UNCERTAINTIES IN THE *vp*-PROCESS: SUPERNOVA DYNAMICS VERSUS NUCLEAR PHYSICS

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ABSTRACT

We examine how the uncertainties involved in supernova dynamics, as well as in nuclear data inputs, affect the νp -process in the neutrino-driven winds. For the supernova dynamics, we find that the wind termination by the preceding dense ejecta shell, as well as the electron fraction ($Y_{\rm e,3}$; at 3×10^9 K), plays a crucial role. A wind termination within the temperature range of $(1.5-3)\times 10^9$ K greatly enhances the efficiency of the νp -process. This implies that the early wind phase, when the innermost layer of the preceding supernova ejecta is still $\sim 200-1000$ km from the center, is most relevant to the νp -process. The outflows with $Y_{\rm e,3}=0.52-0.60$ result in the production of the p-nuclei up to A=108 with interesting amounts. Furthermore, the p-nuclei up to A=152 can be produced if $Y_{\rm e,3}=0.65$ is achieved. For the nuclear data inputs, we test the sensitivity to the rates relevant to the breakout from the p-p chain region (A<12), to the (n, p) rates on heavy nuclei, and to the nuclear masses along the νp -process pathway. We find that a small variation of the rates of triple- α and of the (n, p) reaction on 56 Ni leads to a substantial change in the p-nuclei production. We also find that 96 Pd (N=50) on the νp -process path plays a role as a second seed nucleus for the production of heavier p-nuclei. The uncertainty in the nuclear mass of 82 Zr can lead to a factor of two reduction in the abundance of the p-isotope 84 Sr.

Key words: nuclear reactions, nucleosynthesis, abundances – stars: abundances – stars: neutron – supernovae: general

Online-only material: color figures

1. INTRODUCTION

The astrophysical origin of the proton-rich isotopes of heavy elements (p-nuclei) is not fully understood. The most successful model to date, the photodissociation of pre-existing neutron-rich isotopes (γ -process) in the oxygen–neon layer of core-collapse supernovae (or in their pre-collapse stages), cannot explain the production of some light p-nuclei including ^{92,94}Mo and ^{96,98}Ru (Woosley & Howard 1978; Prantzos et al. 1990; Rayet et al. 1995; Rauscher et al. 2002; Hayakawa et al. 2008). The recent discovery of a new nucleosynthetic process, the vp-process, has dramatically changed this difficult situation (Fröhlich et al. 2006a, 2006b; Pruet et al. 2006; Wanajo 2006). In the early neutrino-driven winds of core-collapse supernovae, $\bar{\nu}_{e}$ capture on free protons gives rise to a tiny amount of free neutrons in the proton-rich matter. These neutrons induce the (n, p) reactions on the β^+ -waiting point nuclei along the classical rp-process path (⁶⁴Ge, ⁶⁸Se, and ⁷²Kr), which bypass these nuclei (with the β^+ -decay half-lives of 1.06 minutes, 35.5 s, and 17.1 s, respectively). Wanajo (2006) has shown that the p-nuclei up to $A \sim 110$, including 92,94 Mo and 96,98 Ru, can be produced by the νp -process in the neutrino-driven winds within reasonable ranges of the model parameters.

All the recent hydrodynamic studies of core-collapse supernovae with neutrino transport taken into account suggest that the bulk of early supernova ejecta is proton rich (Janka et al. 2003; Liebendörfer et al. 2003; Buras et al. 2006; Kitaura et al. 2006; Fischer et al. 2010; Hüdepohl et al. 2010). This supports the νp -process taking place in the neutrino-driven winds of core-collapse supernovae. However, different works end up with somewhat different outcomes. Fröhlich et al. (2006a) showed that the p-nuclei up to $A \sim 80$ were produced with the one-dimensional, artificially induced explosion model of a $20\,M_\odot$

star, while Pruet et al. (2006) obtained up to $A \sim 100$ with the two-dimensional, artificially induced explosion model of a 15 M_{\odot} star. In contrast, Wanajo et al. (2009; also S. Wanajo et al. 2011, in preparation) found negligible contribution of the νp -process to the production of p-nuclei with the one-dimensional, self-consistently exploding model of a 9 M_{\odot} star (electron-capture supernova; Kitaura et al. 2006; Hüdepohl et al. 2010). These diverse outcomes indicate that the νp -process is highly sensitive to the physical conditions of neutrino-driven winds.

Besides the supernova conditions, there could also be uncertainties in some key nuclear rates, in particular of (n, p) reactions, because no attention was paid to neutron-capture reactions on proton-rich nuclei before the discovery of the νp -process. Uncertainties in some reactions relevant to the breakout from the p-p chain region (A < 12), which affect the proton-to-seed ratio at the onset of νp -processing, might also influence the nucleosynthetic outcomes. There are still a number of isotopes without experimental nuclear masses on the νp -process pathway (Weber et al. 2008).

Our goal in this paper is to examine how the variations of supernova conditions, as well as of nuclear data inputs, influence the global trend of the νp -process. This paper is organized as follows. In Section 2, a basic picture of the νp -process is outlined. A semi-analytic neutrino-driven wind model and an up-to-date reaction network code are described, which are used in this study (Section 3). We take the wind-termination radius (or temperature), the neutrino luminosity, the neutron-star mass, and the electron fraction as the key parameters of supernova conditions (Section 4). In previous studies (Fröhlich et al. 2006a, 2006b; Pruet et al. 2006; Wanajo 2006), some of these parameters were varied to test their sensitivities, but only for limited cases. In particular, the effect of wind termination

has not been discussed at all in previous studies. As the key nuclear reactions, we take triple- α , $^7\mathrm{Be}(\alpha,\gamma)^{11}\mathrm{C}$, $^{10}\mathrm{B}(\alpha,p)^{13}\mathrm{C}$ (all relevant to the breakout from the p-p chain region), and the (n,p) reactions on $^{56}\mathrm{Ni}$, $^{60}\mathrm{Zn}$, and $^{64}\mathrm{Ge}$ (Section 5). Sensitivities of the masses of the nuclei along the νp -process path are also discussed. We then discuss the possible role of the νp -process as the astrophysical origin of the p-nuclei (Section 6). A summary of our results follows in Section 7.

2. BASIC PICTURE OF THE vp-PROCESS

The "vp-process" was first identified in Fröhlich et al. (2006a), and the term was introduced by Fröhlich et al. (2006b) and is synonymous with the "neutrino-induced rp-process" in the subsequent works (Pruet et al. 2006; Wanajo 2006). This is a similar process to the *classical* rp-process first proposed by Wallace & Woosley (1981). The νp -process is, however, essentially a new nucleosynthetic process exhibiting a number of different aspects compared with the classical rp-process. The *vp*-process starts with the seed nucleus ⁵⁶Ni (not ⁶⁴Ge, the first β^+ -waiting-point nucleus in the classical rp-process pathway), assembled from free nucleons in nuclear quasi-equilibrium (QSE) during the initial high-temperature phase ($T_9 > 4$; where T_9 is the temperature in units of 10^9 K). The νp -process is therefore a *primary* process, which needs no pre-existing seeds. When the temperature decreases below $T_9 = 3$ (defined as the onset of a vp-process in this study) and QSE freezes out, the *vp*-process starts.

Neutrino capture on free protons, $p(\bar{\nu}_e, e^+)n$, in a proton-rich neutrino-driven wind gives rise to a tiny amount of free neutrons $(10^{-11}$ to 10^{-12} in mass fraction). These neutrons immediately induce the exchange reaction, (n, p), and in part radiative neutron capture, (n, γ) , on the seed nucleus ⁵⁶Ni and subsequent heavier nuclei with decay timescales of a few milliseconds, well below the expansion timescale of the wind and well below the β^+ -decay lifetimes of these nuclei. The nuclear flow proceeds with combination of radiative proton captures, (p, γ) , and neutron captures, the latter replacing the role of β^+ -decays in the classical rp-process.

A large number of free protons relative to that of 56 Ni at $T_9=3$, which allows for neutron capture on the seed nuclei, are required to initiate the νp -process. High entropy and short expansion timescale of the ejecta make the triple- α process, bridging from light (A<12) to heavy ($A\geqslant12$) nuclei, less effective and help to leave a large number of free protons at the onset of the νp -process. It should be noted, however, that proton-rich matter freezing out from nuclear statistical equilibrium (NSE) mainly consists of 56 Ni and free protons (Seitenzahl et al. 2008). This is a fundamental difference from a (moderately) neutron-rich NSE, where no free neutrons exist at freezeout. This makes the requirements for entropy and expansion timescale less crucial, compared with the case of r-process, allowing for the νp -process taking place with typical wind conditions (Fröhlich et al. 2006a; Pruet et al. 2006; Wanajo 2006).

Unlike the *r*-process, the νp -process is not terminated by the exhaustion of free protons, but by the temperature decrease below $T_9 = 1.5$ (defined as the end of a νp -process), where proton capture slows due to the Coulomb barrier. The end of νp -processing is thus a proton-rich freezeout. For this reason, the proton-to-seed ratio, Y_p/Y_h (the number per nucleon for free protons divided by that for nuclei with Z > 2) at $T_9 = 3$ does not necessary serve as a useful guide for the strength of the νp -process as the neutron-to-seed ratios are in the case of the

r-process. Rather, the number ratio of free neutrons created by $p(\bar{\nu}_e, e^+)n$ (for $T_9 \leq 3$) relative to the seed nuclei (at $T_9 = 3$), Δ_n , can be a useful (but still crude) measure for the νp -process as proposed by Pruet et al. (2006). Note that each neutron capture by (n, p) is immediately followed by one or two radiative proton captures, increasing the atomic masses by one or two units. Similar to Equation (2) in Pruet et al. (2006), we define

$$\Delta_{\rm n} = \frac{Y_{\rm p} n_{\bar{\nu}_{\rm e}}}{Y_{\rm h}},\tag{1}$$

where $Y_{\rm p}$ (equal to the mass fraction of free protons, $X_{\rm p}$) and $Y_{\rm h}$ are the values at $T_9=3$. The net number of $\bar{\nu}_{\rm e}$ captured per free proton for $T_9\leqslant 3$, $n_{\bar{\nu}_{\rm e}}$, is defined as

$$n_{\bar{\nu}_{\rm e}} = \int_{T_0 \leqslant 3} \lambda_{\bar{\nu}_{\rm e}} \, dt,\tag{2}$$

where $\lambda_{\bar{\nu}_e}$ is the rate for $p(\bar{\nu}_e, e^+)n$. The seed, a double magic nucleus ⁵⁶Ni, remains the most abundant heavy nucleus throughout the νp -process. Therefore, only a fraction of ⁵⁶Ni is consumed for the production of heavier nuclei. For this reason, $\Delta_n \sim 10$ is enough for the production of nuclei with $A \sim 100$ –110, as we will see in the subsequent sections.

The νp -process flow passes through the even—even nuclei up to $Z=N\sim 40$ and gradually deviates toward the Z< N region. As the flow proceeds toward higher Z nuclei, and as the temperature decreases, (n,γ) competes with (n,p). When Δ_n is large enough, the flow eventually approaches the β -stability line and even crosses into the neutron-rich region. The latter happens when the net number of $\bar{\nu}_e$ captured per free proton after the νp -process, defined as

$$n'_{\bar{\nu}_{\rm e}} = \int_{T_9 \leqslant 1.5} \lambda_{\bar{\nu}_{\rm e}} \, dt,\tag{3}$$

is not negligible compared to $n_{\bar{\nu}_e}$. The end point of the νp -process is thus determined by the supernova dynamics, which enters into Equation (3) through $\lambda_{\bar{\nu}_e} \propto r^{-2}$ (r is the radius from the center), rather than by the nature of nuclear physics as in case of the classical rp-process.

3. NEUTRINO-DRIVEN WIND MODEL AND REACTION NETWORK

The thermodynamic trajectories of neutrino-driven outflows are obtained using a semi-analytic, spherically symmetric, general relativistic model of neutrino-driven winds. This model has been developed in previous r-process (Wanajo et al. 2001; Wanajo 2007) and νp -process (Wanajo 2006) studies. Here, we describe several modifications added to the previous version.

The equation of state for ions (ideal gas) and arbitrarily degenerate, arbitrarily relativistic electrons, and positrons is taken from Timmes & Swesty (2000). The rms-averaged energies of neutrinos are taken to be 12, 14, and 14 MeV, for electrons, anti-electrons, and the other types of neutrinos, respectively, in light of a recent self-consistently exploding model of a 9 M_{\odot} star (Kitaura et al. 2006; Hüdepohl et al. 2010; Müller et al. 2010). These values are consistent with other recent studies for more massive progenitors (Fischer et al. 2010), but substantially smaller than those taken in previous works (e.g., 12, 22, and 34 MeV in Wanajo et al. 2001). The mass ejection rate \dot{M} at the neutrino sphere is determined such that the outflow becomes supersonic (i.e., wind) through the sonic point.

