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Published on: 22 Feb 2011 - International Conference of the IEEE Engineering in Medicine and Biology Society Topics: Hilbert–Huang transform

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Time-Frequency Analysis of EEG Asymmetry Using Bivariate Empirical Mode Decomposition

Cheolsoo Park, David Looney, Preben Kidmose, Michael Ungstrup, and Danilo P. Mandic, Senior Member, IEEE

Abstract—A novel method is introduced to determine asymmetry, the lateralization of brain activity, using extension of the algorithm empirical mode decomposition (EMD). The localized and adaptive nature of EMD make it highly suitable for estimating amplitude information across frequency for nonlinear and nonstationary data. Analysis illustrates how bivariate extension of EMD (BEMD) facilitates enhanced spectrum estimation for multichannel recordings that contain similar signal components, a realistic assumption in electroencephalography (EEG). It is shown how this property can be used to obtain a more accurate estimate of the marginalized spectrum, critical for the localized calculation of amplitude asymmetry in frequency. Simulations on synthetic data sets and feature estimation for a brain–computer interface (BCI) application are used to validate the proposed asymmetry estimation methodology.

Index Terms—Asymmetry ratio, bivariate empirical mode decomposition (BEMD), cognitive task, electroencephalography (EEG), empirical mode decomposition (EMD).

I. INTRODUCTION

B RAIN-COMPUTER interface (BCI) is a novel research paradigm that facilitates computer-aided control using brain activity, and has found application across bioengineering fields, such as neuroprosthetics. Due to its noninvasive nature and affordable recording equipment, the electroencephalography (EEG) is the most convenient means to measure neurophysiological activity in real-time BCI systems [1]. The level of asymmetry observed in EEG, that is, the lateralization of activity between left and right brain hemispheres, has been found to be of much interest in the detection and estimation of brain electrical activity corresponding to cognitive processes [2], [3].

Asymmetry studies have been addressed both the full EEG spectrum [4]–[6] and also specific frequency bands of interest [7]–[9]. For instance, recent work focused on detecting asymmetry in the alpha band [5], [7], as the suppression of EEG activity in low-frequency bands is associated with cognitive engagement. McKee *et al.* [8] found that linguistic tasks, in comparison to music tasks, were characterized by greater alpha suppression. It was established in [9] that the lateral asymmetries in contingent negative variation were caused by cognitive ac-

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tivity of brain. Davidson found that verbal and spatial tasks were characterized by different levels of EEG asymmetry in multiple frequency bands [5]. Furthermore, neuropsychological tasks "Verbal Fluency," "the Tower of London," and "Corsi's Recurring Blocks" produced specific asymmetry patterns in the delta and theta bands [6].

Although these results illustrate that asymmetry is a robust measure for classifying different mental tasks [10], [11], existing studies have employed standard signal processing techniques based on Fourier analysis [1], [11]–[13] and thus inherit the well-known problems associated with standard spectrum estimation. In addition, standard techniques project the data onto linear orthogonal basis functions, and are thus suboptimal for processing of nonlinear and nonstationary real world data (such as EEG).

In this work, we propose to estimate asymmetry using empirical mode decomposition (EMD) [14], a fully data-driven technique for decomposing the signal into AM/FM components which reflect its natural oscillations. EMD makes no prior assumptions on the data and, as such, it is suitable for the analysis of nonlinear and nonstationary processes, and has been successfully employed in the analysis of EEG [15], [16]. Using EMD, frequency and amplitude information can be analyzed locally, providing a highly accurate insight into signal dynamics, making it an ideal candidate for estimating asymmetry. The asymmetry estimation paradigm is compared for both the real-valued and complex-valued EMD algorithm, showing that bivariate EMD (BEMD) produces enhanced spectrum estimation for multichannel recordings that contain similar oscillating components [17], a realistic assumption in EEG. This, in turn, yields a more accurate estimate of the marginalized spectra, critical issue in the localized calculation of amplitude asymmetry in frequency. Simulations on both synthetic signals and real world cognitive EEG tasks illustrate the usefulness of the proposed approach for calculating asymmetry.

