

Understanding Movement Data Quality

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Abstract

Understanding of data quality is essential for choosing suitable analysis methods and interpreting their results. Investigation of quality of movement data, due to their spatio-temporal nature, requires consideration from multiple perspectives at different scales. We review the key properties of movement data and, on their basis, create a typology of possible data quality problems and suggest approaches to identifying these types of problems.

Keywords: Movement data, data quality, visual analytics

1. Introduction: Position Recording

Analysis of movement data is of high relevance in various application domains of data science. As for any analysis, appropriate data preparation, including investigation of the data quality, data cleaning, and error correction, is essential. Data preparation is typically the most time-consuming step in the analysis (Pyle 1999).

Movement data consist of records containing identifiers of moving entities (also called movers), geographic and temporal references, and, possibly, other attributes, called thematic. A chronologically ordered sequence of position records of the same mover (i.e., with the same mover identifier) is called a trajectory of this mover. Thematic attributes may characterize the movement itself (e.g., the velocity and direction) or the context in which the movement occurs (e.g., the air temperature). Such attributes can be originally present in the data or derived from the records of the same trajectory, other trajectories, and other relevant data (Andrienko et al. 2013b).

Evaluation and preparation of movement data requires particular diligence due to their inherent complexity and the variation of properties related to the diversity of the existing methods of data acquisition. Abstracting from the various specific technologies for collecting movement data, we identify several major methods of position recording (Andrienko et al. 2008):

- Time-based: positions of movers are recorded at regularly spaced time moments.
- Change-based: a record is made when mover's position, speed, or movement direction differs from the previous one.
- Location-based: a record is made when a mover enters or comes close to a specific place, e.g. where a sensor is installed.
- Event-based: positions and times are recorded when certain events occur, in particular, when movers perform certain activities, such as cellphone calls or posting georeferenced contents to social media.
- Combinations of these basic approaches. In particular, GPS tracking devices may combine time-based and change-based recording: the positions may be measured at regular time intervals but recorded only when significant changes of position, speed, or direction occur.

In the following, we review the properties of movement data, potential quality problems, and the consequent implications and constraints for analysis and modeling. In the long-term perspective, we aim at defining general rules and procedures for assessing movement data quality. This paper makes first steps towards this goal by systematically considering relevant properties of movement data (section 2) and, based on that, identifying the expectable problems and errors (section 3), divided into three major categories: missing data, accuracy errors, and precision errors. These categories are considered in more detail in sections 4, 5, and 6, respectively. We conclude the paper by considering the role of data transformations and identifying directions for further work.

2. Properties of Movement Data

In analyzing movement data, it is important to take into account their structure and properties

(Andrienko et al. 2013a). The first group of properties relates to the data structure:

- Mover set properties:
 - number of movers: a single mover, a small number of movers, a large number of movers;
 - population coverage: whether there are data about all movers of interest for a given territory and time period or only for a sample of the movers;
 - representativeness: whether the sample of movers is representative, i.e., has the same distribution of properties as in the whole population, or biased towards individuals with particular properties.

- Spatial properties:
 - spatial resolution: what is the minimal change of position of an object that can be reflected in the data?
 - spatial precision: are the positions defined as points or as locations having spatial extents (e.g. areas)? For example, the position of a mobile phone call is typically a cell in a mobile phone network;
 - position exactness: how exactly could the positions be determined? Thus, a movement sensor may detect an object within its range but may not be able to determine the exact coordinates of the object within its detection area. The object position may be specified as a point, but, in fact, it is the position of the sensor and not the object's true position;
 - positioning accuracy: how much error may be in the measurements?

- spatial coverage: are positions recorded everywhere or, if not, how are the locations where positions are recorded distributed over the studied territory (in terms of the spatial extent, uniformity, and density)?
- Temporal properties:
 - temporal resolution: the lengths of the time intervals between the position measurements;
 - temporal regularity: whether the length of the time intervals between the measurements is constant or variable for selected movers and for the whole data set;
 - temporal coverage: whether the measurements were made during the whole time span of the data or in a sample of time units, or there were intentional or unintentional breaks in the measurements;
 - time cycles coverage: whether all positions of relevant time cycles (daily, weekly, seasonal, etc.) are sufficiently represented in the data, or the data refer only to subsets of positions (e.g., only work days or only daytime), or there is a bias towards some positions.

The 2nd group relates to the data collection procedure:

- Data collection properties:
 - position exactness: How exactly could the positions be determined? Thus, a movement sensor may detect an object within its range but may not be able to determine the exact coordinates of the object within its detection area. In this case, the position of the sensor stands in for the object's true position;
 - positioning accuracy, or how much error may be in the measurements;
 - missing positions: in some circumstances, object positions cannot be determined, leading to gaps in the data;

- meanings of the position absence: whether absence of positions corresponds to stops, or to conditions when measurements were impossible, or to device failure, or to private information that has been removed.

These properties of movement data are strongly related to the data collection methods. Thus, only time-based measurement produces temporally regular data. The temporal resolution may depend on the capacities and/or settings of the measuring device. GPS tracking, which may be time-based or change-based, typically yields very high spatial precision and quite high accuracy¹ while the temporal and spatial resolution depends on the device settings. The spatial coverage of GPS tracking is very high (almost complete) in open areas. Location-based and event-based recordings usually produce temporally irregular data with low temporal and spatial resolution and low spatial coverage. The spatial precision of location-based recordings may be low (positions specified as areas) or high (positions specified as points), but even in the latter case the position exactness is typically low. The spatial precision of event-based recording may be high while the accuracy may vary (cf. positions of photos taken by a GPS-enabled camera or phone with positions specified manually by the photographer).

