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Top-quark pair hadroproduction in association with a heavy boson at NLO+NNLL including EW corrections

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ABSTRACT: This work studies the associated production of a top-quark pair with a W, Z, or Higgs boson at the LHC. Predictions for the total cross sections as well as for several differential distributions of the massive particles in the final state are provided. These predictions, valid for the LHC operating at 13 TeV, include without any approximation all the NLO electroweak and QCD contributions of $\mathcal{O}(\alpha_s^i \alpha^{j+1})$ with i + j = 2, 3. In addition, the predictions presented here improve upon the NLO QCD results by adding the effects of soft gluon emission corrections resummed to next-to-next-to-leading logarithmic accuracy. The residual dependence of the predictions on scale and PDF choices is analyzed.

KEYWORDS: NLO Computations, QCD Phenomenology

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1 Introduction

The Run-II at the LHC, with a center of mass energy of 13 TeV and a higher instant luminosity w.r.t. Run-I, made this collider a fully operational top-quark factory. Indeed, the heaviest of the Standard Model (SM) particles can be produced via different channels, many of which have been observed at the LHC. To date, not only top-quark pair [1–4] and single top-production [5–9] modes, but also the production of a top-quark pair in association with a heavy electroweak (EW) boson have been measured. The latter class involves $t\bar{t}W^{\pm}$ [10– 13], $t\bar{t}Z$ [10–14] and $t\bar{t}H$ [15, 16] production processes. These three processes are extremely important in the searches for beyond-the-SM (BSM) effects, both as components of the background and of the signal itself. For example, $t\bar{t}W^{\pm}$ and $t\bar{t}Z$ production constitute the main backgrounds in the measurement of the leptonic signatures emerging from $t\bar{t}H$ production [17–19], which in turn enables the direct measurement of the coupling of the top quark to the Higgs boson. Analogously, the $t\bar{t}Z$ production process can be employed for the measurement of the coupling of the top quark to the Z boson [13, 20]. Finally, it is worth noting that very recently also single-top plus Z associated production was observed [21].

For a correct interpretation of current and future measurements and the possible identification of BSM effects, precise predictions for these processes, and, consequently, the study of their radiative corrections, are of paramount relevance. For top-quark pair and single-top production next-to-next-to-leading (NNLO) QCD corrections were computed in [22–26]. For top pair production, also next-to-leading-order (NLO) electroweak (EW) corrections [27, 28] and/or next-to-next-to-leading-logarithmic (NNLL) accuracy resummation of threshold and small-mass logarithms [29, 30]) were accounted for. This level of accuracy is not yet achievable for processes with three massive particles (two of which are colored) in the final state, nor is it expected in the near future. Still, it is desirable to have the best possible current predictions, i.e. those which include all corrections of QCD and EW origin that can be calculated with current technology. In addition, it is necessary to thoroughly study the phenomenological impact of these predictions at the differential level.

In this paper we provide state-of-the-art SM predictions for top-quark pair hadroproduction in association with an EW heavy boson; we calculate the complete-NLO predictions for $t\bar{t}W^{\pm}$, $t\bar{t}Z$ and $t\bar{t}H$ in proton-proton collisions at 13 TeV and we resum soft gluon emission effects at NNLL accuracy in QCD. All the EW and QCD contributions of $\mathcal{O}(\alpha_s^i \alpha^{j+1})$ with i + j = 2,3 are evaluated without any approximation. In addition, in Mellin space, the resummation procedure accounts for terms proportional $\alpha_s^{2+n} \alpha \ln^k \bar{N}$ with $\max\{0, 2n - 3\} \leq k \leq 2n$ at all orders $(n \geq 1)$ in α_s , where $\bar{N} = Ne^{\gamma_{\rm E}}$ with N the Mellin parameter, and $\bar{N} \to \infty$ is the soft emission limit.

The calculation of the complete-NLO corrections to $t\bar{t}W^{\pm}$ production is based on the work in [31] and has been carried out with the new public version of MAD-GRAPH5_AMC@NLO [32]. This code was also used to obtain complete-NLO corrections to $t\bar{t}H$ and $t\bar{t}Z$ production. The calculations of soft gluon effects to NNLL accuracy in QCD for $t\bar{t}W^{\pm}$, $t\bar{t}Z$ and $t\bar{t}H$ are based on the work in [33–37] and on the in-house parton level Monte Carlo code that was developed for those papers. The resummation of soft emission effects was also studied in [38, 39], where a resummation framework different from the one considered in [33–36] was employed. Very recently, in [40] also the resummation of Coulomb effects for $t\bar{t}H$ production was studied.

The paper is organized as follows. In section 2 we briefly summarize the salient features of the calculational framework used in order to evaluate the various corrections. Section 3 includes a description of the input parameters and PDF sets employed in the calculation, as well a discussion of the values chosen for the factorization and resummation scales. Predictions for the total cross section and differential distributions for the processes considered in this study are collected in section 4. Finally, section 5 contains our conclusions.

2 Calculational framework

In this section we describe the calculational framework on which the phenomenological predictions presented in section 4 are based. In sections 2.1 and 2.2 we briefly summarize

the calculation of the complete-NLO corrections of QCD and EW origin [31, 32] and the resummation of soft-gluon effects at NNLL accuracy [33–36], respectively. In section 2.3 we explain how the combination and matching of complete-NLO and resummation of soft-gluon effects is carried out. We will denote the class of processes considered in this work as $t\bar{t}V$, where V can be W^+, W^-, Z or H. In section 2.4 we recall the most relevant phenomenological features of the different contributions entering the complete-NLO calculation, and comment on the implications for soft gluon resummation.

2.1 Complete-NLO

The fixed order expansion of a generic observable Σ for the processes $pp \to t\bar{t}V(+X)$ (where X indicates that the process is inclusive over extra QCD and QED radiation) in powers of α_s and α can be expressed as

$$\Sigma^{t\bar{t}V}(\alpha_s,\alpha) = \sum_{m+n \ge 2} \alpha_s^m \alpha^{n+1} \Sigma_{m+n+1,n}^{t\bar{t}V}, \qquad (2.1)$$

with m and n positive integers. LO contributions consist of $\sum_{m+n+1,n}^{t\bar{t}V}$ terms with m+n=2and involve tree-level diagrams only. NLO corrections correspond to the terms with m+n=3 and are induced by the interference among all the possible one-loop and tree-level Born diagrams as well among all the possible tree-level diagrams involving one additional quark, gluon or photon in the final state.

In this work, "complete-NLO" is used to indicate the quantity $\Sigma^{t\bar{t}V}(\alpha_s, \alpha)$, in which all terms $\Sigma^{t\bar{t}V}_{m+n+1,n}$ with m + n = 2, 3 are included. On the other hand, a more user-friendly notation can be used to refer to any individual term in eq. (2.1). We denote $t\bar{t}V$ observables at LO as $\Sigma^{t\bar{t}V}_{LO}$ and further redefine the individual perturbative orders as

$$\Sigma_{\rm LO}^{t\bar{t}V}(\alpha_s,\alpha) = \alpha_s^2 \alpha \Sigma_{3,0}^{t\bar{t}V} + \alpha_s \alpha^2 \Sigma_{3,1}^{t\bar{t}V} + \alpha^3 \Sigma_{3,2}^{t\bar{t}V}$$
$$\equiv \Sigma_{\rm LO_1} + \Sigma_{\rm LO_2} + \Sigma_{\rm LO_3} . \tag{2.2}$$

Similarly, NLO corrections and their individual perturbative orders can be defined as

$$\check{\Sigma}_{\rm NLO}^{t\bar{t}V}(\alpha_s,\alpha) = \alpha_s^3 \alpha \Sigma_{4,0}^{t\bar{t}V} + \alpha_s^2 \alpha^2 \Sigma_{4,1}^{t\bar{t}V} + \alpha_s \alpha^3 \Sigma_{4,2}^{t\bar{t}V} + \alpha^4 \Sigma_{4,3}^{t\bar{t}V}
\equiv \check{\Sigma}_{\rm NLO_1} + \check{\Sigma}_{\rm NLO_2} + \check{\Sigma}_{\rm NLO_3} + \check{\Sigma}_{\rm NLO_4}.$$
(2.3)

In contrast to the notation used in previous works [27, 31, 32, 41–44], here and in the rest of the text $\check{\Sigma}$ indicates a quantity that does not include any LO contribution, while Σ indicates a quantity that does include LO contributions. In particular, all the LO_i are included for predictions beyond the LO, unless the subscript "QCD" is present; in this case only the Σ_{LO_1} is included. Consequently, with this convention an observable Σ evaluated at complete-NLO accuracy can be written as

$$\Sigma_{\rm NLO} = \Sigma_{\rm LO} + \dot{\Sigma}_{\rm NLO} \,. \tag{2.4}$$

Observe that the quantities Σ and $\check{\Sigma}$ are in general defined in such a way that they do include the appropriate multiplicative factor of powers of α and α_s , as shown in eqs. (2.2)

and (2.3). We use the symbols $\Sigma_{\text{LO}_i}(\hat{\Sigma}_{\text{NLO}_i})$ or interchangeably their shortened aliases $\text{LO}_i(\text{NLO}_i)$ to indicate individual terms in the l.h.s. of eqs. (2.2) and (2.3). It is important to remember that in the literature the term "LO" usually refers only to LO₁, which instead here is denoted by LO_{QCD}. Therefore, with this notation one has

$$\Sigma_{\rm NLO_{QCD}} \equiv \Sigma_{\rm LO_1} + \dot{\Sigma}_{\rm NLO_1} \,. \tag{2.5}$$

NLO EW corrections, which are of $\mathcal{O}(\alpha)$ w.r.t. the LO₁ observable, correspond to the Σ_{NLO_2} terms, so we also denote them as NLO_{EW}. On occasion, we also refer to the set of Σ_{LO_i} and $\check{\Sigma}_{\text{NLO}_i}$ corrections with $i \geq 2$ as "electroweak corrections" (not to be confused with NLO_{EW} corrections just defined). The prediction at complete-NLO accuracy, which is the sum of all the LO_i and NLO_i ($i \geq 1$) terms, is denoted as "NLO".¹ Consistently with the notation introduced above, the sum of the NLO_i corrections without the LO is indicated by $\check{\Sigma}_{\text{NLO}}$ (see eq. (2.3)).

It is important to point out that for all the $t\bar{t}V$ processes we do not include the (finite) contributions from the real-emission of heavy particles (W^{\pm} , Z and H bosons), also denoted in the literature as heavy-boson-radiation (HBR) contributions. Although they are formally part of the inclusive predictions at complete-NLO accuracy, these finite contributions in general lead to very different collider signatures and are typically small. For $t\bar{t}V$ processes, the HBR contributions to NLO₂ were evaluated in [42].

The calculation of the complete-NLO predictions is carried out by employing the latest version of MADGRAPH5_AMC@NLO [32], which is now public. In MADGRAPH5_AMC@NLO, the FKS method [45, 46] (automated in the module MADFKS [47, 48]) is used in order to deal with infrared singularities. One-loop amplitudes are evaluated by dynamically switching among different kinds of techniques for integral reduction, namely, the OPP method [49], the Laurent-series expansion [50], and the tensor integral reduction [51–53]. These techniques are automated in the module MADLOOP [54], which is used for generating the amplitudes. We remind the reader that MADLOOP employs CUTTOOLS [55], NINJA [56, 57] and COLLIER [58], and includes an in-house implementation of the OPEN-LOOPS optimization [59].

2.2 Resummation

The resummation of the soft-gluon emission corrections to the $t\bar{t}V$ production processes is carried out as described in detail in [34–36], with techniques based on Soft Collinear Effective Theory² (SCET) [61–63] and renormalization-group-improved perturbation theory. We summarize here the salient features of the resummation procedure. In $t\bar{t}V$ production, the underlying partonic processes are of the form

$$i(p_1) + j(p_2) \longrightarrow t(p_3) + \bar{t}(p_4) + V(p_5) + X,$$
 (2.6)

¹In ref. [31] a slightly different notation has been used. Therein NLO and NLO_{QCD} predictions refer to the corrections only, without including LO contributions. On the other hand, note that for the case of EW corrections also here NLO_{EW} \equiv NLO₂.

²For an introductory review of SCET, see [60].

where X indicates unobserved final-state light-quark and/or gluon radiation. The incoming partons i, j which enter the production process depend on the boson V under consideration. At lowest order in QCD, if $V = W^{\pm}$ then $i, j \in q\bar{q}', \bar{q}'q$, where q' indicates the isospin partner of the quark q. If V = H, Z instead, both the quark-annihilation channel and the gluon-fusion channel contribute to the process, so that $i, j \in q\bar{q}, \bar{q}q, gg$.

One can then define the invariants³

$$\hat{s} \equiv (p_1 + p_2)^2 = 2p_1 \cdot p_2, \qquad M^2 \equiv (p_3 + p_4 + p_5)^2, \qquad (2.7)$$

and starting from these quantities one can define the parameter

$$z \equiv \frac{M^2}{\hat{s}} \,. \tag{2.8}$$

At lowest order in QCD, z = 1, while beyond leading order $z \leq 1$. We define the "soft" or "partonic threshold" limit as the limit $z \to 1$, since in this limit the final state radiation X must be soft.

In the partonic threshold limit the $t\bar{t}V$ production cross section factorizes as follows:

$$\sigma(s, m_t, m_V) = \frac{1}{2s} \int_{\tau_{\min}}^{1} d\tau \int_{\tau}^{1} \frac{dz}{z} \sum_{i,j} f_{ij}\left(\frac{\tau}{z}, \mu\right) \\ \times \int dPS_{t\bar{t}V} \operatorname{Tr}\left[\mathbf{H}_{ij}\left(\{p\}, \mu\right) \mathbf{S}_{ij}\left(\frac{M(1-z)}{\sqrt{z}}, \{p\}, \mu\right)\right].$$
(2.9)

In eq. (2.9), s indicates the square of the hadronic center of mass energy, the symbol $\{p\}$ is used to indicate the list of momenta p_1, \dots, p_5 , while

$$\tau \equiv \frac{M^2}{s}, \quad \text{and} \quad \tau_{\min} \equiv \frac{(2m_t + m_V)^2}{s}.$$
(2.10)

The functions \mathbf{H} , \mathbf{S} and f are the hard function, the soft function and the parton luminosity function, respectively. These functions are channel dependent and therefore they appear in eq. (2.9) with an ij subscript. The trace of the product of the hard and soft function is integrated over the $t\bar{t}V$ phase space, whose integration measure is indicated by $dPS_{t\bar{t}V}$. The hard and soft functions are matrices in color space. Only partonic channels that are open at LO_{QCD} contribute to the cross section in the partonic threshold limit. In the quark-annihilation channel, which contributes to $t\bar{t}W^{\pm}$, $t\bar{t}H$ and $t\bar{t}Z$, the hard and soft functions are two-by-two matrices in color space, while in the gluon-fusion channel, which contributes only to $t\bar{t}H$ and $t\bar{t}Z$, the hard and soft functions are three-by-three matrices. Details on the definition of the hard, soft and luminosity functions as well as on the final state phase space can be found in refs. [33–36].

³In refs. [33–36], as well as in a number of papers on top-quark pair production (see for example [64–67]), the invariant mass of the massive particles in the final states is indicated by M, as it is done in this section. However, in section 4 we discuss simultaneously results for $t\bar{t}W^{\pm}, t\bar{t}Z$ and $t\bar{t}H$ production. In that section, in order to avoid any possible source of confusion, we differentiate the three different processes considered by indicating the invariant mass of each one of them as $m(t\bar{t}W), m(t\bar{t}Z), m(t\bar{t}H)$, respectively.

