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Trends in Effective Diffusion Coefficients for Ion-Exchange Strengthening of **Soda-Lime-Silicate Glasses**

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Monovalent cations enable efficient ion-exchange processes due to their high mobility in silicate glasses. Numerous properties can be modified in this way, e.g., mechanical, optical, electrical, or chemical performance. In particular, alkali cation exchange has received significant attention, primarily with respect to introducing compressive stress into the surface region of a glass, which increases mechanical durability. However, most of the present applications rely on specifically tailored matrix compositions in which the cation mobility is enhanced. This largely excludes the major area of soda-lime-silicates (SLS) such as are commodity in almost all large-scale applications of glasses. Basic understanding of the relations between structural parameters and the effective diffusion coefficients may help to improve ion-exchanged SLS glass products, on the one hand in terms of obtainable strength and on the other in terms of cost. In the present paper, we discuss the trends in the effective diffusion coefficients when exchanging Na⁺ for various monovalent cations (K+, Cu+, Ag+, Rb+, and Cs+) by drawing relations to physicochemical properties. Correlations of effective diffusion coefficients were found for the bond dissociation energy and the electronic cation polarizability, indicating that localization and rupture of bonds are of importance for the ion-exchange rate.

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INTRODUCTION

Monovalent cations exhibit pronounced mobility in silicate glasses. This enables highly effective ion-exchange processes. In this context, ion exchange has long been known as a useful tool to modify the surface of glass products (Schulze, 1913; Stern, 1966). Numerous properties can be modified in this way, including mechanical, optical, electrical, and chemical performance. In particular, alkali cation exchange has received significant attention throughout the years, primarily with respect to introducing compressive stresses into the surface layer, which increases mechanical durability (Gy, 2003; Karlsson et al., 2010a; Varshneya, 2010a,b). This specific subject has been developing into a large market, where ion exchange strengthened glasses are now used in displays, handheld electronic devices, pharmaceutical packaging, and many other areas. Monovalent cation exchange has also received much attention for tailoring the refractive index profile of the surface layer, i.e., so as to create microstructured planar or buried waveguides or optical lenses with graded refractive

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index (Ramaswamy and Srivastava, 1988; Opilski et al., 2000; Honkanen et al., 2006; Tervonen et al., 2011).

The ion-exchange process can be described as an interdiffusion reaction where the rate of reaction is described by Fick's laws of diffusion (Nordberg et al., 1964). While usually, the concentration gradient ($\partial c/\partial x$) is considered, the actual driving force for ionic transport is the gradient in chemical potential ($\partial \mu/\partial x$) between the different ionic media (Schaeffer, 2012) (which in many cases, correlates linearly with the gradient in chemical composition). The transport coefficient is usually concentration-dependent (Doremus, 1964),

$$\bar{D} = \frac{D_1 D_2}{N_1 D_1 + N_2 D_2},\tag{1}$$

where in a simplistic approximation, D_1 and D_2 are the coefficients of self-diffusion of contributing species 1 and 2, N_1 and N_2 are the corresponding relative atomic fractions, and \overline{D} is the effective diffusion coefficient.

In the present understanding of ion-exchange kinetics, the transport coefficient is governed by many different parameters, such as salt-bath composition (the diffusion reservoir), glass composition (the structure and free volume of the matrix), exchanging ion species (size and charge), temperature, pressure, etc. The glass composition has received much attention over the years and the specific components of alumina (Burggraaf, 1966), phosphate (Bartholomew and Garfinkel, 1980), and zirconia (Nordberg et al., 1964) have been shown to have beneficial effects on chemical strengthening through acting on free volume, oxygen packing density, and degree of cross-linking of the structural backbone. Transport properties and the relation to glass composition are mostly understood on the basis of conductivity/ diffusion paths across which the considered ions are transported, as originally proposed by Greaves (1985). The presence of such paths was later indicated by, e.g., AFM analyses by Frischat et al. (2004), see Figure 1. For each alkali charge that is added to the glass composition, one non-bridging oxygen (NBO) is created so that the network is depolymerized. The NBOs are negatively charged and are charge-compensated by the positively charged alkali ions. This is what leads to the postulated creation the mentioned paths of mobility. There are various models that aim to describe transport properties in glasses, including the strong electrolyte approach (Anderson and Stuart, 1954) or the weak electrolyte approach (Ravaine and Souquet, 1977). Despite their disadvantages (Martin and Angell, 1986), these models provide a decent understanding that by changing the glass composition (e.g., through introduction of Al₂O₃, B₂O₃, and/or P₂O₅), the number of NBOs is varied. This is discussed by Grandjean et al. (2007) and Smedskjaer et al. (2011) where the latter suggests that the alkali ions diffuse faster when acting as charge compensators to, e.g., Al3+ or B3+, as opposed to acting as a creator of NBO. The model then rationalizes attractive reactions among cation species and their effect on the overall activation energy. Major additional factors which then affect the transport properties (Bunde et al., 1996) include site mismatch, site relaxation (frequently called structural relaxation), interionic interaction, and the mixedmodifier effect (Maass et al., 1992; Karlsson et al., 2015; Poletto Rodrigues et al., 2016; Griebenow et al., 2017).