Irrespectively of the collection method and device settings, there is also indispensable uncertainty in movement data (and, more generally, any time-related data) caused by their discreteness. Since time is continuous, the data cannot refer to every possible instant. For any two successive instants t_1 and t_2 referred to in the data there are moments in between for which there are no data. Therefore, one cannot know definitely what happened between t_1 and t_2 . Movement data with fine temporal and spatial resolution give a possibility of interpolation, i.e., estimation of object positions between the measured positions. In this way, the continuous path of the mover can be approximately reconstructed.

¹ GPS: Error analysis for the Global Positioning System.

http://en.wikipedia.org/wiki/Error_analysis_for_the_Global_Positioning_System

Movement data that do not allow valid interpolation between subsequent positions are called episodic (Andrienko et al. 2012). Episodic data are usually produced by location-based and event-based collection methods but may also be produced by time-based methods when the position measurements cannot be done sufficiently frequently, for example, due to the limited battery lives of the recording devices. Thus, when tracking movements of wild animals, ecologists have to reduce the frequency of measurements to be able to track the animals over longer time periods.

Whatever the measurement frequency is, there may be time gaps between recorded positions that are longer than usual or expected according to the device settings, which means that some positions may be missing. In data analysis, it is important to know the meaning of the position absence: whether it corresponds to absence of movement, or to conditions when measurements were impossible (e.g., GPS measurements in a tunnel), or to device failure, or to private information that has been intentionally removed.

Another set of properties of movement data is related to the physics of the moving objects and the character of their movement. These properties seriously affect the choice of the methods for data pre-processing, transformation, visualization and analysis:

- Whether positions can be considered as two-dimensional, or the third dimension (altitude or depth) is essential.
- Whether the data represent constrained or free movement. When the movement is constrained, e.g., by a street network, there are better possibilities for detecting and correcting positioning errors and for reducing position uncertainties.
- Whether movements may contain abrupt changes of the spatial position in very short time. For example, a pertinent property of eye movement is the presence of instantaneous jumps (saccades) over relatively long distances (Dodge et al. 2008, 2009). Intermediate points between start and

end positions of a saccade are not meaningful: it cannot be assumed that there exists a straight or curved line between two fixation positions such that the eye focus travels along it attending all intermediate points. This prohibits the use of any method involving interpolation between positions.

3. Typology of movement data quality problems

There are three major categories of problems that may exist in any kind of data: *missing data*, *accuracy problems*, and *precision deficiency*. For movement data, these general categories may be specialized in terms of the data components: identities of movers, spatial positions, time references, and thematic attributes.

When any of the main components (i.e., mover identifier, spatial position, or time reference) is *missing* in a data record, this record cannot be used in constructing a trajectory; hence, the absence of one of the main components is equivalent to the absence of the entire position record. Missing values of thematic attributes do not have so dramatic impact. Problems arise only in particular analyses requiring these attributes to be involved. In the following, we shall consider only the cases of missing records.

Accuracy problems (i.e., wrong values, or errors) may occur to any of the movement data components.

Precision deficiency problems may occur to spatial positions, time references, and thematic attributes.

Imprecise mover identifiers are equivalent to wrong identifiers: in both cases, position records cannot be correctly grouped into trajectories of movers.

Hence, for movement data, the specific types of possible problems are: missing position records (abbreviated as M), accuracy problems affecting mover identifiers, spatial positions, time references, and thematic attributes (AM_v, AS, AT, and AAt, respectively), and precision deficiency for spatial positions, time references, and thematic attributes (PS, PT, and PAt).

The scope of problem spread in a dataset can be evaluated from different perspectives. For a single trajectory, problems may occur in some position records, in subsequences of records (segments of the trajectory), or in the whole trajectory. Adapting Bertin (1983) terminology, we call such problems elementary, intermediate, and overall, respectively, and abbreviate as TrE, TrI, and TrO.

Furthermore, the spread of a problem may be characterized with regard to the value domains of the three main components, i.e., the set of movers M_V , space (set of locations) S , and time (set of moments) T . Problems may refer to individual movers, locations, and moments (elementary level $M_V E$, SE , and TE), to groups of movers, areas in space, or periods in time (intermediate level $M_V I$, SI , and TI), or to the entire set of movers, whole territory, and whole time span of the data (overall level $M_V O$, SO , and TO). Assuming one-to-one correspondence between the movers and trajectories, the problem spread over the mover set means the spread over the set of trajectories.

In evaluating the quality of a given dataset, an analyst needs to check, for each problem type, whether it exists in the data and, if so, determine the scope of the problem spread in the trajectories and over the value domains of the three main components.

In the following sections, we shall consider in more detail the problems of missing position records, inaccuracy (errors), and insufficient precision. We shall discuss the possible scopes of the spread of such problems in relation to their possible reasons, propose approaches to problem detection and scope evaluation, and give prominent examples of problems encountered in various real datasets.

4. Missing Position Records

The main focus of this section is consideration of the possible spread of the missing data problem over the space and time. In this relation, we shall also touch upon the problem spread within trajectories and over the set of movers.

4.1. Spatial spread

Missing position records within trajectories are signified by spatio-temporal gaps between available records, i.e., where the spatial and/or temporal distances between consecutive records are larger than usual or expected. This class of problems may be represented as M: TrE/I, where TrE/I means that occasional positions in a trajectory (TrE) or trajectory segments (TrI) may be missing. Trajectory segments with large spatial and/or temporal distances between consecutive positions can be extracted from a set of trajectories by means of threshold-based filtering. To analyze the spatial spread and find the possible reason for the problem, the extracted segments are visualized on a map, which will show either spatial scattering or concentration of the gaps.