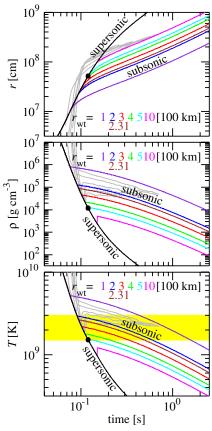


Figure 1. Radius (top), density (middle), and temperature (bottom) as a function of time (set to zero at the neutrino sphere) for $M_{\rm ns}=1.4\,M_{\odot}$ and $L_{\nu}=1\times10^{52}\,{\rm erg\,s^{-1}}$. Subsonic outflows after wind termination at $r_{\rm wt}=100,\,200,\,231,\,300,\,400,\,500,\,{\rm and}\,1000\,{\rm km}$ are color coded. The black line shows the supersonic outflow without wind termination. In each panel, a filled circle marks the sonic point. The yellow band in the bottom panel indicates the temperature range ($T_9=1.5-3$) relevant to the νp -process. The wind trajectories from hydrodynamical results by Buras et al. (2006, gray lines), used in Pruet et al. (2006), are compared with our models.

The neutron star mass $M_{\rm ns}$ is taken to be 1.4 M_{\odot} for our standard model. The radius of the neutrino sphere is assumed to be $R_{\nu}(L_{\nu}) = (R_{\nu 0} - R_{\nu 1})(L_{\nu}/L_{\nu 0}) + R_{\nu 1}$ as a function of the neutrino luminosity L_{ν} (taken to be the same for all the flavors), where $R_{\nu 0} = 30\,{\rm km}$, $R_{\nu 1} = 10\,{\rm km}$, and $L_{\nu 0} = 10^{52.6} = 3.98 \times 10^{52}\,{\rm erg~s^{-1}}$. This roughly mimics the evolution of R_{ν} in recent hydrodynamic simulations (e.g., Buras et al. 2006; Arcones et al. 2007). The wind solution is obtained with $L_{\nu} = 1 \times 10^{52}\,{\rm erg~s^{-1}}$ ($R_{\nu} = 12.5\,{\rm km}$) for the standard model. The time variations of radius r from the center, density ρ , and temperature T for the standard model are shown in Figure 1 (black line).

The time variations of r, ρ , and T after the wind termination by the preceding supernova ejecta are calculated as follows. This phase is governed by the evolution of the preceding slowly outgoing ejecta, independent of the wind solution. In light of recent hydrodynamical calculations (e.g., Arcones et al. 2007), we assume the time evolution of the outgoing ejecta to be $\rho \propto t^{-2}$ and $T \propto t^{-2/3}$, where t is the post-bounce time. With these relations, we have

$$\rho(t) = \rho_{\rm wt} \left(\frac{t}{t_{\rm wt}}\right)^{-2},\tag{4}$$

$$T(t) = T_{\rm wt} \left(\frac{t}{t_{\rm wt}}\right)^{-\frac{2}{3}},\tag{5}$$

$$r(t) = r_{\text{wt}} \left[1 - \frac{u_{\text{wt}} t_{\text{wt}}}{r_{\text{wt}}} + \frac{u_{\text{wt}} t_{\text{wt}}}{r_{\text{wt}}} \left(\frac{t}{t_{\text{wt}}} \right)^3 \right]^{\frac{1}{3}}, \tag{6}$$

$$u(t) = u_{\text{wt}} \left[1 - \frac{u_{\text{wt}} t_{\text{wt}}}{r_{\text{wt}}} + \frac{u_{\text{wt}} t_{\text{wt}}}{r_{\text{wt}}} \left(\frac{t}{t_{\text{wt}}} \right)^3 \right]^{-\frac{2}{3}} \left(\frac{t}{t_{\text{wt}}} \right)^2, \quad (7)$$

for $t > t_{\rm wt}$, where $t_{\rm wt}$, $u_{\rm wt}$, $r_{\rm wt}$, $\rho_{\rm wt}$, and $T_{\rm wt}$ are the time, velocity, radius, density, and temperature, respectively, just after the wind termination. Equation (7) represents the time variation of velocity after the wind termination. In case $r_{\rm wt}$ is larger than that at the sonic point, r_s , the Rankine-Hugoniot shock-jump conditions are applied at $r_{\rm wt}$ to obtain $u_{\rm wt}$, $\rho_{\rm wt}$, and $T_{\rm wt}$ (see, e.g., Arcones et al. 2007; Kuroda et al. 2008). Equations (6) and (7) are obtained from Equation (4) with the steady-state condition, i.e., $r^2 \rho u$ =constant (see Panov & Janka 2009). Note that Equations (6) and (7) give $r(t) \propto t$ and u(t) = constant for $t \gg t_{\rm wt}$. In order to obtain t in Equations (4)–(7) for a given trajectory with L_{ν} , the time evolution of L_{ν} at the neutrino sphere is assumed to be $[L_{\nu}(t)]_{r=R_{\nu}} = L_{\nu 0}(t/t_0)^{-1}$, where $t > t_0 = 0.2$ s (Wanajo 2006). With this relation, the postbounce time is determined to be $t = (L_{\nu 0}/L_{\nu})t_0 + t_{loc}$, where t_{loc} is the local time in each wind trajectory ($t_{loc} = 0$ at the neutrino sphere). The curves for various $r_{\rm wt}$ as a function of $t_{\rm loc}$ obtained from Equations (4)–(6) are shown in Figure 1.

The wind trajectories from a hydrodynamical result by Buras et al. (2006, ~ 0.7 –1.3 s after bounce, gray lines), used in Pruet et al. (2006), are compared with our models. Their wind trajectories were obtained by mapping the two-dimensional model of an exploding 15 M_{\odot} star to a one-dimensional grid at \sim 0.5 s after bounce. In Figure 1, the time coordinate for each trajectory is shifted to roughly match one of our models. We find that their model also exhibits a wind termination at $r \sim 500$ –1000 km. The temperature and density histories are, however, close to our models with $r_{\rm wt} = 100$ –230 km. This is due to their higher neutrino luminosity (\sim 2 × 10⁵² erg s⁻¹) during the relevant core-bounce time, a factor of two higher than assumed in our models shown in Figure 1. This leads to a larger radius for a given wind temperature (see Section 4.2 and Table 1).

The nucleosynthetic abundances in the neutrino-driven outflows are calculated in a post-processing step by solving an extensive nuclear reaction network code. The network consists of 6300 species between the proton- and neutron-drip lines predicted by the recent fully microscopic mass formula (HFB-9; Goriely et al. 2005), all the way from single neutrons and protons up to the Z=110 isotopes. All relevant reactions, i.e., (n,γ) , (p,γ) , (α,γ) , (p,n), (α,n) , (α,p) , and their inverses are included. The experimental data, whenever available, and the theoretical predictions for light nuclei (Z<10) are taken from the REACLIB⁴ compilation. All the other reaction rates are taken from the Hauser–Feshbach rates of BRUSLIB⁵ (Aikawa et al. 2005) making use of experimental masses (Audi et al. 2003)

⁴ http://nucastro.org/reaclib.html

http://www.astro.ulb.ac.be/pmwiki/Brusslib/HomePage

Table 1
Results for Various Wind Models

$M_{\rm ns}$	$\log L_{v}$	$r_{ m wt}$	$Y_{e,9}^{a}$	\dot{M}	\boldsymbol{S}	$\tau_1^{\ b}$	$\tau_2^{\ c}$	$T_{\mathrm{wt,9}}^{\mathrm{d}}$	$Y_{e,3}^{e}$	$Y_{\rm p}/Y_{\rm h}^{\rm f}$	$n_{ar{ u}_{ m e}}$	Δ_n	$\log f_{\max}^{\ \mathrm{g}}$	$nuc(f_{max})^h$	$nuc(A_{max})^i$	Fig.
(M_{\odot})	(erg s ⁻¹)	(100 km)		$(10^{-4}M_\odot)$	$(k_{\rm B})$	(ms)	(ms)									
1.4	52.0	3.00	0.600	2.70	57.0	17.5	245	2.19	0.550	124	0.0834	10.3	7.16	⁹⁶ Ru	¹⁰⁶ Cd	All
1.4	52.0	1.00	0.600	2.70	57.0	359	1160	5.19	0.509	1.78	0.135	0.240	4.44	64 Zn	⁷⁴ Se	2
1.4	52.0	2.00	0.600	2.70	57.0	17.5	516	2.95	0.550	124	0.138	17.1	6.27	$^{78}\mathrm{Kr}$	⁸⁴ Sr	2
1.4	52.0	2.31	0.600	2.70	57.0	17.5	403	2.65	0.550	124	0.114	14.1	7.67	¹⁰⁶ Cd	¹⁰⁸ Cd	2
1.4	52.0	3.00	0.600	2.70	57.0	17.5	245	2.19	0.550	124	0.0834	10.3	7.16	⁹⁶ Ru	¹⁰⁶ Cd	2
1.4	52.0	4.00	0.600	2.70	57.0	17.5	117	1.80	0.550	124	0.0628	7.79	6.86	84 Sr	¹⁰² Pd	2
1.4	52.0	5.00	0.600	2.70	57.0	17.5	44.0	1.55	0.550	124	0.0529	6.56	6.69	84 Sr	⁸⁴ Sr	2
1.4	52.0	10.0	0.600	2.70	57.0	17.5	30.0	1.21	0.550	124	0.0431	5.34	6.13	$^{78}\mathrm{Kr}$	⁸⁴ Sr	2
1.4	52.0	∞	0.600	2.70	57.0	17.5	30.0		0.550	124	0.0323	4.01	5.79	⁷⁸ Kr	⁸⁴ Sr	2
1.4	52.4	8.01	0.600	31.3	33.7	22.8	261	2.19	0.558	42.7	0.0611	2.61	6.00	$^{78}\mathrm{Kr}$	⁸⁴ Sr	3
1.4	52.2	4.29	0.600	8.66	44.7	18.9	236	2.19	0.554	78.3	0.0720	5.64	6.83	⁸⁴ Sr	⁹⁶ Ru	3
1.4	52.0	3.00	0.600	2.70	57.0	17.5	245	2.19	0.550	124	0.0834	10.3	7.16	⁹⁶ Ru	¹⁰⁶ Cd	3
1.4	51.8	2.22	0.600	0.921	70.1	17.8	262	2.19	0.545	166	0.0945	15.7	7.78	¹⁰² Pd	¹⁰⁸ Cd	3
1.4	51.6	1.71	0.600	0.339	83.3	19.9	301	2.19	0.540	185	0.107	19.8	7.99	¹⁰⁶ Cd	¹⁰⁸ Cd	3
1.4	51.4	1.37	0.600	0.131	96.3	24.4	371	2.19	0.535	174	0.121	21.1	8.07	¹⁰⁶ Cd	¹⁰⁸ Cd	3
1.2	52.0	3.27	0.600	3.96	46.8	18.4	241	2.19	0.553	84.4	0.0746	6.30	6.96	84 Sr	¹⁰² Pd	4
1.4	52.0	3.00	0.600	2.70	57.0	17.5	245	2.19	0.550	124	0.0834	10.3	7.16	⁹⁶ Ru	¹⁰⁶ Cd	4
1.6	52.0	2.80	0.600	1.94	68.1	16.4	244	2.19	0.547	178	0.0908	16.2	7.69	¹⁰² Pd	¹⁰⁸ Cd	4
1.8	52.0	2.62	0.600	1.46	80.0	15.4	245	2.19	0.545	243	0.0980	23.8	7.91	¹⁰⁶ Cd	¹⁰⁸ Cd	4
2.0	52.0	2.46	0.600	1.13	93.0	14.4	247	2.19	0.543	335	0.104	34.8	8.12	¹⁰⁸ Cd	¹⁰⁸ Cd	4
1.4	52.0	3.00	0.550	2.70	57.0	17.5	245	2.19	0.523	42.9	0.0834	3.58	6.25	$^{78}\mathrm{Kr}$	84 Sr	5
1.4	52.0	3.00	0.600	2.70	57.0	17.5	245	2.19	0.550	124	0.0834	10.3	7.16	⁹⁶ Ru	¹⁰⁶ Cd	5
1.4	52.0	3.00	0.650	2.70	57.0	17.5	245	2.19	0.576	245	0.0834	20.4	8.14	106 Cd	108 Cd	5
1.4	52.0	3.00	0.700	2.70	57.0	17.5	245	2.19	0.603	428	0.0834	35.7	8.34	¹⁰⁸ Cd	¹²⁰ Te	5
1.4	52.0	3.00	0.750	2.70	57.0	17.5	245	2.19	0.629	703	0.0834	58.6	8.54	¹³⁸ La	¹³⁸ La	5
1.4	52.0	3.00	0.800	2.70	57.0	17.5	245	2.19	0.655	1130	0.0834	94.2	8.37	¹³⁸ La	152 Gd	5

Notes.

whenever available or the HFB-9 mass predictions (Goriely et al. 2005) otherwise. The photodisintegration rates are deduced from the reverse rates applying the reciprocity theorem with the nuclear masses considered.