Industrially, the ion-exchange strengthening process is typically performed on rolled or drawn sheet glass by immersing the glass for a prolonged time into appropriate salt melts (Karlsson et al., 2010a). Employed glass compositions are typically chosen for high ion mobility and high conversion to compressive stress, e.g., alkali-aluminosilicates (Burggraaf and Cornelissen, 1964; Burggraaf, 1966; Ragoen et al., 2017), aluminoborosilicates (Morozumi et al., 2015), and, more recently, aluminophosphosilicates (Zeng et al., 2016). The salt composition is then selected from a trade-off between desired exchange species, high treatment temperature, low vapor pressure, target depth of layer and surface stress, and cost. In the present paper, we discuss trends in the effective diffusion coefficients when exchanging Na+ for various monovalent cations (K+, Cu+, Ag+, Rb+, and Cs+) in the surface

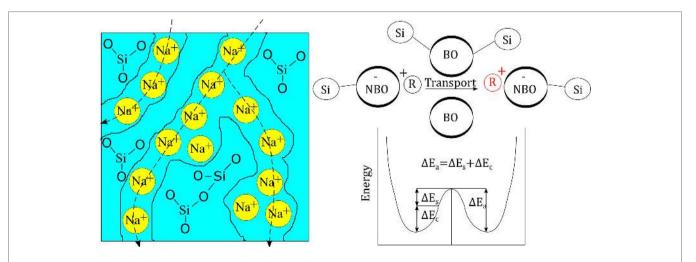


FIGURE 1 | (Left) Schematic view of the glass structure of soda silicate glass as originally proposed by Greaves (1985). (Right) Schematic view of the principle energy landscape for cationic transport (R+ denoting a monovalent cation), redrawn from Martin and Angell (1986). ΔE_s stands for network strain energy and ΔE_c for Coulomb energy (chemical binding energy).

of soda-lime-silicate (SLS) float glass. Knowing more about what affects the effective diffusion coefficients can potentially help to improve the diffusivity in chemically strengthened glasses or planar waveguides. For this, we reconsider previously published data (Karlsson et al., 2010b, 2012, 2013).

MATERIALS AND METHODS

Data used in this report are collected from studies which have previously been published by us (Karlsson et al., 2010b, 2012, 2013). For clarification, we provide a summarized overview of the experimental procedures. In all studies, the employed glass was a commercial SLS float glass (Pilkington Floatglas AB, Halmstad, Sweden), see the nominal composition in **Table 1**.

Other than in the regular immersion technique, for ion exchange, a different approach was used where the salt mixture was applied directly onto the float glass surface as a solid paste before melting and heat treatment. Experimental information on the salts and thermal treatments are summarized in **Table 2**. Salts were applied on the air-side of the glass and the ion exchange itself was performed over a time of 10 h, following the heating procedure to the target temperature, which took 1 h. Subsequent cooling was done at approximate rates of 2 K/min.

The resulting surface concentration profiles were measured by different techniques, UV-VIS spectrophotometry, atomic absorption spectroscopy (AAS), and energy dispersive spectroscopy in Scanning Electron Microscopy. Wet-chemical surface ablation (SAC) was employed before chemical analysis using UV-VIS and AAS. The surface ablation cell (SAC) technique was developed and tested in a round-robin project of Technical Committee 2 of the International Commission on Glass as an efficient tool for multielement determination of glass surface chemistry with scalable matrix dependence, see **Figure 2** (Sundberg et al., 2010). More details on the handling of the SAC and analytical procedures can be found in previous reports (Karlsson et al., 2010b, 2012; Sundberg et al., 2010; Karlsson, 2012). In this way, depth-resolved concentration data were obtained for the various species in the glass.

