

Transition metal ion implantation into AlGaN

R. M. Frazier, G. T. Thaler, C. R. Abernathy, and S. J. Pearton^{a)}

Department of Materials Science and Engineering, University of Florida, Gainesville, Florida 32611

M. L. Nakarmi, K. B. Nam, J. Y. Lin, and H. X. Jiang

Department of Physics, Kansas State University, Manhattan, Kansas 66506

J. Kelly, R. Rairigh, and A. F. Hebard

Department of Physics, University of Florida, Gainesville, Florida 32611

J. M. Zavada

U.S. Army Research Office, Research Triangle Park, North Carolina 27709

R. G. Wilson

Consultant, Stevenson Ranch, California 91381

(Received 29 May 2003; accepted 31 July 2003)

n- and *p*-type Al_xGa_{1-x}N ($x=0.38$ for *n*-type, $x=0.13$ for *p*-type) layers grown on Al₂O₃ substrates were ion implanted with the transition metals Mn, Cr, and Co at high concentrations (peak doping levels ~ 3 at. %). After implantation and annealing at 1000 °C, only impurity transitions at ~ 2.9 and 3.9 eV and no band-edge photoluminescence could be observed in all the samples. X-ray diffraction did not detect any peaks associated with second phase formation. Room-temperature hysteresis loops were obtained for Co-implanted *n*-type AlGaN, while there was no convincing evidence for ferromagnetism in the Mn- or Cr-implanted *n*-AlGaN. By sharp contrast, Mn implantation in *p*-AlGaN did produce ferromagnetic behavior and 300 K hysteresis. Both carrier type and crystalline quality can influence the resulting magnetic properties. © 2003 American Institute of Physics. [DOI: 10.1063/1.1613375]

INTRODUCTION

Very few studies of the properties of ion-implanted AlGaN have been reported,^{1,2} even though the GaN/AlGaN heterostructure is a key component of devices such as high electron mobility transistors,^{3,4} UV lasers, light-emitting diodes,⁵⁻¹¹ and solar blind UV photodetectors.¹²⁻¹⁴ There is also interest in the use of transition metal doped AlGaN for possible applications in spintronic devices such as polarized light emitter or spin transistors.¹⁵ The latter exploits quantum interference effects provided electrons with a particular spin can be injected into the channel of the device and a gate bias can be applied to cause splitting of spin-up and spin-down states.¹⁶ A key requirement for spin-based semiconductor devices is the achievement of ferromagnetism, preferably above room temperature. In this regard, theoretical predictions suggest that the Curie temperature in transition metal doped semiconductors is proportional to the band gap of the material.^{17,18} Accordingly, GaN has been a focus of attention in this regard, with the transition metals introduced during epitaxial or bulk growth or postgrowth by implantation or diffusion.¹⁹⁻³⁹ The use of ion implantation allows for rapid screening of the effectiveness of different transition metal elements in producing ferromagnetic behavior. The properties of implanted transition metals in AlGaN are of particular relevance for realization of polarized light emitters or spin

transistors since they could serve as the cladding layer in the former and the wide-band-gap part of the heterostructure in the latter.

In this article we report on the optical, structural, and magnetic properties of *n*- and *p*-type AlGaN implanted with doses of Mn, Cr, or Co sufficient to produce peak transition metal concentrations of a few atomic percent. The material exhibits carrier concentrations $\leq 3 \times 10^{16} \text{ cm}^{-3}$ after implantation and annealing, indicating that the transition metals introduce deep states into the band gap and that free-carrier-induced ferromagnetism is not likely to be the mechanism for the observed magnetic properties.

EXPERIMENT

The *n*-type undoped ($n \sim 5 \times 10^{17} \text{ cm}^{-3}$) Al_{0.38}Ga_{0.62}N layers were grown on *c*-plane Al₂O₃ substrates by hydride vapor phase epitaxy, as described in detail previously.⁴⁰ The layer thicknesses were $\sim 0.4 \mu\text{m}$ in each case. The *p*-type ($p \sim 3 \times 10^{16} \text{ cm}^{-3}$), Mg-doped Al_{0.13}Ga_{0.87}N layers were also grown on sapphire (0001), but were grown by metal-organic chemical vapor deposition. The layer thickness was $\sim 1 \mu\text{m}$. Implantation of Mn⁺, Cr⁺, or Co⁺ ions was performed at 250 keV energy, corresponding to a projected range of $\sim 1500 \text{ \AA}$. The dose was held constant at $3 \times 10^{16} \text{ cm}^{-2}$, producing a peak concentration of each transition metal of ~ 3 at. % in AlGaN. During the implant step, the samples were held at a temperature of $\sim 300 \text{ °C}$ to produce dynamic annealing and substitutionality of the transition metal atoms.⁴¹ Postimplant annealing was carried out at