The β -decay rates are taken from the gross theory predictions (GT2; Tachibana et al. 1990) obtained with the HFB-9 predictions (T. Tachibana 2005, private communication). Electron-capture reactions on free nucleons and on heavy nuclei (Fuller et al. 1982; Langanke & Martinez-Pinedo 2001) as well as rates for neutrino capture on free nucleons and ⁴He and for neutrino spallation of free nucleons from ⁴He (Woosley et al. 1990; McLaughlin et al. 1996) are also included. Neutrino-induced reactions of heavy nuclei are not taken into account in this study, which are expected to make only minor effects in this study.

Each nucleosynthesis calculation is initiated when the temperature decreases to $T_9 = 9$, at which only free nucleons exist. The initial compositions are then given by the electron fraction $Y_{\rm e,9}$ (proton-to-baryon ratio) at $T_9 = 9$, such as $Y_{\rm e,9}$ and $1 - Y_{\rm e,9}$ for the mass fractions of free protons and neutrons, respectively.

4. UNCERTAINTIES IN SUPERNOVA DYNAMICS

In the following subsections, we examine how the nucleosynthesis of the νp -process is influenced by varying the

wind-termination radius $r_{\rm wt}$ (or temperature; Section 4.1), L_{ν} (Section 4.2), $M_{\rm ns}$ (Section 4.3), and $Y_{\rm e,9}$ (Section 4.4) from their fiducial values 300 km (or 2.19×10^9 K), 1×10^{52} erg s⁻¹, $1.4~M_{\odot}$, and 0.600, respectively, of our standard model (first line in Table 1). These values are taken as those expected in the early wind phase of core-collapse supernovae. All the explored models and their major outcomes are summarized in Table 1 (the first four columns represent the input parameters).

4.1. Wind-termination Radius

Recent hydrodynamic studies of core-collapse supernovae have shown that the neutrino-driven outflows develop to be supersonic, which abruptly decelerate by the reverse shock from the outer layers (e.g., Janka & Müller 1995, 1996; Burrows et al. 1995; Buras et al. 2006). Arcones et al. (2007) have explored the effects of the reverse shock on the properties of neutrino-driven winds by one-dimensional, long-term hydrodynamic simulations of core-collapse supernovae. Their result shows that, in all of their models ($10-25\,M_{\odot}$ progenitors), the outflows become supersonic and form the termination shock when colliding with the slower preceding supernova ejecta. This condition continues until the end of their computations ($10\,\mathrm{s}$ after core bounce) in all of their "standard" models with reasonable parameter choices.

^a $Y_{\rm e}$ at $T_9 = 9$.

^b Time elapsed from $T_9 = 6$ to $T_9 = 3$.

^c Time elapsed from $T_9 = 3$ to $T_9 = 1.5$.

^d Temperature (in units of 10⁹ K) just after the wind termination.

e Y_{e} at $T_{9} = 3$.

f Proton-to-seed ratio at $T_9 = 3$.

g Maximum production factor.

h Nuclide at $f = f_{\text{max}}$.

ⁱ Nuclide at the largest A with $f > f_{\text{max}}/10$.

A recent self-consistently exploding model of a 9 M_{\odot} star also shows qualitatively the same result (Hüdepohl et al. 2010).

In this subsection, we explore the effect of the wind termination on the νp -process. The termination point is located at $r_{\rm wt}=100,\,200,\,231,\,300$ (standard model), 400, 500, and 1000 km on the transonic wind trajectory (black line) shown in Figure 1 (top panel). The other parameters $L_{\nu},\,M_{\rm ns}$, and $Y_{\rm e,9}$ are kept to be the fiducial values (Table 1, second to ninth lines). In Figure 1 (middle and bottom panels), we find shock jumps of density and temperature by wind termination only for the $r_{\rm wt}=1000$ km case, since the termination points are placed below the sonic radius ($r_{\rm s}=515$ km; Figure 1, top panel) for the other cases.⁶

The result of nucleosynthesis calculations is shown in Figure 2. The top panel shows the mass fractions, X_A , of nuclei as a function of atomic mass number, A. We find that the case with $r_{\rm wt}=231$ km has the maximum efficiency of producing nuclei with A=100-110 (including our calculations not shown here). The middle and bottom panels show, respectively, the mass fractions relative to the standard model (= $X_A/X_{A,{\rm standard}}$) and to their solar values (Lodders 2003), i.e., the production factor $f (= X_i/X_{i,\odot})$ for ith isotope), as a function of A. We find a noticeable effect of wind termination on the νp -process; the production of p-nuclei between A=90 and 110 is outstanding for the cases with $r_{\rm wt}=231$ and 300 km (standard model).

It should be noted that the asymptotic entropy S = 57.0 per nucleon in units of the Boltzmann constant $k_{\rm B}$; Table 1) is the same for all the cases here (except for $r_{\rm wt} = 1000$ km owing to the termination-shock heating). These different outcomes can be explained by the different values of $\Delta_{\rm n} = 0.24-17$, 13th column in Table 1), defined by Equation (1), owing to the different expansion timescales after wind termination. As indicated by the yellow band in Figure 1 (bottom panel), we find substantial differences in the temperature histories before or during the νp -process phase (defined as $T_0 = 1.5-3$).

We define two expansion timescales τ_1 and τ_2 (seventh and eighth columns in Table 1); the former is the time elapsed from $T_9 = 6$ to $T_9 = 3$ and the latter from $T_9 = 3$ to $T_9 = 1.5$. These represent the durations of the seed production and of the *vp*-process, respectively. As can be seen in Figure 1 (bottom panel), τ_1 (= 17.5 ms) and thus the proton-to-seed ratio Y_p/Y_h (=124) at $T_9 = 3$ are the same except for the case with $r_{\rm wt} = 100$ km. Nevertheless, the different values of τ_2 and thus Δ_n (see Equation (1)) lead to the different efficiencies of the νp -process. We find that $\Delta_{\rm n}\sim 10$ is needed for an efficient production of p-nuclei with $A \sim 100$. This requires the wind termination at $T_{\rm wt,9}\sim 2$ –3 (in units of 10^9 K) to obtain $n_{\bar{\nu}_e}\sim 0.1$ (Equation (2)). For the standard model ($r_{\rm wt} = 300$ km and $T_{\rm wt,9} = 2.19$), the maximum production factor ($f_{\rm max}$ in Table 1) is obtained at 96 Ru (nuc(f_{max}) in Table 1), a daughter nucleus of 96 Pd (N=50) on the νp -process pathway. We have the optimal production (log $f_{\rm max}=7.67$ at 106 Cd) with $T_{\rm wt,9}=2.65$ when the termination point is set to $r_{\rm wt} = 231$ km.

In Table 1, the nuclide with the largest mass number A_{max} with $f > f_{\text{max}}/10$ is also shown (e.g., ^{106}Cd for the standard model; nuc(A_{max}) in Table 1), which is taken to be the largest A of the

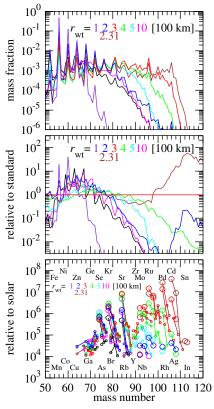


Figure 2. Comparison of the nucleosynthetic results for various wind-termination radii $r_{\rm wt}$. The mass fractions (top) and their ratios relative to those for the standard model (middle) are shown as a function of atomic mass number. The bottom panel shows the abundances of isotopes (connected by a line for a given element) relative to their solar values, where those lower than 10^4 are omitted. The color coding corresponds to different values of $r_{\rm wt}$ as indicated in each panel (red is the standard model). The result for the outflow without wind termination is shown in black. In the bottom panel, the names of elements are specified in the upper (even Z) and lower (odd Z) sides at their lightest mass numbers.

(A color version of this figure is available in the online journal.)

p-nuclei synthesized by the νp -process. Given that our standard model represents a typical supernova condition, this implies that the νp -process can be the source of the solar p-abundances up to $A \sim 110$ (see Section 6 for more detail). However, this favorable condition is not robust against a variation of $r_{\rm wt}$ (and thus $T_{\rm wt}$); the outflows with $r_{\rm wt} = 200$ km ($T_{\rm wt,9} = 2.95$)⁷ and $r_{\rm wt} \geq 500$ km ($T_{\rm wt,9} < 1.55$) end up with $A_{\rm max} = 84$ (⁸⁴Sr; Table 1). Note that the outflow with $r_{\rm wt} = 1000$ km leads to a similar result as that without wind termination (black line in Figure 2; $r_{\rm wt} = \infty$ in Table 1). This indicates that the role of wind termination is unimportant for $T_{\rm wt,9} < 1.5$.

We find no substantial νp -processing for the outflow with $r_{\rm wt}=100\,{\rm km}$ (Figure 2). This is due to the substantially smaller $Y_{\rm e}$ at the beginning of the νp -process ($T_9=3$), $Y_{\rm e,3}=0.509$ (only slightly proton-rich), than those for the other cases (0.550; Table 1). As a result, Y_p/Y_h at $T_9=3$ is only 1.78, resulting in a small Δ_n (= 0.24) in spite of the largest $n_{\bar{\nu}_e}$ among the various $r_{\rm wt}$ models presented here. It should be noted that $Y_{\rm e,3}$ is always lower than $Y_{\rm e,9}$ (= 0.600 in the present cases). This is due to a couple of neutrino effects. One is that the

⁶ The outflows with $r_{\rm wt} < r_{\rm s}$ are subsonic all the way. This happens in the early wind phase when the slowly outgoing ejecta is still close to the core (Arcones et al. 2007). In this case, however, the mass ejection rate from the core is expected to be close to that of the transonic solution (with the maximum \dot{M}). Thus, the time variations of r, ρ , and T may not be substantially different from those of the transonic case for $r < r_{\rm wt}$ (see, e.g., Otsuki et al. 2000). We take, therefore, the transonic solution for all the cases, rather than the subsonic solution by introducing an additional free parameter \dot{M} .

⁷ Despite the largest Δ_n (= 17.1) among the various $r_{\rm wt}$ models, the $r_{\rm wt} = 200$ km model ends up with inefficient νp -processing. This is due to Δ_n defined for $T_9 \leqslant 3$ (Equation (1)), while the maximal efficiency of νp -processing is obtained with $T_{\rm wt} = 2.65$ in this case.

asymptotic equilibrium value of $Y_{\rm e}$ in the non-degenerate matter consisting of free nucleons, which is subject to neutrino capture, is $Y_{\rm e,a}\approx 0.56$ (see, e.g., Qian & Woosley 1996) with the neutrino luminosities and energies taken in this study. Hence, the value starts relaxing from $Y_{\rm e,9}$ toward $Y_{\rm e,a}$ as soon as the calculation initiates. The other effect is due to the continuous α -particle formation ($T_{\rm 9}<7$) from inter-converting free protons and free neutrons that is subject to neutrino capture, which drives $Y_{\rm e}$ toward 0.5 (" α -effect"; Meyer et al. 1998b). In the $r_{\rm wt}=100$ km case, the wind termination takes place at high temperature ($T_{\rm wt,9}=5.19$) and thus the long $\tau_{\rm 1}$ (= 359 ms) leads to the low $Y_{\rm e,3}$ owing to the neutrino effects.

In summary, our exploration here elucidates a crucial role of wind termination on the νp -process. On one hand, a fast expansion above the temperature $T_9 \sim 3$ (more precisely, $T_9 = 2.65$ in the considered conditions) is favored to obtain a high proton-to-seed ratio at the onset of the νp -process. On the other hand, a slow expansion below this temperature, owing to wind termination, is needed to obtain $\Delta_n \sim 10$ for efficient νp -processing.

