

Topics in Torsion Theory

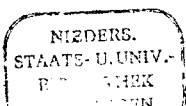
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TABLE OF CONTENTS

Preface	5
Introduction	9
§1. Preliminaries on Torsion Theory	11
§2. The Jacobson Radical, Simple Modules and Chain Conditions Relative to Torsion Theory. Nakayama's Lemma	29
2.1 Simple Modules and Maximal Submodules Relative to a Torsion Theory	29
2.2 The Jacobson Radical and Radical Free Modules Relative to a Torsion Theory	33
2.3 Noetherian Modules Relative to a Torsion Theory	39
2.4 Artinian Modules Relative to a Torsion Theory	49
§3. Composition Series Relative to Torsion Theory. The Generalized Hopkins–Levitzki Theorem	55
§4. Injective and Projective Concepts and Torsion Theory. The Generalized Baer and Fuchs Conditions. Relatively Flat Modules ..	65
4.1 (Quasi–)Injective Modules Relative to a Torsion Theory	65
4.2 (Quasi–)Projective Modules Relative to a Torsion Theory	81
4.3 Flat Modules Relative to a Torsion Theory	88
§5. Covers and Hulls	101
5.1 (Quasi–)Injective Hulls Relative to a Torsion Theory	102
5.2 (Quasi–)Projective Covers Relative to a Torsion Theory	113
5.3 Torsionfree Covers	126



§6. Classical Properties of Rings Relative to a Torsion Theory	135
6.1 (Semi)Primitive, Simple and (Semi)Prime Rings Relative to a Torsion Theory	135
6.2 Semisimple Rings Relative to a Torsion Theory	143
6.3 Primitive Rings and Density Relative to a Torsion Theory	148
References	157
Index	159