^{a)}Electronic mail: spear@mse.ufl.edu

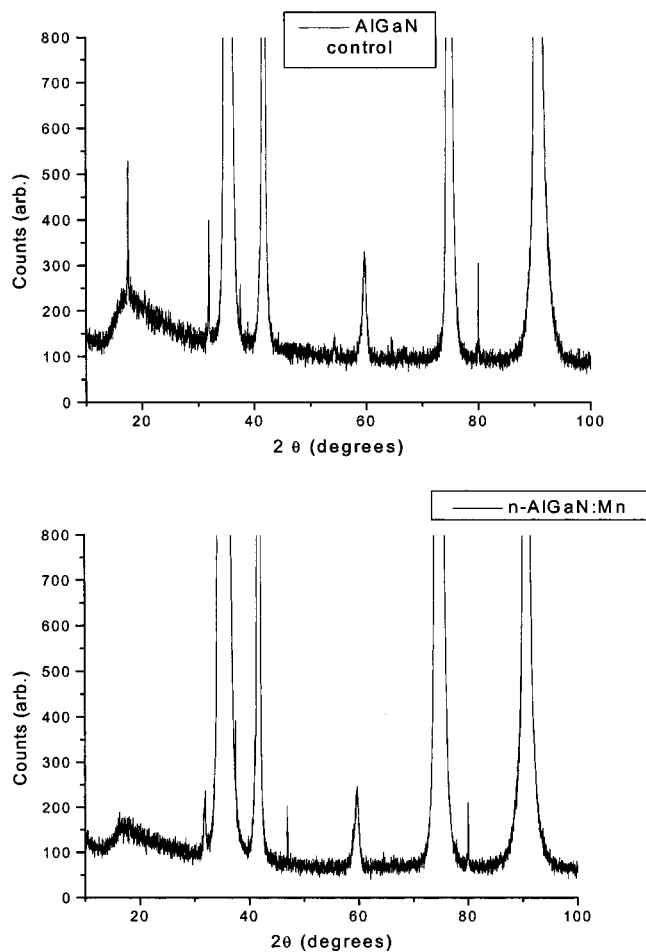


FIG. 1. X-ray diffraction spectra of $\text{Al}_x\text{Ga}_{1-x}\text{N}$ ($x=0.38$) both before (top) and after Mn^+ implantation (3×10^{16} , 250 keV), followed by a 1000 °C, 2 min anneal.

1000 °C for 2 min under a flowing N_2 ambient in a Heatpulse 610T system, with the samples in a face-to-face configuration with other AlGaIn layers. Characterization included photoluminescence (PL) measurements performed with a quadrupled Ti:sapphire laser as an excitation source together with a streak camera.⁴² X-ray diffraction (XRD) was performed in a Philips powder diffractometer. Magnetic characterization was carried out in a quantum design superconducting quantum interference device system.

RESULTS AND DISCUSSION

Figure 1 shows $\theta-2\theta$ XRD scans from the $n\text{-AlGaIn}$ before and after Mn^+ implantation and annealing at 1000 °C. Similar results were found for the Co^+ and Cr^+ implanted samples and the $n\text{-}$ and $p\text{-AlGaIn}$ did not show any observable differences. The highest intensity peaks in all spectra correspond to the expected $\text{AlGaIn}(0\ 0\ 0\ 2)$ and $(0\ 0\ 0\ 4)$ lines and $\text{Al}_2\text{O}_3(0\ 0\ 0\ 2)$, $(0\ 0\ 0\ 6)$, and $(0\ 0\ 0\ 12)$ substrate peaks. We did not observe any peaks due to second phases that could exhibit ferromagnetism. For example, in the Mn implanted material, Mn_xN is ferromagnetic with a Curie temperature of 745 K and GaMn is also ferromagnetic with a Curie temperature near 300 K (metallic Mn is antiferromagnetic).³⁶ In the Co^+ implanted AlGaIn, metallic