When the extracted gaps are scattered over space (which means the elementary level of the spatial spread M:SE), a possible reason may be occasional failures of measuring devices. When the gaps are concentrated in particular parts of space (areas or segments of a transportation network), i.e., the level of the spatial spread is intermediate (M:SI), a possible reason may be impossibility of position measuring in these parts of space, e.g., GPS positioning is impossible in covered spaces. Another possible reason may be a particular way of data filtering. For example, a subset of data may be extracted from a larger data set by setting a bounding rectangle covering some area of interest. Figure 1 demonstrates a case when a data provider just removed all positions that lied beyond the bounding rectangle. This lead to specific cases of data absence when cars temporarily moved out of the area enclosed by the rectangle and returned back after few minutes. When trajectories are represented on a map by lines, the trajectory lines of these cars have unrealistic straight segments connecting the last position before leaving the rectangular area and the first position after returning back. Trajectory segments corresponding to cutting-caused gaps are spatially concentrated at the edges of the studied area. In Figure 1, only the affected trajectories are shown; the segments of the trajectories are colored according to the spatial distance between consecutive points.



Figure 1. Segments are missing in many trajectories due to cutting of the data by a bounding rectangle.

In case of location-based recording, measuring devices are only present in particular locations; therefore, spatio-temporal gaps between records occur in all other parts of the territory. The degree of the spatial spread can be characterized as overall (SO). The same applies to event-based recording: gaps, which occur due to the absence of events during long time intervals, can be distributed over the whole space. In episodic movement data resulting from such methods of measurement, spatio-temporal gaps are usual and pertinent to whole trajectories of all movers, which can be represented as $M: TrO \cup MvO \cup SO \cup TO$. Only in some cases, intermediate positions can be estimated using additional data sets such as street network and speed limits.

In time-based recording, the spatial distances between position records depends on the movement speed. If the speed is high, spatial (but not spatio-temporal) gaps may emerge. This problem refers to parts of trajectories where the speed is high and to the intermediate or overall level with regard to the mover set, space, and time ($M: TrE/I \cup MvI/O \cup SI/O \cup TI/O$), depending on the movers' capacities to develop high speed and the possibilities of fast movement in different parts of space and at different times. Often, missing positions can be restored by interpolation.

In change-based recording, parameter settings may cause systematic omissions of position records. For example, a GPS tracker may skip mover's positions during straight-line movement with constant speed when the distance to the last recorded position is below a certain distance threshold. Such data property can be identified by plotting trajectory points according to the changes of their coordinates (δ_x, δ_y) with respect to the previous points. An example is shown in Fig. 2. The circular area of low point density in the center of the graph has the radius of 20 meters, which reveals the value of the filter threshold. Positions missed due to such straight-line filtering can be quite easily restored by linear interpolation. The scope of the problem may be represented as $M: TrE/TrI \cup MvO \cup SI \cup TO$, where SI means that problems occur in particular parts of space where straight line movement is possible.

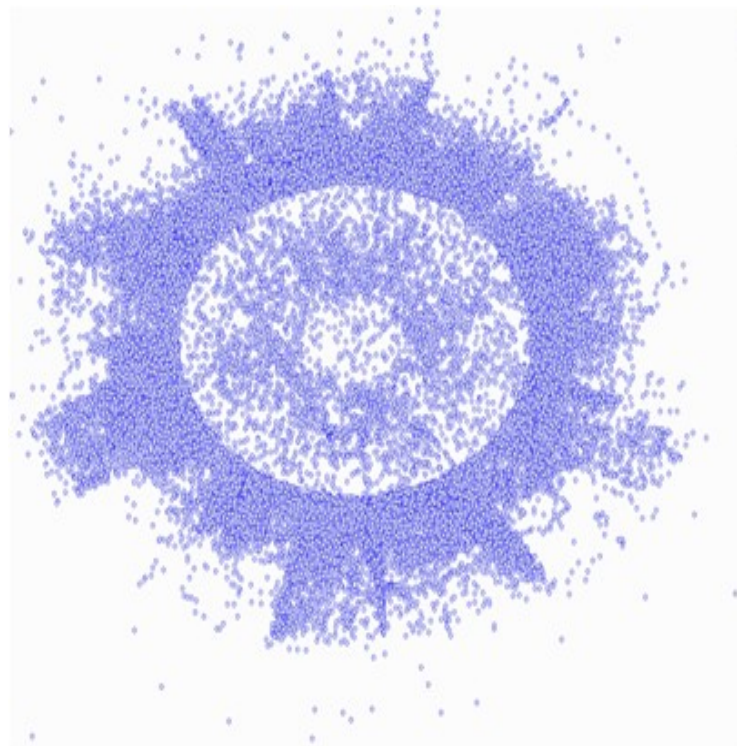


Figure 2. A plot of coordinate changes (δ_x, δ_y) in respect to the previous trajectory points reveals an effect of filtering.

4.2. Temporal spread

To investigate the spread of the missing data problem over time, it is necessary to use temporal displays,

such as a temporal histogram demonstrated in Figure 3. The data used for this example are mobile phone activation records, where the positions are specified by references to antennas of a telecommunication network. The data have been aggregated by the antennas and daily intervals. Each bar of the histogram corresponds to one day; the bars are chronologically ordered. The whole height of each bar corresponds to the whole set of antennas, and the height of a dark blue segment is proportional to the number of antennas for which there are no phone activation records for the day corresponding to the bar. The other segment colors correspond to different numbers of records per antenna and day; the shades of blue represent low numbers and the shades of red high numbers.

An absence of records referring to some antenna during a time interval corresponds to spatio-temporal gaps (missing segments) in trajectories of movers that might have used or attempted to use their phones within the antenna range during that time interval (M: TrI). The histogram in Fig. 3 shows that every day records were missing for some antennas; moreover, the number of antennas with missing data was monotonously increasing over time, except for the last two weeks. Besides, there were days when the numbers of antennas with no or few records (shades of blue) were especially high. The level of the temporal spread of the missing data problem in this dataset can be characterized as overall (M: TO) and the level of the spatial spread as intermediate (M: SI), since subsets of the set of locations (i.e., antenna cells) are affected. The problem, evidently, affects large groups of movers (M: MvI). The whole formula is $M: TrI \cup MvI \cup SI \cup TO$.