II. EMPIRICAL MODE DECOMPOSITION ALGORITHM

A. Empirical Mode Decomposition

Huang *et al.* [14] developed EMD to perform a highly localized time-frequency estimation in a data-driven fashion. This is achieved by decomposing the signal into a finite set of AM/FM components, called "intrinsic mode functions" (IMFs). An IMF is a function for which the number of extrema and the number of zero crossings differ at most by one, and the mean of the two envelopes associated with the local maxima and local minima is approximately zero. The IMF can thus be regarded as a monocomponent signal. The details of the EMD operation are outlined in algorithm 1 [14]. The first IMF is subtracted from the

Manuscript received June 06, 2010; revised November 16, 2010; accepted January 20, 2011. Date of publication February 22, 2011; date of current version August 10, 2011.

original data, r(t) = x(t) - d(t), and the procedure is applied iteratively to the residue, r(t), until it becomes constant or contains no more oscillations. The stopping criterion uses the mode amplitude

Algorithm 1. The standard EMD algorithm

- 1) Let $\tilde{x}(t) = x(t) (x(t) \text{ is original signal}).$
- 2) Identify all local maxima and minima of $\tilde{x}(t)$.
- 3) Find a lower "envelope," $e_l(t)$ that interpolates all local minima.
- 4) Find an upper "envelope," $e_u(t)$ that interpolates all local maxima.
- 5) Calculate the local mean value, $m(t) = (e_l(t) + e_u(t))/2$.
- 6) Subtract the local mean value from $\tilde{x}(t)$, $d(t) = \tilde{x}(t) - m(t)$.
- 7) Let $\tilde{x}(t) = d(t)$ and go to step 2); repeat until d(t) becomes an IMF.

 $a(t) := (e_u(t) - e_l(t))/2$ and the evaluation function $\sigma(t) := |m(t)/a(t)|$, so that sifting is iterated until $\sigma(t) < \theta_1$ for some prescribed fraction $(1-\alpha)$ of the total duration, while $\sigma(t) < \theta_2$ for the remaining fraction [18]. The default value of $[\theta_1, \theta_2, \alpha]$ is [0.05, 0.5, 0.05]. The signal x(t) decomposed by the EMD algorithm can thus be written as

$$x(t) = \sum_{i=1}^{M} c_i(t) + r(t)$$
(1)

 $c_i(t)$, i = 1, ..., M, is the set of IMFs. Due to their monocomponent nature, it is convenient to apply the Hilbert transform to the IMFs to obtain a time-frequency representation. The Hilbert transform of an IMF $c_i(t)$ is given by

$$H[c_i(t)] = \frac{1}{\pi} P \int_{-\infty}^{\infty} \frac{c_i(t')}{t - t'} dt'$$
(2)

where symbol P indicates the Cauchy principal value. The analytic signal is then obtained as

$$X(t) = \sum_{i=1}^{M} (c_i(t) + jH[c_i(t)]) = \sum_{i=1}^{M} a_i(t) \cdot e^{j\theta_i(t)}$$
(3)

and is described by its amplitude and phase functions, $a_i(t)$ and $\theta_i(t)$. The instantaneous frequency is calculated as the derivative of the phase function, $w_i(t) = (d\theta_i)/(dt)$ [19]; a plot of the amplitude $a_i(t)$ versus time t and instantaneous frequency $w_i(t)$, that is, amplitude contours on the time-frequency plane is called the Hilbert-Huang spectrum (HHS), $\mathbf{H}(w, t)$, a three-dimensional time-frequency representation of a signal. The marginal Hilbert spectrum (MHS), h(w), is calculated by marginalising the amplitude of the HHS over time

$$h(w) = \int_0^T \mathbf{H}(w, t) dt \tag{4}$$

where T is the total data length. The advantage of MHS for EEG applications has been addressed in [20]–[22].

B. Complex Extension of EMD

To obtain a set of M complex/bivariate IMFs, $\gamma_i(t)$, i = 1,..., M, from a complex signal z(t), the following procedure, algorithm 2, is adopted (bivariate EMD) [23].

	Algorithm	2.	The	bivariate	EMD	algorithm	
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1) Let $\tilde{z}(t) = z(t)$; 2) To obtain K signal projections, given by $\{p_{\theta_k}\}_{k=1}^K$, project the complex signal $\tilde{z}(t)$, by using a unit complex number $e^{-j\theta_k}$, in the direction of θ_k , as

$$p_{\theta_k}(t) = \Re(e^{-j\theta_k}\tilde{z}(t)), \quad k = 1, \dots, K$$

where $\Re(\cdot)$ denotes the real part of a complex number, and $\theta_k = 2k\pi/K$; 3) Find the locations $\{t_j^k\}_{k=1}^K$ corresponding to the maxima of $\{p_{\theta_k}(t)\}_{k=1}^K$; 4) Interpolate (using spline interpolation) between the maxima points $[t_j^k, \tilde{z}(t_j^k)]$, to obtain the envelope curves $\{e_{\theta_k}(t)\}_{k=1}^K$; 5) Obtain the arithmetic mean of all the envelope curves, m(t), and subtract from the input signal, that is, $d(t) = \tilde{z}(t) - m(t)$. Let $\tilde{z}(t) = d(t)$ and go to step 2); 6) Repeat until d(t) becomes an IMF;