It is important to observe that the soft functions are singular in the partonic threshold limit $z \to 1$. They contain delta functions and plus distributions of the form

$$P_k(z) \equiv \left\lfloor \frac{\ln^k (1-z)}{1-z} \right\rfloor_+ . \tag{2.11}$$

The plus distributions are defined in such a way that they can be integrated up to z = 1; if f(z) represents a smooth test function that is not singular in the $z \to 1$ limit, then one has

$$\int_0^1 f(z) P_k(z) dz \equiv \int_0^1 \frac{\ln^k (1-z)}{1-z} \left[f(z) - f(1) \right] dz \,. \tag{2.12}$$

At each fixed order in perturbation theory, the soft function involves terms proportional to $\alpha_s^n P_k(z)$, where *n* indicates the order of QCD corrections and $0 \le k \le 2n - 1$. For example, NLO QCD corrections include P_1 and P_0 distributions, NNLO QCD corrections include P_3, P_2, P_1 and P_0 distributions, etc. These terms arise from soft gluon emission corrections and provide numerically large contributions to the hadronic cross section and differential distributions. In a sense, the purpose of resummation is to account for some of the terms proportional to the plus distributions to all orders in perturbation theory. One convenient way of achieving this goal is to derive and solve the renormalization group equations satisfied by the hard and soft functions. The renormalization group equations are regulated by anomalous dimensions, which were computed to two loops in refs. [68, 69].

The hard functions and soft functions are free from large logarithmic corrections at appropriately chosen (and different) scales μ_h and μ_s . At those scales, the hard and soft functions are well behaved in fixed-order perturbation theory. In order to achieve NNLL accuracy, one needs to evaluate the hard and soft function up to NLO. The soft functions are process independent. The soft function for the quark-annihilation channel in $t\bar{t}W^{\pm}$ is identical to the quark-annihilation channel soft function for $t\bar{t}Z$ or $t\bar{t}H$, up to a trivial replacement of the mass of the heavy boson $m_W \to m_Z$ or $m_W \to m_H$, respectively. Similarly, the soft functions for the gluon-fusion channel in $t\bar{t}H$ and $t\bar{t}Z$ production are also identical. The NLO hard functions are instead process dependent. They receive contributions only from one-loop QCD corrections to the production channels that are already open at tree level in QCD: quark annihilation channel for $t\bar{t}W^{\pm}$ production, quark-annihilation and gluon-fusion channels for $t\bar{t}H$ and $t\bar{t}Z$ production. The hard functions needed for this work were evaluated by means of a customized version of the code OPENLOOPS [59] run in combination with the tensor reduction library COLLIER [58].

The resummation of the soft emission corrections is carried out in Mellin space, where the integral form of the cross section becomes

$$\sigma(s, m_t, m_V) = \frac{1}{2s} \int_{\tau_{\min}}^{1} \frac{d\tau}{\tau} \frac{1}{2\pi i} \int_{c-i\infty}^{c+i\infty} dN \tau^{-N} \sum_{ij} \widetilde{f}_{ij}(N, \mu) \int d\mathrm{PS}_{t\bar{t}V} \, \widetilde{c}_{ij}(N, \{p\}, \mu) \,.$$

$$(2.13)$$

The Mellin parameter is indicated by N and the threshold limit $z \to 1$ corresponds to the limit $N \to \infty$ in Mellin space. The functions \tilde{f} and \tilde{c} are the Mellin transforms of the luminosity function f and of the trace of the product of the hard and soft function, respectively.

The plus distributions found in the soft function in momentum space are mapped into logarithms of the Mellin parameter in Mellin space, such that in Mellin space the QCD corrections contain terms of the form $\alpha_s^{2+n} \ln^k N$, with $0 \le k \le 2n$. Terms suppressed by inverse powers of N in the partonic cross section in Mellin space are neglected in eq. (2.13).

While the hard and soft functions included in \tilde{c} are evaluated in fixed order perturbation theory at the scales μ_h and μ_s , their product is evolved to a common scale μ_f by solving the renormalization group equations satisfied by the functions. The scale μ_f is the scale which enters in the PDFs and, consequently, in the parton luminosity function \tilde{f} . Ultimately, the resummed hard scattering kernels \tilde{c} have the following structure

$$\widetilde{c}_{ij}(N,\{p\},\mu_f) = \operatorname{Tr}\left[\widetilde{\mathbf{U}}_{ij}(\bar{N},\{p\},\mu_f,\mu_h,\mu_s)\,\mathbf{H}_{ij}(\{p\},\mu_h)\,\widetilde{\mathbf{U}}_{ij}^{\dagger}(\bar{N},\{p\},\mu_f,\mu_h,\mu_s)\right.\\ \left.\times\,\widetilde{\mathbf{s}}_{ij}\left(\ln\frac{M^2}{\bar{N}^2\mu_s^2},\{p\},\mu_s\right)\right],\tag{2.14}$$

with $\bar{N} = Ne^{\gamma_E}$. The evolution factors $\tilde{\mathbf{U}}$ include the full dependence on potentially large logarithms of the ratios μ_h/μ_s , μ_h/μ_f , μ_f/μ_s and are, like the hard and soft functions, channel-dependent matrices in color space. The explicit expression for the evolution factors in terms of the anomalous dimensions regulating the renormalization group equations can be found in eq. (3.7) in reference [34] for the $t\bar{t}W^{\pm}$ case. The evolution factors are identical also for the $t\bar{t}H$ and $t\bar{t}Z$ cases, provided that one accounts for the fact that the explicit expressions of the anomalous dimensions are different for the quark-annihilation and gluonfusion channels.

If all of the factors in the r.h.s. of eq. (2.14) were known at all orders in perturbation theory, the l.h.s. of the equation would not depend on μ_h nor on μ_s . However, since the hard function, the soft function, and the anomalous dimensions entering in the evolution factor are all evaluated up to a certain order in perturbation theory, a residual numerical dependence on the choice of μ_s and μ_h remains in the predictions presented in section 4. This residual dependence on the scale choices is used, as usual in QCD, to estimate the theoretical error induced by the truncation of the perturbative series in the calculation of the various elements in the resummation formula. As discussed above, one should choose the hard and soft scales μ_h and μ_s in such a way that the hard and soft functions are free from large logarithmic corrections and are therefore calculable, at their characteristic scales, in fixed-order perturbation theory. Reasonable choices for these scales are, e.g., $\mu_h \sim M, \mu_s \sim M/\bar{N}$ or $\mu_h \sim H_T, \mu_s \sim H_T/\bar{N}$, where M is the invariant mass of the $t\bar{t}V$ final state and H_T is the sum of the transverse mass of the top quark, antitop quark and heavy vector boson:

$$H_T = \sqrt{m_t^2 + p_{T,t}^2} + \sqrt{m_t^2 + p_{T,\bar{t}}^2} + \sqrt{m_V^2 + p_{T,V}^2} \,. \tag{2.15}$$

The issue of scale choices is discussed in section 3.2. However, at this stage, it is important to observe that, in order to eliminate large logarithms from the soft function in Mellin space, the soft scale must depend on the Mellin parameter \bar{N} . This fact gives rise to a branch cut in \tilde{c} for large values of \bar{N} , which in turn is related to the Landau pole in α_s . The integration path in the complex \bar{N} plane is chosen according to the *Minimal Prescription* [70]. Notice that the ratio $\mu_h/\mu_s \sim \bar{N}$. An alternative to this approach is to perform the resummation directly in momentum space, fixing the soft scale at the hadronic level through a fitting procedure, see for example [65, 71–74]. When resummation is carried out up to NNLL accuracy, as it is the case in this work, one is accounting for terms proportional to $\alpha_s^{2+n} \ln^k \bar{N}$ with $2n \geq k \geq \max\{0, 2n-3\}$ to all orders in α_s in the partonic cross section in Mellin space. Finally, the parton luminosity functions in Mellin space, \tilde{f} , that appear in eq. (2.13) can be obtained using techniques described in refs. [75, 76].

NNLL corrections to differential distributions such as the top-quark transverse momentum distribution, the vector boson transverse momentum distribution, the top-pair invariant mass, the $t\bar{t}V$ system invariant mass etc., can be obtained by evaluating eq. (2.13) by means of the in-house Monte Carlo code developed for [34–36]. The code evaluates the total cross section while simultaneously binning events w.r.t. variables which can be built out of the $t\bar{t}V$ momenta, such as the ones listed above. However, it must be pointed out that, in its current implementation, the code calculates the Mellin transform of the luminosity function in eq. (2.13) and loses the information about the x values at which the PDFs are evaluated. Hence it cannot be employed to evaluate rapidity distributions to NNLL accuracy in the laboratory frame.⁴

Nevertheless, the NNLL resummation formula can also be employed to obtain approximate NNLO_{QCD} results, which are indicated by nNLO_{QCD} in this work. The nNLO_{QCD} cross section can be obtained by solving the renormalization group equation satisfied by the NLO soft function. The nNLO_{QCD} predictions discussed in section 4 include, on top of the complete NLO, all of the terms of order $\alpha_s^4 P_k(z)$ ($3 \ge k \ge 0$) in the partonic QCD cross section in momentum space, as well as part of the terms proportional to $\alpha_s^4 \delta(1-z)$. A detailed description of the terms of the latter class that are included in the nNLO_{QCD} calculations can be found in section 3 in [33]. These calculations depend on a single scale μ_f , in contrast with resummed calculations, which have a residual dependence on the scales also for rapidity distributions.

We conclude this section by returning to a point briefly mentioned in the discussion of the hard function. The resummation carried out in refs. [33–36] and in this work deals with QCD corrections only, meaning that the resummation formulas are linear in the fine structure constant α . While it is in principle possible to consider the resummation of soft-gluon emission corrections to contributions that are proportional to higher powers of α , their implementation is not trivial. However, the contribution of these corrections is expected to be numerically smaller than the contribution of the soft emission to the QCD process. In addition, one can gain some rough sense of the size of neglected higher order mixed QCD-electroweak corrections by comparing the multiplicative and additive approaches to the matching of NLO and NNLL calculations, discussed in the next section. Results given in section 4 indicate that the difference between the matched results in the additive approach and in multiplicative approach is, with few exceptions, a small effect.

⁴Note that this is not a matter of principle, and indeed NNLL resummation for rapidity distributions was recently carried out in [77].

2.3 Matching procedure

The main goal of this paper is to match the NLO QCD and electroweak corrections to $t\bar{t}V$ production (i.e. the complete-NLO corrections) to the resummation of soft gluon emissions to NNLL accuracy in QCD. In order to achieve this goal, it is necessary to avoid the double counting of terms that are included in both the NLO QCD corrections and the NNLL resummation formula. The method that allows one to avoid such a double counting is well understood and goes under the name of *matching procedure*.

In order to understand the details of the matching procedure it is necessary to identify terms in the NLO QCD partonic cross section that are included in the resummation formula in eq. (2.14). If one sets $\mu_s = \mu_h = \mu_f$ in that equation, the evolution factors U become identity matrices in color space. In that situation, the trace of the hard function and Mellin-space soft function (both evaluated to NLO) includes terms proportional to $\alpha \alpha_s^3 \ln^2 \bar{N}$ and $\alpha \alpha_s^3 \ln \bar{N}$, as well as terms that do not depend on the Mellin parameter \overline{N} . The latter class of terms still depends on the Mandelstam invariants; nevertheless, those \overline{N} independent terms are referred to as "constant" terms. Terms proportional to inverse powers of the Mellin parameter, which are present in the full QCD partonic cross section at NLO in Mellin space, cannot be reconstructed starting from the NNLL resummation formula. The trace of the hard function and soft function at NLO in Mellin space, including the terms discussed above, can be inserted in eq. (2.13) to obtain what is referred to as the *approximate* NLO QCD cross section, denoted here with the subscript nLO_{QCD}. The nLO_{QCD} cross section contains the contribution of all of the terms proportional to $\alpha \alpha_s^3 P_k(z)$ (k = 0, 1) and $\delta(1 - z)$ in the partonic cross section in momentum space. In analogy with the notation introduced in section 2.1, we indicate the terms of $\mathcal{O}(\alpha \alpha_s^3)$ included in the nLO_{QCD} corrections to a given observable with $\Sigma_{nLO_{OCD}}$. Consequently, we define the observable Σ evaluated to nLO_{QCD} as

$$\Sigma_{\rm nLO_{QCD}} \equiv \Sigma_{\rm LO_{QCD}} + \tilde{\Sigma}_{\rm nLO_{QCD}} \,. \tag{2.16}$$

Once the QCD and EW complete-NLO corrections (whose sum will simply be referred to as NLO), the NNLL corrections, and the nLO_{QCD} predictions for a given observable Σ are available, it is straightforward to combine them into an NLO+NNLL prediction by using the matching formula

$$\Sigma_{\rm NLO+NNLL} \equiv \Sigma_{\rm NLO} + \left[\Sigma_{\rm NNLL} - \Sigma_{\rm nLO_{QCD}} \right] \,. \tag{2.17}$$

The symbol Σ_{NNLL} indicates the numerical value of the resummed total cross section in eq. (2.13) or, in the case of differential distributions, the value of that resummed cross section in a specific bin of the distribution. The terms included in square brackets in eq. (2.17) are of $\mathcal{O}(\alpha \alpha_s^4)$ and higher, and represent the NNLL corrections to be added to the NLO result. The quantity $\Sigma_{\text{NLO+NNLL}}$ is defined in such a way as to include all of the corrections to the observable Σ considered in this work. In discussing the results of this study, it is also useful to match the resummed formulas to the QCD cross section only, by excluding all the EW corrections. In that case, eq. (2.17) must be modified by replacing $NLO \rightarrow NLO_{QCD}$ in the first term in the r.h.s. of the equation. The predictions obtained in this way include only QCD effects and are indicated by the $NLO_{QCD} + NNLL$ subscript:

$$\Sigma_{\rm NLO_{QCD}+NNLL} \equiv \Sigma_{\rm NLO_{QCD}} + \left[\Sigma_{\rm NNLL} - \Sigma_{\rm nLO_{QCD}}\right] \,. \tag{2.18}$$

Calculations at NLO_{QCD} + NNLL accuracy correspond to the results presented in refs. [34–36].

Analogously, it is possible to match $nNLO_{QCD}$ predictions discussed at the end of section 2.2 to the complete-NLO prediction. A given observable Σ can be evaluated to nNLO by calculating the quantity

$$\Sigma_{\rm nNLO} \equiv \Sigma_{\rm NLO} + \left[\Sigma_{\rm nNLO_{\rm QCD}} - \Sigma_{\rm NLO_{\rm QCD}} \right] \,. \tag{2.19}$$

In eq. (2.19), $\Sigma_{\text{NLO}_{\text{QCD}}}$ includes LO_{QCD} terms of $\mathcal{O}(\alpha \alpha_s^2)$ and NLO_{QCD} terms of $\mathcal{O}(\alpha \alpha_s^3)$. $\Sigma_{\text{nNLO}_{\text{QCD}}}$ contains terms of $\mathcal{O}(\alpha \alpha_s^n)$ ($2 \leq n \leq 4$), including the complete $\Sigma_{\text{NLO}_{\text{QCD}}}$ cross section. Consequently, the square bracket in eq. (2.19) includes only the terms of $\mathcal{O}(\alpha \alpha_s^4)$ that must be added to the complete-NLO calculation in order to evaluate the observable to nNLO. Finally, one can exclude the EW corrections from eq. (2.19) by replacing NLO \rightarrow NLO_{QCD} in the first term on the r.h.s.: in this way one obtains approximate NNLO corrections to the QCD process, which are indicated with nNLO_{QCD}.