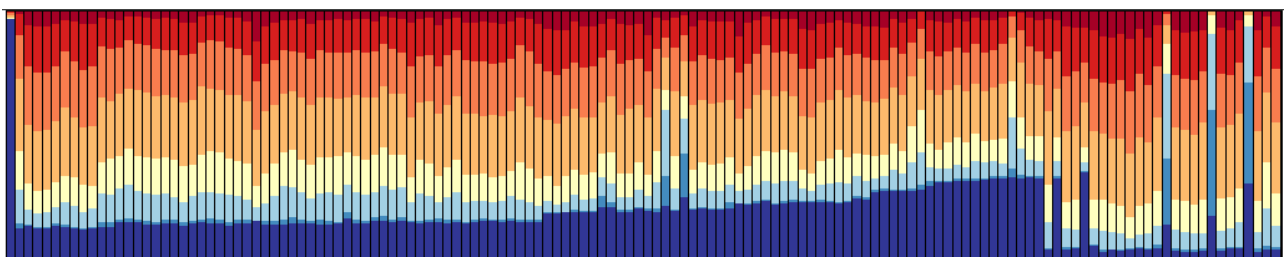


Figure 3. The bars of a time histogram correspond to daily intervals, and the dark blue segments show the numbers of antenna cells with missing data.

Additionally to the distribution of a problem (missing data or any other type) over the time span of the data considered as a linear sequence of time moments, it is appropriate to investigate how the problem is distributed with regard to relevant time cycles, such as daily, weekly, and yearly. Thus, gaps in data may occur or be especially frequent in particular times of a day and/or days of a week. To detect such temporal patterns of problem spread, histograms as in Fig. 3 can be built for relevant time cycles.

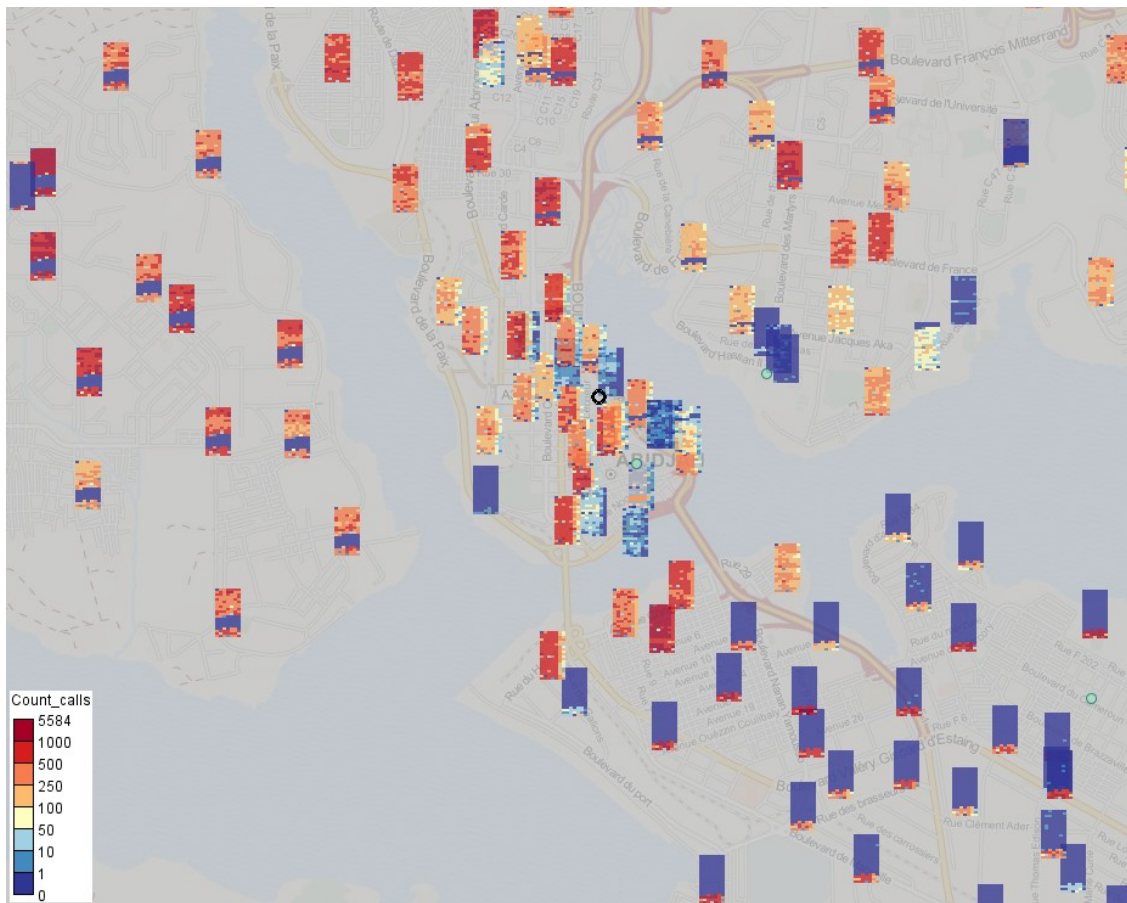


Figure 4. A map with mosaic diagrams represents the same data as in Figure 3. The diagrams placed at the antenna positions show the daily record numbers for the antennas. The dark blue pixels represent days with no records.

4.3. Spatio-temporal spread

It is insufficient to consider the distribution of a problem over space and over time separately. It may

happen that problem occurred at different times in different parts of space. To check whether this is the case, the analyst can use a map with diagrams showing the problem occurrences over time at different locations or in different areas. An example is demonstrated in Fig. 4, where the map represents the same data as in Fig. 3. The mosaic diagrams represent counts of recorded mobile phone activations at different antennas by days. Each day is represented by a colored pixel. The pixels within a diagram are arranged in rows with columns correspond to days of the week (Monday to Sunday), for a total of 20 rows matching the 20-week time span of the data. Dark blue pixels correspond to zero counts, i.e., absence of phone activation records for the given day. It can be seen that on the south the data are available only for the last two weeks. On the west, there are several consecutive weeks with missing data. Time gaps are also noticeable for some antennas on the northeast. In the center of the territory, there is an antenna (highlighted) with no records on the weekends.