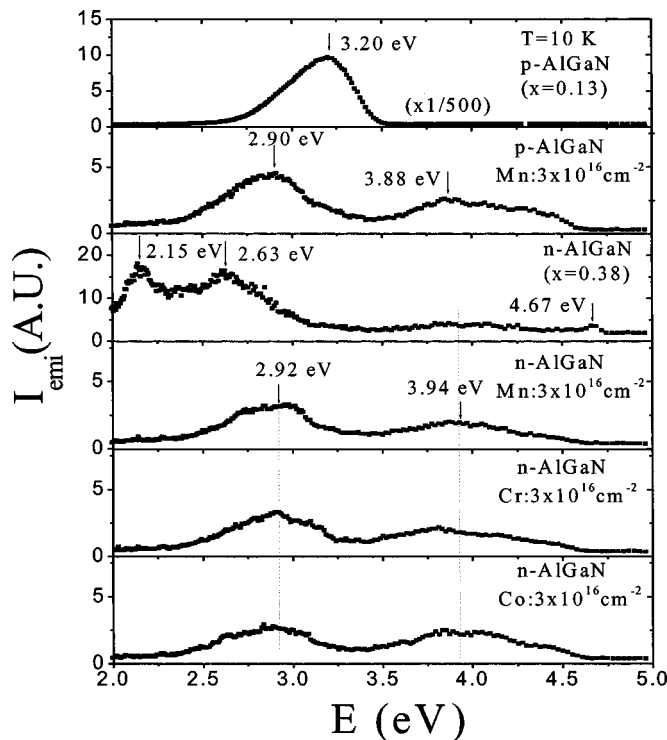


FIG. 2. 10 K PL spectra from $p\text{-AlGaIn}$ before and after Mn^+ implantation and $n\text{-AlGaIn}$ before and after Cr^+ , Co^+ , and Mn^+ implantation (3×10^{16} , 250 keV in all cases), followed in all cases by a 1000 °C, 2 min anneal.

Co has a Curie temperature of 1382 K and Co_xN phases are all Pauli ferromagnetic.³⁶ Finally, in the Cr^+ implanted AlGaIn, CrO is half metallic, while Cr, CrN , Cr_2N , Al_xCr_y , and Ga_xCr_y are not ferromagnetic.³⁶ However, in such thin layers, it could be possible for small quantities of second phases to be present and remain undetectable by XRD.

In the PL characterization, no band-edge luminescence was observed after implantation and annealing of any of the samples and only impurity transitions were observed. Figure 2 shows 10 K PL spectra from the implanted AlGaIn, in which broad deep level emissions at ~ 2.9 and ~ 3.9 eV are observed in all implanted samples, independent of the element introduced. One possible assignment of those lines is that of lattice disorder introduced by the implant step. The absence of appreciable band-edge luminescence in the implanted samples indicates that at least some of the point defect damage is stable to at least 1000 °C, similar to the case of pure AlN.²

Well-defined hysteresis at 300 K was observed for the Co-implanted $\text{Al}_{0.38}\text{Ga}_{0.62}\text{N}$, as shown at the top of Fig. 3. The coercive fields were ~ 85 Oe at 300 K and ~ 75 Oe at 10 K. The saturation magnetization was $\sim 0.4\text{ emu/cm}^3$ or $\sim 0.76\mu_B$ calculated saturation moment. This is slightly higher than the value reported for Co^+ implantation into pure AlN under similar conditions ($0.52\mu_B$),⁴³ which is consistent with the higher vacancy concentrations expected to be created in AlGaIn due to its lower bond strength. The bottom part of Fig. 3 shows the temperature dependence of field-cooled (FC) and zero field-cooled (ZFC) magnetization for the Co^+ implanted AlGaIn. The fact that these have dif-