Eqs. (2.17) and (2.19) combine NLO to NNLL QCD or approximate NNLO QCD corrections in an additive approach, which is well defined in perturbation theory. However, it is possible to combine these contributions within a multiplicative approach, which is often employed in combining NLO QCD and NLO EW corrections, denoted in this work by NLO₁ and NLO₂, respectively. While in the additive approach NLO₁ and NLO₂ are simply summed so that

$$\dot{\Sigma}_{\rm NLO_{QCD+EW}} = \dot{\Sigma}_{\rm NLO_1} + \dot{\Sigma}_{\rm NLO_2} \,, \tag{2.20}$$

in the multiplicative approach these two corrections are combined via the prescription

$$\check{\Sigma}_{\rm NLO_{QCD\times EW}} = \check{\Sigma}_{\rm NLO_1} + \check{\Sigma}_{\rm NLO_2} \left(\frac{\Sigma_{\rm NLO_{QCD}}}{\Sigma_{\rm LO_{QCD}}}\right).$$
(2.21)

By comparing eqs. (2.20) and (2.21), it is possible to see that differences between the two approaches only enters at the level of mixed QCD-EW NNLO corrections of $\mathcal{O}(\alpha_s \alpha)$ relative to LO₁, i.e., in the case of $t\bar{t}V$ cross sections at $\mathcal{O}(\alpha_s^3 \alpha^2)$, which is beyond the accuracy of the calculations presented in this work. However, there are specific configurations where the multiplicative approach is well-motivated and expected to provide improved predictions. The typical case is when the NLO₁ contribution is dominated by soft-QCD physics, and the NLO₂ correction by large EW Sudakov logarithms. Indeed, these two classes of corrections factorize, and therefore the entire mixed QCD-EW NNLO corrections of $\mathcal{O}(\alpha_s \alpha)$ relative to LO₁ are expected to be well approximated by the difference between eq. (2.21) and eq. (2.20), namely

$$\check{\Sigma}_{\rm NLO_{QCD\times EW}} - \check{\Sigma}_{\rm NLO_{QCD+EW}} = \frac{\Sigma_{\rm NLO_2} \Sigma_{\rm NLO_1}}{\Sigma_{\rm LO_{QCD}}} \,.$$
(2.22)

The resummation procedure allows one to account for soft emission corrections at all orders in α_s . In particular, the NNLL resummation discussed in this work accounts for terms in the partonic cross section in Mellin space that are proportional to $\alpha \alpha_s^{2+n} \ln^k \bar{N}$ with $2n \ge k \ge \max\{0, 2n - 3\}$, where the soft configuration corresponds to the limit $\bar{N} \to \infty$. Consequently, one can generalize the multiplicative approach to approximate not only the mixed QCD-EW NNLO corrections of $\mathcal{O}(\alpha_s \alpha)$ relative to the LO_{QCD} observables, but also the corrections to the Mellin space partonic cross section proportional to $\alpha^2 \alpha_s^{1+n} \ln^k \bar{N}$ with $2n \ge k \ge 2n - 3$, for all orders in α_s . A resummed observable Σ can then be evaluated in the multiplicative approach at NLO × NNLL accuracy as follows:

$$\Sigma_{\rm NLO\times NNLL} = \Sigma_{\rm NLO+NNLL} + \check{\Sigma}_{\rm NLO_2} \left(\frac{\Sigma_{\rm NLO_{QCD}} + {\rm NNLL}}{\Sigma_{\rm LO_{QCD}}} - 1 \right) .$$
(2.23)

Similarly, it is also possible to combine $nNLO_{QCD}$ predictions to the complete-NLO ones in the multiplicative approach by using the matching relation

$$\Sigma_{\rm nNLO_{\rm mult}} = \Sigma_{\rm nNLO} + \check{\Sigma}_{\rm NLO_2} \left(\frac{\Sigma_{\rm nNLO_{\rm QCD}}}{\Sigma_{\rm LO_{\rm QCD}}} - 1 \right) \,. \tag{2.24}$$

In the tail of the differential distributions for $t\bar{t}H$ and $t\bar{t}Z$ productions, where Sudakov logarithms are large and QCD radiation is typically soft, NLO × NNLL predictions can be considered as an improvement w.r.t. those at NLO + NNLL accuracy. In the rest of the phase space this is not necessarily true. Therefore, the difference between the two approximations can be considered as an estimate of the impact of missing higher-order QCD-EW terms. The same argument holds for the comparison between nNLO and nNLO_{mult} predictions.

The situation is completely different in the case of $t\bar{t}W^{\pm}$, where the NLO₁ contribution is dominated by hard radiation, as discussed in section 2.4. In addition, the Sudakov logarithms present in NLO_2 are proportional to the LO_1 contribution, which arises from a $q\bar{q}'$ initial state, while the dominant NLO₁ contributions arise from quark radiation in qq initiated processes. Thus, in the case of $t\bar{t}W^{\pm}$ production, the multiplicative approach cannot be motivated by sound theoretical arguments. This is particularly relevant in the tail of the distributions, where both the NLO_1 and NLO_2 corrections are large, the latter due to the presence of Sudakov logarithms. Therefore the multiplicative approach can lead to uncontrolled NNLO terms. Moreover, since in $t\bar{t}W^{\pm}$ production the NLO₃ correction is numerically much larger than the NLO_2 contribution, even if the multiplicative approach as defined in eqs. (2.23) and (2.24) were justified, it would probably not account for the dominant mixed QCD-EW NNLO contributions, which are expected to be those of $\mathcal{O}(\alpha_s^2 \alpha^3)$ relative to the LO_1 cross section. For consistency, in section 4 results in the additive and multiplicative approaches are shown and compared also for the $t\bar{t}W^{\pm}$ process. However, one should bear in mind that only in the case of $t\bar{t}H$ and $t\bar{t}Z$ production can the multiplicative approach be expected to improve the predictions.

2.4 Structure of the fixed-order corrections

This section describes the structures underlying the complete NLO corrections to $t\bar{t}V$ production. We start by reviewing the most important features of $t\bar{t}W^+$ and $t\bar{t}W^-$ production, which are discussed in detail in [31]. Subsequently, we consider $t\bar{t}H$ and $t\bar{t}Z$ production.

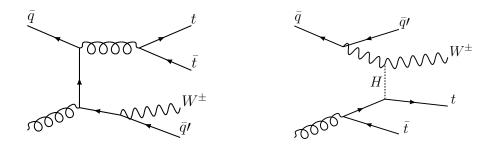


Figure 1. Representative diagrams for the $\bar{q}g \rightarrow t\bar{t}W^{\pm}\bar{q}'$ real-emission amplitudes. The left diagram leads to $\log^2(p_T^2(t\bar{t})/m_W^2)$ terms in the NLO₁ contribution. The right diagram shows an example of $tW \rightarrow tW$ scattering and contributes to the NLO₃.

In $t\bar{t}W^+$ ($t\bar{t}W^-$) production at LO only $u\bar{d}$ ($\bar{u}d$) initial states contribute, where u and d are a generic up- and down-type quarks. The $W^+(W^-)$ boson is radiated from the u(d) quark, while the $t\bar{t}$ pair is produced either via a gluon or a photon/Z boson. The gluon mediated diagrams contribute to the LO₁ cross section, while the diagrams involving a photon/Z boson contribute to the LO₃ cross section. The interference between these two classes of diagrams vanishes after summing over colors, so that the LO₂ cross section also vanishes. On the contrary, all of the NLO_i contributions are non-vanishing.

The NLO₁ contribution to the $t\bar{t}W^{\pm}$ production process is in general large. It was calculated in [54, 78–80] and studied in detail in [19]. Large QCD corrections are mainly induced by the opening of the $gq \rightarrow t\bar{t}W^{\pm}q'$ channel, which depends on the gluon luminosity and therefore is enhanced in high-energy proton-proton collisions. Moreover, the radiation of quarks in $gq \rightarrow t\bar{t}W^{\pm}q'$ is typically hard and in particular very large K-factors are present in the tail of the $p_T(t\bar{t})$ distribution, which receives an additional $\log^2(p_T^2(t\bar{t})/m_W^2)$ enhancement on top of the one due to the gq luminosity (see left diagram in figure 1 and [19] for a detailed discussion). The impact of multiple soft-gluon emissions for this process is scale sensitive and non-negligible [34, 39, 81]; the predictions contained in section 4 account for soft emission up to NNLL accuracy. However, it is important to observe that a large component of NLO₁ corrections, and therefore the associated scale uncertainties, originates from hard radiation in the $gq \rightarrow t\bar{t}W^{\pm}q'$ channel. Therefore, the threshold resummation in the $q\bar{q}' \rightarrow t\bar{t}W^{\pm}$ channels is not expected to drastically reduce the total scale uncertainty. A detailed discussion of the size of the various corrections can be found in section 4.

For what concerns the EW contributions to $t\bar{t}W^{\pm}$ production, the NLO₂ corrections were calculated for the first time in [42] and further phenomenological studies were provided in [82]. In a boosted regime, due to Sudakov logarithms, the NLO₂ corrections can be as large as the NLO QCD scale uncertainty. The NLO₃ contribution is sizable [31] since it contains $gq \rightarrow t\bar{t}W^{\pm}q'$ real-emission channel that involves EW $tW \rightarrow tW$ scattering [83] (see right diagram in figure 1 and [31] for a detailed discussion). Similarly to what happens in the case of the NLO₁ corrections, this channel becomes even more relevant as the LHC center-of-mass energy grows, due to the presence of an initial-state gluon. Although $tW \rightarrow$ tW scattering is present also in the NLO₄ corrections, in that case it is induced by a γq initial state. It is therefore suppressed w.r.t. $tW \rightarrow tW$ scattering contributing to NLO₃ by the smaller luminosity of the photon and also by a factor α/α_s . Similarly, all of the other NLO₄ terms are negligible since they are of $\mathcal{O}(\alpha^4)$.

In contrast to the case of $t\bar{t}W^{\pm}$ production, tree-level Born diagrams for $t\bar{t}H$ and $t\bar{t}Z$ production are induced by both gg and $q\bar{q}$ initial states. In particular, the gluon-fusion channel contributes only to the LO₁ term and, due to the partonic luminosity, yields the largest part of the LO cross section. The $q\bar{q}$ initial states contribute also to LO₃ via squared diagrams featuring $t\bar{t}$ pairs stemming from a photon or Z propagator. Similarly to the $t\bar{t}W^{\pm}$ case, their interference with diagrams contributing to LO₁ vanishes due to color. However, the LO₂ contribution to the cross section is non-vanishing for these two processes. Indeed, some of the $b\bar{b}$ initial-state diagrams feature a *t*-channel *W*-boson that leads to non-vanishing interference contributions. Moreover, the γg initial-state processes contribute to LO₂ via squared diagrams. As shown in [32], the LO₂ and LO₃ contributions to the cross section are numerically negligible.

All of the NLO_i contributions are non-vanishing. The NLO₁ correction is in general large; it was calculated in [84–87] for $t\bar{t}H$ and in [54, 78, 88–90] for $t\bar{t}Z$. In addition, the NLO₁ correction was studied in detail in [19], where, as in the case of $t\bar{t}W^{\pm}$ production, large K-factors for the $p_T(t\bar{t})$ differential distribution were found. On the other hand, in presence of LO contributions involving two gluons in the initial state, the qg luminosity is not providing a significant enhancement of the cross section. Furthermore, in contrast to the case of $t\bar{t}W^{\pm}$ production, the QCD emissions in the NLO₁ corrections are *not* typically hard. Also, the largest contribution from QCD emissions arises from the gg initial state, which is in general the dominant partonic channel both for the LO₁ and the NLO₁. This also applies to the corrections to all the $t\bar{t}H$ and $t\bar{t}Z$ differential distributions considered in this work. For this reason, by resumming soft emission corrections to NNLL accuracy one observes, as expected, a sizable reduction of the residual scale uncertainty affecting the total cross section and differential distributions. Also this feature will be quantified in detail in section 4.

For what concerns the EW corrections to $t\bar{t}H$ and $t\bar{t}Z$ production, the NLO₂ corrections were calculated for the first time in [42] and further phenomenological studies were carried out in [82]. For the total cross section, the relative size of the NLO₂ corrections is smaller than in $t\bar{t}W^{\pm}$ production. However, in the tail of the differential distributions the NLO₂ contribution can be non-negligible in comparison to the NLO QCD scale uncertainty.

For $t\bar{t}H$ and $t\bar{t}Z$ production, the NLO₃ and NLO₄ corrections were calculated in [32]; a phenomenological study involving these contributions to the cross section is presented for the first time in this work. Compared to $t\bar{t}W^{\pm}$ production, not only the NLO₄ but also the NLO₃ correction is small. At this order, $t\bar{t}Z$ ($t\bar{t}H$) production involves $tZ \to tZ$ ($tH \to tH$) scattering in $gq \to t\bar{t}Zq$ ($gq \to t\bar{t}Hq$) real-emission channels. However, as discussed for the case of the $p_T(t\bar{t})$ enhancement, the qg luminosity is not providing a significant enhancement and therefore the relative size of NLO₃ correction in $t\bar{t}Z$ and $t\bar{t}H$ production is smaller than in $t\bar{t}W^{\pm}$ production.

The $t\bar{t}H$ and $t\bar{t}Z$ processes share several features at the diagrammatic level and therefore also at the phenomenological level. This similarity, which is present also at the level of NLO₁ and NLO₂ corrections to these processes, was advocated as a possible proxy to be used to reduce the theoretical uncertainties in the measurements of the top-quark Yukawa coupling [91]. The main kinematic difference between these two processes concerns the rapidity of the V bosons [19], because the Z bosons can be emitted both from initial-state quarks and final-state top-quarks, while the H boson can be emitted only from the latter. This situation is markedly different from the case of $t\bar{t}W^{\pm}$ production, where the W^{\pm} bosons are emitted only from the initial state light quarks. Moreover, as discussed before, NLO₁ and NLO₃ corrections have a very different impact on predictions for $t\bar{t}W^{\pm}$ production compared to $t\bar{t}H$ and $t\bar{t}Z$ production. Similarly, the impact of soft gluon resummation is different for $t\bar{t}W^{\pm}$ production and in $t\bar{t}H$ or $t\bar{t}Z$ production.

3 Input parameters, scales and PDFs

The predictions presented in section 4 depend on the numerical values of physical input parameters, on the PDFs employed in the calculations, and on the choice of the unphysical scales that enter in fixed-order and resummed calculations. The choices made in this work are listed and discussed in this section.

3.1 Masses and couplings

The masses of the heavy SM particles are set equal to

$$m_t = 173.34 \text{ GeV}, \quad m_W = 80.385 \text{ GeV}, \quad m_Z = 91.1876 \text{ GeV}, \quad m_H = 125 \text{ GeV},$$
(3.1)

whereas all the other masses are set equal to zero. The decay widths of all particles are also set to zero. In addition, we use the on-shell renormalization scheme for all masses. The strong coupling α_s is renormalized in the $\overline{\text{MS}}$ -scheme with five active flavors, while the EW input parameters and the renormalization condition for α are in the G_{μ} -scheme, with

$$G_{\mu} = 1.16639 \times 10^{-5} \text{ GeV}^{-2}$$
. (3.2)

The CKM matrix is set equal to the 3×3 unity matrix.

3.2 Scale choices and uncertainties

In the literature, two choices for the (functional form of the) central values for the factorization and renormalization scale entering these processes are commonly adopted. In particular, in [32] it was argued that $H_T/2$, with H_T defined as in eq. (2.15), is a reasonable choice for the factorization and renormalization scale. In [34–36], on the other hand, scales based on the top-antitop-heavy-boson invariant mass, $M \equiv m(t\bar{t}V)$, were used. The former work is based on fixed-order perturbation theory, while the latter also considers the resummation of soft emission corrections. An additional study of the different scale choices was carried out in [19].

