing mass 1031 transport limitations. Afterwards, the slow current decay due to liquid 1032 accumulation in the cathode GDL can be observed, which continues 1033 until the next voltage step. In fact, this particular order of liquid build 1034 up in the porous layers (the CL pores followed by those of the MPL 1035 and GDL) is seen under most typical conditions. However, the observ-1036 ability of this behavior from measurements of current alone depends 1037 on the water retention capabilities of the different layers as well as the 1038 operating conditions used for the experiments. 1039

As for the membrane water content, the most notable observation is that for drier conditions where the gas phase in the CL remains unsaturated, this voltage step results in better membrane humidification due to higher rates of water generation (Fig. 5). However, this trend is reversed for wetter conditions, where the water content drops after this voltage step. This drop is again attributable to water removal to the cathode through higher EOD at higher current densities. Additionally, the variations in membrane water content with the voltage step 1047 are more significant at lower temperatures as was the case during the 1048 previous step change. Average liquid saturation in the cathode GDL 1049 also exhibits trends similar to those for the previous step (Fig. 6). 1050

Voltage step from 0.4 to 0.6 V and from 0.6 to 0.8 V.—Similar to 1051 the previous steps, the current response to the step increase in voltage 1052 is either monotonically decreasing (as is the case at  $T = 60^{\circ}C$  and 1053 RH = 30%) or exhibits an undershoot. Again, this behavior can be 1054 directly correlated with membrane water content and further discussion is omitted here. Instead, we focus on the trends during the dry-out 1056 phase when the voltage is increased. In particular, we note that under 1057 some drier conditions, the performance starts to decay after a while. 1058 This is seen, for instance, for all Pt loadings at  $T = 40^{\circ}C$  and RH = 105930% in Fig. 4. Looking at the membrane water content dynamics in 1060 Fig. 5, we note that this decay in performance is directly related to 1061 membrane water loss. This behavior can be explained by a moving 1062 evaporation front that starts in the GDL and progresses toward the 1063 CL as time goes on. Therefore, immediately after the step change the 1064 ionomer in the cathode CL is in contact with a liquid reservoir, which 1065 improves water uptake. As the evaporation front reaches the CL and 1066 the accumulated liquid evaporates, the membrane starts to lose water, 1067 which results in further performance decay. In these simulations, the 1068 time delay between the step change in voltage and the evaporation of 1069 CL liquid water depends on the operating conditions as well as the CL 1070 thickness, with hotter conditions and thinner CLs generally resulting 1071 in the shortest time delays. More generally though, this time delay is 1072 determined by the HI contact angle of the CL as well as the evaporation 1073 rate used in the model. A lower HI contact angle makes evaporation 1074 of water in the HI pores more difficult and prolongs the time delay, 1075 whereas a high evaporation rate reduces this delay. 1076

Finally, it should be mentioned that based on experimental results, 1077 a better performance may be expected at 0.6 V after the hold at 0.4 V 1078 (220-320 seconds) compared to the performance at 0.6 V before the 1079 hold at 0.4 V (20-120 seconds). This performance gain is attributable to
better membrane hydration as well as clearing of the Pt sites from oxide
coverage at low potentials. This improved performance will diminish
slowly as the membrane dehydrates and oxide species grow on the Pt
surface again. As explained in the Model Formulation section though,
this work only captures the former dynamics, as the oxide growth is
ignored in our model and steady state coverage values are used.

The characteristic responses observed after the last voltage step are
 similar to those discussed so far and further discussion is omitted here.
 To further investigate the transient phenomena through the cell's
 thickness, Fig. 7 illustrates the average liquid saturation in the CL and
 GDL under both channel (CH) and land (LN) regions of the cell, the
 average ionomer water content in the anode and cathode CLs, and the
 normalized membrane water flux defined as:

$$\beta = \frac{N_{\rm w,mb}}{i_{\rm cell}/2F},\tag{54}$$

which is averaged over the area of the membrane. As a convention, a positive value denotes water flux toward the cathode. The presented results are for the cold and dry conditions ( $T = 40^{\circ}C$  and  $RH = 30^{\circ}$ %) with high (0.4 mg/cm<sup>2</sup>) and low (0.05 mg/cm<sup>2</sup>) Pt loading in the cathode CL.