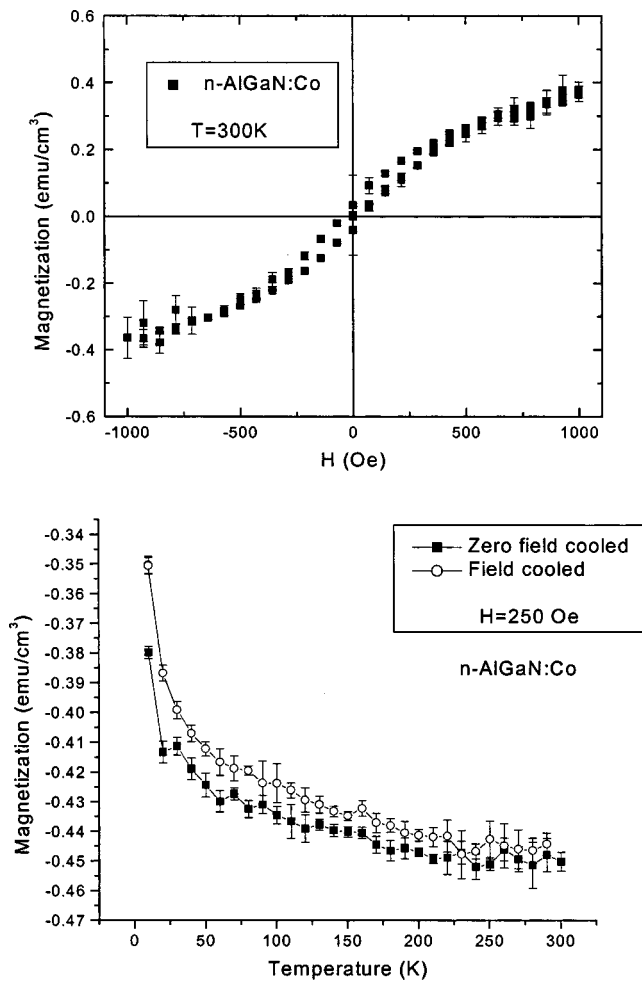


FIG. 3. 300 K magnetization as a function of field (top) and field-cooled (FC) and zero-field-cooled (ZFC) magnetization vs temperature for AlGaIn implanted with $3 \times 10^{16} \text{ Co}^+$ annealed at 1000°C for 2 min.

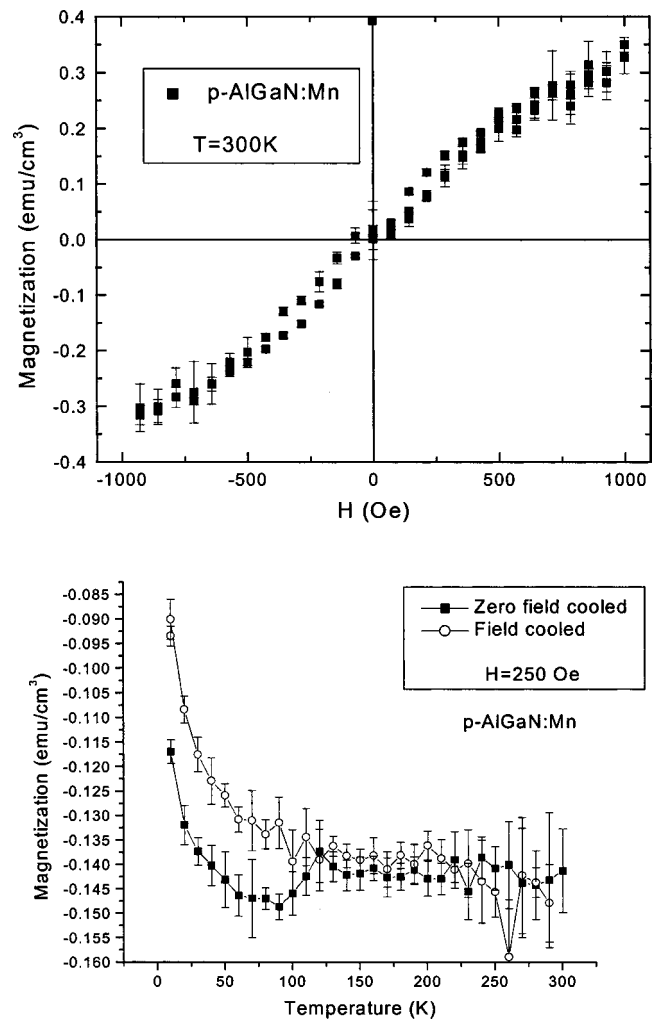


FIG. 4. 300 K magnetization as a function of field (top) and field-cooled (FC) and zero-field-cooled (ZFC) magnetization vs temperature for AlGaIn implanted with $3 \times 10^{16} \text{ Mn}^+$ annealed at 1000°C for 2 min.

ferent values out to $\sim 230 \text{ K}$ is a further indication of the presence of ferromagnetism in the material. In both epitaxial and ion implanted transition metal doped semiconductors, we have found the general result that the hysteresis can be detected to higher temperatures than the difference in FC and ZFC magnetization.⁴⁴ As mentioned earlier, the samples exhibited low carrier densities ($< 3 \times 10^{16} \text{ cm}^{-3}$ from Hall measurements) after implantation and annealing and, therefore, carrier-mediated ferromagnetism by free electrons is not expected to be operative. In addition, the Co ionization level is expected to be deep in the AlGaIn band gap,^{45–47} so that there will be no significant contribution to the carrier density from the substitutional fraction of these atoms. More recent percolation network models for ferromagnetism in dilute magnetic semiconductors suggest that localized carriers may mediate the interaction between magnetic ions in low carrier density systems.^{48,49}