Similarly to real-valued EMD, once the first IMF, $\gamma_1(t)$, is obtained the procedure is applied iteratively to the residual r(t) = z(t) - d(t) to extract all the complex IMFs, which *rotate around zero* [23]. In our simulations, the sifting process was stopped once the magnitude of d(t) satisfied the real-valued stopping criterion described in [18] and the number of projections for all BEMD decomposition, K, was 16.

Earlier results [17] illustrate that in applications involving a pair of real valued sources, x_1 and x_2 , it is advantageous to apply BEMD to the complex signal $z = x_1 + jx_2$. The real and imaginary components of the decomposition can then be viewed as two separate sets of IMFs, corresponding respectively to the real and imaginary components of the input. The advantage of applying this bivariate approach, compared to two individual real valued EMD operations, is that by design it improves the stability and locality of each set of IMFs.

The BEMD operation uses multiple projections of the complex signal; each projection is real-valued and is used to describe the amplitude/envelope of the signal in a given direction. It is important to note that each projection is a function of both the real and imaginary parts and will therefore yield improved instantaneous amplitude estimation if at a given scale the real and imaginary parts share the same oscillatory modes. This is illustrated in more detail in the next section.

C. Performance Comparison of EMD and BEMD

The following two sections investigate the capacity of BEMD to achieve a more robust estimate of spectrum information compared to EMD, as accurate estimation of power spectrum is crucially important for asymmetry analysis. This is achieved by comparing their performance at 1) the IMF level and 2) the level of marginal Hilbert spectrum.

TABLE I SINUSOID RECONSTRUCTION (\hat{s}_{EMD} and \hat{s}_{BEMD}) RESULTS IN SNR FOR DIFFERENT FREQUENCIES AND INITIAL NOISE LEVELS

Algorithm	Freq. SNR _{init.}	2Hz	6Hz	12Hz	25Hz	44Hz
EMD	5dB	17.2dB	13.3dB	11.1dB	9.0dB	6.5dB
BEMD	5dB	18.8dB	13.8dB	11.7dB	9.5dB	7.4dB
EMD	0dB	12.6dB	9.7dB	7.5dB	5.5dB	4.1dE
BEMD	0dB	14.2dB	10.9dB	9.0dB	6.8dB	5.6dE
EMD	-5dB	9.2dB	6.0dB	4.3dB	3.0dB	2.2dE
BEMD	-5dB	10.7dB	7.7dB	5.9dB	4.4dB	3.0dB
EMD	-10dB	6.3dB	3.5dB	2.3dB	1.3dB	0.9dB
BEMD	-10dB	7.6dB	4.2dB	3.0dB	2.1 dB	1.3dB

1) *IMF Estimation:* The aim of asymmetry estimation is to characterise the degree of similarity between two data sources across frequency. In scenarios where the sources share similar components, we shall illustrate, following our previous work in [17], that the BEMD gives advantage by simultaneously modelling joint oscillating modes at each IMF level.

In this work, we decompose the signal $x = s_f + v$ using EMD, where s_f is a sinusoid of frequency f and v is a realisation of white Gaussian noise (WGN), and subsequently apply the Wiener filter.1 to the IMFs to obtain an estimate of the sinusoid, \hat{s}_{EMD} The more accurate the estimate of s_f , the more accurately the IMFs represent the original input components. Additionally, BEMD was performed on $z = (s_f + v_r) + j(s_f + v_i)$ where v_r and v_i denote different realisations of WGN in both the real and imaginary parts of z. For comparison with the EMD operation, the Wiener filter was applied to the *real part only* of the bivariate IMFs to obtain an estimate for the sinusoid, \hat{s}_{BEMD} . This analysis was performed for several frequencies, and over four signal-to-noise ratio (SNRinit.) levels. The analysis was also extended to $x = f_A(s_f) + v$ in the case of EMD and $z = f_A(s_f) + v_r + j(f_A(s_f) + v_i)$ in the case of BEMD where $f_A(\cdot)$ denotes an amplitude modulation operation (using 1 or 2 Hz sinusoid) to illustrate component estimation for signals with changing amplitudes. The sampling frequency was 256 Hz and the signal length 10 s.