The effective diffusion coefficient \overline{D} (cm²/s) was then calculated using Eq. 2, frequently called Green's function, but really

TABLE 1 | Nominal chemical composition of the investigated float glass.

Oxides	SiO ₂	Na ₂ O	CaO	MgO	SO₃	Al_2O_3	Fe ₂ O ₃	K ₂ O	TiO ₂
wt%	72.5	13.7	9.12	4.14	0.247	0.13	0.103	0.04	0.01
mol%	71.0	13.0	9.57	6.05	0.182	0.08	0.038	0.03	0.01

TABLE 2 | Ion-exchange treatments.

lon	Salt	Salt mixture	Mass of salt(s) (g)	H ₂ O (g)	Temperatures °C
K+	KNO₃:KCI	I: 2:1 (wt ratio)	6	1.5	460, 480, 500, 520
K+	KNO₃:KCI	II: 1:2 (wt ratio)	6	1.5	460, 480, 500, 520
Cu+	CuCl	-	6	2	460, 480, 500, 520
Ag+	AgCl	-	5	2	460, 470, 480,
					500, 520
Rb+	RbCl:NaCl	53.75:46.25 mol%	6	1	530, 540
Cs+	CsCl:NaCl	65:35 mol%	6	1	520, 530

a fundamental solution of Fick's second law for a semi-infinite planar situation with finite diffusion reservoir, a starting surface concentration of 100% in an infinitely thin surface layer, and a starting matrix concentration of zero (Karlsson et al., 2010b).

$$C = \frac{A}{\sqrt{t}}e^{-x^2/4\bar{D}t},\tag{2}$$

The analyzed concentration (C) and the calculated depth (x) were plotted by $\ln(C)$ vs. x^2 , yielding the slope $k = (-4\bar{D}t)^{-1}$. This calculation is based on the mathematical assumption that the effective diffusion coefficient is independent of the concentration of diffusing ions and also independent of time. It is further mathematically assumed that the effective diffusion coefficient in the salt is equal to the effective diffusion coefficient in the glass, see **Figure 3** (Crank, 1975; Karlsson et al., 2010b).

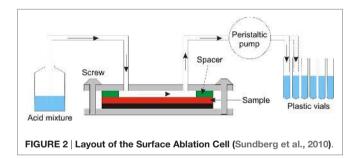
Calculations of the activation energy, E_a (kJ/mol), for ionic interdiffusion were made by use of the Arrhenius equation, Eq. 3. Plotting $\ln \bar{D}$ vs. T^{-1} gives the slope $k = -E_a/R$ and the intercept $m = \ln D_0$. This assumes that the activation energy is independent of temperature (Frischat, 1975).

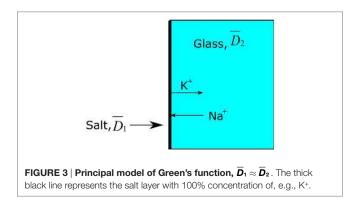
$$\bar{D} = D_0 e^{\left(\frac{-E_a}{RT}\right)},\tag{3}$$

The cation field strength (CFS) is calculated through Eq. 4 (Vogel, 1994), where the z is the charge of the cation and r is the effective ionic radius in ångström of the cation and anion as given by Dietzel (1942). The ionic radii data were taken from Shannon (1976).

$$CFS = \frac{z_{cat}}{\left(r_{cat} + r_{an}\right)^2} \tag{4}$$

The electronic cation polarizability (α) was calculated using the Lorentz–Lorenz relation (Eq. 5), and values of molar refractivity





(A) as calculated by Pauling (1927). N denotes the amount of polarizable ions normally assumed to be equal to Avogadro's number (N_A).