Mn-implanted *p*-type AlGaIn also showed a well-defined hysteresis loop at 300 K, with a coercivity of $\sim 60 \text{ Oe}$ (Fig. 4, top). The saturation moment, $M_0 = g \mu_B S$, where g is the degeneracy factor, μ_B the Bohr magneton, and S the total number of spins, was calculated to be $\sim 0.57 \mu_B$. The theoretical value would be 4 if all of the implanted Mn was

participating towards the ferromagnetism, so the lower experimental value indicates that only a fraction of the Mn is substitutional and magnetically active. The saturation moment for AlGaIn is significantly larger than the value of $0.17 \mu_B$ reported for Mn implantation into pure AlN.⁴³ The temperature dependence of FC and ZFC magnetization is shown at the bottom of Fig. 4. The ferromagnetism is very weak above $\sim 125 \text{ K}$, but is detectable through the hysteresis.

By sharp contrast to the case of Mn implanted into *p*-AlGaIn, when we performed the same implants into *n*-AlGaIn, the resulting differences in FC and ZFC magnetization were very weak (Fig. 5, top) and hysteresis loops even at 10 K did not show clear evidence of ferromagnetism. The differences from the *p*-type material may result from the higher AlN mole fraction in the *n*-type AlGaIn, which makes it harder for the implanted ions to become substitutional upon annealing. An alternative explanation is that holes are more efficient at ferromagnetic coupling between the Mn spins than are electrons. This has been reported previously for both *n*- and *p*-type GaAs (Ref. 17) and GaP doped with Mn.⁴⁴ We also did not observe any clear evidence for ferromagnetism in the Cr implanted *n*-AlGaIn (Fig. 5, bottom).

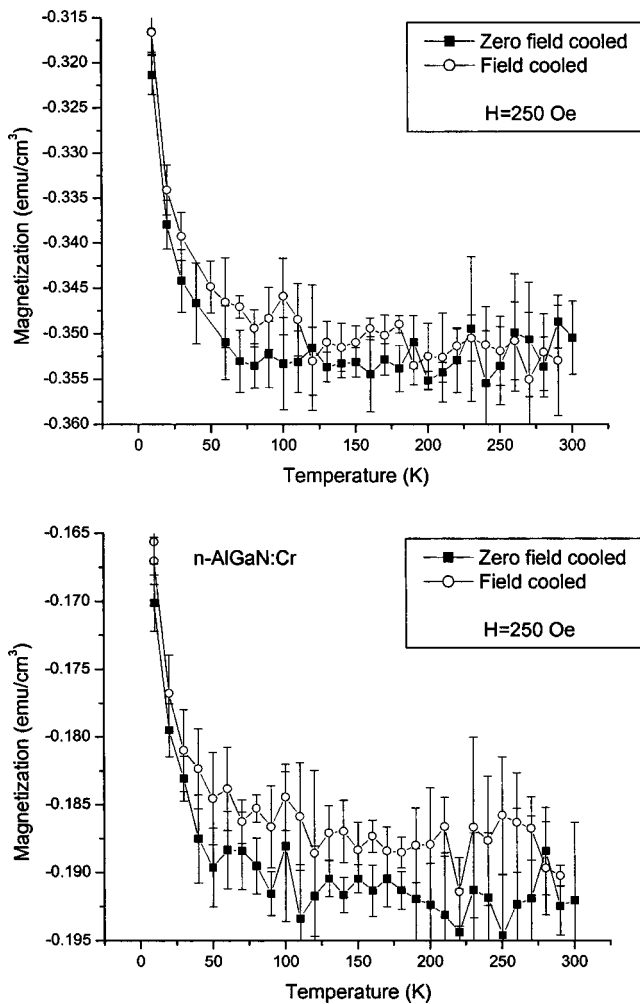


FIG. 5. FC and ZFC magnetization as a function of temperature for *n*-AlGaIn implanted with either Mn (top) or Cr (bottom) to the same dose ($3 \times 10^{16} \text{ cm}^{-2}$) and annealed at 1000 °C for 2 min.

This is a clear difference from the case of Cr-implanted AlN, where hysteresis was reported at 300 K.