The average SNR of the reconstructed uniform amplitude sinusoids over 50 simulations using EMD and BEMD are given in Table I. The superior performance of BEMD is evident for all considered simulations. Component estimation results for sinusoids modulated at 1 and 2 Hz are shown respectively in Tables II and III. The BEMD algorithm consistently allowed for better component estimation.

For rigour, the simulations were performed over a range of parameters for the stopping criterion, as BEMD and EMD often require different numbers of sifting operations even when using the same stopping criterion. Component estimation performance for the signal s_f , for f = 12 Hz and f = 44 Hz and for 0 dB and -10 dB SNR, for different numbers of sifting operations (by adjusting the stopping criterion) are shown in Fig. 1, where, as before, BEMD consistently outperform EMD. These results illustrate that the enhanced BEMD performance is caused by more accurate component estimation and not by virtue of better sifting.

¹For more detail on the combination of EMD and Wiener filter we refer to [24].

 $\begin{array}{c} \text{TABLE II} \\ \text{Reconstruction Results of a 1 Hz Amplitude Modulated} \\ \text{Sinusoid } (\hat{s}_{\text{EMD}} \text{ and } \hat{s}_{\text{BEMD}}) \text{ in SNR for Different} \\ \text{Frequencies and Initial Noise Levels} \end{array}$

Algorithm	Freq. SNR _{init.}	2Hz	6Hz	12Hz	25Hz	44Hz
EMD	5dB	17.1dB	12.6dB	10.6dB	8.8dB	6.5dB
BEMD	5dB	18.1dB	13.8dB	11.6dB	9.5dB	6.9dB
EMD	0dB	12.7dB	9.5dB	7.5dB	5.4dB	3.8dB
BEMD	0dB	14.1dB	10.3dB	8.1dB	6.1dB	5.1dB
EMD	-5dB	9.0dB	5.8dB	4.2dB	2.8dB	2.1dB
BEMD	-5dB	10.0dB	7.5dB	5.9dB	4.3dB	3.0dB
EMD	-10dB	5.8dB	3.3dB	2.2dB	1.3dB	0.9dB
BEMD	-10dB	7.0dB	4.3dB	3.0dB	2.1dB	1.3dB

 TABLE III

 RECONSTRUCTION RESULTS OF 2 HZ AMPLITUDE MODULATED

 SINUSOID (\hat{s}_{EMD} and \hat{s}_{BEMD}) IN SNR FOR DIFFERENT

 FREQUENCIES AND INITIAL NOISE LEVELS

Algorithm	Freq. SNR _{init.}	2Hz	6Hz	12Hz	25Hz	44Hz
EMD	5dB	16.8dB	13.0dB	11.0dB	8.7dB	6.5dB
BEMD	5dB	18.0dB	13.9dB	11.7dB	9.5dB	6.9dB
EMD	0dB	12.3dB	9.6dB	7.4dB	5.4dB	3.8dB
BEMD	0dB	13.9dB	10.4dB	8.4dB	6.2dB	5.1dB
EMD	-5dB	9.0dB	6.0dB	4.4dB	2.8dB	2.1dB
BEMD	-5dB	10.4dB	7.5dB	5.9dB	4.2dB	3.0dB
EMD	-10dB	5.9dB	3.3dB	2.2dB	1.3dB	0.9dB
BEMD	-10dB	7.0dB	4.1dB	3.0dB	2.1dB	1.3dB



Fig. 1. Reconstruction results of 1 Hz amplitude modulated sinusoid for different frequencies, average number of sifting operations and SNR ("--" EMD, "-" BEMD). (a) f = 12 Hz, SNR = 0 dB, (b) f = 12 Hz, SNR = -10 dB, (c) f = 44 Hz, SNR = 0 dB, (d) f = 44 Hz, SNR = -10 dB.

It can therefore be deduced that mutual information between the real and the imaginary parts of the BEMD allowed for a more accurate estimate of the common components at the IMF level. This is intuitive, as the performance of any EMD algorithm is dependent on accurate local mean estimation which, in the case of BEMD, is enhanced by two observations of any shared signal elements.

2) Spectrum Estimation: We shall now illustrate that the superior performance of BEMD over EMD supports a more accurate estimate of the marginal Hilbert spectrum (MHS) compared to EMD. As before, EMD and BEMD were applied to sinusoids with added WGN. In the case of BEMD, the MHS



Fig. 2. The marginal Hilbert spectrum of EMD and BEMD. In all scenarios, the MHS of BEMD is more localized in frequency. (a) 6 Hz with 0 dB noise. (b) 6 Hz with -5 dB noise. (c) 25 Hz with 0 dB noise. (d) 25 Hz with -5 dB noise.