We presume that the reason for somewhat different outcomes in previous studies of the νp -process described in Section 1 is largely due to their different behaviors of wind termination. The temperature histories of trajectories taken by Pruet et al. (2006, an exploding $15 M_{\odot}$ star), similar to our models with $r_{\rm wt} = 100-230 \ (T_{\rm wt,9} = 2.7-5.2)$, lead to the production of p-nuclei up to $A \sim 100$. The reason of weak vp-processing in Fröhlich et al. (2006a; a $20 M_{\odot}$ explosion) may be rather due to the moderate proton richness (up to $Y_e \sim 0.54$) in their simulations (see Section 4.4 and Figure 6). In contrast, negligible production of p-nuclei in the electron-capture supernova of a 9 M_{\odot} star (Wanajo et al. 2009, also S. Wanajo et al. 2011, in preparation) is due to the absence of a wind-termination shock within the relevant temperature range ($T_9 = 1.5-3$) owing to the steep density gradient of the oxygen-neon-magnesium core progenitors surrounded by a diluted outer H/He envelope.

4.2. Neutrino Luminosity

The neutrino luminosity L_{ν} decreases with time from its initial value of a few 10^{52} erg s $^{-1}$ to $\sim 10^{51}$ erg s $^{-1}$ during the first 10 s (Fischer et al. 2010; Hüdepohl et al. 2010). In this subsection, we examine the effect of L_{ν} on the νp -process, by varying its value from $10^{52.4}=2.51\times 10^{52}$ erg s $^{-1}$ to 10 times smaller than that with an interval of 0.2 dex (from 10th to 15th lines in Table 1 and Figure 3). $M_{\rm ns}$ and $Y_{\rm e,9}$ are taken to be the fiducial values of $1.4~M_{\odot}$ and 0.600, respectively. In Section 4.1, we found that the temperature at the wind termination, $T_{\rm wt}$, plays a crucial role for the νp -process. Hence, we adjust $r_{\rm wt}$ (Table 1) such that the fiducial value of $T_{\rm wt,9}=2.19$ is obtained for each L_{ν} .

The results of nucleosynthesis calculations are shown in Figure 3 and Table 1. We clearly see the increasing efficiency of νp -processing with a decrease of L_{ν} . This is due to the larger entropy for a smaller L_{ν} (Table 1), while the expansion timescales τ_1 (prior to the νp -process) are similar. This leads to a higher Y_p/Y_h at the onset of the νp -process for a lower L_{ν} . In addition, the somewhat larger timescale τ_2 for a smaller

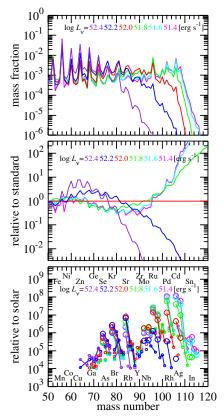


Figure 3. Same as Figure 2, but for various neutrino luminosities (L_{ν}) . (A color version of this figure is available in the online journal.)

 L_{ν} increases $n_{\bar{\nu}_e}$ (12th column in Table 1). For these reasons, a smaller L_{ν} model achieves larger Δ_n , leading to a more efficient νp -process.

It should be noted that in our explored cases, $r_{\rm wt}$ decreases with decreasing L_{ν} (Table 1) in order to obtain the fiducial value of $T_{\rm wt,9} = 2.19$ (to figure out solely the effect of L_{ν}). However, if $r_{\rm wt}$ increases with time and thus $T_{\rm wt}$ decreases with decreasing L_{ν} , as in many explosion models, only the early stage of the neutrino-driven wind with $L_{\nu} \sim 10^{52}$ erg s⁻¹ may be relevant to the high $T_{\rm wt,9} = 1.5$ –3 (see, e.g., Arcones et al. 2007) that is needed for efficient νp -processing (Section 4.1).

4.3. Neutron Star Mass

The mass of the proto-neutron star $M_{\rm ns}$ can be somewhat different from its canonical value of 1.4 M_{\odot} , depending on its progenitor mass. In this subsection, we examine the nucleosynthesis calculations with $M_{\rm ns}=1.2,1.4,1.6,1.8$, and $2.0\,M_{\odot}$, while L_{ν} and $Y_{\rm e,9}$ are kept to be their fiducial values of 10^{52} erg s⁻¹ and 0.600. For each case, the fiducial value of $T_{\rm wt,9}=2.19$ is obtained by adjusting $r_{\rm wt}$ (from 16th to 20th lines in Table 1) as in Section 4.2.

We find a clear correlation between an increase of $M_{\rm ns}$ and an increasing efficiency of νp -processing in Figure 4 and Table 1. This is due to a larger S and a smaller τ_1 for a larger $M_{\rm ns}$ (e.g., Otsuki et al. 2000; Wanajo et al. 2001), both of which help to increase Y_p/Y_h and thus $\Delta_{\rm n}$. This means that a more massive progenitor (up to $\sim 30\,M_\odot$, which forms a neutron star) is favored for the νp -process, given that all the other parameters are the same. In reality, however, other factors, such as the evolutions of L_{ν} , $r_{\rm wt}$, and $Y_{\rm e}$ should be dependent on the progenitor mass (e.g., Arcones et al. 2007), which prevents us

⁸ When the radius of the neutrino sphere R_{ν} is fixed to a constant value, the expansion timescale increases with decreasing L_{ν} (see, e.g., Otsuki et al. 2000; Wanajo et al. 2001). In this study, however, R_{ν} is assumed to decrease with decreasing L_{ν} (Section 2), which is more realistic. As a result, the difference of τ_1 in the range of L_{ν} explored here is moderate.

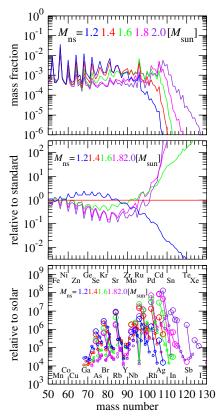


Figure 4. Same as Figure 2, but for various neutron star masses (M_{ns}) . (A color version of this figure is available in the online journal.)

from drawing any firm conclusions. It should be emphasized, however, that the outflow with a typical mass of $M_{\rm ns} = 1.4\,M_{\odot}$ can already provide physical conditions sufficient for producing the p-nuclei up to $A \sim 110$.

4.4. Electron Fraction

The electron fraction Y_e is obviously one of the most important ingredients in the vp-process as it controls the proton richness in the ejecta. Recent hydrodynamical studies with elaborate neutrino transport indicate that Y_e exceeds 0.5 and increases up to \sim 0.6 during the neutrino-driven wind phase (Fischer et al. 2010; Hüdepohl et al. 2010). It should be noted that Y_e substantially decreases from its initial value owing to the neutrino effects (Section 4.1). In our standard model, the value decreases from $Y_{e,9} = 0.600$ (at $T_9 = 9$) to $Y_{e,3} = 0.550$ at the onset of the vp-process ($T_9 = 3$). However, these neutrino effects would be highly dependent on the neutrino luminosities and energies of electron and anti-electron neutrinos assumed in this study. In this subsection, therefore, we take the value at the onset of the vp-process, $Y_{e,3}$, as a reference, rather than the initial value $Y_{e,9}$.

Figure 5 and Table 1 (the last six lines) show the nucleosynthetic results for $Y_{\rm e,3}=0.523,\ 0.550,\ 0.576,\ 0.603,\ 0.629,$ and 0.655 (see Table 1 for their initial values $Y_{\rm e,9}$). The other parameters $M_{\rm ns}$, L_{ν} , and $r_{\rm wt}$ (and thus $T_{\rm wt}$) are kept to be their fiducial values (first line in Table 1). We find a great impact of the $Y_{\rm e}$ variation; an increase of only $\Delta Y_{\rm e,3}\sim 0.03$ leads to a 10 unit increase of $A_{\rm max}$, while $f_{\rm max}$ is similar for $Y_{\rm e,3}>0.550$. This is due to the larger $Y_{\rm p}/Y_{\rm h}$ (at $T_{\rm 9}=3$) for a larger $Y_{\rm e,3}$, leading the larger Δ_n despite the same $n_{\bar{\nu}_{\rm e}}$ (Table 1).

In order to elucidate the effect of Y_e in more detail, the production factor f for each p-nucleus is drawn in Figure 6

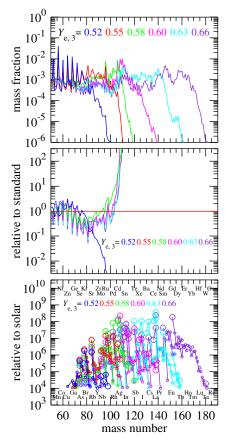


Figure 5. Same as Figure 2, but for various electron fractions $(Y_{e,3})$. (A color version of this figure is available in the online journal.)

as a function of $Y_{\rm e,3}$, where $M_{\rm ns}$, L_{ν} , and $r_{\rm wt}$ are kept to be their fiducial values. Each element is color coded with the solid, dashed, and long-dashed lines for the lightest, second-lightest, and third-lightest (115 Sn is only the case) isotopes, respectively (see the first column of Table 4 for the list of p-nuclei). We find in the top panel of Figure 6 that the p-nuclei up to A = 108 (108 Cd) take the maximum production factors between $Y_{\rm e,3} = 0.53$ and 0.60. Given the maximum $Y_{\rm e,3}$ to be \sim 0.6 according to some recent hydrodynamic results (e.g., Fischer et al. 2010; Hüdepohl et al. 2010), this implies that the maximum mass number of the p-nuclei produced by the νp -process is $A \sim 110$.

In principle, the heavier p-nuclei can be synthesized if the matter is more proton-rich than $Y_{\rm e,3}=0.6$. The middle panel of Figure 6 shows that the production factors of the p-nuclei from A=113 ($^{113}{\rm In}$) up to A=138 ($^{138}{\rm Ce}$) are maximal between $Y_{\rm e,3}=0.61$ and 0.63. Furthermore, $^{144}{\rm Sm}$ and $^{152}{\rm Gd}$ reach the maximum production factors at $Y_{\rm e,3}=0.64$ and 0.66, respectively (bottom panel in Figure 6). The end point of the vp-process appears to be at $A\sim180$ ($^{180}{\rm Ta}$) in our explored cases. It should be noted that the wind termination also plays a crucial role as explored in Section 4.1. This is evident if we compare Figures 6 and 7, where the latter is the result for $r_{\rm wt}=\infty$. Without wind termination, more proton richness ($\Delta Y_{\rm e,3}\sim0.05$) is required for a given p-nucleus to be produced, but with a substantially smaller production factor. The p-nuclei heavier than A=140 cannot be produced at all without wind termination (bottom panel in Figure 7).

We can understand the reason for the above result from Figure 8, which displays the snapshots of nucleosynthesis

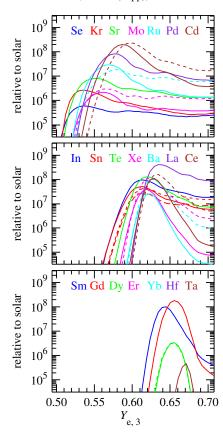


Figure 6. Nucleosynthetic p-abundances relative to their solar values (production factors) as a function of $Y_{\rm e,3}$. $M_{\rm ns}$, L_{ν} , and $r_{\rm wt}$ are kept to be their fiducial values (first line in Table 1). Each element is color coded with the solid, dashed, and long-dashed lines for the lightest, second-lightest, and third-lightest ($^{115}{\rm Sn}$ is only the case) isotopes, respectively (see the first column of Table 4 for the list of p-nuclei).

for selected cases on the nuclear chart when the temperature drops to $T_9=2$ (left) and 1 (right). Top, middle, and bottom panels are for the standard model, that with $Y_{\rm e,9}$ replaced by 0.800 ($Y_{\rm e,3}=0.655$), and that with $Y_{\rm e,9}$ and $r_{\rm wt}$ replaced by 0.800 and ∞ (without wind termination), respectively. In the standard model ($Y_{\rm e,3}=0.550$), the nuclear flow proceeds along the proton-drip line and encounters the proton-magic number Z=50 ($A\sim100-110$). There are α -unbound nuclei of $^{106-108}$ Te (Z=52) just above Z=50 along the proton-drip line, which is the end point of the classical rp-process (Schatz et al. 2001). This is why the νp -process stops at $A\sim110$ for $Y_{\rm e,3}\lesssim0.6$.

As $Y_{\rm e,3}$ exceeds 0.6, radiative neutron capture becomes more important and competes with proton capture (Pruet et al. 2006; Wanajo 2006). This is due to the large amount of free protons $(Y_{\rm p}/Y_{\rm h}=1130~{\rm at}~T_9=3~{\rm for}$ the middle panels of Figure 8; the last line in Table 1) that release free neutrons owing to neutrino capture ($\Delta_{\rm n}=94.2$). As a result, the nuclear flow detours the end point of the classical rp-process (N=54-56) at Z=52 toward the larger atomic number through the nuclei with N>60, as can be seen in Figure 9. The stagnation of the flow at the neutron-magic number N=82 in the middle panels of Figure 8 clearly shows the importance of neutron capture. The concentration of nuclei at N=82 leads to the large production factors of the p-nuclei with A=130-150 as seen in Figure 6. Note that the p-nuclide $^{144}{\rm Sm}$ is located on the N=82 line.

