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Group size allometry in humans, primates, and mammals

Unique allometry of group size and collective brain mass in humans and primates relative to other mammals

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12 Abstract

13 Group living is common in mammals, particularly in primates and humans. Across species, groups are social networks where co-residing members exchange information and balance 14 15 trade-offs between competition and cooperation for space, resources, and reproductive opportunities. From a macroecological perspective, species-specific group sizes are ultimately 16 constrained by body size, population density, and the environmental supply rate of home 17 18 ranges. Here, we derive an allometric null model for group size in mammals based on individual energy demands and ecological constraints. Using Bayesian phylogenetic mixed models we 19 show that primates exhibit unique allometries relative to other mammals. Moreover, as large-20 bodied primates, human hunter-gatherers have among the largest social groups of any 21 22 mammal. We then explore the consequences of this unique social allometry by considering how mammalian brain size scales up in social groups that differ in size across mammals. We show 23 similarly unique allometries in what we term the collective brain mass of social groups in 24 primates relative to all other mammals. These results show that for a given body size primates 25 have both larger brains and larger social networks than other mammals. Consequently, 26 27 proportionally larger primate brains interact in proportionally larger social networks with important consequences for group cognition. We suggest that the size, scale, and complexity of 28 human social networks in the 21st century have deep evolutionary roots in primate ecology and 29 30 mammalian brain allometry.

31

32 Keywords: brain; social network; group size; hunter-gatherers; mammals; macroecology

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33 **1. Introduction**

Two of the most conspicuous features of the human species are large brains and intense 34 sociality. How the two interact to influence cognition has become the focus of research across 35 36 many disciplines (Clark and Chalmers, 1998; Dunbar, 1998; Richerson and Boyd, 2005; Dunbar and Shultz, 2007; Krubitzer, 2009; Woolley et al., 2010; Whiten and Erdal, 2012; Hutchins, 2014; 37 Dennett, 2017; Everett, 2017; Graziano, 2017; Muthukrishna et al., 2018). Human brains are 38 large, complex, and metabolically expensive, constituting ~25% of the basal metabolic budget 39 40 but only ~2% of the body size. However, the computational returns on metabolic investment have been considerable. The initial doubling of hominin brain size to ~800 cm³ in *Homo erectus* 41 (senso lato) ~2 MYA correlated with the expansion of the geographic range throughout Africa 42 and southern Eurasia. The next major increase in brain size to ~1,350 cm³ ~300 KYA saw 43 another expansion where modern humans replaced other hominins wherever they existed. 44 eventually extending the human geographic range to include the majority of the planet's 45 46 terrestrial habitats. Humans began to genetically reengineer the biosphere ~ 12 KYA by redirecting flows of environmental net primary production to net agricultural production, and 47 ~0.2 KYA humans leveraged thermodynamic principles to engineer machines to convert heat 48 49 into work using fossilized biomass (Smil, 2008, 2019). Currently, the human species numbers 50 about 7.7 billion, most of whom are connected by global communication networks, and now, through various technologies, have near-instant access to the majority of cultural knowledge 51 52 accumulated over the last several thousand years. Humans now actively explore the solar system, are capable of manipulating matter at the smallest scales and gathering information at 53 54 the largest. These innovations were facilitated not only by an initial increase in brain size and 55 function, but by the intensity of social interactions.

The story of this evolutionary sequence is told, however incompletely, 56 bv the 57 paleoanthropological, archaeological, and historical records (Christian, 2011). Explaining how and why humans are capable of such innovations is less clear. While the human brain is large 58 59 for a mammal of our body size (~7 times the predicted size of a mammal, and ~3 times that of a primate), human cognition is not just a function of brain size, but brain specialization, where 60 61 increasing size facilitates increasing diversity of function (Fuster, 1999; Elston et al., 2006; Striedter, 2006; Passingham, 2008; Barton, 2012; Bullmore and Sporns, 2012; Herculano-62 Houzel, 2012, 2016; Passingham and Wise, 2012; Roth and Dicke, 2012; Schneider, 2014; 63 64 Wittmann et al., 2018). While the number of neurons in the mammalian brain increases with 65 size, in primates an increasing proportion are located in the cerebral cortex (Herculano-Houze). 2012). As the human brain is largely a linearly scaled-up primate brain, as large-bodied 66 primates, humans have particularly neuron-rich cerebral cortices compared to other mammals 67 68 (Herculano-Houzel, 2009, 2012). Consequently, in contrast to other primates, humans can mentalize at high orders, engaging in both self-reflection and on the mental state of others 69 (Frith and Frith, 2006; Passingham, 2008; Tomasello, 2009). Humans can place themselves in 70 alternative circumstances, set goals, plan ahead and monitor progress, weigh alternatives, 71 engage in mental time travel, use schema to simulate outcomes, or use theories to predict 72