Fig. 3. The kurtosis of the periodogram based power spectrum for a sine wave increasing noise levels. Kurtosis increases for high SNR, indicating a more concentrated spectrum.

was calculated for the real part of the bivariate IMFs for $z = s_f + v_r + j(s_f + v_i)$ where s_f is a sinusoid of frequency f and v_r and v_i are different realizations of WGN with identical statistics. In the case of EMD, the MHS was estimated for the IMFs of $s_f + v_r$. Fig. 2 compares the MHS of EMD and BEMD for several frequencies and SNRs, showing a more localized result produced by BEMD, particularly at low SNR.

To quantify the performance, the kurtosis of x, defined as

$$k = \frac{E\{(x - \mu)^4\}}{\sigma^4}$$
(5)

was used, where μ is the mean of x, σ is the standard deviation of x and $E\{\cdot\}$ the expected value operates. Since kurtosis measures the peakedness of a distribution, for spectra of narrow band components localized in frequency such as a sinusoid, a high kurtosis value indicates an accurate MHS. This is illustrated in Fig. 3 for the marginalized spectrum of a single sinusoid with added WGN; the graphs were calculated for increasing levels of



Fig. 4. The kurtosis for the MHS of the sinusoids of frequency f by EMD (cross) and BEMD (black squares) for the different noise levels. Even though the kurtosis of spectrum estimates based on EMD and BEMD are similar for -10 dB, the results of BEMD are almost always greater than those based on EMD, implying a more accurate MHS estimate. The values in the square boxes are one-tailed p-values of the t-test for the kurtosis of EMD and BEMD results. Their overall statistical significance, as determined by p-values, was less than 0.05. (a) f = 2 Hz, (b) f = 6 Hz, (c) f = 12 Hz, (d) f = 25 Hz, (e) f = 44 Hz.

noise.² Fig. 4 shows average results over 100 trials where kurtosis values were calculated for EMD and BEMD for different frequencies and different SNR.

²Every plot was produced as an average of 50 realizations of WGN for the different frequency sinusoids (64, 44, 32, 25, 16, 12, 8, 6, 4, 2, and 1 Hz, with 256 Hz sampling frequency), using periodogram.

For rigour, the degree of separation between the performance of BEMD and EMD was determined using the one-tailed t-test. The p-value, for each SNR and value for frequency, is also shown in Fig. 4. In 27 of the 30 considered simulations, the performance of the BEMD MHS was significantly better than that of EMD (p-values less than 0.05).

III. ASYMMETRY

Asymmetry is defined as the normalised difference between brain activity from a location on the left hemisphere and its corresponding location on the right hemisphere. In practice, the absolute value of this difference is used, however this is controversial among brain researchers as it produces results that can be highly correlated. In our analysis, the absolute value of the difference was considered as results without a modulus operation tend to be highly skewed [5].

A. BEMD Based Asymmetry

For a pair of sources, x_1 and x_2 , the complex IMFs are calculated for $z = x_1 + jx_2$. The real and imaginary components of the decomposition are then separated giving two sets of IMFs for the two input sources. The Hilbert transform is applied to obtain the instantaneous amplitudes $a_{1,i}(t)$ and $a_{2,i}(t)$, symbols "i" and "t" denote the order of IMF and the time index, and the instantaneous phases $\theta_{1,i}(t)$ and $\theta_{1,i}(t)$ using (3) for each set of IMFs. The instantaneous frequencies, $w_{1,i}(t)$ and $w_{2,i}(t)$, are computed by differentiating $\theta_{1,i}(t)$ and $\theta_{2,i}(t)$, which can be assumed to contain similar scales [17] since they are obtained from the real and imaginary components of a single complex IMF. It is therefore feasible to compare two spectral magnitudes $a_{1,i}(t)$ and $a_{2,i}(t)$, their common instantaneous frequency can be defined by the average of their respective instantaneous frequencies as

$$w_{1,2,i}(t) = \frac{w_{1,i}(t) + w_{2,i}(t)}{2}.$$
(6)

The corresponding marginal Hilbert spectra $h_1(w)$ and $h_2(w)$ (for x_1 and x_2 , respectively) are calculated according to (4). The asymmetry ratio, within the frequency range w_1 to w_2 , can now be expressed as

$$\Gamma_{(w_1,w_2)} = \frac{\left|\sum_{w_1}^{w_2} h_1^2(w) - \sum_{w_1}^{w_2} h_2^2(w)\right|}{\sum_{w_1}^{w_2} h_1^2(w) + \sum_{w_1}^{w_2} h_2^2(w)}.$$
(7)