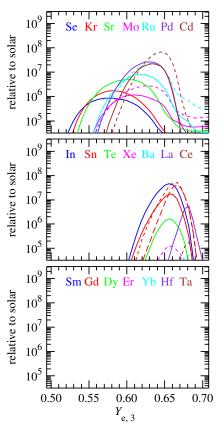


Figure 7. Same as Figure 6, but for the case without wind termination $(r_{\rm wt} = \infty)$. (A color version of this figure is available in the online journal.)

Beyond N=82, the increasing atomic number and the decreasing temperature inhibit further proton capture. Note that $n'_{\bar{\nu}_e} \sim 0.3 n_{\bar{\nu}_e}$ in our explored models (see Equations (1) and (2)). Thus, neutron capture still continues at this stage. As a result, the nuclear flow approaches the β -stability line and finally enters to the neutron-rich region at $A\sim 160$ as seen in the middle-right panel of Figure 8. Without wind termination (but with the same parameters otherwise), however, the rapidly decreasing temperature does not allow the nuclear flow to reach N=82 as seen in the bottom panels of Figure 8. This is the reason for the inefficiency of producing heavy p-nuclei in Figure 7.

5. UNCERTAINTIES IN NUCLEAR PHYSICS

There have been continuing experimental works relevant to the νp -process (e.g., Weber et al. 2008; Hayakawa et al. 2010) since its discovery. However, we still rely upon theoretical or limited experimental estimates for the vast majority of nuclear reactions accompanied with the νp -process, which may suffer from uncertainties. There are also a number of isotopes without experimental mass measurements on the νp -process pathway (Weber et al. 2008).

The νp -process is unique in the following aspects, different from the classical rp-process. First is that the seed nuclei are directly formed from free nucleons (i.e., the primary process), while the classical rp-process needs CNO seeds. Thus, the triple- α process and some two-body reactions relevant to the breakout from the p-p chain region (A < 12) play important roles for setting the proton-to-seed ratio Y_p/Y_h (and thus Δ_n) at the beginning of the νp -process (Section 5.1). Second is the role

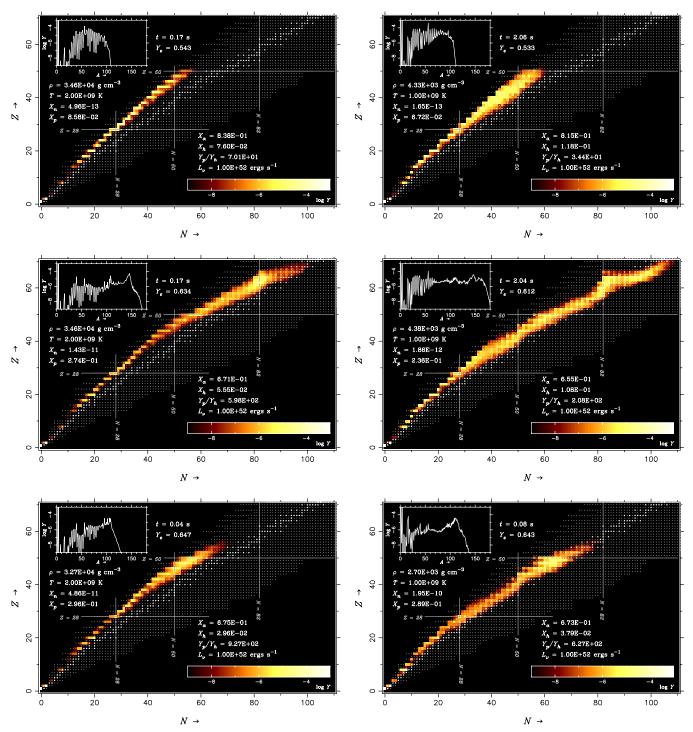


Figure 8. Snapshots of nucleosynthesis on the nuclear chart when the temperature drops to $T_9 = 2$ (left) and 1 (right). Top, middle, and bottom panels are for the standard model (first line in Table 1), that with $Y_{e,9}$ replaced by 0.800 ($Y_{e,3} = 0.655$), and that with $Y_{e,9}$ and r_{wt} replaced by 0.800 and ∞ (without wind termination). The nucleosynthetic abundances are color coded. The species included in the reaction network are shown by dots (with the thick dots for the stable isotopes). The abundance distribution as a function of atomic mass number is shown in the inset of each panel.

of neutron capture, in particular of (n, p) reactions on heavy nuclei in the proton-rich matter, which bypass the β^+ -waiting points on the classical rp-process path (Section 5.2). Third, the νp -process path is limited to $Z \leq N$, where most of the nuclear masses of relevance are measurable (Weber et al. 2008; Section 5.3). This is an advantage compared with the classical rp-process that proceeds through even—even Z = N nuclei with radiative proton capture to Z > N isotopes (Brown et al. 2002).

In Section 5.1 and 5.2, we test the effect of uncertainties in some selected reactions by simply multiplying or dividing their original values by factors of 2 and 10 with the standard model (first line in Tables 1 and 3). All the explored results are listed in Table 3. In Section 5.3, the effect of new mass measurements by Weber et al. (2008) is discussed, along with possible uncertainties of other unmeasured nuclear masses on the νp -process pathway.

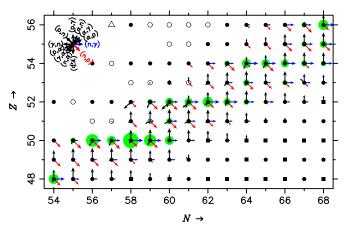


Figure 9. Nuclear flows (arrows) and the abundances (circles) near the end point of the classical rp-process (Z=52) in logarithmic scale for the model with $Y_{\rm e,3}=0.655$ (last line in Table 1) when the temperature decreases to $T_9=2$ (that corresponds to the middle-left panel in Figure 8). The nuclei included in the reaction network are denoted by squares (stable isotopes), filled circles (with measured masses of Audi et al. 2003), open circles (with extrapolated masses of Audi et al. 2003), and triangles (with the HFB-9 masses of Goriely et al. 2005). The flows by β^+ -decays (not shown here) are negligible compared with those by (n, p) reactions (red arrows). Radiative neutron capture (blue arrows) also plays a significant role.

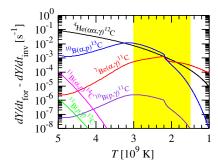


Figure 10. Nuclear flows for the reactions that bridge from A < 12 (the p–p chain region) to $A \geqslant 12$ as a function of temperature. The nuclear flow is defined as the deference of the time derivatives (per second) of abundance between the forward and inverse reactions for a given channel. The yellow band indicates the temperature range relevant to the vp-process ($T_9 = 1.5$ –3).

(A color version of this figure is available in the online journal.)

5.1. Breakout from the p-p Chain Region

In Figure 10, the nuclear flows for the reactions that bridge from A < 12 (the p-p chain region) to $A \ge 12$ (the CNO region) are shown as a function of the temperature before $(T_9 > 3)$ and after $(T_9 < 3)$ the onset of the νp -process. The nuclear flows at $T_9 = 2.5$ for the relevant N-Z region are also shown in Figure 11. Here, the nuclear flow is defined as the difference between the time derivatives of abundances for the forward and inverse reactions of a given channel. It is clear that, at a high temperature $(T_9 > 3)$, the triple- α process (with the rate of Caughlan & Fowler 1988) plays a dominant role for the breakout from the p-p chain region. We find, however, a couple of two-body reaction sequences $^7\text{Be}(\alpha, \gamma)^{11}\text{C}(\alpha, p)^{14}\text{N}$ and $^7\text{Be}(\alpha, p)^{10}\text{B}(\alpha, p)^{13}\text{C}$ compete with the triple- α process during the νp -process phase.

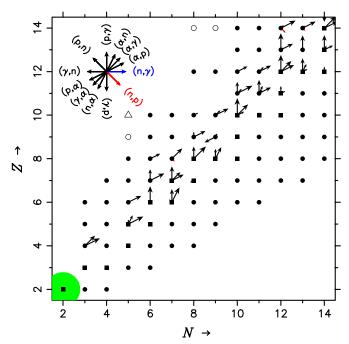


Figure 11. Same as Figure 9, but for the standard model when the temperature decreases to $T_9 = 2.5$ for a lighter N–Z region. At this temperature, the nuclear flows through $^7\text{Be}(\alpha, \gamma)^{11}\text{C}(\alpha, p)^{14}\text{N}$ and $^7\text{Be}(\alpha, p)^{10}\text{B}(\alpha, p)^{13}\text{C}$ play dominant roles for the breakout from the p–p chain region, along with the triple- α process (not shown here).

(A color version of this figure is available in the online journal.)

 Table 2

 Rates and Decay Timescales for Selected Reactions

Species	$\lambda_{2.5}^{a}$	$\tau_{2.5}{}^{a}$	λ _{2.0} ^b	$\tau_{2.0}{}^{\rm b}$
	$(\text{mol}^{-1} \text{ cm}^3 \text{ s}^{-1})$	(ms)	$(\text{mol}^{-1} \text{ cm}^3 \text{ s}^{-1})$	(ms)
3α	3.07×10^{-10}	8.32×10^{4}	3.86×10^{-10}	2.96×10^5
$^{7}\mathrm{Be}(\alpha,\gamma)$	4.48	1.45×10^{-2}	1.29	0.107
$^{7}\mathrm{Be}(\alpha, p)$	4.22×10^{4}	1.55×10^{-6}	5.89×10^{3}	2.34×10^{-5}
$^{10}\mathrm{B}(\alpha,p)$	5.76×10^{5}	1.13×10^{-7}	1.36×10^{5}	1.01×10^{-6}
$^{10}\mathrm{B}(p,\alpha)$	1.14×10^{7}	1.25×10^{-8}	6.04×10^{6}	5.59×10^{-8}
11 C(α , p)	6.98×10^{4}	9.34×10^{-7}	1.61×10^{4}	8.58×10^{-6}
12 C (p, γ)	4.69×10^{2}	3.05×10^{-4}	5.11×10^{2}	6.59×10^{-4}
13 C(α , n)	2.01×10^{4}	3.24×10^{-6}	1.27×10^{4}	1.09×10^{-5}
56 Ni(<i>n</i> , <i>p</i>)	1.61×10^{8}	11.3	1.28×10^{8}	454
60 Zn (n, p)	7.40×10^{8}	2.46	6.82×10^{8}	85.5
64 Ge (n, p)	6.85×10^{8}	2.65	6.15×10^{8}	94.8
68 Se(<i>n</i> , <i>p</i>)	9.38×10^{8}	1.94	8.12×10^{8}	71.8
72 Kr (n, p)	1.38×10^{9}	1.32	1.24×10^{9}	46.9
76 Sr(n, p)	1.81×10^{9}	1.00	1.69×10^{9}	34.6
80 Zr (n, p)	1.99×10^{9}	0.913	1.92×10^{9}	30.4
84 Mo(<i>n</i> , <i>p</i>)	1.44×10^{9}	1.26	1.31×10^{9}	44.5
96 Pd (n, p)	2.06×10^{8}	8.84	1.66×10^{8}	351

Notes.

Table 2 lists the reaction rates and decay timescales for the relevant isotopes at $T_9 = 2.5$ and 2.0. It is clear that $^7\mathrm{Be}(\alpha, \gamma)^{11}\mathrm{C}$, four orders of magnitude slower than $^{11}\mathrm{C}(\alpha, p)^{14}\mathrm{N}$, governs the former sequence. For the latter, $^{10}\mathrm{B}(\alpha, p)^{13}\mathrm{C}$, although a factor of 10 smaller than $^7\mathrm{Be}(\alpha, p)^{10}\mathrm{B}$, mainly controls the reaction flow, which takes away nuclear abundances from $^{10}\mathrm{B}$ formed by the endothermic reaction.

 $^{^9}$ $^7\mathrm{Be}(\alpha,p)^{10}\mathrm{B}$ is an endothermic reaction. Because of its small (negative) Q-value of -1.146 MeV and the larger abundance of α particles, a small amount of $^{10}\mathrm{B}$ (that is immediately taken away by the subsequent (α,p) reaction) exists in the present case.

^a Rates and decay timescales at $T_9 = 2.5$ ($\rho = 7.20 \times 10^4$ g cm⁻³, $X_n = 7.64 \times 10^{-12}$, $X_p = 0.0970$, $X_\alpha = 0.852$).

b Rates and decay timescales at $T_9 = 2.0$ ($\rho = 3.46 \times 10^4$ g cm⁻³, $X_n = 4.96 \times 10^{-13}$, $X_p = 0.0858$, $X_\alpha = 0.838$).