5. Accuracy problems

5.1. Mover identity errors

Trajectories of movers are constructed by uniting consecutive positions of each mover. The positions of different movers are distinguished based on the identifiers contained in the position records. Hence, each mover needs to have a unique identifier. However, this condition may not always hold. Two kinds of mover identity errors are possible: (1) the use of the same identifier for two or more different movers and (2) the use of different identifiers for the same mover. If two distinct movers have the same identifier, their positions will be mixed in one trajectory. This is especially well noticeable when the movers move simultaneously. An example is demonstrated in Figure 5. The cases of occasionally duplicated mover identifiers can be recognized from unrealistic values of derived speeds and/or unusually long spatial distances between consecutive positions. Identification of such errors can be supported by calculation of aggregates such as travelled path or average speed. However, when positions

of different movers with the same identifier are separated in time, the duplication of the identifier may be undetectable. Cases of occasional duplication of mover identifiers may be represented as AMv: MvE.

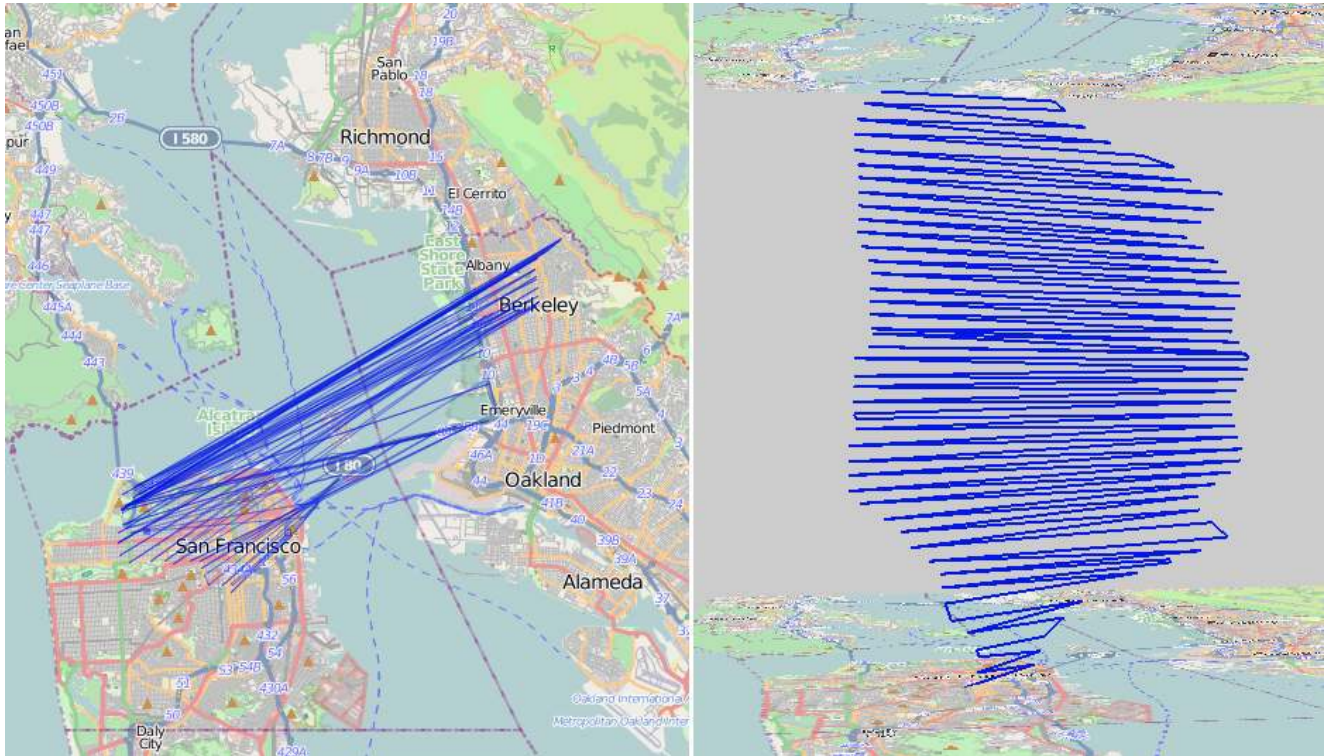


Figure 5. Positions of two distinct movers with the same identifier have been mixed in one trajectory, which therefore has a zigzag shape.

Identifiers given to movers are not necessarily kept constant throughout the whole time of data collection. For preserving personal privacy or other reasons (e.g., hiding sensitive repeated patterns in business-related movement data), movers may be assigned new identifiers at certain time intervals, e.g., every day or every two weeks. The previous identifiers may be reused for different movers. Moreover, in different time intervals, the data may correspond to different samples of the population. Hence, in such cases, both problems arise: same identifiers may be used for different movers and different identifiers for same movers. The problems affect the whole set of movers (AMv: MvO). Such problems can be discovered by exploring the trajectories constructed from the records with coinciding mover

identifiers. Assignments of previously used identifiers to new movers will be manifested by unusually long jumps in space occurring in many trajectories at regular time intervals. An example is shown in a space-time cube in Figure 6, where a sample of trajectories is drawn with 1% opacity. Bunches of long near-horizontal lines occur every two weeks. It is very unlikely that they reflect real movements; most probably, they reflect re-assignments of mover identifiers. A case when old identifiers are not reused but new unique identifiers are assigned to movers can be recognized from the statistics of trajectory durations. The maximal duration will not exceed the length of the time interval between the changes of the identifiers.