$$A = \frac{4\pi}{3}N\alpha\tag{5}$$

TRENDS IN EFFECTIVE DIFFUSION COEFFICIENTS

The employed approach provides a simplistic approximation of the practical diffusion rate, expressed through the effective diffusion coefficient according the Green's function. It has been shown before that the obtained values are in reasonable agreement with other published data (Pask and Parmelee, 1943; Shaisha and Cooper, 1981; Gonella et al., 1998; Liu and Pun, 2004; Karlsson et al., 2010b, 2012). In a practical consideration, the effective diffusion coefficient represents the efficiency of the ion-exchange reaction, in other words, the rate of the ion exchange. The effective diffusion coefficients are calculated from the concentration vs. depth profile data. In the present case, the penetration depths of K+ for the two salt mixtures on the air-side of float glass are exceeding or equal to 25-30 µm for all temperatures after 10 h of ion exchange (Karlsson et al., 2010b). The penetration depth is approximately 8-10 µm for Rb⁺ (Karlsson et al., 2012). In the periodic table, Rb is the next element in the group after potassium. Despite the considerably larger ionic radius, it is possible to perform ion exchange thermally with Rb⁺. Cs⁺ has an even larger ionic radius than Rb+, but still, also Cs+-Na+ ion exchange is possible. The corresponding penetration depth of Cs+ was found at approximately 5-7 μm. Compared to Rb+-Na+ ion exchange, much smaller concentrations of Cs₂O were found in the surface layers (Karlsson et al., 2012). The determined concentration vs. depth profiles of copper ion exchange revealed that the total copper concentration, expressed as mol% [Cu], is relatively high at the top surface layers, but decreases substantially in the top ~5 µm of the samples. Deeper in the sample, the slope of the concentration profile appears to change, indicating a change in the underlying transport mechanism. According to our previous interpretation (Karlsson et al., 2012), the shape of the diffusion profile suggests that for a depth of >5 μm, copper diffusion is unaffected by variations of the chemical composition. From it is indicated that in the range of 0 to \sim 5 µm, the profile is controlled by sodium outward-diffusion and whereas beyond ~5 μm, it is controlled by the movement of Cu+ species. The reason for this is that Na⁺ will eventually be depleted at the top surface whereas the opposite is the case for the interior (Karlsson et al., 2012). The copper ion exchanged air-sides were transparent and uncolored after the treatment. This indicates that no substantial amounts of Cu²⁺ or nanoparticles (Cu⁰ or Cu₂O) were formed and that most of the copper is incorporated as Cu⁺ ions in the glass (Karlsson et al., 2012) as compared to treatments on the tin-side (Karlsson et al., 2013). The diffusion of Ag+ in glass is known to be relatively high, confirmed by the data in **Table 3**. The penetration depth of Ag+ ion exchange ranges from 80-100 μm for samples treated at 460°C to 150–200 μm for samples treated at 520°C. The Ag⁺-Na⁺ ion exchanged samples were colored yellowish after treatment.

The corresponding profiles and discussions of ion exchange with noble metal ions can be found in Karlsson et al. (2010b, 2012). All effective diffusion coefficients from our previous work are summarized in **Table 3**. Note that these data are in good agreement with the data published by others, thus the below described trends should be regarded as general observations.

The diffusivities of the studied monovalent cations follow the order $Ag^+ > K^+ > Cu^+ > Rb^+ > Cs^+$. This is in accordance with the order of ionic radii for the alkali ions ($K^+ < Rb^+ < Cs^+$). However, an opposite pattern is found for the noble metal ions, where the ionic radii $Cu^+ < Ag^+$. This trend is evident in **Figure 4**, where ln \bar{D} is plotted vs. CFS. A similar trend is seen when plotting $\ln \bar{D}$ vs. ionic radii as the value of CFS is physically equivalent to the ionic radius when charge and anion species are of equivalent ionic radius. Several different values of the ionic radii were used for calculating CFS, depending on the coordination numbers (CN), see Table 4. When assuming CN6, K+, Rb+, Cs+, and Ag+ seem to follow a relatively linear relationship. However, for the commonly assumed CN2 of noble metal ions in silicate glass, this trend cannot be seen. CN for Cu⁺ are given in Kamiya et al. (1992), d'Acapito et al. (1997), Lee et al. (2000), Gonella et al. (2005), Arletti et al. (2006), Farges et al. (2006), Gliozzo et al. (2010), and Klysubun et al. (2011) and for Ag+ in Houde-Walter et al. (1993), Dubiel et al. (1997), Yang et al. (2003), and Yang and Dubiel (2007).