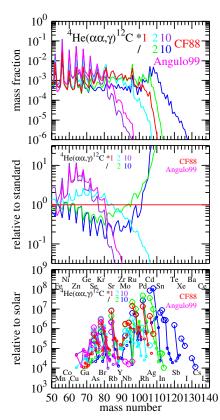


Figure 12. Same as Figure 2, but for variations on the triple- α rate. (A color version of this figure is available in the online journal.)

Figure 10 shows that ${}^{7}\text{Be}(\alpha, \gamma){}^{11}\text{C}$ and ${}^{10}\text{B}(\alpha, p){}^{13}\text{C}$ exhibit similar roles to triple- α in the temperature range relevant to the νp -process. Therefore, we select these three reactions for the sensitivity tests. Note that the unstable isotope ${}^{11}\text{C}$ produced is followed by ${}^{11}\text{C}(\alpha, p){}^{14}\text{N}$ (see Hayakawa et al. 2010 for a recent experimental evaluation of this rate) before decaying back to ${}^{11}\text{B}$.

All the data of these three reactions, from Wagoner (1969, for 10 B(α , p) 13 C) and Caughlan & Fowler (1988, for the remainder) in the REACLIB compilation, are based on experimental information of single resonance states. Contribution from (possible) resonances at higher excitation energies could thus sizably change these rates. As an example, the triple- α rate of Angulo et al. (1999), which includes contribution from the 9.2 MeV 2^+ state that is predicted theoretically, leads to a factor of 2–10 higher values (for the temperature range relevant to seed production, $T_9 = 7$ –3) than that of Caughlan & Fowler (1988) based on the single 7.6 MeV 0^+ (Hoyle) state. Recent experimental works did not confirm the presence of the 9.2 MeV state, but other levels in this energy region as well as those at higher energies might contribute to this rate (Austin 2005; Diget et al. 2005, 2009).

The result of sensitivity tests for the triple- α rate is shown in Figure 12, where the forward and inverse rates are multiplied or divided by factors of 2 and 10. We find substantial changes in the production of p-nuclei with $A \sim 100$ –110 for a factor of two variation on the rate, and more drastic changes for a factor of 10 variation. It can be mainly attributed to the resulting protonto-seed ratio Y_p/Y_h (at $T_9=3$) and thus Δ_n (third and fourth lines in Table 3). Note that $n_{\bar{\nu}_e}$ (= 0.0834; first line in Table 1) remains the same for all the cases here. A larger triple- α rate leads to a more efficient seed production and thus smaller Y_p/Y_h

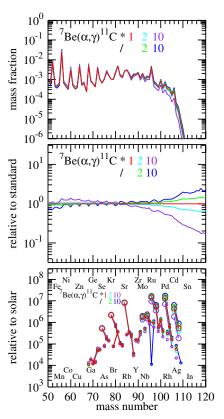


Figure 13. Same as Figure 2, but for variations on the ${}^{7}\text{Be}(\alpha, \gamma)^{11}\text{C}$ rate. (A color version of this figure is available in the online journal.)

and Δ_n . A larger rate during the νp -process phase ($T_9 = 1.5-3$) also yields more carbon and other intermediate-mass nuclei that act as proton poison. As a result, efficiency of the νp -process for heavy element synthesis decreases. The same interpretation is applicable to the opposite case with a smaller rate.

We find that a replacement of the triple- α rate by that of Angulo et al. (1999) inhibits production of p-nuclei for A > 80 (Figure 12). In fact, the net effect of including the 9.2 MeV state (not confirmed by recent experiments) by Angulo et al. (1999) corresponds to the rate of Caughlan & Fowler (1988) multiplied by a factor of 10. This demonstrates the importance of future re-evaluations of (possible) contribution from higher levels than the 7.64 MeV state in 12 C.

Figures 13 and 14 show the result for ${}^{7}\text{Be}(\alpha, \gamma)^{11}\text{C}$ and ${}^{10}\text{B}(\alpha, p)^{13}\text{C}$. We find non-negligible differences in the p-abundances with $A \sim 100$ –110, although the impact is much smaller than that for triple- α . Note that a larger rate has a stronger impact than a smaller rate (middle panels). This is a consequence of the fact that the larger rate of a given channel increases the total efficiency for the breakout from the p–p chain region, while the other two channels are still active for the smaller rate (see Figure 10).

 7 Be(α , γ) 11 C competes with triple- α only during the late phase of the νp -process ($T_9 \lesssim 2$; Figure 10). A larger rate during this phase leads to more production of intermediate-mass nuclei that act as proton poison. A variation of this rate does not substantially affect Y_p/Y_h (at $T_9=3$) and Δ_n at the onset of νp -processing (Table 3). 10 B(α , p) 13 C however competes with triple- α at $T_9 \sim 2$ –3.5 (Figure 10). Hence, a variation on the rate also affects Y_p/Y_h at the beginning of νp -processing and Δ_n (Table 3).

 Table 3

 Results for the Changes of Reaction Rates

Reaction	Factor	Y_p/Y_h^a	$\Delta_n^{\ \mathrm{b}}$	$\log f_{\rm max}^{\ \ c}$	nuc(f)d	nuc(A)e	Fig.
Standard	1.00	124	10.3	7.16	⁹⁶ Ru	¹⁰⁶ Cd	All
3α	1.00^{f}	25.6	2.14	6.47	⁷⁸ Kr	⁸⁴ Sr	12
3α	2.00	73.5	6.13	6.93	⁸⁴ Sr	¹⁰² Pd	12
3α	10.0	25.2	2.10	6.15	$^{78}\mathrm{Kr}$	⁸⁴ Sr	12
3α	1/2.00	204	17.0	7.67	¹⁰² Pd	108 Cd	12
3α	1/10.0	482	40.2	8.04	108 Cd	108 Cd	12
3α	1/100	719	60.0	8.02	108 Cd	¹²⁰ Te	12
$^{7}\mathrm{Be}(\alpha, \gamma)$	2.00	124	10.3	7.11	⁹⁶ Ru	106 Cd	13
$^{7}\mathrm{Be}(\alpha,\gamma)$	10.0	122	10.2	6.98	⁹⁶ Ru	106 Cd	13
$^{7}\mathrm{Be}(\alpha, \gamma)$	100	117	9.76	6.89	⁸⁴ Sr	¹⁰⁶ Cd	13
$^{7}\mathrm{Be}(\alpha, \gamma)$	1/2.00	124	10.3	7.19	⁹⁶ Ru	106 Cd	13
$^{7}\mathrm{Be}(\alpha, \gamma)$	1/10.0	124	10.3	7.24	¹⁰² Pd	¹⁰⁶ Cd	13
$^{10}\mathrm{B}(\alpha,p)$	2.00	119	9.92	7.09	⁹⁶ Ru	106 Cd	14
10 B(α , p)	10.0	112	9.34	6.96	⁹⁶ Ru	106 Cd	14
$^{10}\mathrm{B}(\alpha,p)$	1/2.00	129	10.8	7.23	¹⁰² Pd	106 Cd	14
$^{10}\mathrm{B}(\alpha,p)$	1/10.0	135	11.3	7.35	¹⁰² Pd	¹⁰⁶ Cd	14
56 Ni(<i>n</i> , <i>p</i>)	2.00	124	10.3	7.01	⁹⁶ Ru	106 Cd	16
56 Ni (n, p)	10.0	124	10.3	7.02	⁸⁴ Sr	¹⁰² Pd	16
56 Ni (n, p)	1/2.00	124	10.3	7.45	¹⁰² Pd	106 Cd	16
56 Ni(<i>n</i> , <i>p</i>)	1/10.0	124	10.3	7.92	106 Cd	108 Cd	16
60 Zn (n, p)	2.00	124	10.3	7.15	⁹⁶ Ru	106 Cd	19
60 Zn (n, p)	10.0	124	10.3	7.15	⁹⁶ Ru	106 Cd	19
60 Zn (n, p)	1/2.00	124	10.3	7.22	102 Pd	¹⁰⁶ Cd	19
60 Zn (n, p)	1/10.0	124	10.3	7.51	¹⁰² Pd	108 Cd	19
64 Ge (n, p)	2.00	124	10.3	7.16	⁹⁶ Ru	106 Cd	20
64 Ge (n, p)	10.0	124	10.3	7.16	⁹⁶ Ru	106 Cd	20
64 Ge (n, p)	1/2.00	124	10.3	7.19	¹⁰² Pd	106 Cd	20
64 Ge (n, p)	1/10.0	124	10.3	7.41	102 Pd	108 Cd	20

Notes.

5.2. (n, p) Reactions on Heavy Nuclei

The νp -process starts at $T_9 \sim 3$ from the seed nucleus 56 Ni, which is formed from free nucleons earlier. During the νp -process, the (n,p) reactions play an important role for determining the nuclear flows. Figure 15 shows the nuclear flows starting from 56 Ni (Z=N=28) up to 80 Zr (Z=N=40). The isotopes included in the reaction network are denoted by squares (stable isotopes), filled circles (with measured masses of Audi et al. 2003), open circles (with extrapolated masses of Audi et al. 2003), and triangles (with the HFB-9 masses of Goriely et al. 2005). We find that the nuclear flow of the νp -process proceeds through even—even Z=N isotopes up to Z=N=40 as in the classical rp-process. All the nuclear masses on the νp -process path (up to Z=N=40), which determine the abundance distribution for given isotones, were measured by experiments (Audi et al. 2003). 10

Currently, there are no experiment-based estimates for the (n, p) reactions on proton-rich isotopes along the νp -process path. We rely upon the theoretically predicted Hauser–Feshbach rates, which are generally considered to involve uncertainties up to a factor of a few (this reduces to $\sim 40\%$ if the nuclear levels

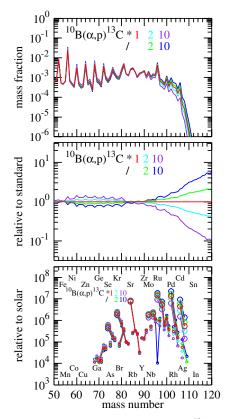


Figure 14. Same as Figure 2, but for variations on the ${}^{10}B(\alpha, p){}^{13}C$ rate. (A color version of this figure is available in the online journal.)

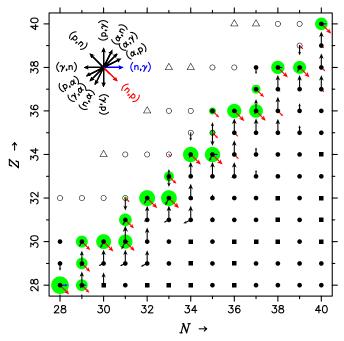


Figure 15. Same as Figure 9, but for the standard model when the temperature decreases to $T_9 = 2.0$.

(A color version of this figure is available in the online journal.)

are well determined and the level densities are large enough, Rauscher et al. 1997). Rauscher (2010) also finds sizable shifts of effective energy windows for (n, p) at high temperature, which might modify these rates. In this subsection, therefore,

^a Proton-to-seed ratio at $T_9 = 3$.

^b Δ_n at $T_9 = 3$.

^c Maximum production factor.

^d Nucleus at $f = f_{\text{max}}$.

^e Nucleus at the largest A with $f > f_{\text{max}}/10$.

f Triple- α rate from Angulo et al. (1999).

¹⁰ We do not take the mirror-mass evaluations of Brown et al. (2002) for Z > N nuclei into account, as the vp-process path is limited to the $Z \le N$ region (except for a flow to ⁵⁹Zn but with measured masses; Figure 15).

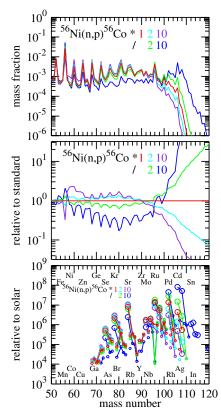


Figure 16. Same as Figure 2, but for variations on the 56 Ni(n, p) 56 Co rate. (A color version of this figure is available in the online journal.)

the sensitivity tests for (n, p) reactions are made with factors of 2 and 10 variations as in Section 5.1.

We here pick up three (n, p) reactions starting from the seed nuclei along the νp -process path, i.e., on 56 Ni, 60 Zn, and 64 Ge. The last one, 64 Ge, is the first β^+ -waiting point nucleus encountered in the classical rp-process path. Note that the variations on these rates do not affect Y_p/Y_h at the onset of the νp -process nor Δ_n (Table 3). All these rates are from theoretical estimates in BRUSLIB (Aikawa et al. 2005) making use of experimental masses (Audi et al. 2003). Our test calculations with the (n, p) rates replaced by those in the REACLIB compilation (Rauscher et al. 2002) are in reasonable agreement (within factor of a few) with our standard case (see also Wanajo et al. 2009).