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probabilities, communicate directly with each other using language, learn complex tasks quickly, and use past events to inform actions in the present or future (Fuster, 1999; Passingham, 2008; Graziano, 2013; Tomasello, 2014; Everett, 2017). However, the intelligence of an individual human brain is a necessary, but not sufficient condition for human innovation; adaptation, innovation, and creativity results not from individuals *per se*, but from networks of interacting individuals (Hutchins, 1995, 2014; Richerson and Boyd, 2005; Whiten and Erdal, 2012; Bettencourt, 2013).

In this paper we take a macroecological approach to understanding the allometry of group size 80 81 and brain size across mammals by combining principles of metabolic ecology (Brown et al., 2004) with Bayesian phylogenetic mixed models (Bürkner, 2017). We first derive and test an 82 allometric null model of group size across mammals. Next, we consider the allometry of brain 83 size scaling in social groups across mammals; we term this quantity *collective brain mass*. We 84 do not assume the size of a social group necessarily equates to the degree of social complexity 85 (Silk. 2007): the size of the network is the number of nodes (i.e., individuals), whereas the 86 complexity would be the statistics of the network structure (i.e., connectomics). Here, we use 87 the size of a network to quantify the collective brain mass within a group to which an individual 88 89 brain contributes and interacts. Clearly, the nature of interactions varies widely within 90 mammalian social groups, from prairie dog warning vocalizations to elephant infrasonic rumbling to human story-telling traditions. However, by definition, social species co-reside in 91 groups of conspecifics who benefit, in one way or another, from living with others who share 92 similar cognitive abilities and who use information received from others, intentional or not, to 93 modify their behavior. 94

95

96 **2. Theory and results**

a) Scaling relations for group size and collective brain mass.

98 i) Data

We compiled a large database of mammalian ecology from published sources, including body 99 size, basal metabolic rate, group size, home range, population density, and brain size (see 100 *Electronic Supplementary Material (ESM)* for details). To quantify the scaling behavior, we use 101 ordinary least squares regression models and Bayesian phylogenetic mixed models (BPMM) 102 (Bürkner, 2017). In the BPMMs the dependent variable is weighted by the variance-covariance 103 matrix of evolutionary relationships between all species, thus controlling for phylogenetically-104 structured residuals. Intercepts and slopes of the dependent variable are allowed to vary using 105 106 mammalian order as the random factor. This modeling technique allows us to isolate scaling 107 behavior within different mammal orders while controlling for their phylogenetic history. All data and code used in this paper are available as *Electronic Supplementary Material* attached to 108 109 this paper.

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110 ii) Theoretical development