The coordination environment of different cations is complex. Na⁺ cations have been reported with a mean CN in the range of 4-6 (Greaves, 1981; Greaves et al., 1981; Vessal et al., 1992; Houde-Walter et al., 1993; Cormack and Du, 2001; Du and Cormack, 2004; Bernasconi et al., 2012; Kreski et al., 2012) in silicate glass, but also lower (Dubiel et al., 1997) or higher (McKeown et al., 1985; George and Stebbins, 1996; Weigel et al., 2008) values have been mentioned, depending on compositional changes. K+ cations have been reported to most likely have a CN of 8-10 (Jackson et al., 1987; Cormier et al., 2010; Kreski et al., 2012), but here as well, 4-6 have also been reported (Greaves et al., 1991; Kamijo et al., 1996), again depending on composition. Rb+ (Vessal et al., 1992) and Cs⁺ (Greaves et al., 1991) cations have been reported to have a CN of 5-6, apart from the study of Stefanovsky and Purans (2012) in nuclear waste glasses where Cs⁺ was found to have CNs of 6-12. Finally, similar versatility is found in literature for Li+, with CN of 3-4 (Uhlig et al., 1996; Zhao et al., 1998) and 3–6 (Xu and Stebbins, 1995). As can be seen in **Table 4**, the effects of the CN differences for the alkalis are not as strong as for the noble metal ions.

The Pauling electronegativity of the elements vs. $\ln \overline{D}$ does not give the same trend (Ag⁺ fitting-in with the alkali metal ions) as was the case for ionic radii and CFS, see **Figure 5**. It also does not give any further insight as to why Ag⁺ is faster diffusing than Cu⁺. The noble metal cations have considerably higher ionization energies than the alkalis and, thereby, higher electronegativity. Tabulated electronegativity values do not provide a reasonable answer to this, and one reason can be that the electronegativity may also change depending on the environment of the cation. The enthalpy of formation, $\Delta H_{\rm f}$, of the oxides, gives a decreasing exponential trend for the alkali down in the group and it does not fit with neither Cu₂O nor Ag₂O, see **Figure 6**. The Gibbs free energy of formation gives a similar trend as enthalpy of formation,

TABLE 3 | Overview of effective diffusion coefficients (cm²s⁻¹) of several monovalent cations in commercial float glass during 10 h of ion exchange (Karlsson et al., 2010b, 2012, 2013).

Temperatures °C	Ag ⁺	K+(I)	K+(II)	Cu+	Rb⁺	Cs+
540	_	_	_	_	1.4 (±0.1) 10 ⁻¹²	_
530	_	_	_	_	9.8 (±0.5) 10 ⁻¹³	5.0 (±0.3) 10 ⁻¹³
520	9.6 (±1.0) 10 ⁻¹⁰	6.1 (±0.3) 10 ⁻¹¹	6.0 (±0.3) 10 ⁻¹¹	3.4 (±0.2) 10 ⁻¹¹	_	4.8 (±0.2) 10 ⁻¹³
500	6.2 (±0.6) 10 ⁻¹⁰	3.2 (±0.2) 10 ⁻¹¹	3.5 (±0.2) 10 ⁻¹¹	2.3 (±0.1) 10 ⁻¹¹	_	_
480	4.3 (±0.4) 10 ^{-10a}	2.1 (±0.1) 10 ⁻¹¹	2.1 (±0.1) 10 ⁻¹¹	1.3 (±0.1) 10 ⁻¹¹	_	_
470	3.1 (±0.3) 10 ^{-10a}	_	_	_	_	_
460	2.8 (±0.3) 10 ⁻¹⁰	1.5 (±0.1) 10 ⁻¹¹	1.8 (±0.1) 10 ⁻¹¹	8.4 (±0.4) 10 ⁻¹²	_	_
Activation energy, Ea (kJ/mol)	105 (±21)	111 (±11)	100 (±10)	115 (±12)	_	-
Penetration depth at lowest temperature (µm)	80-100	25-30	25–30	20-25	8–10	5–7

⁽I), salt mixture KNO3:KCl2:1; (II), salt mixture KNO3:KCl1:2.

^aCalculated as an average of a double sample.