Since the factorization/renormalization scale and the hard and soft scales are unphysical, it is acceptable and even recommendable to explore different scale choices. Numerical differences among values of the same observables evaluated for different scale choices can be used as an estimate of the uncertainty associated to the truncation of the perturbative series. In this work, we consider both H_T and $m(t\bar{t}V)$ based scale choices. In particular, when relating the central value of the three scales μ_f, μ_h, μ_s involved in the calculations to the value of $m(t\bar{t}V)$, we choose

$$\mu_f^0 = \frac{m(t\bar{t}V)}{2}, \qquad \mu_h^0 = m(t\bar{t}V), \qquad \mu_s^0 = \frac{m(t\bar{t}V)}{\bar{N}}.$$
(3.3)

When we relate the scales μ_f, μ_h, μ_s to H_T we set instead

$$\mu_f^0 = \frac{H_T}{2}, \qquad \mu_h^0 = \frac{H_T}{2}, \qquad \mu_s^0 = \frac{H_T}{\bar{N}}.$$
(3.4)

The uncertainty associated to missing higher-order corrections can be estimated by considering the dependence of the predictions for a given observable on the non-physical scales that enter the calculation. At fixed order, this is done by varying the renormalization and factorization scales in the range $\mu_i \in {\{\mu_i^0/2, 2\mu_i^0\}}$ (i = r, f). The uncertainty estimate is then given by the bin-by-bin envelope of the 9 predictions obtained in this way. For the resummed results, the hard, soft and factorization scales are varied in the range $\mu_i \in {\{\mu_i^0/2, 2\mu_i^0\}}$ (i = s, h, f). In particular, by introducing the notation $\kappa_i \equiv \mu_i/\mu_i^0$ $(i \in {f, h, s})$, one can rewrite eq. (2.17) by making explicit the dependence of each element on κ_i :

$$\Sigma_{\text{NLO+NNLL}}(\kappa_f, \kappa_h, \kappa_s) = \Sigma_{\text{NLO}}(\kappa_f) + \left[\Sigma_{\text{NNLL}}(\kappa_f, \kappa_h, \kappa_s) - \Sigma_{\text{nLO}_{\text{QCD}}}(\kappa_f)\right].$$
(3.5)

In contrast to the case of NLO calculations, in eq. (3.5) no distinction is made between the renormalization and factorization scales. One can then define an upper and lower scale uncertainty for the variation of each scale in eq. (3.5) as follows

$$\Delta \Sigma_{\text{NLO+NNLL},i}^{+} = \max_{\kappa_i \in \{1/2,1,2\}} \left[\Sigma_{\text{NLO+NNLL}} \left(\kappa_i \right) \right] - \Sigma_{\text{NLO+NNLL}} \left(\kappa_i = 1 \right) ,$$

$$\Delta \Sigma_{\text{NLO+NNLL},i}^{-} = \min_{\kappa_i \in \{1/2,1,2\}} \left[\Sigma_{\text{NLO+NNLL}} \left(\kappa_i \right) \right] - \Sigma_{\text{NLO+NNLL}} \left(\kappa_i = 1 \right) , \qquad (3.6)$$

for $i \in \{f, h, s\}$. In eqs. (3.6) the two scales that are not varied are kept fixed to their central values: $\kappa_j = 1$ if $j \neq i$. The residual theoretical uncertainty affecting a given resummed observable is then obtained by combining in quadrature the uncertainties associated to each of the three scale variations in each of the histogram bins as done in refs. [34–36]. With reference to eq. (3.6) one can then define the upper and lower scale uncertainty as

$$\Delta \Sigma_{\text{NLO+NNLL}}^{\pm} = \pm \sqrt{\left(\Delta \Sigma_{\text{NLO+NNLL},f}^{\pm}\right)^2 + \left(\Delta \Sigma_{\text{NLO+NNLL},h}^{\pm}\right)^2 + \left(\Delta \Sigma_{\text{NLO+NNLL},s}^{\pm}\right)^2}.$$
(3.7)

As discussed in section 4, results with the two scale choices in eqs. (3.3) and (3.4) are compatible with each other at the level of total cross sections, although somewhat less so at the level of differential distributions. Since there is no conclusive argument in favor of either scale choice, we opt for taking the bin-by-bin average of the two results as the best prediction for the central value of each given observable. Moreover, we use the envelope of the uncertainty bands generated with the two scale choices as an estimate of the missing higher-order corrections. This combined-scale method is particularly relevant in the case of $t\bar{t}W^{\pm}$ production, where for the two choices in eqs. (3.3) and (3.4) individually one observes that the NNLL corrections lead to a reduction of scale uncertainty for the total cross section, but the difference between the central values obtained with the two scale choices increases when NNLL corrections are accounted for. Hence, we think that considering only a single central scale choice and its corresponding uncertainty band underestimates the uncertainties due to missing higher orders. On the other hand, we believe that our procedure of taking the envelope of the scale uncertainty bands of the two calculations considered results in a reliable and robust uncertainty estimate.

With the notation introduced above, one can rewrite eq. (2.19) as

$$\Sigma_{\rm nNLO}(\mu_f) = \Sigma_{\rm NLO}(\mu_r = \mu_f) + \left[\Sigma_{\rm nNLO_{QCD}}(\mu_f) - \Sigma_{\rm nLO_{QCD}}(\mu_f)\right] \,. \tag{3.8}$$

The scale uncertainty associated to this quantity is obtained varying μ_f in the range $\{\mu_f^0/2, 2\mu_f^0\}$. Finally, in calculations where the matching between NLO and NNLL corrections is carried out within the multiplicative approach, the scale uncertainty is obtained by applying the method described in eqs. (3.5) and (3.8) to eqs. (2.23) and (2.24).

3.3 PDF uncertainties

Results in section 4 are obtained by using the LUXged17_plus_PDF4LHC15_nnlo_100 PDF set [92, 93], which in turn was obtained starting from the PDF4LHC PDF set [94–97]. The PDFs in refs. [92, 93] include NLO QED effects in the DGLAP evolution [98, 99] and they provide the most precise determination of the photon PDF available to date. In complete-NLO calculations, the PDF uncertainties are evaluated by means of MAD-GRAPH5_AMC@NLO thanks to the procedure introduced in [100]. In this way, one can calculate an observable for each PDF replica in a given PDF set. The PDF uncertainties related to the NNLL resummation corrections, i.e., the terms between square brackets in eq. (2.17), are instead evaluated with an approximation. This is necessary because the evaluation of the NNLL resummation formulas for all of the PDFs in a given set would require an excessive amount of computer time. The approximation relies on the assumption that the relative PDF uncertainty associated to the part of the NLO_1 corrections that does not depend on the qg luminosity, denoted here by NLO_1^{no-qg} , is the same relative PDF uncertainty affecting $\Sigma_{\text{NLO+NNLL}} - \Sigma_{\text{NLO}}$. In this approximation, NLO₁ corrections arising from quark-gluon channel diagrams are excluded from the calculation of the relative error induced by PDFs in resummed calculations because this channel is subleading in the threshold limit. Therefore, for each replica i in the PDF set we assume that

$$(\Sigma_{\rm NLO+NNLL})_i = (\Sigma_{\rm NLO})_i + (\Sigma_{\rm NLO+NNLL} - \Sigma_{\rm NLO})|_{\rm central} \times \frac{\Sigma_{\rm NLO_1^{\rm no}-qg}|_i}{\check{\Sigma}_{\rm NLO_1^{\rm no}-qg}|_{\rm central}}, \qquad (3.9)$$

where the subscript "central" refers to the central PDF prediction. In conclusion, for each replica *i* the value of $(\check{\Sigma}_{\text{NLO}_1^{\text{no}-qg}})|_i$ is evaluated via MADGRAPH5_AMC@NLO, rescaled as prescribed by eq. (3.9) and added back to $\Sigma_{\text{NLO}}|_i$, to provide an estimate of the NLO+NNLL calculation carried out with the replica *i* in the PDF set. Once an NLO+NNLL prediction is available for each replica i, PDF uncertainties are evaluated following the standard procedure for the PDF set considered.

The same procedure can be employed for the nNLO predictions via the substitution $NLO + NNLL \rightarrow nNLO$ in eq. (3.9). In the case of the combination of NLO predictions and NNLL corrections in the multiplicative approach we do not evaluate PDF uncertainties, but it is reasonable to think that they would be similar in size to those calculated in the additive approach.

4 Results

In this section we present predictions for each of the four processes considered in this work, namely $t\bar{t}W^+$, $t\bar{t}W^-$, $t\bar{t}H$, and $t\bar{t}Z$ production. We start by considering total cross sections and charge asymmetries, and then give results for differential distributions in section 4.2.

4.1 Total cross sections and asymmetries

The total cross sections for the four processes, calculated within different perturbative approximations, can be found in the middle columns of tables 1–4. Each table is subdivided in three sections:

- In the top section of each table the cross sections are evaluated with the $m(t\bar{t}V)$ -based scale choices listed in eq. (3.3).
- In the middle section of the tables the cross sections are evaluated with the H_T -based scale choices listed in eq. (3.4).
- Finally, the lower section of each table shows the combination of the results for the two aforementioned scale choices. The results for the scale choices in eqs. (3.3) and (3.4) are combined as explained in section 3.2; the results for the total cross section listed in the lower portion of the tables represent one of the main results of this paper.

In each of the three parts of the tables, the predictions become more accurate as one moves from the highest line to the lowest line. Each line starts with a label that indicates the accuracy of the calculations found on that line. For convenience, we summarize the notation introduced in section 2 and used to label the various rows:

- LO_{QCD}: rows labeled in this way are based on tree-level QCD calculations, i.e., they include only the LO₁ contribution to the cross section.
- NLO_{QCD}: lines labeled in this way include the LO_{QCD} calculation added to the NLO QCD corrections. For example, for the total cross section

$$\sigma_{\rm NLO_{QCD}} \equiv \sigma_{\rm LO_1} + \check{\sigma}_{\rm NLO_1} \,, \tag{4.1}$$

where, consistent with the notation introduced in section 2, $\check{\sigma}_{\text{NLO}_1}$ includes only terms of $\mathcal{O}(\alpha_s^3 \alpha)$.

• NLO: rows labeled in this way correspond to complete-NLO results, which include NLO QCD corrections ($\mathcal{O}(\alpha_s^3 \alpha)$), NLO EW corrections ($\mathcal{O}(\alpha_s^2 \alpha^2)$), and further sub-leading contributions. For example, for the case of the total cross section, one has

$$\sigma_{\rm NLO} \equiv \sum_{i=1}^{3} \sigma_{\rm LO_i} + \sum_{i=1}^{4} \check{\sigma}_{\rm NLO_i} \,. \tag{4.2}$$

- nNLO_{QCD}: indicates the approximate-NNLO predictions evaluated by adding to the NLO_{QCD} results the contribution of the corrections of $\mathcal{O}(\alpha_s^2)$ relative to the LO QCD cross section that are obtained from the NNLL resummation formula for the QCD process.
- nNLO: same as nNLO_{QCD}, but including in addition the NLO EW corrections and further subleading contributions from the complete-NLO calculation.
- NLO_{QCD}+NNLL: this label indicates the NLO_{QCD} predictions improved by NNLL resummation.
- NLO+NNLL: lines labeled this way include the complete-NLO predictions improved by NNLL resummation. These must be considered our most accurate predictions.

In the cases where beyond-NLO predictions are combined with NLO results, i.e., nNLO and NLO+NNLL calculations, the matching is carried out with the additive approach discussed in section 2.3. For total cross sections and charge asymmetries, which are the quantities considered in the tables 1–4, results based on the multiplicative approach differ from the additive combination by less than 1%. For this reason, results obtained with the multiplicative approach are not shown in the tables. However, in the case of differential distributions discussed in section 4.2, the differences between additive approach and multiplicative approach are presented in a separate ratio inset in the figures. The labels employed to identify calculations in the multiplicative approach are the following:

- NLO × NNLL: this label indicates a calculations that includes the same corrections found in NLO+NNLL calculations, but with NLO_{EW} and purely QCD corrections combined in the multiplicative approach, according to eq. (2.23).
- nNLO_{mult}: this label indicates calculations analogous to nNLO but with NLO_{EW} and QCD corrections combined with the multiplicative approach, according to eq. (2.24).

4.1.1 $t\bar{t}W^+$ and $t\bar{t}W^-$

Values for the total cross sections for the $t\bar{t}W^+$ and $t\bar{t}W^-$ processes are shown in tables 1 and 2, respectively. The results for $t\bar{t}W^-$ are quantitatively rather similar to the results for $t\bar{t}W^+$; consequently, we comment almost exclusively on the latter.

The central value of the LO_{QCD} cross section for $t\bar{t}W^+$ production is about 225 fb or 241 fb for the $m(t\bar{t}W^+)$ -based or H_T -based scale choices, respectively. This difference is

$m(t\bar{t}W^+)$ -based scales		
Order	σ [fb]	$A_C[\%]$
$\rm LO_{QCD}$	$225.45(1)$ $^{+51.61(+22.9\%)}_{-39.41(-17.5\%)}$ $^{+5.85(+2.6\%)}_{-5.85(-2.6\%)}$	0
$\rm NLO_{QCD}$	$355.69(4) \stackrel{+43.50(+12.2\%)}{_{-39.29(-11.0\%)}} \stackrel{+8.12(+2.3\%)}{_{-8.12(-2.3\%)}}$	$2.58(1) \begin{array}{c} +0.50(+19.4\%) + 0.08(+2.9\%) \\ -0.37(-14.3\%) - 0.08(-2.9\%) \end{array}$
NLO	$376.58(5) \begin{array}{c} +46.52(+12.4\%) \\ -41.73(-11.1\%) \\ -8.02(-2.1\%) \end{array}$	$2.76(2) \begin{array}{c} +0.45(+16.1\%) + 0.09(+3.2\%) \\ -0.33(-12.0\%) - 0.09(-3.2\%) \end{array}$
$\mathrm{nNLO}_{\mathrm{QCD}}$	$363.13(4) \begin{array}{c} +37.14(+10.2\%) \\ -27.29(-7.5\%) \end{array} \begin{array}{c} +8.3(+2.3\%) \\ -8.3(-2.3\%) \end{array}$	$3.33(2) \begin{array}{c} +0.16(+4.7\%) & +0.08(+2.4\%) \\ -0.12(-3.6\%) & -0.08(-2.4\%) \end{array}$
nNLO	$384.02(5) \begin{array}{c} +40.16(+10.5\%) \\ -29.73(-7.7\%) \end{array} \begin{array}{c} +8.20(+2.1\%) \\ -8.20(-2.1\%) \end{array}$	$3.47(2) \stackrel{+0.18(+5.1\%)}{_{-0.15(-4.3\%)}} \stackrel{+0.09(+2.7\%)}{_{-0.09(-2.7\%)}}$
$\rm NLO_{QCD} + \rm NNLL$	$347.1(1) \begin{array}{c} +23.9(+6.9\%) & +7.9(+2.3\%) \\ -14.4(-4.2\%) & -7.9(-2.3\%) \end{array}$	
NLO+NNLL	$368.0(1) \begin{array}{c} +26.5(+7.2\%) & +7.8(+2.1\%) \\ -16.2(-4.4\%) & -7.8(-2.1\%) \end{array}$	_
H_T -based scales		
Order	σ [fb]	$A_C[\%]$
$\mathrm{LO}_{\mathrm{QCD}}$	$241.146(9) \begin{array}{c} +57.030(+23.6\%) + 6.367(+2.6\%) \\ -43.182(-17.9\%) - 6.367(-2.6\%) \end{array}$	0
$\rm NLO_{QCD}$	$375.64(4) \stackrel{+47.98(+12.8\%)}{-42.76(-11.4\%)} \stackrel{+8.4(+2.2\%)}{-8.43(-2.2\%)}$	$2.78(1) \begin{array}{c} +0.56(+20.3\%) + 0.08(+2.9\%) \\ -0.41(-14.9\%) - 0.08(-2.9\%) \end{array}$
NLO	$397.90(6) \begin{array}{c} +51.39(+12.9\%) \\ -45.48(-11.4\%) \end{array} \\ +8.3(+2.1\%) \\ -8.32(-2.1\%) \end{array}$	$2.94(2) \begin{array}{c} +0.51(+17.7\%) + 0.10(+3.2\%) \\ -0.38(-13.0\%) - 0.10(-3.2\%) \end{array}$
$\mathrm{nNLO}_{\mathrm{QCD}}$	$380.31(4) \begin{array}{c} +42.52(+11.2\%) & +8.55(+2.2\%) \\ -32.34(-8.5\%) & -8.55(-2.2\%) \end{array}$	$3.26(3) \begin{array}{c} +0.17(+5.3\%) & +0.09(+2.6\%) \\ -0.02(-0.7\%) & -0.09(-2.6\%) \end{array}$
nNLO	$402.57(6) \begin{array}{c} +45.94(+11.4\%) & +8.44(+2.1\%) \\ -35.06(-8.7\%) & -8.44(-2.1\%) \end{array}$	$3.39(3) \begin{array}{c} +0.19(+5.7\%) & +0.10(+2.9\%) \\ -0.06(-1.8\%) & -0.10(-2.9\%) \end{array}$
$\rm NLO_{QCD} + \rm NNLL$	$378.1(1) \begin{array}{c} +32.4(+8.6\%) & +8.5(+2.2\%) \\ -21.7(-5.7\%) & -8.5(-2.2\%) \end{array}$	—
NLO+NNLL	$400.4(1) \begin{array}{c} +35.3(+8.8\%) & +8.4(+2.1\%) \\ -23.4(-5.9\%) & -8.4(-2.1\%) \end{array}$	—
Combined scales		
Order	σ [fb]	$A_C[\%]$
$\mathrm{LO}_{\mathrm{QCD}}$	$233.297(8) \begin{array}{c} +64.88(+27.8\%) \\ -47.26(-20.3\%) \\ -6.16(-2.6\%) \end{array}$	0
$\rm NLO_{QCD}$	$365.66(3) \stackrel{+57.95(+15.85\%)}{_{-49.27(-13.5\%)}} \stackrel{+8.35(+2.3\%)}{_{-8.35(-2.3\%)}}$	$2.68(1) \begin{array}{c} +0.66(+24.6\%) + 0.08(+2.9\%) \\ -0.47(-17.4\%) - 0.08(-2.9\%) \end{array}$
NLO	$387.24(4) \begin{array}{c} +62.05(+16.0\%) \\ -52.39(-13.5\%) \end{array} \\ +8.25(+2.1\%) \\ -8.25(-2.1\%) \end{array}$	$2.85(1) \begin{array}{c} +0.60(+21.1\%) + 0.09(+3.2\%) \\ -0.42(-14.7\%) - 0.09(-3.2\%) \end{array}$
$\mathrm{nNLO}_{\mathrm{QCD}}$	$371.72(3) \begin{array}{c} +51.11(+13.8\%) & +8.50(+2.3\%) \\ -35.88(-9.7\%) & -8.50(-2.3\%) \end{array}$	$3.30(2) \begin{array}{c} +0.19(+5.8\%) & +0.09(+2.6\%) \\ -0.08(-2.5\%) & -0.09(-2.6\%) \end{array}$
nNLO	$393.29(4) \begin{array}{c} +55.21(+14.0\%) \\ -39.00(-9.9\%) \end{array} \begin{array}{c} +8.40(+2.1\%) \\ -8.40(-2.1\%) \end{array}$	$3.43(2) \begin{array}{c} +0.21(+6.2\%) & +0.10(+2.9\%) \\ -0.11(-3.3\%) & -0.10(-2.9\%) \end{array}$
$\rm NLO_{QCD} + \rm NNLL$	$362.59(8) \begin{array}{c} +47.94(+13.2\%) & +8.26(+2.3\%) \\ -29.95(-8.3\%) & -8.26(-2.3\%) \end{array}$	—
NLO+NNLL	$384.17(9) \begin{array}{c} +51.52(+13.4\%) & +8.16(+2.1\%) \\ -32.36(-8.4\%) & -8.16(-2.1\%) \end{array}$	—