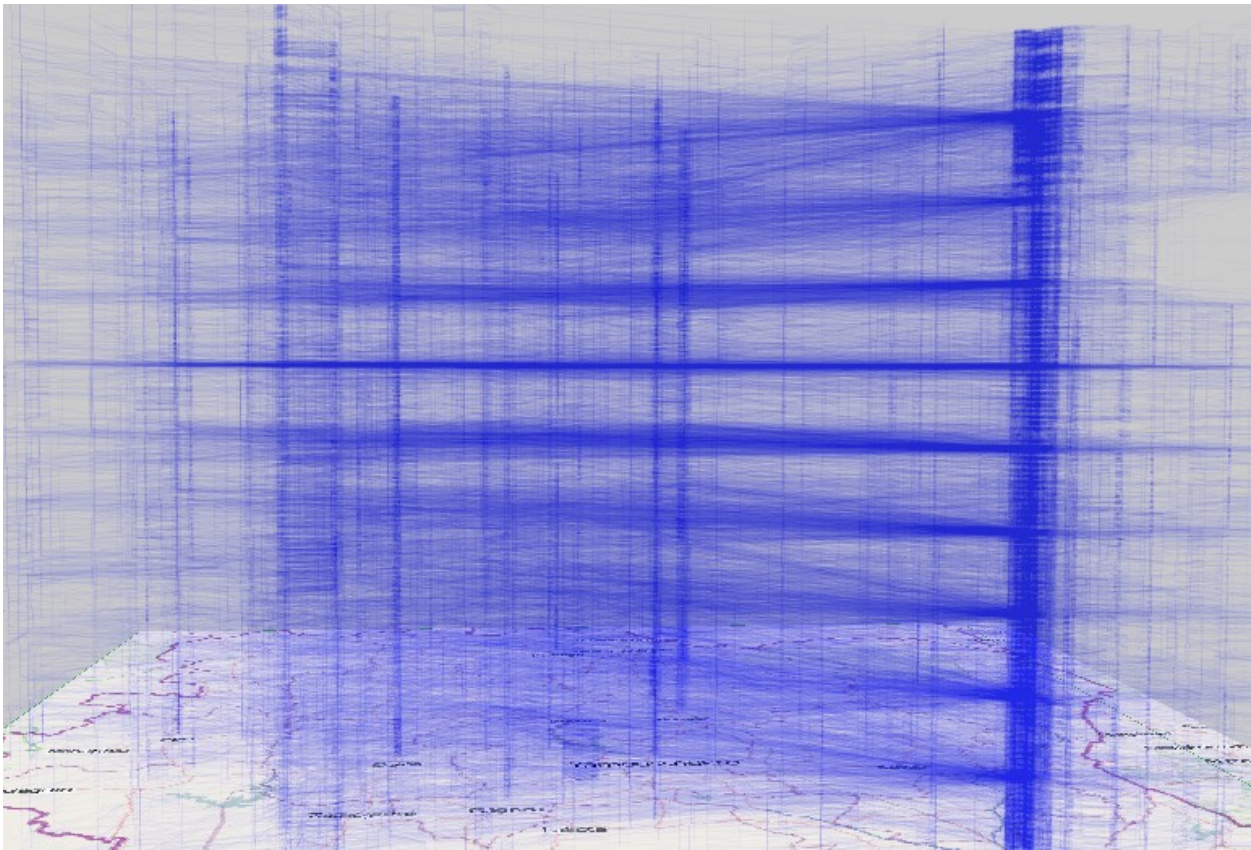


Figure 6. Long “jumps” in multiple trajectories indicate re-assignments of mover identifiers.

5.2. Spatial errors

Spatial accuracy problems are often caused by malfunctioning positioning devices or difficult conditions for measurements. Thus, GPS positioners need to establish connections with several satellites, which takes time. During this time, the recorded positions, if any, may be inaccurate. If such a device is turned on only when a trip begins, the departure position of the trip and the trajectory segment representing the initial part of the trip may be missing or wrong (Figure 7). This case may be represented by the formula $M \cup AS: TrI$. The spread of the problem over the set of movers, space, and time depends on how many movers and for how long were tracked by such devices and whether the data reflect repeated trips of the movers.

Figure 8 demonstrates another example, where the spatial positions in a whole trajectory, shown in red, are erroneous (AS: TrO), combining noise (jitter) with a systematic shift to the northwest with regard to the true positions. The shift was detected by comparing the spatial footprints of different trajectories available in the dataset. In this dataset, only one trajectory was erroneous (AS: $TrO \cup MvE$).

Jitter may also occur in parts of trajectories corresponding to stops or movement with low speed. In such conditions, GPS readings may be inaccurate. Very often stops appear in data as fake jittered movement (Figure 9). Such problems may occur in segments of many or all trajectories (AS: $TrI \cup MvI/O$).