111 Allometric relations are captured by power functions that take the general form

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$$y = y_0 x^\beta \tag{1}$$

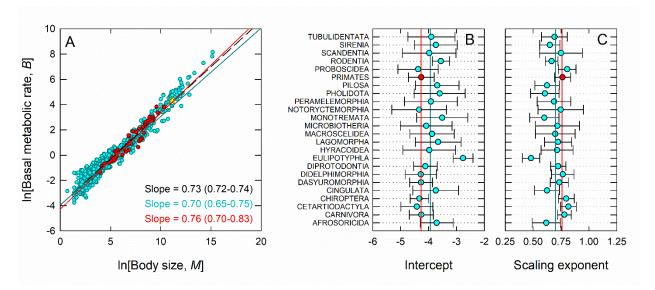
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115 where y is a dependent variable, such as basal metabolic rate, brain size, group size, or home range size; x is an independent variable, commonly body size in allometry; β is the scaling 116 exponent, an elasticity $(d \ln y / d \ln x)$ capturing the proportional response of a change in y to 117 a change in x; and y_0 is a normalization constant. In biological systems when the independent 118 119 variable is body size and the dependent variable is some measure of life history or physiology. β is commonly less than 1 (i.e., sublinear). As such, there is an inherent economy of scale in 120 biological systems as mass-specific efficiency increases with size. In human social systems, 121 122 properties relating to energy and infrastructure show similar economies of scale for similar reasons (Bettencourt et al., 2007; Hamilton et al., 2007a; Brown et al., 2011). However, when 123 the independent variable is group size or population size and the dependent variable is a 124 measure of collective productivity, such as wealth, innovation, crime, or incidence of disease, 125 126 β is often greater than 1 (i.e., superlinear) (Bettencourt et al., 2007). This is because socioeconomic outputs are not the result of the number of people in a social network, but their 127 interaction (Bettencourt, 2013); in a fully-connected unweighted social network the number of 128 interactions, c, increases with network size, n, as $c \sim n^2$ and so connectivity increases 129 multiplicatively with size. As such, social networks achieve increasing returns to scale from 130 131 intensified rates of interaction as they grow in size. This paper combines these approaches to understand how collective social phenomena scale with body size across mammals. 132

133 b) Basal metabolic rate.

Group living begins with the metabolic energy required to support individual organisms. The 134 135 basal metabolic rate is a fundamental rate in biology setting the energy demand of all biological functions (Brown et al., 2004). Across mammals, the relationship between the basal metabolic 136 rate, B, and body size, M, is described by a power function $B = B_0 M^{3/4}$, where B_0 is a mass-137 specific normalization constant; in our data the empirical scaling across all mammals from OLS 138 is $B \propto M^{0.73}$ (Figure 1A; Table 1). The BPMM shows no statistical difference in the metabolic 139 scaling of primates to any other mammalian order (see Figure 1 A-C and *ESM*)). The human 140 basal metabolic rate of ~75 watts (the yellow star in figure 1A) is much as expected for a 141 mammal of our body size (~60,000 g, or 60 kg). 142

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Figure 1. Basal metabolic rate and brain size allometries in mammals, primates and humans. Red data points, lines, and text are non-human primates, blue are non-primate mammals, and yellow diamonds are human. The red and blue lines are the scaling estimates from Bayesian phylogenetic mixed models and the dashed black line and text is the OLS model estimate of the slope. A) Scaling of basal metabolic rate in watts and body size in grams; B) Intercepts from the phylogenetic mixed model by order; C) Scaling exponents from the Bayesian phylogenetic mixed model by order.

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Figure	OLS Model	Constant	95% CI	Slope	95% CI	d.f.	P-value	r²
1A	$B \propto M$	-3.94	-3.88, -4.00	0.73	0.72, 0.74	793	<0.001	0.95
1D	$W \propto M$	-2.78	-2.72, -2.84	0.73	0.72, 0.74	1366	<0.001	0.96
1G	$W \propto B$	-1.09	1.22, 1.14	0.98	0.96, 1.00	585	<0.001	0.93
3A	$D \propto M$	8.63	8.35, 8.92	-0.69	-0.73, -0.65	1117	<0.001	0.53
4A	$H \propto M$	-9.82	-10.19, -9.45	1.01	0.97, 1.06	950	<0.001	0.64
4D	$H' \propto M$	-9.32	-9.78, -8.86	0.81	0.75, 0.87	785	<0.001	0.49
5A	$N \propto M$	-0.35	-0.29, -0.51	0.17	0.15, 0.19	1205	<0.001	0.21
6A	$G \propto M$	-2.79	-2.49, -3.09	0.87	0.85, 0.89	716	<0.001	0.77

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Table 1. Summary of OLS regression models and parameter estimates. For full details of ANOVA
 tables and results see the *Supplementary Information*.

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157 c) Group size, population density, and home range.