Table 1. Cross section and charge asymmetry for $t\bar{t}W^+$ production for the 13 TeV LHC at various accuracies. The top portion of the table corresponds to scales based on $m(t\bar{t}W^+)$, the middle portion on H_T . The lower part contains predictions based on the combination of the results for the two scale choices. The first number in brackets corresponds to the statistical uncertainty in the Monte Carlo integration. The first number in the subscript/superscript is the uncertainty due to scale variations (the number in the bracket is the uncertainty expressed as a percentage of the central value). The last number in the subscript/superscript is the PDF uncertainty.

$m(t\bar{t}W^{-})$ -based scales		
Order	σ [fb]	$A_C[\%]$
LO _{QCD}	$114.305(6) \begin{array}{c} +26.261(+23.0\%) + 3.563(+3.1\%) \\ -20.056(-17.5\%) - 3.563(-3.1\%) \end{array}$	0
$\rm NLO_{QCD}$	$181.65(2) \begin{array}{c} +22.74(+12.5\%) & +5.20(+2.9\%) \\ -20.36(-11.2\%) & -5.20(-2.9\%) \end{array}$	$2.04(1) \begin{array}{c} +0.41(+19.9\%) & +0.05(+2.5\%) \\ -0.30(-14.7\%) & -0.05(-2.5\%) \end{array}$
NLO	$193.26(2) \begin{array}{c} +24.55(+12.7\%) & +5.29(+2.7\%) \\ -21.81(-11.3\%) & -5.29(-2.7\%) \end{array}$	$2.04(2) \begin{array}{c} +0.37(+18.1\%) & +0.05(+2.3\%) \\ -0.27(-13.2\%) & -0.05(-2.3\%) \end{array}$
$\mathrm{nNLO}_{\mathrm{QCD}}$	$186.20(2) \begin{array}{c} +18.89(+10.14\%) + 5.33(+2.9\%) \\ -13.67(-7.34\%) & -5.33(-2.9\%) \end{array}$	$2.69(2) \begin{array}{c} +0.09(+3.5\%) & +0.06(+2.0\%) \\ -0.11(-4.0\%) & -0.06(-2.0\%) \end{array}$
nNLO	$197.80(3) \begin{array}{c} +20.68(+10.5\%) & +5.42(+2.7\%) \\ -15.11(-7.6\%) & -5.42(-2.7\%) \end{array}$	$2.64(2) \begin{array}{c} +0.10(+4.0\%) & +0.05(+1.8\%) \\ -0.12(-4.4\%) & -0.05(-1.8\%) \end{array}$
$\rm NLO_{QCD} + NNLL$	$178.16(4) \begin{array}{c} +12.29(+6.9\%) & +5.09(+2.9\%) \\ -7.13(-4.0\%) & -5.09(-2.9\%) \end{array}$	—
NLO+NNLL	$189.77(5) \begin{array}{c} +13.82(+7.3\%) & +5.19(+2.7\%) \\ -8.09(-4.3\%) & -5.19(-2.7\%) \end{array}$	—
H_T -based scales		
Order	$\sigma~[{ m fb}]$	$A_C[\%]$
$\mathrm{LO}_{\mathrm{QCD}}$	$121.754(5) \begin{array}{c} +28.824(+23.7\%) + 3.854(+3.2\%) \\ -21.843(-17.9\%) - 3.853(-3.2\%) \end{array}$	0
$\rm NLO_{QCD}$	$191.40(2) \begin{array}{c} +25.09(+13.1\%) & +5.44(+2.8\%) \\ -22.13(-11.6\%) & -5.44(-2.8\%) \end{array}$	$2.19(1) \begin{array}{c} +0.45(+20.5\%) & +0.06(+2.5\%) \\ -0.33(-15.1\%) & -0.06(-2.5\%) \end{array}$
NLO	$203.81(3) \begin{array}{c} +27.13(+13.3\%) & +5.53(+2.7\%) \\ -23.74(-11.6\%) & -5.53(-2.7\%) \end{array}$	$2.16(2) \begin{array}{c} +0.41(+18.9\%) & +0.05(+2.4\%) \\ -0.30(-13.7\%) & -0.05(-2.4\%) \end{array}$
$\mathrm{nNLO}_{\mathrm{QCD}}$	$194.43(2) \begin{array}{c} +21.73(+11.2\%) & +5.52(+2.8\%) \\ -16.14(-8.3\%) & -5.52(-2.8\%) \end{array}$	$2.60(2) \begin{array}{c} +0.14(+5.5\%) & +0.06(+2.3\%) \\ -0.01(-0.4\%) & -0.06(-2.3\%) \end{array}$
nNLO	$206.83(3) \begin{array}{c} +23.78(+11.5\%) & +5.62(+2.7\%) \\ -17.76(-8.6\%) & -5.62(-2.7\%) \end{array}$	$2.54(2) \begin{array}{c} +0.15(+6.0\%) & +0.05(+2.2\%) \\ -0.03(-1.0\%) & -0.05(-2.2\%) \end{array}$
$\rm NLO_{QCD} + NNLL$	$193.33(5) \begin{array}{c} +16.66(+8.6\%) & +5.49(+2.8\%) \\ -10.65(-5.5\%) & -5.49(-2.8\%) \end{array}$	—
NLO+NNLL	$205.73(5) \begin{array}{c} +18.43(+9.0\%) & +5.59(+2.7\%) \\ -11.68(-5.7\%) & -5.59(-2.7\%) \end{array}$	—
Combined scales		
Order	σ [fb]	$A_C[\%]$
LO _{QCD}	$118.030(4) \begin{array}{c} +32.548(+27.6\%) + 3.736(+3.2\%) \\ -23.781(-20.1\%) - 3.735(-3.2\%) \end{array}$	0
$\rm NLO_{QCD}$	$186.53(1) \begin{array}{c} +29.96(+16.1\%) & +5.34(+2.9\%) \\ -25.24(-13.5\%) & -5.34(-2.9\%) \end{array}$	$2.12(1) \begin{array}{c} +0.52(+24.8\%) & +0.05(+2.5\%) \\ -0.38(-17.7\%) & -0.05(-2.5\%) \end{array}$
NLO	$198.53(2) \begin{array}{c} +32.41(+16.3\%) \\ -27.08(-13.6\%) \end{array} + 5.43(+2.7\%) \\ -5.43(-2.7\%) \end{array}$	$2.10(1) \begin{array}{c} +0.47(+22.3\%) & +0.05(+2.4\%) \\ -0.33(-15.63\%) & -0.05(-2.4\%) \end{array}$
$\mathrm{nNLO}_{\mathrm{QCD}}$	$190.31(1) \begin{array}{c} +25.85(+13.6\%) & +5.45(+2.9\%) \\ -17.78(-9.3\%) & -5.45(-2.9\%) \end{array}$	$2.64(1) \begin{array}{c} +0.14(+5.2\%) & +0.06+2.3\%) \\ -0.06(-2.4\%) & -0.06(-2.3\%) \end{array}$
nNLO	$202.32(2) \begin{array}{c} +28.29(+14.0\%) & +5.54(+2.7\%) \\ -19.63(-9.7\%) & -5.54(-2.7\%) \end{array}$	$2.59(1) \begin{array}{c} +0.16(+6.0\%) & +0.06(+2.2\%) \\ -0.08(-3.0\%) & -0.06(-2.2\%) \end{array}$
$\rm NLO_{QCD} + NNLL$	$185.75(3) \begin{array}{c} +24.25(+13.1\%) & +5.31(+2.9\%) \\ -14.71(-7.9\%) & -5.31(-2.9\%) \end{array}$	_
NLO+NNLL	$197.75(4) \begin{array}{c} +26.41(+13.4\%) & +5.41(+2.7\%) \\ -16.07(-8.1\%) & -5.41(-2.7\%) \end{array}$	—

Table 2. Total cross section and charge asymmetry for $t\bar{t}W^-$ production. Same structure as in table 1.

well captured by the uncertainty due to scale variation, which is roughly $\frac{+23\%}{-18\%}$ in both cases. Since the central values for the two scale choices differ by about 7%, when combining the two scale choices the cross section gets a value of 233 fb, with a slightly increased scale dependence of $^{+27\%}_{-20\%}$. As discussed in section 2.4, the large NLO QCD corrections to this process are due to the opening of the qg-induced real-emission channel. This contribution is particularly sizable since the gluon luminosity is rather large at the LHC. Indeed, the NLO_{QCD} predictions are more than 50% larger than the LO_{QCD} cross section. The corrections are only slightly larger for the H_T -based scale choice than for the $m(t\bar{t}W^+)$ -based choice. This fact brings the two NLO_{QCD} cross section results closer to each other (in relative terms) as compared to the LO_{QCD} cross sections, as expected from perturbation theory. At NLO_{QCD} the relative uncertainty from scale variation is $^{+15.9\%}_{-13.5\%}$ for the combined-scales result, which is significantly smaller than the corresponding LO_{QCD} uncertainty. The inclusion of the EW corrections further increases the cross section by about 6%, mainly due to NLO₃ corrections. Even though this contribution is suppressed by a factor $(\alpha/\alpha_s)^2$ w.r.t. the NLO₁ corrections, there is a large enhancement due to the opening of the t-channel-enhanced $tW \rightarrow tW$ scattering contribution [31, 83].

For both the $m(t\bar{t}W^+)$ and H_T -based scale choices, approximate NNLO corrections increase the cross section. These corrections for the $m(t\bar{t}W^+)$ -based scale choice are slightly larger than for the H_T -based scale choice. Therefore, the central values of the nNLO_{OCD} cross sections for the two scale choices are closer to each other than the values of the NLO_{QCD} cross sections. By including the approximate NNLO QCD corrections the crosssection scale dependence is reduced to $\sim +14\% -10\%$ for the combined-scale calculation. Hence, perturbation theory seems to converge well. On the other hand, if one considers NNLL resummed results, either matched to NLO_{QCD} or to complete-NLO predictions, a slightly different picture emerges. For both scale choices, the corrections due to resummation are small and well-behaved. Moreover, they reduce significantly the scale dependence, to about $^{+7\%}_{-4\%}$ and $^{+8\%}_{-6\%}$ for the total cross section obtained with the $m(t\bar{t}W^+)$ and H_T based scales, respectively. However, the corrections move the cross-section central values further apart from each other than in the case of NLO_{QCD} calculations. The corrections for the $m(t\bar{t}W^+)$ -based scales are negative, while for the H_T -based scales the corrections are positive. The net effect is that the central value for the combined-scale result is very much compatible with the corresponding NLO_{QCD} predictions, with a scale uncertainty equal to $^{+13\%}_{-8\%}$, which is larger than the NLO_{QCD}+NNLL scale uncertainties for the two separate scale choices. The reason behind this feature resides in the origin of the NLO QCD corrections. The NLO₁ term is dominated by hard radiation and especially by the qq initialstate contribution. Therefore, in this case, the reduction of the scale dependence due to the resummation of soft emission does not reflect the theoretical uncertainty associated to missing higher-order corrections. However, by combining the results obtained with the two different scale choices, one obtains a more reliable estimate of the uncertainty due to missing higher order corrections. Nevertheless, by following this approach an improvement in the scale uncertainty in the combined-scales results is observed; the scale uncertainty affecting the combined-scales NLO_{QCD} cross section is larger than the scale uncertainty for the NLO_{QCD}+NNLL cross section. Since scale uncertainties primarily affect QCD corrections,

this argument still holds when EW effects are included, as can be seen by comparing the scale uncertainties of NLO, nNLO, and NLO + NNLL calculations of the cross section.

The PDF uncertainties on the total $t\bar{t}W^{\pm}$ cross section are significantly smaller than the corresponding scale uncertainties, and are at the level of $\pm 2\%$ for $t\bar{t}W^+$ production and $\pm 3\%$ for $t\bar{t}W^-$ production.

The third column in tables. 1 and 2 shows predictions for the charge asymmetry A_C . At the LHC, the charge asymmetry is defined as

$$A_C = \frac{\sigma(\Delta > 0) - \sigma(\Delta < 0)}{\sigma(\Delta > 0) + \sigma(\Delta < 0)}, \qquad (4.3)$$

where $\Delta \equiv |y(t)| - |y(t)|$, and y(t) (y(t)) indicates the top-quark (antiquark) rapidity in the laboratory frame. Consequently, Δ is positive when the top is emitted less centrally than the antitop. An analogous asymmetry was measured at the Tevatron for top-pair production.⁵ The Tevatron asymmetry received considerable attention due to a tension between the measured asymmetry and the SM predictions [101], which were initially known only at the lowest non-vanishing order (NLO QCD) [102]. The tension could be interpreted as a BSM effect. With improved measurements and especially with the calculation of NLO EW [103] and then NNLO QCD corrections [28, 104], the tension between theory predictions and experimental data decreased considerably. It is therefore essential to have precise predictions for such observables.

At the LHC, the A_C asymmetry for top-pair production is rather small (see e.g. [28]) due to the fact that the cross section is dominated by the gluon-fusion channel, which is charge symmetric. It is therefore interesting to consider top-pair production in association with a W boson [19, 80]. Since at lowest order the W boson only couples to initial state quarks, the contribution of the gg channel to the asymmetry is suppressed and only enters at NNLO and beyond. As a result of this situation, the asymmetry in $t\bar{t}W^{\pm}$ production is significantly larger than in the case of top-pair production. For $t\bar{t}W^+$ production at NLO_{QCD}, which is the lowest perturbative order for which the asymmetry is non-zero, one finds that A_C is equal to about 2.6% and 2.8% for the $m(t\bar{t}W^+)$ and H_T -based scale choices, respectively, with scale uncertainties of $^{+20\%}_{-15\%}$.⁶ The inclusion of the EW corrections increases the asymmetry by a small amount, about 0.16 percent.