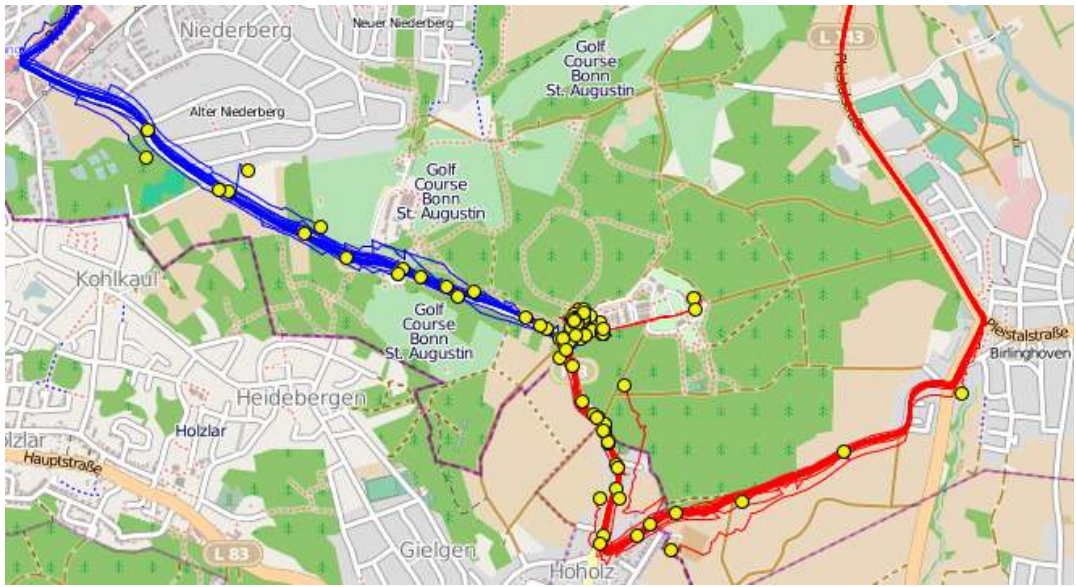


Figure 7. The starting parts of many trips are missing. The yellow dot symbols show the recorded positions of the trip starts.

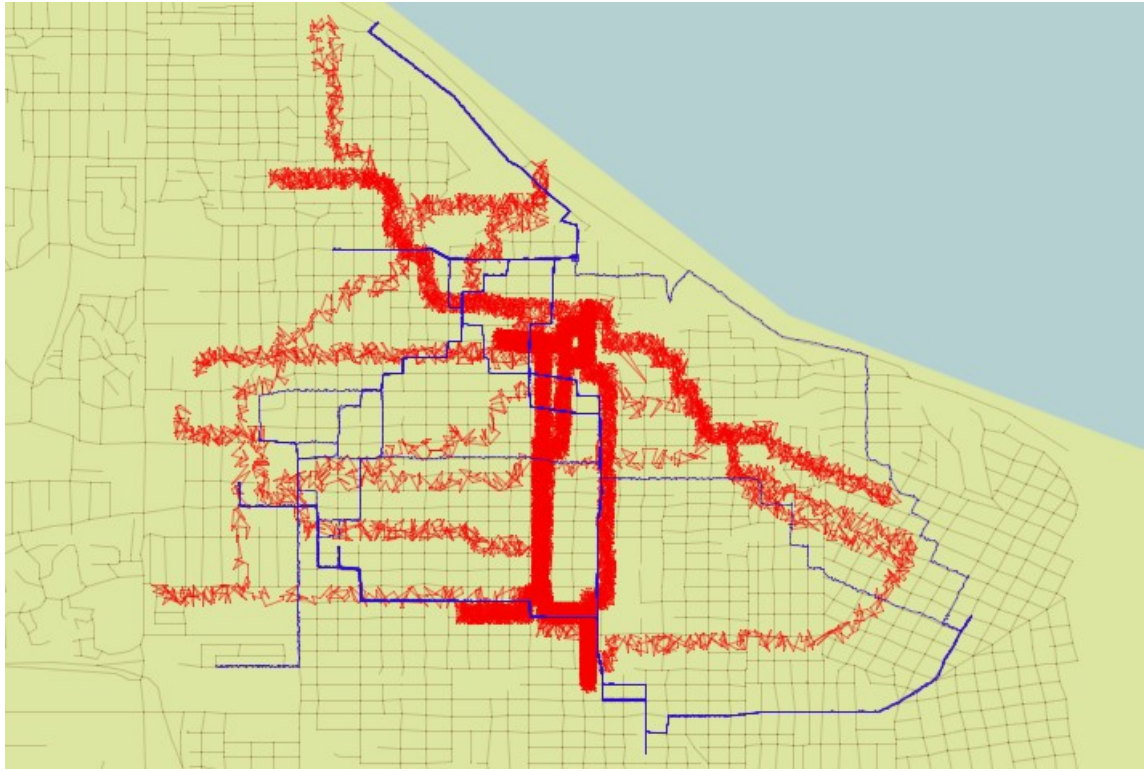


Figure 8. Example of a normal (blue) and jittered trajectory (red).



Figure 9. Stop positions appearing as jittered movement.

5.3. Temporal errors

Generally, time references in movement data are more accurate when spatial positions. However, we are aware of three cases when temporal errors may have significant spread. Thus, trajectories built from metadata of flickr photos of tourists often have shifted time references because users forget to change the time zone in their cameras or mobile devices. The second case is one-hour shift occurring if the daylight saving time is not adjusted properly. Third, often photo capture time is replaced by upload time. While the second and third cases are quite easy to detect by inspecting temporal histograms of position counts, the first case requires more sophisticated processing.

5.4. Attribute errors

Obviously, missing data and errors in the main components of movement data cause errors in thematic attributes derived on the basis of the main components. Thus, many thematic attributes characterizing

movement are calculated from pairs of sequential positions. Both first derivatives (e.g. speed) and higher order derivatives (e.g. acceleration) are affected by spatio-temporal gaps and incorrect identities, spatial, and temporal references. Furthermore, aggregated attributes for whole trajectories, such as total length or average speed, are also affected.

Generally, derived thematic attributes depend on the sampling rate in the data, i.e., temporal frequency of recorded positions (Laube and Purves 2011). Thus, due to the triangle inequality, a decrease of the sampling rate causes a decrease of the computed distance between position records and, further on, a decrease of the speed.

6. Precision deficiency

While spatial positions in the real world are continuous, their computer representation is discrete. Depending on the precision of position representation, different real spatial positions may be represented in data as the same position. Moreover, due to rounding, all position records may form spatial clusters of frequently recorded positions (PS: TrO∪MvO∪SO). These are false patterns that do not correspond to real-world phenomena.

Specific cases of spatial precision errors occur in trajectories constructed from mobile phone use data. When a phone is in the range of two or more neighboring antennas, it can switch from one antenna to another without any movement of the phone carrier. As a result, the trajectory may contain jumps between positions of different antennas that do not represent real movement of the user. In Figure 10, an example of such trajectory is shown on a map (left) and in a space-time cube (right). Some of the jumps are characterized by unrealistic speeds and are therefore easy to detect.