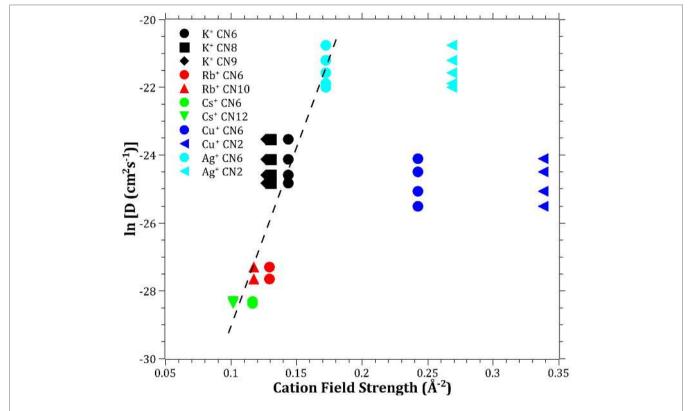


FIGURE 4 | Logarithm of the effective diffusion coefficient vs. cation field strength. Data calculated from ionic radii data (Shannon, 1976) according to Eq. 3 (Dietzel, 1942). The dashed line is a guide to the eye.

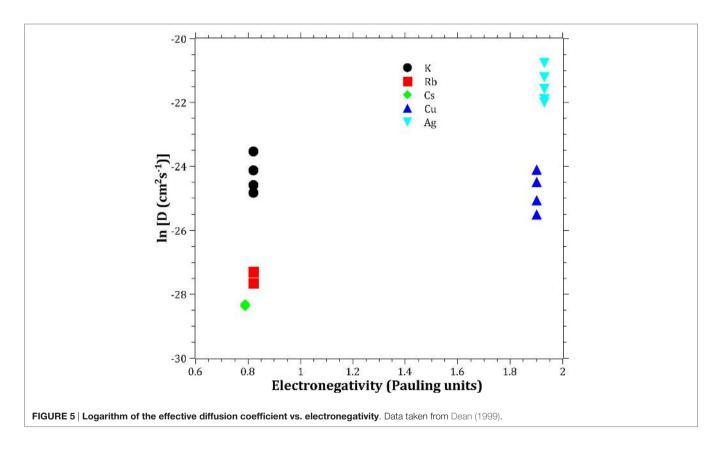
which is perfectly reasonable as it includes the enthalpy of formation. The dissociation energy of the bond to oxygen, on the other hand (**Figure 7**), gives a rather linear relationship between the alkali species and Ag-O. Cu-O has a considerably higher bond dissociation energy than the others, which perhaps offers the best explanation as to why Cu⁺ is diffusing slower than Ag⁺. The bond dissociation energy includes all oxide bonds in the cation coordination sphere, in contrast to single bond strengths that can be estimated from the bond dissociation energy divided by the coordination number (Varshneya, 2006). It shall be noted that the bond dissociation energy shows a minimum for K⁺ in the alkali series, see **Table 3**, indicating that K⁺ is efficient for ion-exchange strengthening. The electronic ionic polarizability is a measure of

the effect that surrounding atoms in the vitreous network has on the dipole moment or orbital structure of the mobile species that we are considering. It is not just important for the optical properties (Karlsson et al., 2016) but also important for transport properties as electric fields are constantly changing as the ions diffuses in the glass (Frischat, 1975). The logarithm of the effective diffusion coefficient as a function of the electronic ionic polarizability is given in **Figure 8**, where Cu⁺ fits into the trend with the alkali ions, while Ag⁺ with relatively high polarizability has an unusually high effective diffusion. High electronic ionic polarizability can be argued to be a positive property on the activation energy of the diffusion as the ions are deformable during the diffusion, a concept that is considered when choosing materials as solid electrolytes

TABLE 4 | Data collected for understanding trends in the effective diffusion coefficients, following a representation in Vogel (1994).

Element	Ionic radius (Å) (Shannon, 1976)		Cation field strength (Å ⁻²)	Electronegativity (Pauling units)	Enthalpy of formation (800 K), ΔH _f (kJ/mol)	Bond dissociation energy per MO _x (kJ/mol)	Estimated single bond strength (kJ/mol)	Electronic ionic polarizability (ų) (Pauling, 1927)	Aqueous ionic conductivity (S cm²/mol)
Li	0.59	4	0.292	0.98	-597.6	341 ± 6	85.3	0.029	38.69
Li	0.76	6	0.245	do	do	do	56.8	do	do
Li	0.92	8	0.210	do	do	do	42.6	do	do
Na	0.99	4	0.198	0.93	-414.2	257 ± 15	64.3	0.181	50.11
Na	1.02	6	0.192	do	do	do	42.8	do	do
Na	1.18	8	0.168	do	do	do	32.1	do	do
K	1.38	6	0.13	0.82	-367.4	239 ± 34	39.8	0.840	73.5
K	1.51	8	0.143	do	do	do	29.9	do	do
K	1.55	9	0.130	do	do	do	26.6	do	do
Rb	1.52	6	0.127	0.82	-315.9	255 ± 84	42.5	1.415	77.8
Rb	1.66	10	0.129	do	do	do	25.5	do	do
Cs	1.67	6	0.117	0.79	-301.2	297 ± 25	49.5	2.438	77.3
Cs	1.88	12	0.116	do	do	do	24.75	do	do
Cu	0.77	6	0.101	1.9	-165.3	343 ± 63	57.2	0.428	56.6 (Cu ²⁺)
Cu	0.46	2	0.243	do	do	do	171.5	do	do
Ag	1.15	6	0.338	1.93	-26.4	213 ± 84	35.5	1.717	61.9
Ag	0.67	2	0.172	do	do	do	106.5	do	do