In our framework, it is not possible to evaluate the charge asymmetry to NLO + NNLL or NLO_{QCD} + NNLL accuracy, since the resummation is carried out inclusively w.r.t. the rapidities. Hence, the nNLO calculations are the most accurate predictions for the charge asymmetry that we present in this paper. On the other hand, the NNLO QCD corrections to $t\bar{t}W^+$ (and $t\bar{t}W^-$) production involve $gg \rightarrow t\bar{t}Wq\bar{q}'$ processes, which are expected to be large due to the gg luminosity and are completely symmetric, so that they contribute only to the denominator of eq. (4.3). These effects cannot be estimated via scale variations

⁵At $p\bar{p}$ colliders such as the Tevatron the relevant observable was the forward-backward asymmetry, defined as in eq. (4.3) but with $\Delta \equiv y(t) - y(\bar{t})$.

⁶Both for scale and PDF uncertainties a full correlation is assumed for the numerator and the denominator of eq. (4.3). In the case of combined-scale predictions we proceed similarly to the case of total cross sections, by looking at the envelope of the $m(t\bar{t}W^+)$ and H_T -based scale choices directly for A_C .

and may substantially alter the A_C prediction for $t\bar{t}W^+$ (and $t\bar{t}W^-$). However, when the approximate NNLO corrections are included, the $t\bar{t}W^+$ charge asymmetry increases by 0.6 and 0.8 percent for the $m(t\bar{t}W^+)$ and H_T -based scale choices, bringing the central values for the two scale choices rather close to each other. More significantly, by including these terms, which constitute the first order correction to the asymmetry, the scale dependence is reduced to $^{+6\%}_{-3\%}$ for the combined-scales prediction. In this case, the uncertainties coming from the PDFs can no longer be neglected, since they are similar in size the scale uncertainties ($\pm 2.9\%$ for $t\bar{t}W^+$ production). Similar remarks apply to the charge asymmetry calculation in $t\bar{t}W^-$ production.

4.1.2 $t\bar{t}H$

The total cross section for $t\bar{t}H$ production is shown in the second column of table 3. When NLO QCD corrections are included, the cross-section central values obtained with the two scale choices differ by 8.5 fb, roughly half of the difference between the central values of the cross section calculated with the two scale choices at LO_{QCD}. For both scale choices, EW corrections increase the cross section by 2.5% w.r.t. the NLO_{QCD} result; this is a small correction when compared to the scale uncertainty. Indeed, although the scale uncertainty at NLO_{QCD} is more than a factor two smaller than at LO_{QCD}, it remains of the order of ±10%.

When QCD corrections beyond NLO are included, the agreement between the predictions obtained with the two scale choices is very good: for nNLO_{QCD} and nNLO calculations the difference between the two values of the cross section is below the permille. The scale uncertainties, which are of the order of $^{+4\%}_{-2\%}$ for nNLO calculations, are significantly reduced w.r.t. NLO calculations. Compared to these small uncertainties, EW corrections can no longer be neglected.

In contrast to the $t\bar{t}W^{\pm}$ processes, the NLO+NNLL cross sections come with a larger scale uncertainty than the nNLO ones and the central values with $m(t\bar{t}H)$ and H_T -based scale choices are further apart than at nNLO. By combining results for the two scale choices one obtains a total cross section of approximately 500 fb with a scale uncertainty just below the $^{+8\%}_{-6\%}$ level. The scale uncertainty in the resummed calculations is obtained by separately varying three different non-physical scales, while the scale uncertainty associated to approximate NNLO results is obtained by varying only one scale. For this and other reasons, as discussed in refs. [34–36], we consider NLO+NNLL predictions to be more complete and reliable than the approximate NNLO predictions. Hence, the cross section in the last line of table 3 should be considered the most accurate prediction for the $t\bar{t}H$ total cross section presented in this paper.

The charge asymmetry for the top and the antitop quarks in $t\bar{t}H$ production is given in the third column of table 3. As expected, the asymmetry for $t\bar{t}H$ production is smaller than for $t\bar{t}W^{\pm}$ production, since the latter does not contain (up to NLO) the large and symmetric gg-induced contributions, which enter only in the denominator of eq. (4.3). The difference between the central values of the asymmetry calculated with the $m(t\bar{t}H)$ and H_T based scale choices is small. By comparing NLO and NLO_{QCD} predictions it is possible to see that the contribution of the EW corrections to the asymmetry is sizable. Going beyond NLO, the nNLO_{QCD} and nNLO predictions show very asymmetric uncertainty bands. For

$m(t\bar{t}H)$ -based scales		
Order	σ [fb]	$A_C[\%]$
LO _{QCD}	$327.65(4) \begin{array}{c} +94.18(+28.7\%) & +7.11(+2.2\%) \\ -68.46(-20.9\%) & -7.11(-2.2\%) \end{array}$	0
$\rm NLO_{QCD}$	$463.70(8) \begin{array}{c} +45.1(+9.7\%) & +11.08(+2.4\%) \\ -49.72(-10.7\%) & -11.08(-2.4\%) \end{array}$	
NLO	475.68(8) + 46.94(+9.9%) + 11.21(+2.4%) - 51.11(-10.7%) - 11.21(-2.4%)	1.01(2) $+0.19(+19.0%)+0.04(+4.0%)$
$\mathrm{nNLO}_{\mathrm{QCD}}$	$490.38(8) \begin{array}{c} +18.46(+3.8\%) \\ -9.61(-2.0\%) \end{array} \begin{array}{c} +11.82(+2.4\%) \\ -11.82(-2.4\%) \end{array}$	0.79(5) + 0.30(+38.5%) + 0.04(+5.1%)
nNLO	$502.36(8) \begin{array}{c} +20.27(+4.0\%) & +11.95(+2.4\%) \\ -10.99(-2.2\%) & -11.95(-2.4\%) \end{array}$	0.95(5) + 0.28(+29.5%) + 0.05(+4.7%)
$\rm NLO_{QCD} + NNLL$	$479.1(1) \begin{array}{c} +29.0(+6.1\%) \\ -24.2(-5.0\%) \end{array} \begin{array}{c} +11.5(+2.4\%) \\ -11.5(-2.4\%) \end{array}$	_
NLO+NNLL	$491.1(1) \begin{array}{c} +27.8(+5.7\%) \\ -24.0(-4.9\%) \end{array} \begin{array}{c} +11.6(+2.4\%) \\ -11.6(-2.4\%) \end{array}$	_
H_T -based scales		
Order	$\sigma \; [{ m fb}]$	$A_C[\%]$
LO _{QCD}	$344.86(4) \begin{array}{c} +101.38(+29.4\%) + 7.61(+2.2\%) \\ -73.22(-21.2\%) & -7.61(-2.2\%) \end{array}$	0
$\rm NLO_{QCD}$	$472.22(7) \begin{array}{c} +41.31(+8.7\%) & +11.41(+2.4\%) \\ -48.83(-10.3\%) & -11.41(-2.4\%) \end{array}$	
NLO	$484.31(7) \begin{array}{c} +43.15(+8.9\%) & +11.55(+2.4\%) \\ -50.24(-10.4\%) & -11.55(-2.4\%) \end{array}$	1.00(2) + 0.23(+20.9%) + 0.04(+4.0%)
$\mathrm{nNLO}_{\mathrm{QCD}}$	$490.17(8) \begin{array}{c} +15.35(+3.1\%) & +11.92(+2.4\%) \\ -8.95(-1.8\%) & -11.92(-2.4\%) \end{array}$	0.94(5) + 0.003(+0.3%) + 0.04(+4.6%)
nNLO	$502.26(7) \begin{array}{c} +17.19(+3.4\%) & +12.06(+2.4\%) \\ -10.37(-2.1\%) & -12.06(-2.4\%) \end{array}$	1 11(5) +0.03(+2.5%) +0.05(+4.3%)
$\rm NLO_{QCD} + NNLL$	$489.58(9) \begin{array}{c} +34.35(+7.0\%) & +11.91(+2.4\%) \\ -22.54(-4.6\%) & -11.91(-2.4\%) \end{array}$	
NLO+NNLL	$501.67(9) \begin{array}{c} +33.34(+6.6\%) & +12.05(+2.4\%) \\ -22.54(-4.5\%) & -12.05(-2.4\%) \end{array}$	—
Combined scales		
Order	σ [fb]	$A_C[\%]$
LO _{QCD}	$336.25(3) \begin{array}{c} +109.98(+32.7\%)+7.42(+2.2\%) \\ -77.07(-22.9\%) \end{array}$	0
$\rm NLO_{QCD}$	$467.96(5) \begin{array}{c} +45.57(+9.7\%) \\ -53.98(-11.5\%) \end{array} \\ \begin{array}{c} +11.31(+2.4\%) \\ -11.31(-2.4\%) \end{array}$	
NLO	$479.99(5) \begin{array}{c} +47.46(+9.9\%) & +11.45(+2.4\%) \\ -55.42(-11.5\%) & -11.45(-2.4\%) \end{array}$	
$\mathrm{nNLO}_{\mathrm{QCD}}$	$490.27(6) \begin{array}{c} +18.56(+3.8\%) \\ -9.50(-1.9\%) \end{array} \begin{array}{c} +11.93(+2.4\%) \\ -11.93(-2.4\%) \end{array}$	$0.87(4)$ $^{+0.23(+26.4\%)+0.04(+5.1\%)}$
nNLO	$502.31(6) \begin{array}{c} +20.32(+4.0\%) & +12.06(+2.4\%) \\ -10.95(-2.2\%) & -12.06(-2.4\%) \end{array}$	1.03(4) $+0.20(+19.5%)+0.05(+4.7%)$
$\rm NLO_{QCD} + NNLL$	$484.33(7) \begin{array}{c} +39.60(+8.2\%) & +11.78(+2.4\%) \\ -29.43(-6.1\%) & -11.78(-2.4\%) \end{array}$	
NLO+NNLL	$496.36(7) \begin{array}{c} +38.64(+7.8\%) & +11.92(+2.4\%) \\ -29.35(-5.9\%) & -11.92(-2.4\%) \end{array}$	

Table 3. Total cross section and charge asymmetry for $t\bar{t}H$ production. Same structure as in table 1.

the $m(t\bar{t}H)$ -based scale choice, the central value of the asymmetry lies at the lower edge of the uncertainty band and the overall size of the band does not decrease significantly compared to NLO. For the H_T -based scale choice, the band in the nNLO and nNLO_{QCD} calculations does decrease in size w.r.t. the NLO calculation, but its central value lies near the upper edge of the uncertainty band. The combination of the $m(t\bar{t}H)$ and H_T -based calculations leads to a nNLO result that has a central value close to the NLO calculation, but with a significantly smaller scale dependence. However, overall, the charge asymmetry is rather small for $t\bar{t}H$ production and can be challenging to measure.

The PDF uncertainties are small for $t\bar{t}H$ production, of the order of $\pm 2.4\%$ for the total cross sections and slightly larger for the charge asymmetry.

4.1.3 $t\bar{t}Z$

Results for the $t\bar{t}Z$ production total cross section are listed in the second column of table 4. Similarly to the processes considered so far, the predictions show good perturbative convergence for both the $m(t\bar{t}Z)$ and H_T -based scale choices. The difference between the values of the cross section obtained with the two scale choices is large at LO_{QCD}: at that order, the H_T -based scale choice leads to a cross section that is about 9% larger than the one found with the $m(t\bar{t}Z)$ -based scales. The difference between the two scale choices at NLO is reduced to less than 5%; nNLO calculations further reduce it to just over 1%. For all of the perturbative orders considered, the uncertainty bands obtained through scale variations are compatible with these differences. In the results that combine the two scale choices (lower part of table 4) the uncertainty bands at LO_{QCD} are $^{+35\%}_{-24\%}$, and they reduce to $^{+15\%}_{-14\%}$ at NLO and to $^{+5\%}_{-4\%}$ at nNLO. Similar to $t\bar{t}H$ production, the resummed calculation produces a larger difference in central values for the total cross section calculated with $m(t\bar{t}Z)$ and H_T -based scales than the nNLO one, and also has larger uncertainty bands. Again, this fact indicates that scale variation in nNLO calculations does not lead to a reliable estimate of the uncertainty associated to missing higher-order corrections. For this reason, the most accurate and reliable prediction for the total cross section in $t\bar{t}Z$ production is given by the combined-scales calculation at NLO+NNLL accuracy, yielding a total cross section of about 811 fb, with an uncertainty from missing higher orders corrections of $^{+11\%}_{-10\%}$. This prediction includes the contributions of the EW corrections, which are rather small for the total cross sections. In fact, NLO calculations increase the total cross section by about 1%w.r.t. NLO_{OCD} calculations; this difference falls well within the theory uncertainty band.

Similarly to the case of $t\bar{t}H$ production, the charge asymmetry is small for $t\bar{t}Z$ production. This is expected since the cross section is dominated by the gluon-fusion channel.⁷ The contribution of EW corrections to the asymmetry is not negligible. However, contrary to $t\bar{t}H$ production, the approximate nNLO QCD corrections do play a prominent role: indeed they increase the asymmetry by about 20%. Furthermore, similarly to $t\bar{t}W^{\pm}$ production, the asymmetry calculated to nNLO has smaller scale-uncertainty bands than

⁷However, observe that a small and negative charge asymmetry is present in $t\bar{t}Z$ production already at LO_{QCD} [19].