First, we observe that immediately after the second step decrease in 1099 voltage (0.6 to 0.4 V at 120 seconds), the cathode CL becomes flooded. 1100 This flooding takes place within 10 seconds of the step change. Also, 1101 note that the CL flooding occurs slightly faster under the land location 1102 compared to the channel location. After all the hydrophilic pores in the 1103 CL are filled, water starts to condense in the GDL. Most of the conden-1104 sation happens under the land, where lower temperature and higher 1105 resistance to vapor transport promotes the phase change process. This 1106 liquid water then flows toward the channel location. This can be seen 1107 in the figure, as there is a delay between liquid accumulation under the 1108 land and channel regions of the GDL. This delay is governed by the 1109 time it takes for the liquid water condensed under the land to reach the 1110 channel location. After the voltage is increased back to 0.6 V at 220 1111 seconds, we see that the GDL dry out is initiated under the channel. 1112 The dry out happens at a slower pace under the land location. Once 1113 the GDL is completely dry, the CL starts to lose its liquid water. As 1114 for the ionomer water content in the CL, two main observations can 1115 be made. First, at lower loads the ionomer water contents in both CLs 1116 are close and as the load is increased, a more significant distribution 1117 develops across the membrane thickness with intensified EOD and 1118

back diffusion. Second, we note that after the load is decreased, the 1119 CLs maintain a high ionomer water content as long as the liquid water 1120 in the CL has not evaporated. After that liquid water has evaporated 1121 though, the cathode ionomer loses water to its pore space, which also 1122 diminishes the water back diffusion to anode, which in turn results in 1123 dry out of the anode CL. This behavior can also be seen in the last 1124 column of Fig. 7, where the smallest values for β are obtained when 1125 the cathode CL has liquid water while the anode CL is dry, which is in 1126 agreement with experimental measurements by Adachi et al.<sup>147</sup> It is 1127 also seen that this flux is significantly reduced after the liquid reservoir 1128 in the cathode CL has evaporated (see the plots between 220 and 300 1129 seconds). This is specially pronounced for the case with low Pt loading. 1130 Another important observation from the normalized water flux plots 1131 is the significant overshoots and undershoots during the step changes. 1132 This behavior is associated with EOD that immediately drives water to 1133 the cathode side, whereas the back diffusion requires time to establish 1134 a balancing water flux to counter EOD. Such transients qualitatively 1135 agree with experimental measurements.<sup>148,149</sup> In addition, it can be 1136 seen that higher current densities generally tend to force more water 1137 toward the cathode (larger  $\beta$  values) due to intensified EOD, which is 1138 in agreement with experimental results.<sup>150,151</sup> 1139

Finally, the distribution of critical variables for some conditions are 1140 shown in Figs. 8-9. In particular, the distributions for the membrane 1141 and cathode temperatures, cathode liquid saturation, ionomer water 1142 content, and volumetric ORR current density are shown for high (0.4 1143 mg/cm<sup>2</sup>) and low (0.05 mg/cm<sup>2</sup>) Pt loadings. These distributions 1144 are obtained at the end of the hold at 0.4 V. The temperature plots 1145 show a rather significant temperature gradient (about 1.5°C) across 1146 the MPL thickness, which is due to its low thermal conductivity. This 1147 low conductivity also results in heating the CL and enhances water 1148 evaporation.<sup>23</sup> The cathode MPL and GDL remain free of liquid wa- 1149 ter under these hot conditions, whereas the hydrophilic pores in the 1150 cathode CL are filled with liquid water for the hot and wet ( $T = 80^{\circ}C$ , 1151 RH = 90% conditions. A considerable gradient of water content is 1152 established across the thickness of the CCM, with a dry anode CL and 1153 a wet cathode CL. There is a close correspondence between the loca-1154 tion of maximum water content in the cathode CL and the volumetric 1155 rate of ORR. In particular, under the dry conditions (Fig. 8), protonic 1156 resistance is a major contributor to performance loss. Therefore, the 1157 highest volumetric current is observed under the land location, where 1158 the membrane water content is highest. At higher humidities (Fig. 9) 1159 the location of maximum current generation moves toward the channel 1160



Figure 7. Average dynamics of liquid saturation, ionomer water content in the CLs, and normalized membrane water flux for the potentio-dynamic simulations at  $T = 40^{\circ}$ C and RH = 30 % with cathode Pt loading of a) 0.4, and b) 0.05 mg/cm<sup>2</sup>.