In conventional dilute magnetic semiconductors such as (Ga,Mn)As, the magnetization is given by¹⁷

$$M = \mu_g \mu_B S N_0 x_{\text{eff}} B_S \left[\frac{g \mu_B (-\partial F_C[M] / \partial M + H)}{k_B (T + T_{AF})} \right],$$

in the mean-field approach, where *S* is the localized spin, *N*₀ is the concentration of cation sites, *X*_{eff} is the effective spin concentration, *B*_{*S*} is the Brillouin function, and *F*_{*C*}(*M*) is the hole contribution to the free-energy function *F* (which depends on the magnetization of the localized spin). The validity of this model depends on having a high carrier concentration in the magnetic semiconductor, and experimentally we do not observe this in AlGaIn, and correspondingly, we do not observe a Brillouin-like dependence of magnetization on temperature. In pure AlN, Mn produces an absorption line at ~1.5 eV from the valence band, suggesting the Mn^{3+/2+} acceptor level is deep in the gap and makes the realization of carrier-mediated ferromagnetism unlikely.⁴⁵ The mean-field models have also shown that Mn clustering can enhance the Curie temperature through localization of carriers at these clustered regions.⁴⁸ Some calculations suggest it is energeti-

cally favorable to form ferromagnetic transition metal ion dimers and trimers at second nearest-neighbor sites.⁵⁰ Distant pairs would be weakly ferromagnetic or antiferromagnetic. These predictions suggest that the ferromagnetism will be a very strong function of the synthesis conditions used for the magnetic semiconductor. They also suggest that nonequilibrium methods such as ion implantation possess inherent advantages in trying to maximize the Curie temperature because of their ability to achieve solid solubilities for dopants well above those possible with equilibrium synthesis methods.^{1,2}

SUMMARY AND CONCLUSIONS

Atomic percent concentrations of Mn, Cr, or Co were introduced into epitaxial AlGaIn layers by ion implantation. X-ray diffraction did not observe any secondary phase formation after annealing at 1000 °C. No band-edge luminescence was detected in these samples, indicating that nonradiative recombination centers related to implantation damage are not removed at this annealing temperature. Ferromagnetic ordering was observed for Co-implanted samples, but not for Cr. The saturation moments for the ferromagnetic samples were higher than those reported for AlN doped using similar conditions.

ACKNOWLEDGMENTS

The work at UF is partially supported by NSF Grant No. DMR 0101438 and ECS Grant No. 02242203 and by ARO Contract Nos. DAAF 190110701 and DAAD 1902140. The work at KSU was partially supported by ARO and NSF Grant No. DMR 0203373.

- ¹S. O. Kucheyev, J. S. Williams, J. Zou, G. Li, C. Jagadish, M. O. Manasreh, M. Pophristic, S. Guo, and I. T. Ferguson, *Appl. Phys. Lett.* **80**, 787 (2002).
- ²S. O. Kucheyev, J. S. Williams, J. Zou, C. Jagadish, M. Pophristic, S. Guo, I. T. Ferguson, and M. O. Manasreh, *J. Appl. Phys.* **92**, 3554 (2002).
- ³L. F. Eastenan, V. Tilak, J. Smart, B. M. Green, E. M. Chumbes, R. Dmitrov, H. Kim, O. S. Ambacher, N. Weimann, T. Prunty, M. Murphy, W. J. Schaff, and J. R. Shealy, *IEEE Trans. Electron Devices* **48**, 479 (2001).
- ⁴W. Lu, J. Yang, M. Asif Khan, and I. Adesidu, *IEEE Trans. Electron Devices* **48**, 581 (2001).
- ⁵K. B. Nam, J. Li, M. L. Nakarmi, J. Y. Lin, and H. X. Jiang, *Appl. Phys. Lett.* **82**, 1694 (2003).
- ⁶E. Kuokstis, J. Zhang, Q. Fareed, J. W. Yang, G. Simin, M. Asif Khan, R. Gaska, M. S. Shur, C. Rojo, and L. Schowalter, *Appl. Phys. Lett.* **81**, 2755 (2002).
- ⁷R. Gaska, C. Chen, J. Yang, E. Kookstis, M. Asif Khan, G. Tamulaitis, I. Yilmog, M. S. Shur, J. C. Rojo, and L. J. Schowalter, *Appl. Phys. Lett.* **81**, 4658 (2002).
- ⁸T. Nishida, N. Kobayashi, and T. Ban, *Appl. Phys. Lett.* **82**, 1 (2003).
- ⁹G. Kipshidze, V. Kuryatkov, K. Zhu, B. Vorizov, M. Holtz, S. Nikishin, and H. Temkin, *J. Appl. Phys.* **93**, 1363 (2003).
- ¹⁰K. Dovidenko, S. Oktyabusky, J. Narayan, and M. Razeghi, *J. Appl. Phys.* **79**, 2439 (1996).
- ¹¹A. Yasan, R. McClintock, K. Mayes, S. R. Darvish, P. Kung, and M. Razeghi, *Appl. Phys. Lett.* **81**, 801 (2002).
- ¹²D. Walker, V. V. Kumar, K. Mi, P. Sandvik, P. Kung, X. H. Zhang, and M. Razeghi, *Appl. Phys. Lett.* **76**, 403 (2000).
- ¹³V. V. Kuryatov, H. Temkin, J. C. Campbell, and R. D. Dupuis, *Appl. Phys. Lett.* **78**, 3340 (2001).
- ¹⁴D. Ciplis, R. Rimeika, M. S. Shur, S. Rumyantsev, R. Gaska, A. Sereika, J. Yang, and M. Asif Khan, *Appl. Phys. Lett.* **80**, 1701 (2002).
- ¹⁵S. J. Pearton, C. R. Abernathy, M. E. Overberg, G. T. Thaler, D. P. Norton,