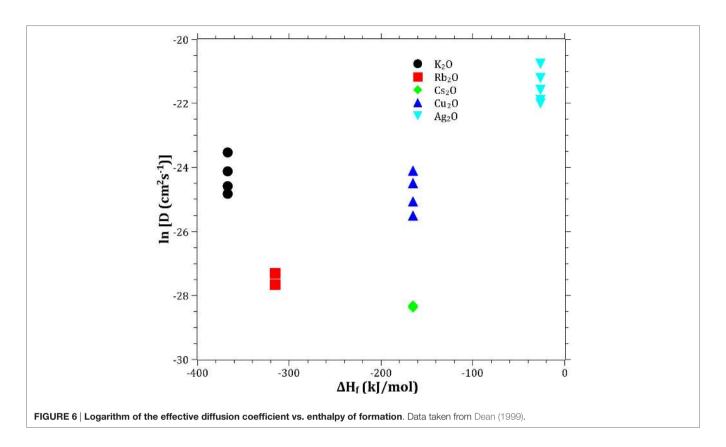
Data are taken from Dean (1999) unless otherwise stated.

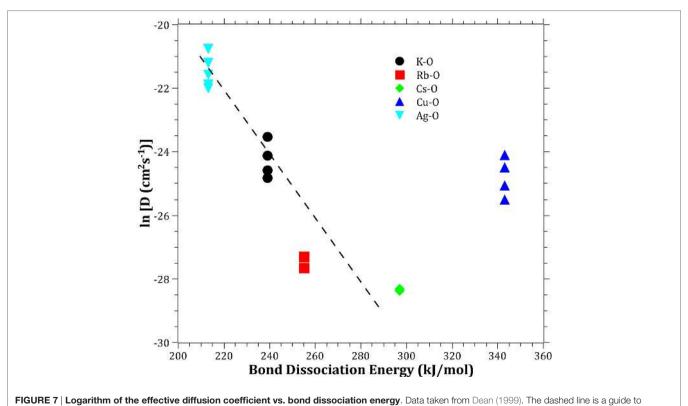


(Cao et al., 2014). As for comparison, the ionic conductivity in aqueous solution as a function of the logarithmic effective diffusion coefficient also gives a similar trend as for the bond dissociation energy (**Figure 9**). While data for Cu⁺ was not found in literature, the other species clearly follow the order Ag⁺ > K⁺ > Rb⁺ > Cs⁺. The simple reason for the lack of data on Cu⁺ is probably that it is difficult to stabilize Cu⁺ in aqueous solutions.

DISCUSSION

To understand and ultimately design glasses with increased mobility for chemically strengthening of glass, it is likely important to learn from the experiences in the field of solid electrolytes (Cao et al., 2014). The structural properties are of much importance, hence the following criteria should be





the eye.

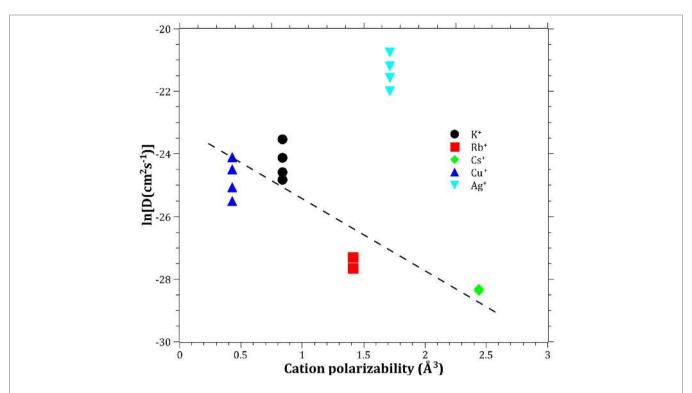


FIGURE 8 | Logarithm of the effective diffusion coefficient vs. electronic cation polarizability. Molar refraction data taken from Pauling (1927). The dashed line is a guide to the eye.