Figure 8. Distribution of temperature, liquid saturation, ionomer water content, and ORR volumetric current density for the potentio-dynamic simulations under the hot-dry ( $T = 80^{\circ}$ C and RH = 30%) operating condition at t = 219 s (highest load just before the following voltage step up) with Pt loadings of: a) 0.4 and b) 0.05 mg/cm<sup>2</sup>.

region, where the mass transport limitations are minimal. Furthermore, 1161 a higher portion of the Pt is utilized, as the region close to the MPL 1162 is not severely limited by proton transport resistance. Comparing the 1163 low and high Pt loading cases, the most notable difference is in the 1164 volumetric current distributions, which stems from the thinness of the 1165 CL with low Pt loading and the resulting increase in volumetric cur-1166 rent density. In particular, note that the current distribution across the 1167 CL thickness is more uniform for the thin CL as seen previously.<sup>72</sup> 1168

**Galvano-dynamic simulations.**—For this set of simulations, a current profile shown in Fig. 3 is applied and the cell voltage is calculated. The profile is made up of the following steps:  $0.2-1.0 \text{ A/cm}^2$ ,  $1.0-1.8 \text{ A/cm}^2$ ,  $1.8-1.0 \text{ A/cm}^2$ , and  $1.0-0.2 \text{ A/cm}^2$ . The magnitude of the steps are chosen to be relatively high in order to excite the system dynamics. Similar to the voltage steps, these step changes are smooth and happen over a period of 1 second.

Overall, 16 simulations are conducted under the galvano-dynamic mode with variations in RH (60, and 90%), operating temperature (60, and 80°C), and cathode Pt loading (0.4, 0.2, 0.1, 0.05 mg/cm<sup>2</sup>). The driest and coldest conditions used for the potentio-dynamic simulations could not be simulated in the galvano-dynamic mode with the 1180 selected current profile. This is due to the severe anode dry out with 1181 EOD that occurs during a step change in current density<sup>12</sup> and results 1182 in numerical issues under these dry conditions, where the membrane 1183 hydration is low prior to the increase in load. 1184

The resulting voltage dynamics for all 16 simulations are shown 1185 in Fig. 10. The corresponding average water content in the membrane 1186 for all the cases are shown in Fig. 11 and the average liquid saturations 1187 in the cathode GDL are shown in Fig. 12. Similar to the analysis for 1188 the potentio-dynamic case, below we organize the discussion in terms 1189 of the current density step. 1190

*Current density step from 0.2 to 1.0 A cm*<sup>2</sup>.—After the first step 1191 in the current density, the voltage drops and a steady state value is 1192 achieved within 20 seconds. Only the case with  $T = 80^{\circ}$ C and RH = 119390% with a Pt loading of 0.4 mg/cm<sup>2</sup> demonstrates a slight undershoot 1194 that is a characteristic response of PEM fuel cells due to dry out of 1195 the membrane by EOD as mentioned earlier.<sup>146</sup> This dry out can also 1196 be observed in Fig. 11. It should be noted that mass transport limita-1197 tions at higher loads can also contribute to this behavior.<sup>152</sup> However, 1198



**Figure 9.** Distribution of temperature, liquid saturation, ionomer water content, and ORR volumetric current density for the potentio-dynamic simulations under the hot-wet ( $T = 80^{\circ}C$  and RH = 90%) operating condition at t = 219 s (highest load just before the following voltage step up) with Pt loadings of: a) 0.4 and b) 0.05 mg/cm<sup>2</sup>.

membrane dry out is the only contributing factor in this case, since the operation is well within the ohmic region and mass transport effects are relatively insignificant. To finalize our discussion of the voltage response, it is worth mentioning that higher Pt loading is observed to consistently result in improved performance under all four simulated conditions at  $1.0 \text{ A/cm}^2$ .