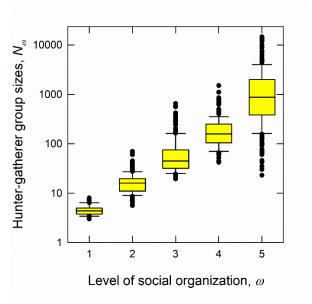
At all body sizes some species live solitarily, but many live in social groups. Living in groups may help individuals maximize fitness by reducing predation risk, increasing foraging success, providing opportunities for alloparental care, increasing mating opportunities, or reducing

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- 161 mortality risk, for example (Krause et al., 2002; Silk, 2007; Beauchamp, 2013). On the other
- 162 hand, group living may increase competition for space, resources, and mates, increase disease
- 163 loads and the risk of free-riders. Ultimately the calculus of group size reduces to whether the
- 164 net benefits of group living outweigh the costs (see Silk, 2007).
- Human hunter-gatherer societies are organized into a complex hierarchy of social groups that form metapopulations (Figure 2) (Binford, 2001; Hamilton et al., 2007b; Bird et al., 2019). Interactions at all levels occur through fission-fusion dynamics that operate at different timescales, from days to years (Hill et al., 2011, 2014). Using data from Binford (2001) we consider
- 169 the five levels of hunter-gatherer social groups in Table 2.
- 170
- 171 Table 2. The five levels of hunter-gatherer social group sizes.

Level	Group	Geometric mean	95% CI	Sample
1	Families	4.48	4.31-4.67	116
2	Dispersed bands	15.60	14.68-16.58	228
3	Aggregated bands	53.66	49.86-58.29	298
4	Regional populations	165.32	152.25-181.00	214
5	Ethnolinguistic metapopulations	839.19	736.36-954.03	340

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Figure 2. Boxplots of hunter-gatherer group sizes across five levels of social organization. The horizontal bars in the box bodies are medians, the height of the box is the middle 50% of the data, and the whiskers are +/-25%. At all scales of social organization hunter-gatherer group size are approximately normally distributed on the log scale, and so lognormally distributed on the linear scale. 1 = families, 2 = dispersed bands, 3 = aggregated bands, 4 = regional populations, and 5 = ethnolinguistic metapopulations (see Table 2 for details).

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181 In mammals social group size, N, is defined as the number of individuals that co-reside within 182 a shared home range, H, and is usually measured in the field as the average number of 183 individuals with whom a set of focal individuals interact over a 24-hour time period (Jones et 184 al., 2009). The allometry of group size is inherently noisy as there are solitary species at all body 185 sizes and so there is no simple correlation between group size and body size that holds for all 186 mammal species. In other words, while average group size may increase with body size, the 187 variance will also increase as group size is bounded at N = 1 for all body sizes.

188 We derive a simple allometric null model for group size from the definitions of home range and population density. Let us assume the daily encounter rate of conspecifics, λ , is a function of 189 the population density of conspecifics within a home range, and so the number of individuals 190 encountered during a day, N, will be the product of the encounter rate, λ , and the home 191 192 range size, H, both of which scale allometrically. Mammal population density, D, scales with body size as the inverse of metabolic rate; $D = N / A \propto M^{-3/4}$, where A is a sampled area in 193 km². This allometric relationship is known as Damuth's Law in ecology (Damuth, 1981). We see 194 this scaling empirically in Figure 3A and Table 1. Note that primate population densities are 195 shallower than the mammalian average (Figure 3C). In mammals, home range size scales 196 linearly with body size; $H \propto M^1$, (Peters, 1986; Kelt and Van Vuren, 2001; Jetz et al., 2004). We 197 see this empirically in Figure 4A and Table 1. Figures 4B and C show the remarkable consistency 198 of home range scaling across mammalian orders, where only Rodentia deviate from all other 199 mammals. Combining these two results we have a null allometric expectation for group size, N200 201 2

- 202
- 203

 $N \propto \lambda H \propto M^{-3/4} M^1 \propto M^{1/4}$ ⁽²⁾

204

205 We first test this model using an approach developed by Jetz et al. (2004). The size of a home range, H, is the space required by a mammal to meet their metabolic demand, B, the 206 207 resource supply rate from the local environment, R, and the spatial overlap with conspecifics; thus $H = B / \alpha R$, where α is the proportion of the environmental resource supply rate used 208 exclusively by an individual (Jetz et al., 2004). Therefore, the home range used by an individual 209 in a group is estimated by dividing the home range, H, by group size, N. The group size-210 corrected home range is then defined as H' = H / N. Following equation 2 and the allometry of 211 212 home range the expected scaling of the group size-corrected home range is then