We find a remarkable change in the p-abundances with $A \sim 110$ by a factor of 10 with only a factor of two variation on 56 Ni(n, p) 56 Co (Figure 16 and Table 3). This demonstrates that the (n, p) reaction on the first (n, p)-waiting nucleus 56 Ni plays a key role for the progress of nuclear flows.

It should be noted that a smaller rate leads to more efficient νp -processing as can be seen in the bottom panel of Figure 16 and in Table 3 (see $f_{\rm max}$ and $A_{\rm max}$). The reason can be explained as follows: Figure 17 extends the nuclear flows in Figure 15. We find that the νp -process path proceeds through even—even Z=N isotopes and deviates from ⁸⁴Mo (Z=N=42) toward Z< N, reaching ⁹⁶Pd on the N=50 shell closure. These isotopes have large abundances during the whole νp -process phase, as can be seen in Figures 15 and 17 (filled green circles). The top panel of Figure 16 shows that the abundances with A=60, 64, 68, 72, 76, 80, and 84 are similar to that of A=96. Table 2 lists the (n,p) rates and decay timescales

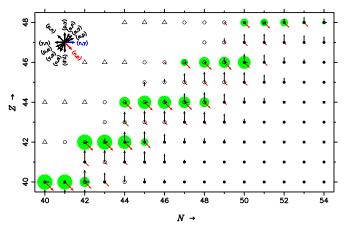


Figure 17. Same as Figure 9, but for the standard model when the temperature decreases to $T_9 = 2.0$.

(A color version of this figure is available in the online journal.)

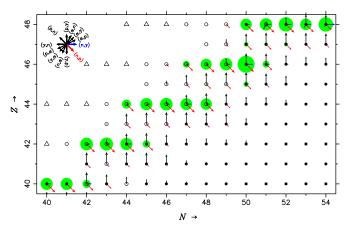


Figure 18. Same as Figure 17, but for the model with the 56 Ni $(n, p)^{56}$ Co rate and its inverse reduced by a factor of 10 (at $T_9 = 2.0$).

(A color version of this figure is available in the online journal.)

for the corresponding isotopes at $T_9 = 2.5$ and 2.0. The (n, p) rates on 56 Ni and 96 Pd, neutron magic nuclei on N = 28 and 50, respectively, are a factor of 4–10 times smaller than the others. This indicates that the free neutrons created by neutrino capture (Δ_n) are preferentially consumed by the even-Z nuclei with $30 \leqslant Z \leqslant 42$ (that act as neutron poisons), rather than by 96 Pd.

A reduction of the 56 Ni(n, p) rate (by a factor of 2 or 10) reduces the abundances of these neutron poisons by a similar factor ($A \sim 60$ –90; Figure 16, middle panel). Despite this, the abundance of 96 Pd does not decrease (even increases). This is due to the faster (n, p) rates for the Z = N (= 30–42) nuclei, causing the nuclear flows from 56 Ni to immediately reach 96 Pd and to stagnate there. As a result, a larger number of free neutrons become available for the 96 Pd(n, p) reaction.

The nuclear flows for the 56 Ni(n, p) rate reduced by a factor of 10 are shown in Figure 18. Smaller abundances of Z = N nuclei 80 Zr and 84 Mo can be seen, which leads to the larger flows beyond N = 50 through 96 Pd. This clearly demonstrates that 96 Pd plays a role as a "second seed nucleus" for producing nuclei heavier than A = 96. In short, a reduction of the 56 Ni(n, p) rate increases the number of free neutrons available for the second seed nuclei of 96 Pd.

Figures 19 and 20 show the results for the second and third (n, p)-waiting nuclei, 60 Zn and 64 Ge (the first β^+ -waiting

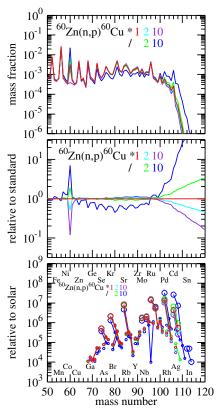


Figure 19. Same as Figure 2, but for variations on the 60 Zn $(n, p)^{60}$ Cu rate. (A color version of this figure is available in the online journal.)

nucleus on the classical rp-process). The variations on these rates also lead to visible changes in the nucleosynthetic p-abundances, being however less prominent than in the case of 56 Ni. Note that a reduced (n, p) rate leads to a larger impact on the nucleosynthetic p-abundances than an increased value of this rate. This is due to the fact that the (n, p) reaction on 56 Ni is substantially slower than those on 60 Zn and 64 Ge (Table 2), where the strength of the nuclear flow is limited by the former reaction.

5.3. Nuclear Masses on the vp-Process Pathway

Nuclear masses on the nucleosynthetic path are fundamental for all the relevant nuclear (or weak) processes. In particular, the flow strength of radiative proton capture during νp -processing $(T_9=3-1.5)$ is mostly determined from proton separation energies, where $(p,\gamma)\leftrightarrow(\gamma,p)$ is generally faster than (n,p) and (n,γ) and thus in a QSE. This explains the concentration of abundances on even-Z isotopes in Figures 8 (left panel; in particular for $Z\leqslant 50$), 9, 15, 17, and 18.

There are a number of isotopes without measured masses in the compilation of Audi et al. (2003) for $40 \le Z \le 50$ (denoted by open circles in Figures 17 and 18), including the parent nuclei of light *p*-nuclei, ⁸⁴Sr, ^{92,94}Mo, and ^{96,98}Ru. Pruet et al. (2006) noted that the unmeasured masses of ⁹²Ru and ⁹³Rh (i.e., the proton separation energy of ⁹³Rh) on the N = 48 isotones are crucial for determining the ratio of ⁹²Mo/⁹⁴Mo.

Recently, Weber et al. (2008) obtained precision measurements of a number of nuclear masses along the νp -process pathway, including those of 92 Ru and 93 Rh. Here, we present the nucleosynthetic result with inclusion of their new masses, denoted by star symbols in Figure 21, with our standard model

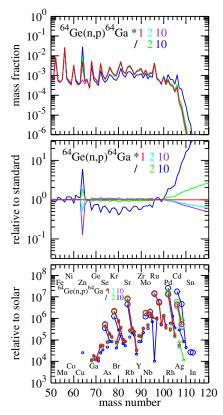


Figure 20. Same as Figure 2, but for variations on the 64 Ge(n, p) 64 Ga rate. (A color version of this figure is available in the online journal.)

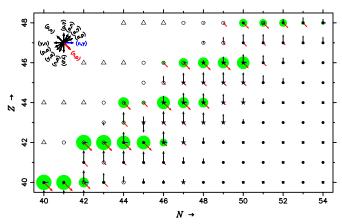


Figure 21. Same as Figure 17, but for the standard model with the new experimental masses of Weber et al. (2008, stars).

(A color version of this figure is available in the online journal.)

(first line in Tables 1 and 3). We confirm the suppression of the flow through $^{87}\text{Mo}(p,\gamma)^{88}\text{Tc}$ (N=45; see Figure 17), which has been reported in Weber et al. (2008). This leads to a factor of three enhancement of ^{87}Sr and a factor of two reduction of ^{89}Y , which are however not p-isotopes (and with small production factors). The other p-abundances, including $^{92,94}\text{Mo}$, are almost unchanged, as reported in Weber et al. (2008) and Fisker et al. (2009)

Our calculations of sensitivity tests for all other unmeasured masses on the νp -process path show that the mass of 82 Zr (or the proton separation energy of 83 Nb) on N=42 plays an important role for production of a light p-nuclei 84 Sr. The others have only minor roles for the sensitivity tests with variations of

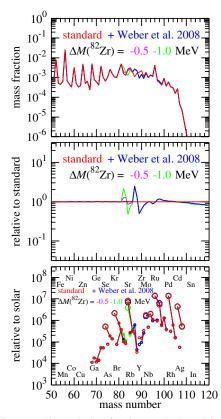


Figure 22. Same as Figure 2, but for the standard model (red) with the new experimental masses of Weber et al. (2008, blue). Also shown are the calculations with reductions (-0.5 and -1.0 MeV) of the 82 Zr mass.

up to ± 1 MeV on the nuclear masses. We find in Figure 22 that a 1.0 MeV reduction of the 82 Zr mass (equivalent to a reduction of the proton separation energy of 83 Nb) leads to a reduction of the 84 Sr abundance by a factor of two (middle panel). An increase of the 82 Zr mass has no effect on the p-abundances.

This is particularly important when we consider the role of the νp -process to the solar inventory of most mysterious p-nuclei, 92 Mo and 94 Mo. As can be seen in Figure 22 (bottom panel, and in other similar figures), the production factors of 92 Mo and 94 Mo are always substantially smaller than the neighboring p-isotopes, in particular, 84 Sr (see Figures 6 and 7). A reduction of the 84 Sr would in part reduce this large gap. Note that the experimental mass of 93 Nb in Audi et al. (2003) involves a large uncertainty (315 keV). Future precision measurements of both 82 Zr and 83 Nb are thus highly desired.

6. vp-PROCESS AS THE ORIGIN OF p-NUCLEI

In the previous sections (Sections 4 and 5), we find that uncertainties in both the supernova dynamics and nuclear reactions can substantially affect the productivity of p-nuclei. This makes it difficult to determine the role of the vp-process as the source of the solar p-nuclei. Keeping such uncertainties in mind, we discuss a possible contribution of the vp-process to the solar p-abundances based on our result by comparing with other possible sources.

Table 4 lists the currently proposed astrophysical origins for each *p*-nuclide (first column) with its solar abundance and fraction relative to its elemental abundance (second and third columns; Lodders 2003). All these sources are associated with core-collapse supernovae. Photodissociation of pre-

existing neutron-rich abundances in the oxygen-neon layer of core-collapse supernovae (or in their pre-collapse phases), i.e., the γ -process (Woosley & Howard 1978; Prantzos et al. 1990; Rayet et al. 1995; Rauscher et al. 2002; Hayakawa et al. 2008) is currently regarded as the most successful scenario. In the fourth column of Table 4, the p-nuclei whose origins can be explained by the γ -process in Rayet et al. (1995) are specified by "yes." The bracketed ones are those underproduced in a more recent work by Rauscher et al. (2002). The origins of up to 24 out of 35 p-isotopes can be explained by the γ -process. However, the light p-isotopes (92,94Mo, 96,98Ru, 102Pd, 106,108Cd, 113In, and 115Sn), which account for a large fraction in the solar p-abundances, and some heavy p-isotopes (138 La and 152 Gd) need other sources (specified by "no" in Table 4).

The ν -process (fifth column in Table 4; Woosley et al. 1990) in core-collapse supernovae is suggested to account for the production of a couple of heavy p-isotopes ¹³⁸La and ¹⁸⁰Ta (the former is underproduced in the γ -process). The α -rich and slightly neutron-rich ($Y_e \approx 0.47-0.49$; slightly more protonrich than the β -stability values) neutrino-driven outflows were also suggested as the production site of some light p-isotopes including ⁹²Mo (but not ⁹⁴Mo; Hoffman et al. 1996; Wanajo 2006; Wanajo et al. 2009). The proton richness relative to the β -stability line in the fragmented QSE clusters (Hoffman et al. 1996; Meyer et al. 1998a) at $T_9 \sim 4-3$ leads to the formation of these p-nuclei with $N \leq 50$. Such QSE clusters on the protonrich side of the β -stability line will be denoted as "p-QSE," hereafter. A recent study of nucleosynthesis in the electroncapture supernovae of a $9 M_{\odot}$ star shows that the lightest p-nuclei ⁷⁴Se, ⁷⁸Kr, ⁸⁴Sr, and ⁹²Mo can be produced in p-QSE enough to account for their solar amounts (sixth column in Table 4; Wanajo et al. 2009). However, these additional sources still cannot fill the gap for some light p-isotopes such as 94 Mo, 96,98 Ru, 102 Pd, 106,108 Cd, 113 In, 115 Sn, and for a heavy p-isotope 152Gd.

Our result in this study is based on a semi-analytic model of neutrino-driven winds, while the results for the γ -process, the ν -process, and the p-QSE listed in Table 4 are all based on realistic hydrodynamic studies. Nevertheless, we attempt to present a list of the p-isotopes whose origin can be attributed to the νp -process, as follows. The requisite overproduction factor for a given nuclide per supernova event, which explains it solar origin, is inferred to be >10 (e.g., Woosley et al. 1994). Assuming the masses of the total ejecta and of the neutrino-driven ejecta to be $\sim 10~M_{\odot}$ and $\sim 10^{-3}~M_{\odot}$ (e.g., Wanajo 2006), the overproduction factor per supernova event is diluted by about four orders of magnitude compared with our result. We thus apply the condition $f > 10^5$ and $f > f_{\rm max}/10$ to each p-isotope abundance in Figure 6 (the standard model with $Y_{\rm e,3}$ ranging between 0.5 and 0.7).