As for the GDL liquid saturation, only the coolest ( $T = 60^{\circ}C$ ) and 1205 most humidified (RH = 90%) condition results in vapor condensation 1206 after this step change in the current density (Fig. 12). This condensa-1207 tion continues throughout the entire 100 seconds hold at  $1.0 \text{ A/cm}^2$ , 1208 where the higher Pt loadings result in slightly higher liquid accumula-1209 tion in the GDL. This higher liquid saturation is due to the fact that the 1210 thicker catalyst results in higher cell voltage and reduced volumetric 1211 heat generation, which lowers the overall cell temperature by about 1212 0.4°C. The average saturation of 0.2 agrees with the in-operando re-1213

sults by Banerjee et al.<sup>153</sup> They also propose fitting the time evolution <sup>1214</sup> of liquid saturation with a first order dynamic equation and obtain a <sup>1215</sup> time constant of 2.3 minutes for similar operating conditions using an <sup>1216</sup> SGL 25BC diffusion medium. Similar dynamics are observed by others as well.<sup>154</sup> Our results indicate a time constant of about 33 seconds, <sup>1218</sup> which is more than 4 times faster than that reported by Banerjee et al.<sup>153</sup> This discrepancy between the model predictions and experimental results may be attributed to differences in cell geometry, membrane and <sup>1221</sup> work. <sup>1223</sup>

*Current density step from 1.0 to 1.8 A/cm*<sup>2</sup>.—The voltage response to the second step increase in current density is seen to be monotonically decreasing in most cases, while some cases ( $T = 60^{\circ}C_{1226}$ and RH = 60% in Fig. 10) exhibit the characteristic undershoot dis-



Figure 11. Average membrane water content dynamics for the galvano-dynamic simulations.



Figure 12. Average liquid saturation dynamics in the cathode GDL for the galvano-dynamic simulations.

cussed earlier. The monotonic voltage decay is a sign of well humidi-1228 fied membrane and increasing mass transport limitations with slowly 1229 accumulating liquid water (e.g.,  $T = 60^{\circ}C$  and RH = 90% in Fig. 10 1230 and Fig. 12). For the operating condition where a voltage undershoot 1231 is observed, the performance recovers to some extent after the step 1232 change with water back diffusion and rehydration of the anode side of 1233 the membrane. However, this voltage recovery is followed by a further 1234 decay as the cathode GDL floods with liquid water (Fig. 12). 1235

An important observation is the fact that at  $T = 60^{\circ}C$  and RH =1236 90%, reducing the Pt loading from 0.4 to  $0.2 \text{ mg/cm}^2$  seems to improve 1237 performance. This seemingly peculiar behavior is directly related to 1238 the changes in the membrane water content with CL thickness. In par-1239 ticular, Fig. 11 shows that at 60°C and 1.8 A/cm<sup>2</sup>, thinner catalysts 1240 consistently result in better membrane hydration. This is explained fur-1241 ther when discussing the water balance in the cell later in this section. 1242 The higher membrane water content achieved at  $0.2 \text{ mg/cm}^2$  reduces 1243 the ohmic drop, while the Pt reduction at this level does not impose 1244 significant mass transport issues. Therefore, the performance is im-1245 proved. Yet another interesting observation is related to the impact of 1246 Pt loading on voltage dynamics at  $T = 80^{\circ}C$  and RH = 90%. Specifi-1247 cally, we observe that immediately after the load increase, the highest 1248 Pt loading achieves the best performance. But this performance decays 1249 more rapidly than the cases with lower Pt loading, to the point that at 1250 the end of the 100 second hold at  $1.8 \text{ A/cm}^2$ , the cell with a Pt loading 1251 of  $0.2 \text{ mg/cm}^2$  has a higher voltage than that with a Pt loading of 0.4 1252 mg/cm<sup>2</sup>. This is directly related to faster liquid accumulation in the 1253 GDL with a thick CL which is due to lower cell temperatures (Fig. 12). 1254 The heat generation in the two thinnest CLs is high enough to inhibit 1255 any liquid accumulation (Fig. 12), which results in lower membrane 1256 water contents as seen in Fig. 11 and reduced performance. 1257