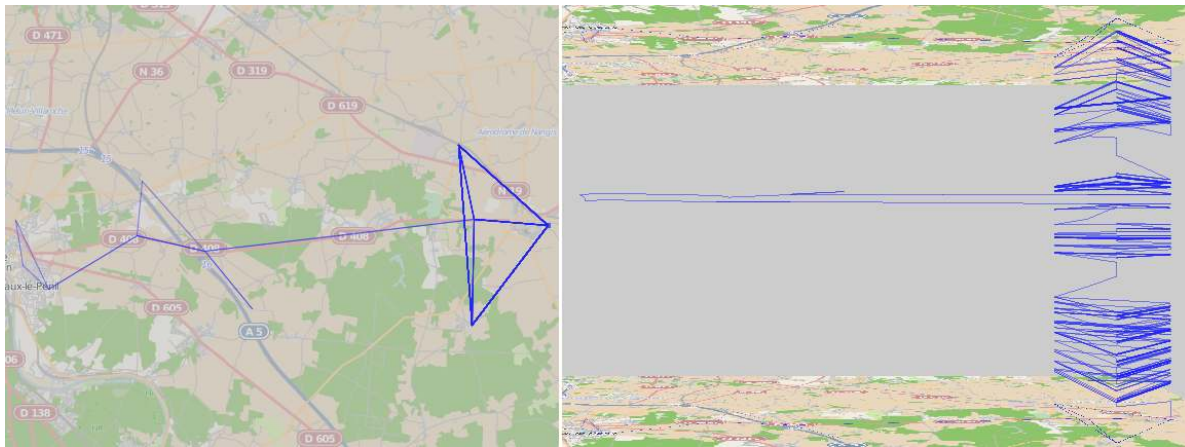


Figure 10. A trajectory of a mobile phone user contains segments of false movement caused by switching the phone connection between neighboring antennas.

Loss of precision in time references may lead to appearance of multiple position records of the same mover referring to the same time. It may be impossible to put these records in the right order for reconstructing the corresponding trajectory segment. Therefore, the segment has to be replaced by one representative position, e.g., the most central position or the average of all positions.

7. Conclusion

Different representations of the same data may be more suitable for answering specific analysis questions depending on what data aspect(s) (what, where, when) (Peuquet 2002) are in focus. For movement data, there are three principal representations (Andrienko et al. 2013a) (Fig. 11). Conversions between these representations may be useful not only for supporting different types of analysis tasks but also for detecting different kinds of problems. One example is shown in Fig. 4, where movement data are viewed as spatial time series. After transforming data to another representation, it is advisable to search for patterns such as spatial or spatio-temporal clusters, extreme values, etc. Any kind of unexpected irregularity or regularity, either temporal or spatial, may correspond to problems in original data.

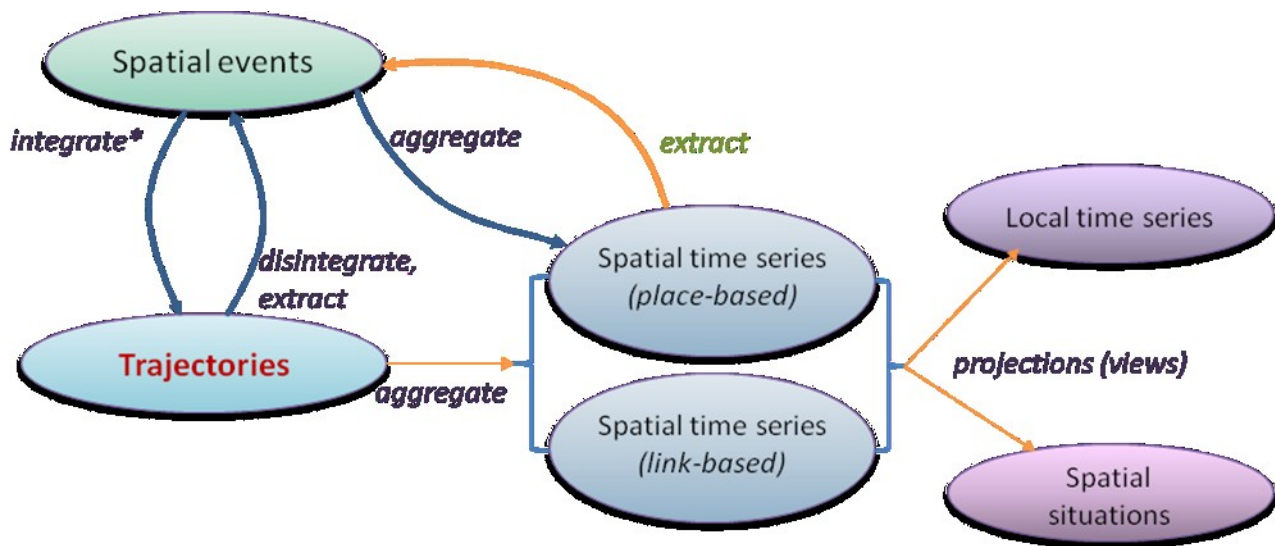


Figure 11. The principal transformations applicable to movement data, depending on the task/analysis goal.

Data preparation is typically the most time-consuming step in the analysis process, and thus proper tool support for this phase is highly important. This holds especially true for movement data with its inherent complexities. In this paper, we have shown visualizations that reveal the existence of different problems and the degrees of their spread. We have also mentioned some computational operations that help in problem detection. Since data quality analysis requires human judgement, it cannot be done fully automatically; however, the work of a human analyst may be supported by an “intelligent checklist” tool reminding what kinds of problems need to be investigated, making appropriate computations and data transformations, and generating informative visualizations.

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