$m(t\bar{t}Z)$ -based scales		
Order	σ [fb]	$A_C[\%]$
LO _{QCD}	$463.90(4) \begin{array}{c} +133.53(+28.8\%)+10.30(+2.2\%) \\ -96.96(-20.9\%) \end{array} -10.30(-2.2\%)$	$-0.10(1) \begin{array}{c} +0.005(-4.7\%) & +0.02(-16.3\%) \\ -0.004(+4.4\%) & -0.02(16.3\%) \end{array}$
$\rm NLO_{QCD}$	$732.9(1) \begin{array}{c} +92.7(+12.6\%) & +17.0(+2.3\%) \\ -90.1(-12.3\%) & -17.0(-2.3\%) \end{array}$	$0.76(2) \begin{array}{c} +0.16(+21.6\%) & +0.05(+6.3\%) \\ -0.12(-16.1\%) & -0.05(-6.3\%) \end{array}$
NLO	$741.5(1) \begin{array}{c} +92.3(+12.4\%) & +17.2(+2.3\%) \\ -89.9(-12.1\%) & -17.2(-2.3\%) \end{array}$	$0.85(2) \begin{array}{c} +0.16(+18.80\%) + 0.05(+5.3\%) \\ -0.12(-13.9\%) & -0.05(-5.3\%) \end{array}$
$\mathrm{nNLO}_{\mathrm{QCD}}$	$811.9(1) \begin{array}{c} +36.7(+4.5\%) & +18.9(+2.3\%) \\ -24.7(-3.0\%) & -18.9(-2.3\%) \end{array}$	$0.91(6) \begin{array}{c} +0.06(+6.8\%) & +0.05(+5.9\%) \\ -0.03(-2.9\%) & -0.05(-5.9\%) \end{array}$
nNLO	$820.5(1) \begin{array}{c} +36.4(+4.4\%) & +19.1(+2.3\%) \\ -24.4(-3.0\%) & -19.1(-2.3\%) \end{array}$	$0.99(6) \begin{array}{c} +0.06(+5.8\%) & +0.05(+5.2\%) \\ -0.02(-2.3\%) & -0.05(-5.2\%) \end{array}$
$\rm NLO_{QCD} + NNLL$	$790.7(2) \begin{array}{c} +61.5(+7.8\%) & +18.4(+2.3\%) \\ -66.2(-8.4\%) & -18.4(-2.3\%) \end{array}$	—
NLO+NNLL	$799.3(2) \begin{array}{c} +61.7(+7.7\%) & +18.6(+2.3\%) \\ -66.3(-8.3\%) & -18.6(-2.3\%) \end{array}$	—
H_T -based scales		
Order	$\sigma~[{ m fb}]$	$A_C[\%]$
LO _{QCD}	$504.63(8) \begin{array}{c} +150.89(+29.9\%)+11.2(+2.3\%) \\ -108.36(-21.5\%)-11.52(-2.3\%) \end{array}$	$-0.09(2) \begin{array}{c} +0.005(-6.2\%) & +0.02(-17.7\%) \\ -0.005(+5.8\%) & -0.02(+17.7\%) \end{array}$
$\rm NLO_{QCD}$	$769.5(3) \begin{array}{c} +92.7(+12.1\%) & +18.2(+2.4\%) \\ -93.6(-12.2\%) & -18.2(-2.4\%) \end{array}$	$0.82(4) \begin{array}{c} +0.20(+24.5\%) & +0.05(+5.9\%) \\ -0.13(-16.6\%) & -0.05(-5.9\%) \end{array}$
NLO	$777.4(3) \begin{array}{c} +92.1(+11.8\%) & +18.3(+2.4\%) \\ -93.2(-12.0\%) & -18.3(-2.4\%) \end{array}$	$0.90(4) \begin{array}{c} +0.19(+21.7\%) & +0.05(+5.1\%) \\ -0.13(-14.1\%) & -0.05(-5.1\%) \end{array}$
$\mathrm{nNLO}_{\mathrm{QCD}}$	$822.3(3) \begin{array}{c} +37.1(+4.5\%) & +19.5(+2.4\%) \\ -25.2(-3.1\%) & -19.5(-2.4\%) \end{array}$	$1.00(5) \begin{array}{c} +0.00(+0.0\%) & +0.05(+5.3\%) \\ -0.05(-4.7\%) & -0.05(-5.3\%) \end{array}$
nNLO	$830.2(3) \begin{array}{c} +36.5(+4.4\%) & +19.6(+2.4\%) \\ -24.7(-3.0\%) & -19.6(-2.4\%) \end{array}$	$1.08(5) \begin{array}{c} +0.00(+0.0\%) & +0.05(+4.7\%) \\ -0.05(-4.5\%) & -0.05(-4.7\%) \end{array}$
$\rm NLO_{QCD} + NNLL$	$814.5(3) \begin{array}{c} +77.4(+9.5\%) & +19.3(+2.4\%) \\ -51.8(-6.4\%) & -19.3(-2.4\%) \end{array}$	_
NLO+NNLL	$822.5(3) \begin{array}{c} +77.7(+9.4\%) & +19.4(+2.4\%) \\ -51.9(-6.3\%) & -19.4(-2.4\%) \end{array}$	—
Combined scales		
Order	$\sigma~[{ m fb}]$	$A_C[\%]$
$\mathrm{LO}_{\mathrm{QCD}}$	$484.26(4) \begin{array}{c} {}^{+171.26(+35.4\%)+11.05(+2.3\%)}_{-117.32(-24.2\%)-11.05(-2.3\%)}$	$-0.09(1) \begin{array}{c} +0.01(-11.1\%) & +0.02(-16.3\%) \\ -0.009(+9.9\%) & -0.02(+16.3\%) \end{array}$
$\rm NLO_{QCD}$	$751.2(1) \begin{array}{c} +111.1(+14.8\%) & +17.7(+2.4\%) \\ -108.5(-14.4\%) & -17.7(-2.4\%) \end{array}$	$0.79(2) \begin{array}{c} +0.23(+29.0\%) & +0.05(+6.3\%) \\ -0.15(-19.1\%) & -0.05(-6.3\%) \end{array}$
NLO	$759.5(1) \begin{array}{c} +110.1(+14.5\%) & +17.9(+2.4\%) \\ -107.8(-14.2\%) & -17.9(-2.4\%) \end{array}$	$0.87(2) \begin{array}{c} +0.22(+25.0\%) & +0.05(+5.3\%) \\ -0.14(-16.2\%) & -0.05(-5.3\%) \end{array}$
$\mathrm{nNLO}_{\mathrm{QCD}}$	$817.1(1) \begin{array}{c} +42.3(+5.2\%) & +19.3(+2.4\%) \\ -29.9(-3.7\%) & -19.3(-2.4\%) \end{array}$	$0.96(4) \begin{array}{c} +0.02(+1.7\%) & +0.06(+5.8\%) \\ -0.07(-7.5\%) & -0.06(-5.8\%) \end{array}$
nNLO	$825.4(1) \begin{array}{c} +41.3(+5.0\%) & +19.5(+2.4\%) \\ -29.3(-3.5\%) & -19.5(-2.4\%) \end{array}$	$1.03(4) \begin{array}{c} +0.01(+1.4\%) & +0.05(+5.2\%) \\ -0.07(-6.3\%) & -0.05(-5.2\%) \end{array}$
$\rm NLO_{QCD} + \rm NNLL$	$802.6(2) \begin{array}{c} +89.4(+11.1\%) & +19.0(+2.4\%) \\ -78.1(-9.7\%) & -19.0(-2.4\%) \end{array}$	—
NLO+NNLL	$810.9(2) \begin{array}{c} +89.2(+11.0\%) & +19.1(+2.4\%) \\ -77.8(-9.6\%) & -19.1(-2.4\%) \end{array}$	_

Table 4. Total cross section and charge symmetry for $t\bar{t}Z$ production. Same structure as in table 1.

the asymmetry calculated to NLO. The nNLO asymmetry in $t\bar{t}Z$ production is about 1% with a scale uncertainty of $^{+0.01}_{-0.07}$.

For the total cross section, the uncertainties due the PDFs are of the order of 2.3-2.4%, independently from the level of accuracy in the theory predictions. They are therefore smaller than the residual scale uncertainty in all cases. However, as for $t\bar{t}H$ production, they are slightly larger for the charge asymmetry. Given the fact that, for the charge asymmetry, the scale uncertainties are much smaller for $t\bar{t}Z$ production than for the $pp \rightarrow t\bar{t}H$ process, the PDF uncertainty cannot be neglected for the former process.

4.2 Differential distributions

In this section, we present predictions for binned differential distributions for invariant mass, transverse momentum, and rapidity observables. Transverse momentum and invariant mass distributions are evaluated up to NLO+NNLL accuracy (NNLL-resummed results, matched to the complete-NLO predictions). Rapidity distributions are evaluated up to nNLO (approximate NNLO QCD results, matched to complete-NLO calculations), since the NNLL resummed results in our framework are integrated over rapidities. Only predictions that combine calculations carried out with $m(t\bar{t}V)$ -based and H_T -based scale choices are shown in figures 2–8.

In each of the figures there are four plots. Each of them corresponds to one of the four processes considered in this work: the top-left plot of each figure refers to $t\bar{t}W^+$ production, the top-right plot shows the $t\bar{t}W^-$ process, the bottom-left plot refers to $t\bar{t}H$ production, and the bottom-right plot shows the $t\bar{t}Z$ process.

Each of these plots has the same layout, consisting of a main (top) panel and three ratio insets below it. The four components of each plot show the following information:

- The top panel shows the absolute predictions for the differential distribution. The central value of the distribution in each bin (calculated to NLO+NNLL accuracy for the invariant mass and transverse momentum distributions, and to nNLO for the rapidity distributions), is plotted in blue. The differential distribution calculated to complete-NLO (denoted simply as NLO) is plotted in red. In this panel the vertical axis indicates the *cross section per bin*. Consequently, the total cross section is simply the sum of the heights of the distribution in each bin (including the bins that fall outside the range shown). For the invariant mass and transverse momentum distributions the horizontal axis is logarithmic.
- In the ratio inset just below the main panel, the NLO+NNLL (or nNLO in the case of rapidity distributions) and NLO predictions are shown as a ratio w.r.t. the central value of the NLO calculations. Here, also the uncertainties from scale variations (dark shaded band) and PDFs (light shaded band) are shown, with the latter added linearly⁸ to the former. The purpose of this inset is to show the impact of the soft emission corrections on the shape of the distribution.

 $^{^8\}mathrm{By}$ linearly adding scale and PDF uncertainties we adopt a conservative approach, assuming full correlation among the two classes of effects.

- The middle ratio inset shows the difference between the additive and the multiplicative combination for the NLO_{QCD}+NNLL and the EW corrections, together with the corresponding scale uncertainties. PDF uncertainties are not shown in this panel. In particular, the inset shows the ratio between the NLO + NNLL distribution (nNLO for rapidities) and the central value of the NLO + NNLL (nNLO) calculation in each bin, as well as the ratio between the NLO × NNLL distribution (nNLO_{mult} for rapidities) and the central value of the NLO + NNLL (nNLO) calculation in each bin, as well as the ratio between the NLO + NNLL (nNLO) calculation in each bin. Multiplicative results are shown as a dark yellow band, while the additive-approach results are shown, as before, by a blue band.
- In the lower inset the effect of EW corrections is shown by plotting the NLO + NNLL (nNLO for rapidity distributions) calculations and the NLO_{QCD}+NNLL (or, in the case of rapidity distributions, to $nNLO_{QCD}$) calculations, both divided by the central value of the NLO_{QCD} +NNLL ($nNLO_{QCD}$) calculation in each bin. Also in the lower inset, NLO+NNLL (nNLO) calculations are indicated by the blue band, while results at NLO_{QCD} +NNLL ($nNLO_{QCD}$) accuracy are shown by the brown band.

4.2.1 Invariant masses

The invariant mass distribution of the $t\bar{t}V$ system is shown in figure 2. The upper-left (upper-right) plot shows the invariant mass of the $t\bar{t}W^+$ ($t\bar{t}W^-$) system. From the first ratio-inset it can be seen that the resummation has a relatively small impact on the shape of the distribution w.r.t. the NLO calculation. Even though the uncertainties affecting the NLO+NNLL calculation are slightly smaller than the NLO uncertainties, they remain large, in particular for large values of the invariant mass. The reason for the rather large scale dependence at high invariant mass is that the predictions for the $m(t\bar{t}W^+)$ -based and H_T -based scales differ significantly in this region of phase space. This observation applies to NLO calculations as well as to NLO+NNLL accuracy calculations. The tail of the invariant mass distribution is dominated by real radiation from quark emissions in the qg-initiated channel. Consequently, soft-gluon resummation cannot improve its description, since the qg channel is subleading in the threshold limit.

The difference between the additive and multiplicative methods of combining EW corrections and QCD resummed calculations is small, as it can be seen by examining the middle inset in the two plots at the top of figure 2; indeed, the blue and dark-yellow bands overlap almost entirely. Moreover, from the lower inset in the same plots it can be seen that EW corrections have a significant impact on the distribution only for small invariant masses. Indeed, the expected EW Sudakov suppression at large invariant masses is not observed since the NLO QCD corrections are rather large and dominated by hard real-emission corrections. As shown in [31], a jet-veto can suppress the large QCD corrections, which results in an enhancement of the relative impact of EW corrections.

The situation is somewhat different for the $t\bar{t}H$ and $t\bar{t}Z$ invariant mass distributions, shown in the lower-left and lower-right plots of figure 2, respectively. Since the NLO corrections for these processes are not dominated by the opening of new channels, the resummation of soft radiation reduces the scale dependence significantly. In addition,

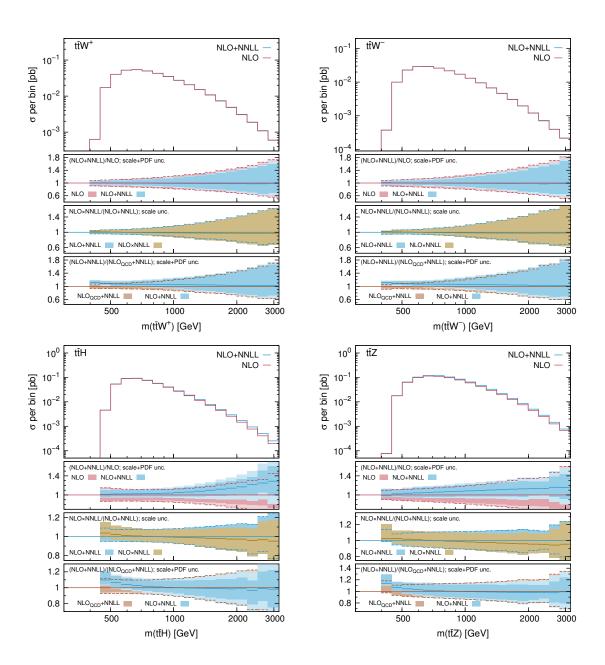


Figure 2. Distribution of the invariant mass of the $t\bar{t}V$ system at 13 TeV. The upper plots refer to $t\bar{t}W^+$ (left) and $t\bar{t}W^-$ (right), while the lower ones to $t\bar{t}H$ (left) and $t\bar{t}Z$ (right). In the first inset we focus on the resummation effects (NLO vs. NLO+NNLL), in the second one on the difference between the additive and multiplicative approach (NLO + NNLL vs. NLO × NNLL) including only scale uncertainties, and in the third on the impact of EW corrections (NLO_{QCD} + NNLL vs NLO + NNLL). More details can be found in the main text.

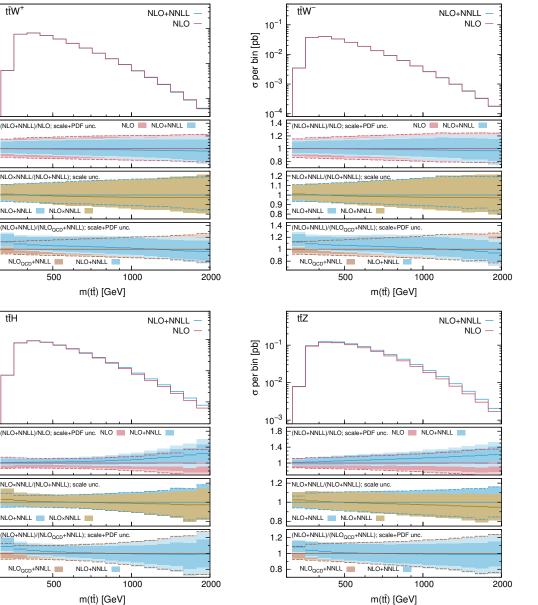
NLO+NNLL calculations lead to an increase of the cross-section central value in each bin, ranging from a few percents for small invariant masses, to about 30% (20%) for $t\bar{t}H$ ($t\bar{t}Z$) production at 3 TeV. By looking at the first inset in the lower line of figure 2 one sees that for $t\bar{t}Z$ production the entire uncertainty band at NLO+NNLL is contained in the NLO uncertainty band over the whole mass range shown in the figure. For $t\bar{t}H$ production, the central value of the NLO+NNLL distributions remains well within the NLO uncertainty, as one would expect from a well-behaved perturbative expansion. However, the NLO+NNLL uncertainty band only has a partial overlap with the NLO uncertainty band in the far tail of the invariant mass distribution.

Given that resummation changes the central value of the NLO predictions, there is a slight dependence on how these effects are combined with the NLO corrections. As shown in the middle inset, the additive and multiplicative approaches lead to slightly different shapes for the $m(t\bar{t}H/Z)$ invariant mass distribution. This difference is marginal, though, and remains well within the uncertainty band. Nevertheless, for large values of $m(t\bar{t}H/Z)$, this difference in shape amounts to a few percent. In this phase-space region, predictions in the multiplicative approach can be preferred, as discussed in section 2.3.

EW corrections in the $t\bar{t}Z$ and $t\bar{t}H$ invariant mass distributions are more relevant near the production threshold, as was already observed in [42]. This effect is due to a Sommerfeld enhancement arising, e.g., from one-loop diagrams with Higgs propagators connecting two of the final-state particles [105, 106], which contribute to the NLO₂ corrections. In contrast with the analysis in [42], here also the subleading EW contributions are included: the LO₃ and NLO₃ contributions are positive and almost completely cancel the negative NLO₂ corrections at large invariant masses, resulting in a negligible difference between the NLO+NNLL and NLO_{QCD}+NNLL predictions. Note that the multiplicative approach spoils this cancellation, since it rescales only the NLO₂ corrections according to eq. (2.23).

The distributions differential w.r.t. the $t\bar{t}$ pair invariant mass are shown in figure 3. For the $t\bar{t}W^+$ and $t\bar{t}W^-$ processes (upper-left and upper-right plots, respectively) the corrections from threshold resummation to NNLL matched to the NLO corrections reduce the uncertainty band over the whole invariant mass range considered. The effect of the resummation on the central value of each bin is negligible. In comparison to the $m(t\bar{t}W^{\pm})$ invariant mass distributions (figure 2), the scale-uncertainty band at large top-pair invariant masses is narrower. The reason is that the two scale choices ($m(t\bar{t}W^{\pm})$ -based and H_T based) give predictions that lie much closer to each other, in comparison to the case of $m(t\bar{t}W^{\pm})$ invariant mass distributions.