<sup>1258</sup> Current density steps from 1.8 to 1.0 A/cm<sup>2</sup> and from 1.0 to <sup>1259</sup> 0.2 A/cm<sup>2</sup>.—For the simulated conditions, the step decreases in cur-<sup>1260</sup> rent density result in monotonic voltage increase with relatively fast <sup>1261</sup> dynamics. A hysteresis effect may be expected due to membrane hydration-dehydration and Pt oxide coverage dynamics. The former 1262 effect can be seen to some extent in the simulations results at T = 1263 60°C and RH = 60%. The most notable feature of the voltage response to load decreases at this condition is a drop in performance 1265 after a considerable time delay. This is due to evaporation of liquid 1266 water reservoir in the cathode CL and the ensuing loss of membrane 1267 water (Fig. 11) and was discussed in detail for the potentio-dynamic 1268 are well humidified. Furthermore, as mentioned in the Model Formulation section, the Pt oxide growth dynamics are neglected in our model, 1271 which further contributes to the lack of hysteresis in our results.

Further insight about the water balance in the cell can be gained by 1273 comparing the normalized membrane water fluxes (B) shown in Fig. 1274 13. The figure illustrates  $\beta$  values (defined by Eq. 54) for different 1275 operating conditions and cathode Pt loadings at 119 seconds, which 1276 corresponds to the hold at 1.0 A/cm<sup>2</sup> just before the following step 1277 increase in the load. Some clear trends can be observed in these results. 1278 First, we note that increasing the RH increases  $\beta$ . This is due to the fact 1279 that the cathode CL typically has a high RH under all conditions due 1280 to the electrochemical water generation. A low RH dries out the anode 1281 CL and promotes water back diffusion, which explains lower  $\beta$  values. 1282 Another important observation is the impact of temperature on  $\beta$ . At 1283 lower RH conditions (RH = 60%), we observe that  $\beta$  increases with 1284 temperature. This is due to the fact that parts of the cathode CL remain 1285 subsaturated at low RH and high temperatures, which reduce water 1286 back diffusion and increases  $\beta$ . At higher RH conditions (RH = 90%), 1287 the cathode CL remains saturated at both low and high temperatures. 1288 Therefore, the water activity in the anode CL determines the driving 1289 force for water back flow. As this water activity diminishes at higher 1290 temperatures, the water back diffusion is more pronounced, which 1291 yields a lower value of  $\beta$ .

Similar arguments can be used to explain the seemingly counterintuitive impact of Pt loading on the water balance. In particular, we note that at lower temperature,  $\beta$  increases with Pt loading and the resulting increase in CL thickness. This trend is reversed at higher temperature, 1296



Figure 13. Normalized average water flux in the membrane (positive is toward cathode) at t = 119 s (medium load just before the following current step up) for the galvano-dynamic simulations.

where a higher Pt loading reduces  $\beta$ . The trend at T = 60°C can be ex-1297 plained by the fact that at this lower temperature, the CL is saturated 1298 for all Pt loadings. A lower Pt loading means that the water that is 1299 produced in the CL close to the MPL has a lower resistance to diffuse 1300 back to the anode, since the cathode CL is thinner and the diffusion 1301 path is shorter. This means that a thinner CL reduces  $\beta$ . When the tem-1302 perature is increased, subsaturated conditions emerge in parts of the 1303 CL as mentioned before. Therefore, an increase in the temperature di-1304 minishes the driving force for water back diffusion and increases  $\beta$ . As 1305 thinner CLs generate more heat, the local CL temperature increases 1306 further, which in turn increases  $\beta$ . This result bears significance as 1307 it shows that in addition to changes in local transport resistance, Pt 1308 loading impacts the performance by influencing the water balance in 1309 the cell. This overall observation partially confirms the hypothesis by 1310 Muzaffar et al.,<sup>77</sup> who claimed that the performance changes with Pt 1311 loading reduction may mostly stem from a tipping water balance in 1312 the cell. However, their conclusion was based on the assumption that 1313

the CL is the main source of vaporization in the cell and a thinner CL 1314 makes the cell inherently more susceptible to flooding. On the other 1315 hand, the phase change rate is assumed to be relatively high in our 1316 model based on the experimental evidence in the literature that suggest the phase change kinetics should be fast enough not to impose 1317 any limitations.<sup>143</sup> This high rate of phase change allows the GDL to 1319 vaporize a relatively large amount of liquid. Nevertheless, our results 1320 also highlight the role of Pt loading and CL thickness in the cell water 1321 balance. 1322