We shall now illustrate the calculation of asymmetry ratio on two signals containing sinusoids at two frequencies

$$f_{1} = 13 \text{ Hz} \text{ and } f_{2} = 47 \text{ Hz}$$

$$t = 1/fs, \dots, 2s \text{ and } fs = 10 \text{ kHz}$$

$$x_{1} = \cos(2\pi f_{1}t) + \cos(2\pi f_{2}t)$$

$$x_{2} = 1.7\cos(2\pi f_{1}t) + 1.3\cos(2\pi f_{2}t).$$
(8)

Fig. 5 shows the asymmetry ratio with the lateralization evident at frequencies $f_1 = 13$ Hz and $f_2 = 47$ Hz.

IV. COGNITIVE EXPERIMENTS

To illustrate the advantages of using BEMD for estimating asymmetry, we considered its performance in two experimental



Fig. 5. Asymmetry ratio obtained using BEMD, for two channels. $x_1 = \cos(2\pi f_1 t) + \cos(2\pi f_2 t)$ and $x_2 = 1.7 \cos(2\pi f_1 t) + 1.3 \cos(2\pi f_2 t)$ with $f_1 = 13$ Hz and $f_2 = 47$ Hz.

settings. In the first experiment, EEG was band-pass filtered to occupy a certain frequency band and the level of asymmetry is calculated between noisy realisations of the conditioned signal. In the second experiment, EEG asymmetry features are used to identify different mental tasks in a BCI application.

A. Bandpass Filtered EEG

1) Setting: EEG data with a sampling frequency of 250 Hz was obtained from electrode P3 according to the 10–20 system [25] and filtered using a Butterworth filter such that it occupied specific frequency bands. For an EEG signal conditioned to occupy a frequency region denoted by "band," x_{band} , the asymmetry ratio was calculated for the signal pair

$$x_{\text{band}} + v_1, \quad x_{\text{band}} + v_2$$

where v_1 and v_2 are different realisations of WGN. Thus, the expected asymmetry result should be zero in the frequency region denoted by band and nonzero within the remainder of the spectrum. The asymmetry ratios obtained using three different spectrum estimation techniques (periodogram P_{xx} using Bartlett window, EMD and BEMD) were calculated for x_{band} conditioned to occupy different frequency bands (delta, theta, alpha, beta and gamma bands) for four different levels of SNR (5, 0, -5, -10 dB). Their performances were evaluated by the index $(\rho_{\text{band}})/(\rho_{\text{spec}}) \times 100$, where ρ_{band} is the total asymmetry detected in the correct frequency band, as dictated by the frequency range that x_{band} is conditioned to occupy for a given simulation, and $\rho_{\rm spec}$ is the total asymmetry detected in the full spectrum. The performance index for an accurate estimation of asymmetry will therefore give zero while poorer results will approach unity. The index was estimated and averaged over 50 independent trials for different realisations of v_1 and v_2 .

2) Results: Fig. 6 shows the asymmetry ratio calculated for the signal pair $x_{\text{band}} + v_1, x_{\text{band}} + v_2$ at intervals of 0.125 Hz where x_{band} was conditioned to occupy the alpha band and with SNR 0 dB. As expected, all the algorithms showed lower asymmetry in the alpha band than in the other frequency regions. The BEMD asymmetry estimate was the most accurate of all the considered algorithms.



Fig. 6. Asymmetry graphs for the alpha band signals (between the dashed lines) in 0 dB WGN. These asymmetry ratios were computed at intervals of 0.125 Hz. BEMD produced the lowest and most stable asymmetry in the alpha band. (a) Periodogram. (b) EMD. (c) BEMD.

Table IV shows a comparison of the performance for all the three algorithms, periodogram P_{xx} , EMD and BEMD, using the performance index $(\rho_{\text{band}})/(\rho_{\text{spec}}) \times 100$ for all considered frequency bands and noise levels. In 16 of the 20 considered simulations, the performance of BEMD exceeds those of the periodogram and EMD. In the other four cases, the performance difference between BEMD and the superior algorithm was not significant. In several instances the periodogram outperformed the standard EMD algorithm, due to the linearity of the data, for which the periodogram is ideally suited.³

B. BCI Application

1) Setting: The EEG data was recorded by Keirn and Aunon who conducted several mental task experiments⁴. These tasks were specially chosen for their known hemispheric brainwave asymmetry [11].