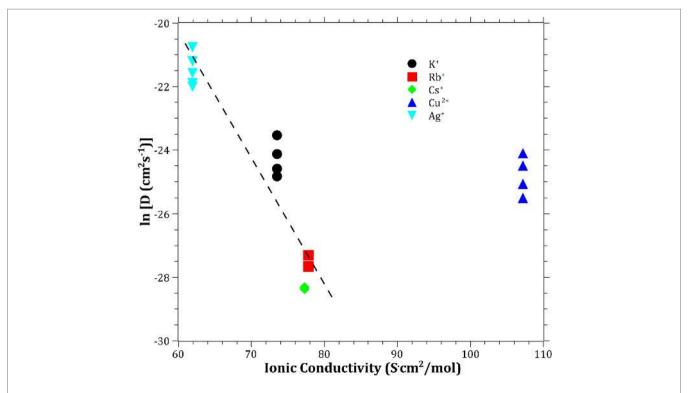


FIGURE 9 | Logarithm of the effective diffusion coefficient vs. aqueous ionic conductivity. Data taken from Dean (1999). The dashed line is a guide to the eye.

considered: (i) large enough structural transport channels (c.f. Figure 1), (ii) disordered mobile ion sub-lattice, (iii) highly polarizable mobile ions and anion sub-lattices, and (iv) size of the ions in the vitreous network. The effective diffusion coefficients will always be a complex trade-off between different properties; however, in the current paper, we have found a correlation using bond dissociation energy and electronic cation polarizability. The unusually high effective diffusion coefficient of Ag⁺ as compared to Cu⁺ can at least partly be explained by Ag+ having a comparable bond dissociation energy and a high cation polarizability, while Cu⁺ have a high bond dissociation energy and a comparable cation polarizability. This indicates that the breakage of bonds and structural deformability are keys to improving the ion-exchange rate. By identifying the key properties, it will give the possibility for modeling the diffusion by topological, atomistic, or quantum mechanics modeling (Mauro et al., 2016). One should bear in mind that the mobile cations are only one component in the creations of bonds and polarizability in the vitreous network. The anions, most often consisting of oxygen, can also be exchanged for other anions (Wondraczek et al., 2011), such as nitrogen (Becher et al., 2011; Ali et al., 2015) or carbon (Renlund et al., 1991). The understanding that the bond dissociation energy and the polarizability can be correlated to the effective diffusion coefficient also provides a perspective how ionic diffusion and ion-exchange strengthening behave in different types of glasses, including, e.g., chalcogenide or chalcohalide glasses (Calvez et al., 2009). Furthermore, it provides the insight that the alkali ions bond less strongly when charge compensating Al3+, B3+, or P5+ than when creating NBO, i.e., likely a significant difference in the type of bonding, in accordance with (Smedskjaer et al., 2011).

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CONCLUDING REMARKS

The effective diffusivities of the studied monovalent cations follow the order $Ag^+ > K^+ > Cu^+ > Rb^+ > Cs^+$. This is in accordance with the order of ionic radii for the alkali ions ($K^+ < Rb^+ < Cs^+$). However, an opposite pattern is found for the noble metal ions, where the ionic radii $Cu^+ < Ag^+$. The Cu^+ cation behaves with respect to its small ionic radius peculiar compared to the other ions. The bond dissociation energy offers the best explanation as to why Cu⁺ is slower than Ag⁺. The polarizability of ions adds another dimension by offering increased structural deformability, which can be a route to enhance the ionic transport. A better understanding of ionic diffusion in glass can give rise to stronger and less expensive chemically strengthened glasses, using adapted combinations of diffusing species. Correlations between bond dissociation energies and polarizability provide an understanding of how different anions in glass affect effective diffusion coefficients and how ionic diffusion in different types of glasses may be tailored.

AUTHOR CONTRIBUTIONS

SK and LW perceived the idea of the paper. SK wrote the draft of the manuscript. All authors were involved in the discussions and elaborating the manuscript text.

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Conflict of Interest Statement: The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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