- N. Theodoropoulou, A. F. Hebard, Y. D. Park, F. Ren, J. Kim, and L. A. Boatner, *J. Appl. Phys.* **93**, 1 (2003).
- ¹⁶J. Singh, *Electronic and Optoelectronic Properties of Semiconductor Structures* (Cambridge University Press, New York, 2003).
- ¹⁷T. Dietl, *Semicond. Sci. Technol.* **17**, 377 (2002).
- ¹⁸T. Dietl, H. Ohno, and F. Matsukura, *Phys. Rev. B* **63**, 195205 (2001).
- ¹⁹S. Sonoda, S. Shimizu, T. Sasaki, Y. Yamamoto, and H. Hori, *J. Cryst. Growth* **237–239**, 1358 (2002).
- ²⁰T. Sasaki, S. Sonoda, Y. Yamamoto, K. Suga, S. Shimizu, K. Kindo, and H. Hori, *J. Appl. Phys.* **91**, 7911 (2002).
- ²¹G. T. Thaler, M. E. Overberg, B. Gila, R. Frazier, C. R. Abernathy, S. J. Pearton, J. S. Lee, S. Y. Lee, Y. D. Park, Z. G. Khim, J. Kim, and F. Ren, *Appl. Phys. Lett.* **80**, 3964 (2002).
- ²²K. H. Kim, K. J. Lee, D. J. Kim, H. J. Kim, Y. E. Ihm, D. Djayaprawira, M. Takahashi, C. S. Kim, C. G. Kim, and S. H. Yoo, *Appl. Phys. Lett.* **82**, 1775 (2003).
- ²³N. Theodoropoulou, A. F. Hebard, M. E. Overberg, C. R. Abernathy, S. J. Pearton, S. N. G. Chu, and R. G. Wilson, *Appl. Phys. Lett.* **78**, 3475 (2001).
- ²⁴Y. L. Soo, G. Kioseoglou, S. Kim, S. Huang, Y. H. Kaa, S. Kubarawa, S. Owa, T. Kondo, and H. Munekata, *Appl. Phys. Lett.* **79**, 3926 (2001).
- ²⁵M. E. Overberg, C. R. Abernathy, S. J. Pearton, N. A. Theodoropoulou, K. T. McCarthy, and A. F. Hebard, *Appl. Phys. Lett.* **79**, 1312 (2001).
- ²⁶S. Dhar, O. Brandt, A. Trampert, L. Daeweritz, K. J. Friedland, K. H. Ploog, J. Keller, B. Beschoten, and G. Guntherodt, *Appl. Phys. Lett.* **82**, 2077 (2003).
- ²⁷S. Kuwabara, T. Kondo, T. Chikyow, P. Ahmet, and H. Munekata, *Jpn. J. Appl. Phys., Part 2* **40**, L724 (2001).
- ²⁸H. Hori, S. Sonoda, T. Sasaki, Y. Yamamoto, S. Shimizu, K. Suga, and K. Kindo, *Physica B* **324**, 142 (2002).
- ²⁹M. C. Park, K. S. Huh, J. M. Myoung, J. M. Lee, J. Y. Chang, K. I. Lee, S. H. Han, and W. Y. Lee, *Solid State Commun.* **124**, 11 (2002).
- ³⁰M. Sato, H. Tanida, K. Kato, T. Sasaki, Y. Yamamoto, S. Sonoda, S. Shimiyu, and H. Hori, *Jpn. J. Appl. Phys., Part 1* **41**, 4513 (2002).
- ³¹M. Hastimoto, Y.-K. Zhou, H. Tampo, M. Kanamura, and H. Asahi, *J. Cryst. Growth* **252**, 499 (2003).
- ³²J. Y. Chang, G. H. Kim, J. M. Lee, S. H. Han, H. J. Kim, W. Y. Lee, M. H. Ham, K. S. Huh, and J. M. Myoung, *J. Appl. Phys.* **93**, 7858 (2003).