Our discussion of the galvano-dynamic simulations has focused 1323 on average response of the cell so far. However, the distribution of 1324 temperature, water, and reaction rates are also of critical importance. 1325 An example of such distributions is provided in Fig. 14 for high (0.4 1326 mg/cm<sup>2</sup>) and low (0.05 mg/cm<sup>2</sup>) cathode Pt loading. The figure shows 1327 a rather significant in-plane temperature gradient in the membrane and 1328 CL, where a temperature difference of up to 4°C is observable. This 1329 temperature difference is due to the high current generation under the 1330



Figure 14. Distribution of temperature, liquid saturation, ionomer water content, and ORR volumetric current density for the galvano-dynamic simulations under  $T = 60^{\circ}$ C and RH = 90% operating condition at t = 219 s (highest load just before the following current step down) with Pt loadings of: a) 0.4 and b) 0.05 mg/cm<sup>2</sup>.

channel location along with the limited heat dissipation through thechannel boundary.

Furthermore, we see that the cathode GDL has a very high sat-1333 uration at this operating condition, which imposes significant mass 1334 transport limitations and results in limited current generation under 1335 the land area. It should be pointed out that a higher liquid saturation 1336 is observed under the land while a rather uniform distribution is seen 1337 through the GDL thickness. Zenyuk et al. found a higher liquid sat-1338 uration under the channel in a compressed GDL due to the in-plane 1339 porosity distribution resulting from land compression.<sup>155</sup> However, 1340 the temperature distribution in an operating fuel cell usually shifts the 1341 water accumulation toward the land region.<sup>153</sup> This flooding under the 1342 land has much less pronounced impact on the overall performance 1343 compared to flooding under the channel,<sup>156</sup> since the land region is 1344 already transport limited by the longer diffusion paths. In terms of 1345 the through-plane liquid distributions, there is evidence in the litera-1346 ture for increased saturation in higher porosity regions of the GDL.<sup>113</sup> 1347 Furthermore, Banerjee et al.<sup>153</sup> found the highest level of saturation 1348 to occur close to the land. Finally, capillary fingering is believed to 1349 be a major transport mechanism for liquid water.<sup>155,157</sup> The model in 1350 this work assumes a constant GDL porosity through the thickness, so 1351 the pooling effects cannot be captured. The rather uniform through-1352 plane liquid distribution stems from the temperature distributions in 1353 our simulations. Finally, the macro-homogeneous model in this work 1354 does not allow for simulation of capillary fingering. Therefore, the liq-1355 uid saturations predicted by the proposed model are only insightful on 1356 an aggregate level and detailed knowledge about the micro-structures 1357 are needed to obtain accurate distributions.<sup>10</sup> 1358

The non-uniform current generation pattern also affects water dis-1359 tribution in the ionomer phase. In particular, we see that under the 1360 land, the water content is more uniform across the thickness of the 1361 CCM, whereas significant gradients emerge under the channel, where 1362 current generation is high. Comparing the low and high Pt loading 1363 cases, we observe that the lower Pt loading results in slightly higher 1364 temperatures, which in turn reduce liquid saturation in the cathode 1365 GDL. Moreover, the current distribution through the thickness of the 1366 1367 cathode CL is more uniform for the lower loaded CL as discussed earlier. 1368