 $\begin{array}{c} \mbox{TABLE IV} \\ \mbox{Performance Evaluation, } (\rho_{\rm band})/(\rho_{\rm spec}) \times 100, \mbox{ for} \\ \mbox{Asymmetry Estimation Between Signals } x_1 \\ \mbox{and } x_2 \mbox{ at Different Frequencies and SNR} \end{array}$

Band	Algorithm SNR _{init}	P_{xx}	EMD	BEMD
	5	1.4 ± 0.6	2.7 ± 1.1	1.3 ± 1.2
Delta	0	$1.4 {\pm} 0.8$	2.2 ± 0.6	1.3 ± 0.5
	-5	1.9 ± 0.8	2.0 ± 0.5	1.3 ± 0.9
	-10	1.6 ± 0.8	2.0 ± 0.3	1.7 ± 0.4
	5	0.5 ± 0.2	$1.4{\pm}0.3$	$0.4 {\pm} 0.1$
Theta	0	0.8 ± 0.3	1.6 ± 0.2	$0.6 {\pm} 0.2$
	-5	1.7 ± 0.6	1.7 ± 0.3	1.1 ± 0.3
	-10	$2.2 {\pm} 0.9$	1.6 ± 0.4	1.7 ± 0.4
	5	1.4 ± 0.6	2.0 ± 0.4	1.0 ± 0.3
Alpha	0	2.1 ± 0.8	1.9 ± 0.3	1.1 ± 0.3
	-5	$2.4 {\pm} 0.9$	1.8 ± 0.3	1.6 ± 0.5
	-10	2.5 ± 1.2	2.2 ± 0.3	2.1 ± 0.5
	5	5.1 ± 1.1	7.5 ± 0.5	3.4±0.3
Beta	0	7.5 ± 1.7	7.8 ± 0.5	5.1 ± 0.5
	-5	9.9 ± 2.0	8.0 ± 0.5	5.2 ± 0.7
	-10	$11.8 {\pm} 2.6$	8.1 ± 0.6	7.9±0.8
	5	1.4±0.5	3.7±0.3	1.6 ± 0.2
Gamma	0	$2.4{\pm}0.7$	3.9 ± 0.4	2.6 ± 0.3
	-5	4.0 ± 1.2	4.3 ± 0.5	3.4 ± 0.4
	-10	5.3 ± 1.6	4.5 ± 0.5	4.4 ± 0.5

- Task 1—Baseline Measurements (B): No mental task was performed in this experiment. The subject was told just to relax and think of nothing.
- Task 2—Complex Problem Solving (M): The subject was required to solve a nontrivial multiplication problem without vocalizing. The problems were nonrepeating and were designed so that an immediate answer was not apparent. The subject verified at the end of the task whether or not he had arrived at a solution and no subject completed the task before the end of the 10 s recording session.
- Task 3—Geometric Figure Rotation (R): The subject was given a drawing of a complex three dimensional block figure to study. After 30 s, the figure was removed and the subject was instructed to visualize the object being rotated about an axis.
- Task 4—Mental Letter Composing (L): The subject composed a letter to a friend or relative without vocalizing.
- Task 5—Visual Counting (C): The subject was instructed to imagine a blackboard and to visualize numbers being written on the board. And the subject counted from the previous number and wrote it on the board after erasing the previous number.

Electrodes P3 and P4 were selected to calculate the asymmetry ratio between left and right hemisphere among all the recorded channels on the position O1, O2, P3, P4, C3, and C4 defined by the 10–20 system of electrode placement, at a 250 Hz data rate. The data were measured for 10 s during each task and each task was repeated five times per session. Recordings were made with reference to electrically linked mastoids A1 and A2. For more details about the experiments we refer to [11].

Asymmetry ratios in the delta, theta, alpha, beta and gamma bands, $\Gamma_{(1,3)}$, $\Gamma_{(4,7)}$, $\Gamma_{(8,13)}$, $\Gamma_{(14,30)}$, $\Gamma_{(36,44)}$, calculated using the periodogram (P_{xx}), EMD and BEMD were used in a classifier. A support vector machine (SVM) [27] with Gaussian

³The linearisation of nonlinear data is a well-known consequence of linear filtering operations [26].

⁴Publicly available from http://www.cs.colostate.edu/eeg/index.html.