- ³³M. B. Haider, C. Constantin, H. Al-Britthen, H. Yang, E. Trifan, D. Iagram, A. R. Smith, C. V. Kelly, and Y. Ijiri, *J. Appl. Phys.* **93**, 5274 (2003).
- ³⁴M. Zajac, J. Gosk, E. Grzanka, M. Kaminska, A. Twardowski, B. Strojek, T. Szyszko, and S. Podsiadlo, *J. Appl. Phys.* **93**, 4715 (2003).
- ³⁵S. E. Park, H.-J. Lee, Y. C. Cho, S.-Y. Jeong, C. R. Cho, and S. Cho, *Appl. Phys. Lett.* **80**, 4187 (2002).
- ³⁶S. J. Pearton, C. R. Abernathy, D. P. Norton, A. F. Hebard, Y. D. Park, L. A. Boatner, and J. D. Budai, *Mater. Sci. Eng., R.* **40**, 137 (2003).
- ³⁷J. M. Baik, H. W. Jang, J. K. Kim, and J. M. Lee, *Appl. Phys. Lett.* **82**, 583 (2003).
- ³⁸Y. Shon, Y. H. Kwon, S. U. Yuldashev, Y. S. Park, D. J. Fu, D. Y. Kim, H. S. Kim, and T. W. Kang, *J. Appl. Phys.* **93**, 1546 (2003).
- ³⁹M. L. Reed, N. A. El-Masry, H. Stadelmaier, M. E. Ritums, N. J. Reed, C. A. Parker, J. C. Roberts, and S. M. Bedair, *Appl. Phys. Lett.* **79**, 3473 (2001).
- ⁴⁰Y. V. Melnick, K. V. Vassilevski, I. P. Nikitina, A. H. Balanin, Y. Davydov, and V. A. Dmitriev, *MRS Internet J. Nitride Semicond. Res.* **2**, 39 (1997).
- ⁴¹J. S. Williams, *Mater. Sci. Eng., A* **253**, 9 (1998).
- ⁴²K. B. Nam, J. Li, K. H. Kim, J. Y. Lin, and H. X. Jiang, *Appl. Phys. Lett.* **78**, 3690 (2001).
- ⁴³R. M. Frazier, J. Stapleton, G. T. Thaler, C. R. Abernathy, S. J. Pearton, R. Rairigh, J. Kelly, A. F. Hebard, M. C. Nakarmi, K. B. Nam, J. Y. Lin, H. X. Jiang, J. M. Zavada, and R. G. Wilson, *J. Appl. Phys.* **94**, 1592 (2003).
- ⁴⁴N. Theodoropoulou, A. F. Hebard, M. E. Overberg, C. R. Abernathy, S. J. Pearton, S. N. G. Chu and R. G. Wilson, *Phys. Rev. Lett.* **89**, 107203 (2003).
- ⁴⁵T. Gral, M. Gjukic, M. S. Brandt, M. Stutzmann, and O. Ambacher, *Appl. Phys. Lett.* **81**, 5159 (2002).
- ⁴⁶R. Y. Korobkov, J. M. Gregie, and B. W. Wessels, *Physica B* **308**, 30 (2001).
- ⁴⁷A. Y. Polykov, A. V. Govorkov, N. B. Smirnov, N. Y. Pashkova, G. T. Thaler, M. E. Overberg, R. M. Frazier, C. R. Abernathy, S. J. Pearton, J. Kim, and F. Ren, *J. Appl. Phys.* **92**, 4989 (2002).
- ⁴⁸M. Bercui and R. N. Bhatt, *Phys. Rev. Lett.* **87**, 107203 (2001).
- ⁴⁹V. K. Dugnov, V. I. Litvinov, J. Barnas, and M. Viera, *Phys. Rev. B* **67**, 033201 (2003).
- ⁵⁰M. van Schilfgaarde and O. N. Mryasov, *Phys. Rev. B* **63**, 233205 (2001).