The preceding analysis provides some insight about the quasi 1369 steady state distributions of critical variables. To better understand 1370 the water transport transients during the following current step down, 1371 the distributions of liquid pressure in the cathode CL and the mem- 1372 brane water content before and after the step change are shown in Fig. 1373 15 and Fig. 16, respectively, for the high Pt loaded CL  $(0.4 \text{ mg/cm}^2)$ . 1374 Fig. 15 shows that immediately before the step change at 219.5 sec- 1375 onds, liquid pressure is highest under the channel. The flow directions 1376 provided in the figure show an interesting pattern, where the liquid 1377 water is found to flow mostly toward the membrane in the land re- 1378 gion and mostly toward the MPL in the channel region. This behavior 1379 is closely tied to a similar flow pattern in the membrane as seen in 1380 Fig. 16, where a recirculation is observed at 219.5 seconds. More 1381 specifically, it is seen that at the furthest location under the land, the 1382 membrane water flux is toward the anode. As we move closer to the 1383 channel location, the flux turns progressively toward the cathode. As 1384 the load is reduced to 1.0 A/cm<sup>2</sup>, EOD is relieved and water back 1385 diffusion dominates during the transients (as was observed in Fig. 7 1386 for the potentio-dynamic simulations). This results in the membrane 1387 water flux to be dominantly toward the anode (Fig. 16 at 221 seconds), 1388 which also pushes liquid water toward the membrane to compensate 1389 for the back diffusion (Fig. 15 at 221 seconds). Two seconds after 1390 the step change, a smoother water profile is established across the 1391 membrane thickness and water back diffusion has diminished (Fig. 1392 16 at 222.5 seconds). This creates a dominant flux toward the cath- 1393 ode. At the same time, a higher liquid pressure is observed in the 1394 cathode CL, where a stagnation front has emerged in the middle (Fig. 1395 15 at 222.5 seconds). In particular, in the half of the CL close to the 1396 membrane, the flow is found to be toward the membrane, whereas in 1397 the other half to the right of the stagnation front, the flow is found 1398 to be toward the MPL. As time goes on and a quasi steady state is 1399 achieved at this reduced load, the stagnation front moves further to- 1400 ward the membrane (Fig. 15 at 230 seconds), while the membrane 1401 water flux turns toward the cathode throughout the membrane thick- 1402 ness (Fig. 16 at 230 seconds). The existence of the stagnation front 1403 is in agreement with our earlier observation that a thick catalyst layer 1404 increases the resistance to water flow toward the anode. The transients 1405 during a step increase in the load are the reverse of those presented 1406 here. 1407



Figure 15. Liquid pressure (in [Pa]) and flow in the cathode CL during load decrease from  $1.8 \text{ to } 1 \text{ A/cm}^2$  at  $T = 60^{\circ}\text{C}$  and RH = 90% (Pt loading of  $0.4 \text{ mg/cm}^2$ ). From left to right: immediately before the step change, 0.5 seconds after the step change, 2 seconds after the step change, the quasi steady state achieved after the step change.



Figure 16. Membrane water content and flow during load decrease from 1.8 to  $1 \text{ A/cm}^2$  at T = 60°C and RH = 90% (Pt loading of 0.4 mg/cm<sup>2</sup>). From left to right: immediately before the step change, 0.5 seconds after the step change, 2 seconds after the step change, the quasi steady state achieved after the step change.

The dynamics of in-plane current density distribution during load 1408 changes can also improve understanding of the transient phenomena. 1409 To this end, the corresponding distributions for the hot and wet operat-1410 ing condition (T =  $80^{\circ}$ C and  $\tilde{R}H = 90\%$ ) during the load increase from 1411 1.0 to 1.8 A/cm<sup>2</sup> are shown in Fig. 17 for both low  $(0.05 \text{ mg/cm}^2)$  and 1412 high  $(0.4 \text{ mg/cm}^2)$  cathode Pt loading. We see that immediately before 1413 the step change, both Pt loadings result in a relatively uniform in-plane 1414 current distribution. However, as the load is increased to 1.8 A/cm<sup>2</sup> 1415

the region under the channel tends to generate more current with both 1416 Pt loadings. It can be seen, however, that the in-plane distribution is 1417 more uniform for the lower Pt loading case. This is attributable to the 1418 fact that the thinner CL results in higher cell temperatures and lower 1419 liquid build up, which reduces the mass transport limitations under the 1420 land region. We also note that current generation under the land is low 1421 even immediately after the load increase and before any liquid accumulation. This agrees with experimental results by Schneider et al., 1423



Figure 17. In-Plane current density distribution for the galvano-dynamic simulations during load increase from 1 to  $1.8 \text{ A/cm}^2$  at T = 80°C and RH = 90% for high and low cathode Pt loadings. From left to right: immediately before the step change, mid-way through the step change, immediately after the step change has completed, the quasi steady state achieved after the step change.