The p-isotopes that satisfy the above condition are listed in the last column of Table 4. According to recent hydrodynamic studies (Fischer et al. 2010; Hüdepohl et al. 2010), the maximum $Y_{\rm e}$ in the neutrino-driven outflows is \sim 0.6. Therefore, the p-isotopes that satisfy the above condition only with $Y_{\rm e,3} > 0.6$ are indicated by "[yes]." This implies that the νp -process in core-collapse supernovae is the possible astrophysical origin of the light p-nuclei up to A=108. In principle, however, the νp -process can account for the origin of the heavy p-isotopes up to A=152 as well, if $Y_{\rm e,3}\approx 0.65$ (Figure 6) is achieved in the neutrino-driven outflows. If this is true, a reasonable combination of the astrophysical sources considered here can explain all the origins of the solar p-isotopes. It should be noted

Table 4 *p*-Nuclei Abundances and Their Possible Sources

Species	Abundance ^a	Fraction ^b (%)	γ-Process ^c	ν-Process ^d	p-QSE ^e	νp-Process ^f
⁷⁴ Se	0.58	0.889	Yes	No	Yes	Yes
⁷⁸ Kr	0.20	0.362	Yes	No	Yes	Yes
⁸⁴ Sr	0.13124	0.5551	Yes	No	Yes	Yes
⁹² Mo	0.386	14.8362	No	No	Yes	Yes
⁹⁴ Mo	0.241	9.2466	No	No	No	Yes
⁹⁶ Ru	0.1053	5.542	No	No	No	Yes
⁹⁸ Ru	0.0355	1.8688	No	No	No	Yes
¹⁰² Pd	0.0146	1.02	No	No	No	Yes
¹⁰⁶ Cd	0.01980	1.25	No	No	No	Yes
¹⁰⁸ Cd	0.01410	0.89	No	No	No	Yes
¹¹³ In	0.0078	4.288	No	No	No	[Yes]
¹¹² Sn	0.03625	0.971	[Yes]	No	No	[Yes]
¹¹⁴ Sn	0.02460	0.659	[Yes]	No	No	[Yes]
¹¹⁵ Sn	0.01265	0.339	No	No	No	[Yes]
¹²⁰ Te	0.0046	0.096	[Yes]	No	No	[Yes]
¹²⁴ Xe	0.00694	0.129	[Yes]	No	No	[Yes]
¹²⁶ Xe	0.00602	0.112	Yes	No	No	[Yes]
¹³⁰ Ba	0.00460	0.1058	Yes	No	No	[Yes]
¹³² Ba	0.00440	0.1012	Yes	No	No	[Yes]
¹³⁸ La	0.000397	0.09017	No	Yes	No	[Yes]
¹³⁶ Ce	0.00217	0.186	Yes	No	No	[Yes]
¹³⁸ Ce	0.00293	0.251	Yes	No	No	[Yes]
¹⁴⁴ Sm	0.00781	3.0734	Yes	No	No	[Yes]
¹⁵² Gd	0.00067	0.2029	No	No	No	[Yes]
¹⁵⁶ Dy	0.000216	0.056	[Yes]	No	No	No
¹⁵⁸ Dy	0.000371	0.096	[Yes]	No	No	No
¹⁶² Er	0.000350	0.137	[Yes]	No	No	No
¹⁶⁴ Er	0.004109	1.609	[Yes]	No	No	No
¹⁶⁸ Yb	0.000323	0.13	Yes	No	No	No
¹⁷⁴ Hf	0.000275	0.1620	Yes	No	No	No
¹⁸⁰ Ta	0.00000258	0.0123	Yes	Yes	No	No
^{180}W	0.000153	0.1198	Yes	No	No	No
¹⁸⁴ Os	0.000133	0.0198	Yes	No	No	No
¹⁹⁰ Pt	0.000185	0.013634	Yes	No	No	No
¹⁹⁶ Hg	0.00063	0.15344	Yes	No	No	No

Notes.

that most of the maximum production factors of these heavy p-nuclei are $\gtrsim 10^8$. This is three orders of magnitude larger than the above requisite value ($f=10^5$). Thus, only $\sim 0.1\%$ of neutrino-driven ejecta with $Y_{\rm e,3}\approx 0.60$ –0.65 is enough to account for the origin of these heavy p-nuclei. Future multi-dimensional hydrodynamic studies of core-collapse supernovae with full neutrino transport will be of particular importance if such a condition is indeed obtained.

A word of caution for the molybdenum isotopes is needed here. The production factors of 92 Mo and 94 Mo satisfy the above condition only marginally with $Y_{\rm e,3}=0.53-0.54$. The future measurements of the nuclear masses of 82 Zr and 83 Nb might in part cure this problem as discussed in Section 5.3. This is rather serious for the origin of 94 Mo that can be produced only by the νp -process, while 92 Mo can be explained by the p-QSE. Fisker et al. (2009) concluded that the ratio 92 Mo/ 94 Mo is about five times smaller than the solar value, when applying the proton separation energy of 93 Rh in Weber et al. (2008). This might imply that 92 Mo has another origin, presumably the p-QSE. We

however obtain a reasonable ratio with our standard model (see, e.g., the bottom panel of Figure 22) and many other cases (see the $Y_{\rm e,3} \leqslant 0.55$ range in Figure 6). This is due to the significant role of $^{92}{\rm Ru}(n,\,p)^{92}{\rm Tc}$ that competes with $^{92}{\rm Ru}(p,\,\gamma)^{93}{\rm Rh}$ in our cases. This is a consequence of the values of $\Delta_{\rm n}$ in the present cases being about a factor of three higher than those in Pruet et al. (2006). This suggests that $^{92}{\rm Mo}/^{94}{\rm Mo}$ is highly sensitive to the details of supernova dynamics.

7. SUMMARY

We investigated the effects of uncertainties in supernova dynamics as well as in nuclear data inputs on the νp -process in the neutrino-driven outflows of core-collapse supernovae. The former includes the wind-termination radius $r_{\rm wt}$ (or temperature $T_{\rm wt}$), neutrino luminosity L_{ν} , neutron-star mass $M_{\rm ns}$, and electron fraction $Y_{\rm e,9}$ (or $Y_{\rm e,3}$, at $T_9=9$ and 3, respectively). The latter includes the reactions relevant to the breakout from the p-p chain region (A<12), the (n,p) reactions on heavy

^a Lodders (2003); $Si = 10^6$.

^b Lodders (2003); relative to its elemental abundance.

^c Rayet et al. (1995) (nuclei indicated by "[yes]" are those underproduced in Rauscher et al. 2002).

^d Woosley et al. (1990).

e Wanajo et al. (2009).

^f This work (nuclei indicated by "[yes]" are produced only with $Y_{e,3} > 0.6$).

nuclei ($Z \ge 56$), and the nuclear masses ($40 \le Z \le 50$) on the νp -process pathway. Our result is summarized as follows.

- 1. Wind termination of the neutrino-driven outflow by colliding with the preceding supernova ejecta causes a slowdown of the temperature decrease and thus plays a crucial role on the νp -process. The termination within the temperature range of $T_9=1.5-3$ (relevant to the νp -process) substantially increases the number of neutrons captured by the seed nuclei (Δ_n) and thus enhances efficiency of the p-nuclei production. In the current case, the efficiency is maximal at $T_{\rm wt,9}=2.65$ ($r_{\rm wt}=231$ km for $L_{\nu}=10^{52}$ erg s⁻¹). This implies that the early wind phase with the termination radius close to the proto-neutron star surface is favored for the νp -process.
- 2. A lower L_{ν} (with the other parameters $T_{\rm wt}$, $M_{\rm ns}$, and $Y_{\rm e,9}$ unchanged) leads to more efficient νp -processing. This is due to the larger entropy per nucleon for a lower L_{ν} , which increases the proton-to-seed ratio $Y_{\rm p}/Y_{\rm h}$ and thus $\Delta_{\rm n}$. However, the role of the wind termination is more crucial and thus we presume that the maximum efficiency is obtained during the early phase with $L_{\nu} \sim 10^{52}$ erg s⁻¹.
- 3. A larger $M_{\rm ns}$ (with the other parameters $T_{\rm wt}$, L_{ν} , and $Y_{\rm e,9}$ unchanged) results in a larger efficiency of the νp -process. This is a consequence of the larger entropy per nucleon and the faster expansion of the neutrino-driven outflow for a larger $M_{\rm ns}$, both of which help to increase $Y_{\rm p}/Y_{\rm h}$ and thus $\Delta_{\rm n}$. This implies that a more massive progenitor is favored for more efficient νp -processing, if other parameters remain unchanged. In reality, however, the evolutions of L_{ν} , $r_{\rm wt}$, and $Y_{\rm e}$ will be dependent on the progenitor mass, making it difficult to draw definitive conclusions.
- 4. The νp -process is highly sensitive to the electron fraction $Y_{\rm e,3}$ that controls $Y_{\rm p}/Y_{\rm h}$ at the onset of the νp -process and thus $\Delta_{\rm n}$. An increase of only $\Delta Y_{\rm e,3} \sim 0.03$ results in $\Delta A_{\rm max} \sim 10$. The models with $Y_{\rm e,3} = 0.52$ –0.60 (with the other parameters unchanged) produce sufficient amounts of the light p-nuclei up to A = 108. Furthermore, the models with $Y_{\rm e,3} = 0.60$ –0.65 produce the p-nuclei up to A = 152. Note that this is a combined effect of the high $Y_{\rm e,3}$ and the wind termination at sufficiently high temperature ($T_{\rm wt,9} = 2.19$ in the standard model). Our result shows no substantial enhancement of the p-nuclei with A > 152, since the nuclear flow reaches the β -stability line and enters to the neutron-rich region at $A \sim 130$ –160. This is a consequence that a large $\Delta_{\rm n}$ leads to the strong (n, γ) flows that compete with those by (p, γ) for Z > 50.
- 5. Variations on the nuclear reactions relevant to the breakout from the p–p chain region (A < 12), namely, of triple- α , $^7\mathrm{Be}(\alpha,\gamma)^{11}\mathrm{C}$, and $^{10}\mathrm{B}(\alpha,p)^{13}\mathrm{C}$ affect the νp -process by changing Y_p/Y_h (and Δ_n) or producing intermediate-mass nuclei (proton poison) during νp -processing. Among these reactions, triple- α has the largest impact, although the other two show non-negligible effects, on the production of the p-nuclei at $A \sim 100$ –110.
- 6. Variations on the (n, p) reactions on ⁵⁶Ni (seed nuclei), ⁶⁰Zn, and ⁶⁴Ge (first β^+ -waiting point on the classical rp-process) show great impact on efficiency of the νp -process for heavy element synthesis. Only a factor of two variation leads to a factor of 10 or more changes in the production of the p-nuclei with $A \sim 100$ –110 for the first reaction (but somewhat smaller changes for the latter two reactions). This is a consequence of the fact that these reactions control the strength of the nuclear flow passing

- through the (n, p)-waiting points (56 Ni, 60 Zn, and 64 Ge) on the νp -process path. We also find that the N=50 nucleus 96 Pd plays a role of the "second seed" for production of heavier nuclei.
- 7. Application of the new experimental masses of Weber et al. (2008; for $39 \le Z \le 46$) exhibits a suppression of the flow ⁸⁷Mo(p, γ)⁸⁸Tc (N=45), which, however, does not affect the nucleosynthetic p-abundances. Our sensitivity tests for unmeasured nuclear masses indicate that a future measurement of the ⁸²Zr mass (and of ⁹³Nb with a large estimated error) on N=42 could reduce the abundance of ⁸⁴Sr by a factor of two.
- 8. Our result implies that, within possible ranges of uncertainties in supernova dynamics as well as in nuclear data inputs, the solar inventory of the light p-nuclei up to A = 108 (108 Cd) can be attributed to the vp-process, including the most mysterious ones, 92,94 Mo and 96,98 Ru. The molybdenum isotopes, however, tend to be underproduced compared with the neighboring p-isotopes. If highly proton-rich conditions with $Y_{\rm e,3} = 0.60$ –0.65 are realized in neutrinodriven ejecta, the solar origin of the p-nuclei up to A = 152 (152 Gd) can be explained by the vp-process.

Our explorations in this study suggest that more refinements both in supernova conditions and in nuclear data inputs are needed to elucidate the role of the νp -process as the astrophysical origin of the p-nuclei. In particular, multi-dimensional studies of core-collapse simulations with full neutrino transport, as well as experiment-based rates of triple- α and the (n, p) reactions on heavy nuclei will be important in the future works.

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