On the other hand, for $t\bar{t}H$ and $t\bar{t}Z$ production, the corrections to the $m(t\bar{t})$ invariant mass distributions due to resummation are similar to the case of the $m(t\bar{t}H/Z)$ invariant mass distribution, i.e., they enhance the cross section over the full invariant mass range shown in the figure, starting with small effects at threshold and reaching up to about 20 - 30% at $m(t\bar{t}) = 2$ TeV. The theory uncertainties at these large invariant masses are still larger than the difference in central values between NLO and NLO+NNLL calculations, resulting in a stable perturbative expansion. For all four processes, the difference between the additive and multiplicative combination is small, even though there is a trend: the multiplicative approach gives a slightly softer invariant mass spectrum in the tail of the distribution.



tī₩

10

10⁻²

10⁻³

1.4

1.2

1

0.8

1.2 1.1

0.9

0.8

1.4

1.2

0.8

10

10⁻²

10⁻³

1.8

1.4

1 1.2

1

0.8

1.2 1

0.8

σ per bin [pb]

tīH

σ per bin [pb]

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Figure 3. Distributions differential w.r.t. the invariant mass of the top-quark pair. Same structure as in figure 2.

The lowest inset in each of the four plots in figure 2 shows that the EW corrections, included in the NLO+NNLL predictions, distort the shape of the distributions calculated to NLO_{QCD}+NNLL accuracy. For all four processes, the EW corrections result in a positive contribution to the cross section at small invariant masses, where they enhance the distribution in each bin by 5 - 10% for $m(t\bar{t}) < 400 \,\text{GeV}$. At larger invariant masses the EW corrections are negligible in $t\bar{t}H$ and $t\bar{t}Z$ production. For $t\bar{t}W^+$ and $t\bar{t}W^-$ production, the EW corrections remain positive up to $\sim 1 \text{ TeV}$, where they turn negative, as expected from EW Sudakov suppression.

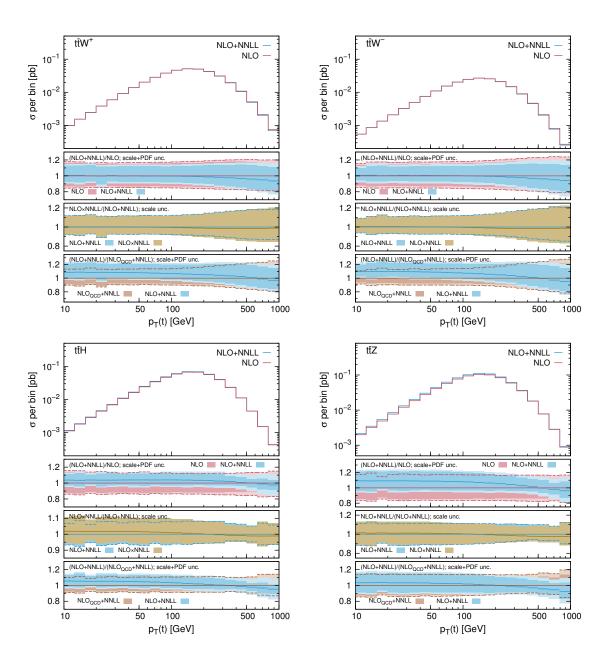


Figure 4. Distributions differential w.r.t. the transverse momentum of the top quark. Same structure as in figure 2.

4.2.2 Transverse momenta

The distributions differential w.r.t. the top quark (figure 4) and antitop quark (figure 5) transverse momentum are very similar. For these two observables, the NNLL resummation reduces the scale uncertainty in comparison to NLO calculations. In addition, NNLL resummed results lead to slightly smaller cross sections at large transverse momenta $(p_T(t/\bar{t}) > 500 \text{ GeV})$. For $t\bar{t}H$ production and especially for $t\bar{t}Z$ production, NNLL resummation increases the cross section in comparison to NLO calculations for transverse momenta smaller than ~ 500 GeV. Hence, the corrections due to soft-gluon emission affect

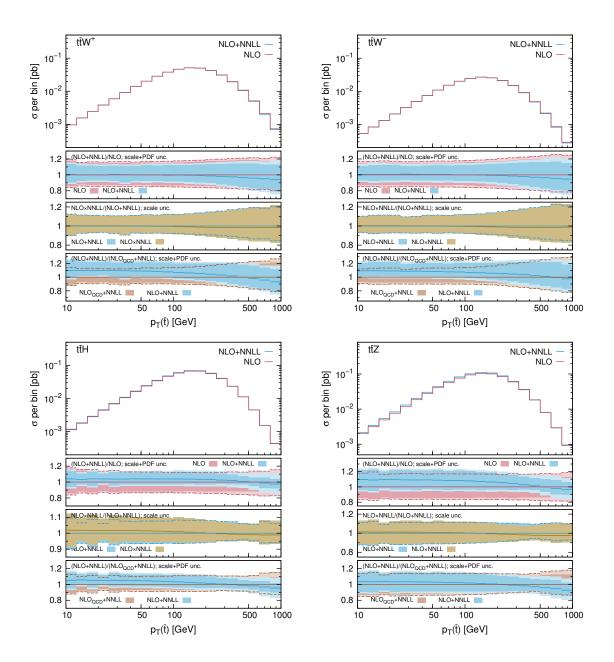


Figure 5. Distributions differential w.r.t. the transverse momentum of the antitop quark. Same structure as in figure 2.

the shape of the distribution, even though the NLO+NNLL and NLO uncertainty bands always have a large overlap. Even more than in the case of invariant mass distributions, the differences between calculations carried out in the additive and multiplicative approaches are marginal. The EW corrections show their typical behavior: for small transverse momenta, they induce a constant upward shift in the central value of the distribution in each bin, of the order of 5% for $t\bar{t}H$ and $t\bar{t}Z$ production and somewhat larger, 10%, for $t\bar{t}W^+$ and $t\bar{t}W^-$ production. These effects decrease rapidly as the transverse momentum increases, until the EW corrections start lowering the QCD cross section in each bin for

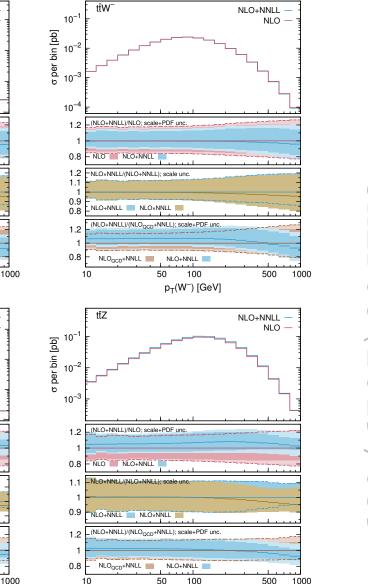


Figure 6. Distributions differential w.r.t. the transverse momentum of the EW boson. Same structure as in figure 2.

10

50

p_T(Z) [GeV]

500

1000

tīW

NLO+NNLL)/NLO; scale+PDF

NLO_NNLL/(NLO+NNLL): scale un

NLO+NNLL NLO×NNLL

(NLO+NNLL)/NLO; scale+PDF und

NNLL/(NLO+NNLL); scale und

NLO+NNLL)/(NLO_{QCD}+NNLL); scale+PDF und

50

NLO+NNLL

100

p_T(H) [GeV]

NLO+NNLL

EO+NNLL NLO×NNLL

NLO_{OCD}+NNLL

NLO_{OCD}+NNLL

(NLO+NNLL)/(NLO_{QCD}+NNLL); scale+PDF und

50

NLO+NNLL

100

 $p_T(W^+)$ [GeV]

NLO NLO+NNLL

10

10⁻²

10⁻³

 10^{-4}

1.2

1

0.8

1.2 1.1

0.9

0.8

1.2

1

0.8

10

10⁻²

10-3

 10^{-4}

1.2

1 0.8

1.1 1

0.9

1.2 1

0.8

10

σ per bin [pb]

10

tťH

σ per bin [pb]

NLO+NNLL

NLO

500

NLO

500

1000

NLO+NNLL

large transverse momenta. The large positive correction at small transverse momenta in $t\bar{t}W^+$ and $t\bar{t}W^-$ production is mainly due to the large NLO₃ correction in these processes. In this region of phase space, the EW corrections are of a size similar to the scale uncertainties of the resummed calculations; this results in a NLO+NNLL prediction for the distribution whose central value in each bin lies just within the uncertainty band of the NLO_{QCD}+NNLL calculation, and vice versa.

The distributions differential w.r.t. the transverse momentum of the heavy EW boson are shown in figure 6. Qualitatively, the corrections beyond NLO_{QCD}, either from resummation of soft emission, or from EW corrections in fixed order perturbation theory, are very similar to the corresponding corrections to the distributions for the transverse momenta of the top and the antitop quarks. For this reason, many of the remarks made in the discussion of those distributions apply to figure 6 as well. There is, however, one important exception, i.e., the non-negligible difference (~ 5% at $p_T(V) = 1$ TeV) between the additive and multiplicative matching of the resummed results with the NLO corrections at very large transverse momenta. The reason is that in the tail of these distributions both the NLO₁ and NLO₂ corrections are large and therefore the difference between the two approaches, which is dominated by the product of these two corrections, is not negligible.

4.2.3 Rapidities

Figures 7 and 8 show the predictions for the distributions differential w.r.t. the top-quark and top-antiquark rapidities, respectively. In each individual process, antitop quarks are produced more centrally than top quarks. This fact is particularly evident for the $t\bar{t}W^+$ and $t\bar{t}W^-$ processes. Indeed, this property is responsible for the large charge asymmetry for these processes.

In addition, by comparing the nNLO predictions to the NLO predictions for the y(t) differential distribution, (as it is done in first inset in each of the plots in figure 7), it can be seen that approximate NNLO corrections enhance the distributions at large forward and backward rapidities. On the contrary, the region of forward and backward rapidities in the $y(\bar{t})$ differential distribution receives relatively large corrections only in $t\bar{t}Z$ and $t\bar{t}H$ production, but not in $t\bar{t}W^{\pm}$ production. For $t\bar{t}W^{\pm}$ production, the different behavior of the nNLO corrections to the y(t) and $y(\bar{t})$ differential distributions in the forward and backward rapidity regions is the cause of the relatively large nNLO corrections to the charge asymmetry in these processes.

For these distributions, the additive and multiplicative approaches to matching lead to almost identical results. The EW corrections do not have a large impact on the shape of the top and antitop rapidity differential distributions, apart from the case of $t\bar{t}W^{\pm}$ production, where the EW corrections enhance the small rapidity region of the distributions. Finally we observe that, for the distributions shown in figures 7 and 8, when one compares nNLO calculations to NLO calculations, distributions for $t\bar{t}H$ and $t\bar{t}Z$ production show a larger reduction of the relative size of the uncertainty bands than distributions for $t\bar{t}W^{\pm}$ production.

5 Conclusions

The purpose of this paper is to provide the most complete predictions to date for the total cross section and several differential distributions for the $t\bar{t}W^{\pm}$, $t\bar{t}Z$, and $t\bar{t}H$ production processes at the LHC operating at a center of mass energy of 13 TeV. In order to achieve this goal, we combined complete-NLO corrections, accounting for both QCD and electroweak effects, with the resummation of soft emission corrections to NNLL accuracy in QCD. The complete-NLO calculations were carried out with the most recent version of MADGRAPH5_AMC@NLO, while the NNLL resummation formulas were evaluated with an in-house parton level Monte Carlo code.

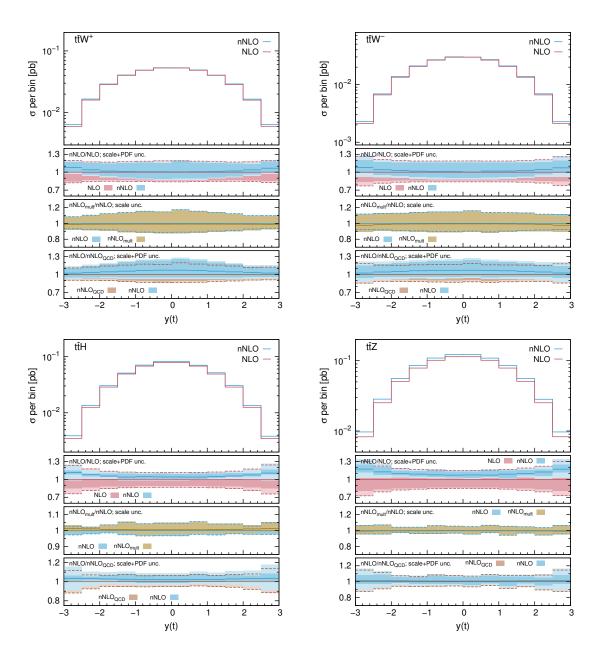


Figure 7. Distributions differential w.r.t. the top-quark rapidity. Same structure as in figure 2, but with the substitution $NLO_{QCD} + NNLL \rightarrow nNLO_{QCD}$, $NLO + NNLL \rightarrow nNLO$, and $NLO \times NNLL \rightarrow nNLO_{mult}$.

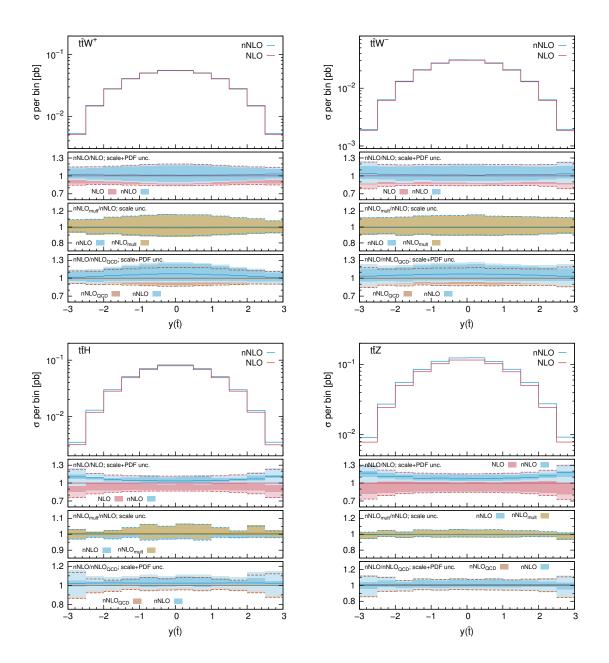


Figure 8. Distributions differential w.r.t. the antitop-quark rapidity Same structure as in figure 7.

After considering theoretical uncertainties related to the choice of PDFs and to the residual dependence of the calculation on unphysical scales, we find the following predictions for the total cross section of the three processes

$$\begin{aligned}
\sigma_{t\bar{t}W^+} &= 384.17(9)^{+51.52(+13.4\%)+8.16(+2.1\%)}_{-32.36(-8.4\%)-8.16(-2.1\%)}, \\
\sigma_{t\bar{t}W^-} &= 197.75(4)^{+26.41(+13.4\%)+5.41(+2.7\%)}_{-16.07(-8.1\%)-5.41(-2.7\%)}, \\
\sigma_{t\bar{t}H} &= 496.36(7)^{+38.64(+7.8\%)+11.92(+2.4\%)}_{-29.35(-5.9\%)-11.92(-2.4\%)}, \\
\sigma_{t\bar{t}Z} &= 810.9(2)^{+89.2(+11.0\%)+19.1(+2.4\%)}_{-77.8(-9.6\%)-19.1(-2.4\%)}.
\end{aligned}$$
(5.1)

These predictions have NLO+NNLL accuracy. The number in parentheses next to the central value of the cross section indicates the statistical uncertainty due to the Monte Carlo integration. The first set of uncertainties is related to scale choices, and the second to PDFs.

Several differential distributions were analyzed in section 4: the invariant masses of the $t\bar{t}$ and $t\bar{t}V$ systems, the transverse-momenta of the top quark, antitop quark and vector boson, all calculated to NLO+NNLL accuracy, and the rapidities of the top quark and antitop quark, evaluated to nNLO. The behavior of the perturbative series and the relative size of the residual theoretical uncertainties indicate that the predictions for the observables considered here are stable and sufficiently accurate when compared to current and expected experimental errors.

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