Figure 18. In-Plane current density distribution difference between high- and low-loaded CLs during load increase from 1 to 1.8 A/cm<sup>2</sup>.

<sup>1424</sup> who found the land region to be transport limited even prior to any <sup>1425</sup> liquid build up in the GDL.<sup>158,159</sup>

To further investigate the impact of Pt loading on the dynamics of 1426 in-plane current distribution, the difference between the current den-1427 sities with high and low Pt loadings during the same load change are 1428 shown in Fig. 18 for all simulated operating conditions. The figure 1429 shows that at 1.0 A/cm<sup>2</sup> the difference between the current distri-1430 butions is relatively insignificant as was seen earlier. As the load in-1431 creases, however, the cathode Pt loading and CL thickness seem to 1432 have varying impacts on the current distribution at different operat-1433 ing conditions. In particular, under drier conditions (RH = 60%), the 1434 higher Pt loading and CL thickness result in improved performance 1435 under the land region immediately after the step change. At  $T = 60^{\circ}C$ 1436 this performance enhancement under the land fades toward the new 1437

quasi equilibrium state, as more liquid builds up in the GDL when a the thicker CL is used. However, at the higher temperature ( $T = 80^{\circ}$ C) that inhibits liquid accumulation, the new equilibrium results in a distribution difference that is close to that obtained immediately after the load change. When the RH is increased to 90%, the response is the dominated by liquid accumulation dynamics in the GDL. More specifically, thicker CLs make the GDL more susceptible to rapid liquid the build up, as they generate less heat. Therefore, the performance is the diminished under the land region. This results in a particularly significant difference at  $T = 80^{\circ}$ C and RH = 90%, where the thick CL the thin CL leads to a relatively dry GDL. Therefore, the high Pt the boaded cathode CL shows a remarkable performance drop in the land tegion.

# Conclusions

A comprehensive model that captures the most salient transient 1453 phenomena across the thickness of a unit cell is developed in this 1454 work. The model draws from and extends the existing models in the 1455 literature by incorporating state of the art reaction kinetics for the 1456 HOR and ORR, the mixed wettability model for porous layers, a con-1457 sistent homogeneous model for the CL micro-structure, as well as the 1458 ionomer relaxation dynamics. The model predictions are compared 1459 with experimental data obtained through voltammetry and voltage step 1460 experiments under a variety of conditions and a good agreement is ob-1461 tained. 1462

The developed model is executed with different humidity and tem-1463 perature conditions under both current and voltage control operational 1464 modes and varying Pt loadings in the cathode CL. The results of these 1465 1466 simulations shed light into the transient processes that determine the dynamic response of PEM fuel cells to load changes. In particular, we 1467 have found the transient response to be dominated by water redistri-1468 bution in the cell. The timescales of this redistribution are dependent 1469 on the operating conditions and are controlled by the membrane wa-1470 ter uptake and two phase flow in the DM for dry and wet conditions, 1471 respectively. Furthermore, the modeling results suggest that changing 1472 the cathode Pt loading, and thereby, the cathode CL thickness, can 1473 influence the performance by affecting the water balance in the cell. 1474 Specifically, the thiner CL results in higher rates of heat generation on 1475 a volumetric basis while leading to a shorter diffusion path for water 1476 transport toward the anode. Our simulation results suggest that, based 1477 on the operating conditions, the combination of these effects lead to 1478 distinctly observable trends in normalized membrane water flux with 1479 respect to changes in the cathode Pt loading. Additionally, we have 1480 found that through its effect on water balance in the cell, the cathode 1481 Pt loading can have a profound impact on the transient response to 1482 load changes for some operating conditions. These findings can fur-1483 ther improve understanding of the impacts of Pt reduction on various 1484 aspects of PEM fuel cell performance and its transient response. More 1485 broadly, the model can be used to develop further insight into spatio-1486 1487 temporal distribution of variables that are critical to performance and degradation. 1488

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