	Subject 1			Subject 2			Subject 3			Subject 4		
	BEMD	EMD	P_{xx}	BEMD	EMD	P_{xx}	BEMD	EMD	P_{xx}	BEMD	EMD	P_{xx}
B, C	86.3	77.5	79.5	83.3	45	71.8	77.4	58.8	53.8	69	58.8	59.3
B, L	52.5	63.8	49.5	58.1	47.5	63.8	50.8	37.5	53.6	56	55	53.8
B, M	51.3	28.8	38	51.3	60	59.4	85.7	62.5	71.8	85.5	67.5	83.5
B, R	95.5	78.8	70	51.3	45	46	50.8	70	48	55.4	45	54
L, C	70.6	70	63.1	51.3	61.3	46	88	77.5	72.5	64	53.8	51.8
L, R	64.5	68.8	62.5	65	70	61.9	47	73.5	44	55.8	46.3	44.3
M, C	85	71.8	81.8	75.8	42.5	43	58.5	55	56.2	88.5	88.5	68.8
M, L	49.5	48.8	43.5	72	45	51	74.8	56.3	76.5	81.25	58.8	60.3
M, R	96	83.75	74	78	63.8	40.3	70.5	63.8	57.2	58	73.8	55.5
R, C	57.8	42.5	50.3	87.5	46.3	71.3	81.25	66.3	59.75	81	72.5	61.5
Average	70.9	63.8	61.2	67.3	52.6	55.5	68.5	62.1	59.3	69.5	62	59.3
Max	96	83.8	81.8	87.5	63.8	71.25	88	77.5	76.5	88.5	88.5	83.5
Best	M,R	M,R	M,C	R,C	M,R	B,C	L,C	L,C	M,L	M,C	M,C	B,M

CLASSIFICATION RATES OBTAINED USING PERIODOGRAM (SHOWN AS " P_{xxx} "), EMD and BEMD Based on Asymmetry Estimation for Four Subjects and Multiple Mental Task Combinations (Baseline Measurement (B), Complex Problem Solving (M), Geometric Figure Rotation (R), Mental Letter Composing (L), and Visual Counting (C)). Note the Improved Classification for Asymmetry Obtained Using BEMD

kernel, (the code obtained from [28]), was used to classify between two different mental tasks. The different combinations of two mental tasks are shown in Table V. Each combination had 20 samples of 4 s segment data because in the original recording [11] each subject had five trials for a task and the length of each EEG data was 8 s long discarding the first and last 1 s concerned about noise. The numbers of training sets and test sets were respectively 12 and 8. The classification was repeated 50 times while mixing the sample order, and the final classification result was the average of these outcomes.

2) *Results:* Table V shows the classification performances for the four subjects using the BEMD, EMD and periodogram. Of the 40 considered simulation scenarios, EMD and BEMD asymmetry outperformed periodogram asymmetry for 36. On average, the BEMD-based asymmetry calculation had a classification accuracy of 70%, a 10% improvement over periodogram-based asymmetry and a 7% improvement over EMD-based asymmetry.

These results fully illustrate the advantages of empirical mode decomposition and its algorithms for asymmetry estimation of real-world data. In simulations presented in previous sections of this paper, the signals of interest were linear: band-pass filtered EEG data. Algorithms based on Fourier theory such as the Periodogram are, by design, suitable for linear signal statistics and its performance exceeded that of standard EMD, and BEMD to a lesser extent, in some instances. However, for fully nonlinear and nonstationary data sources, the performance of both EMD and BEMD facilitated an improvement over traditional linear asymmetry estimates.

In practice, asymmetry features are often combined with spectral power features to achieve separation between mental tasks [29]. As our aim was to address only asymmetry performance, it is shown that BEMD asymmetry achieved classification accuracy exceeding 85% in some instances.

Recently, empirical mode decomposition has been extended to multivariate EMD by Rehman *et al.* [30] in order to make EMD suitable for multichannel signal processing. It was also illustrated [31] how the noise assisted MEMD allows for enhanced localization in time-frequency analysis. In future work, multivariate EMD techniques will be utilized to extract more accurate and robust asymmetry features.

V. CONCLUSION

It has been shown that complex extension of the EMD algorithm provides a robust estimate of asymmetry for nonlinear and nonstationary data. One such extension, bivariate empirical mode decomposition facilitates enhanced multicomponent analysis and improved marginal Hilbert spectrum estimation, critical to the calculation of asymmetry. A statistical assessment of the proposed framework has been presented for both synthetic signals and for EEG from a BCI application. The BEMD-based asymmetry results are shown to be highly localized in frequency and robust to additive noise.

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