213

214
$$H' \propto H / N \propto M^{1} M^{-1/4} \propto M^{3/4}$$
 (3)

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We find support for this predicted scaling in Figures 4D-F, where the scaling estimates are 216 217 consistent this prediction. It is important to make two observation here. First, note that the group size-corrected home range, H' = H / N (Figure 4D), is the inverse of population density, 218 D = N/A (Figure 3A), and so Jetz et al.'s model directly links home range scaling with 219 220 Damuth's Law. Consequently, group size-corrected home ranges in primates deviate from the 221 overall mammal scaling (Figures 4D and F) in the same way that we see in primate population densities (Figures 3A and C). Thus, for their body size primate species tend to be denser on the 222 landscape than most other mammals because individuals overlap in space with conspecifics 223 within their home ranges more so than other mammals. In other words, primate species in 224 general sustain larger group sizes per unit area than other mammals with the exception of 225 Rodentia and Eulipotyphia (shrews, moles, and hedgehogs) (Figure 4F). Interestingly, most 226 species in the orders Primates, Rodentia, and Eulipotyphia are either arboreal or fossorial. As 227 228 such, their home ranges include an additional vertical dimension that could explain the higher 229 observed population densities.

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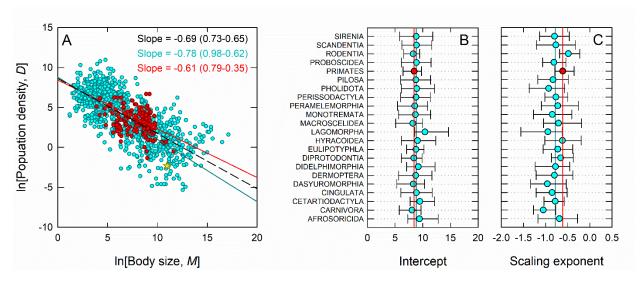


Figure 3. Population density allometries in mammals. A) The scaling of population density and body size; B) Intercepts for each order from the phylogenetic mixed model; and C) Slopes for each order.

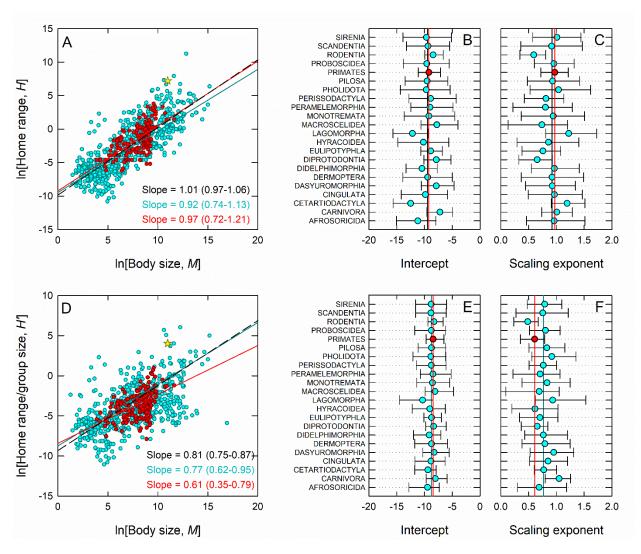
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In Figure 3A, the hunter-gatherer average population density (yellow star) was estimated from the geometric mean of total population sizes divided by the geometric mean of territory sizes using data from Binford (2001) (see *ESM* for data). Hunter-gatherers have relatively low population densities for mammals of their body size and have the lowest average population densities of any primate. In Figure 4A, hunter-gatherer home ranges are residential patch sizes estimated from mobility data in Binford (2001). The geometric mean distance of the average

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length of a residential move from the centroid of one patch to the centroid of an adjacent patch 242 is d (see Hamilton et al., 2016). Assuming patch sizes are circular the patch size (i.e., home 243 range), H, is estimated as $H = \pi (d/2)^2$. To estimate the group size-corrected home range we 244 then divide this quantity by the average size of dispersed bands (level 2 in Table 2), as this is the 245 246 number of individuals with which a hunter-gatherer will spend most of the year co-residing 247 (Binford, 2001; Hill et al., 2011). Figures 4A and D show that hunter-gatherers have particularly large home ranges for mammals of their body size, and by far the largest of any primate (both 248 absolutely and relatively). 249



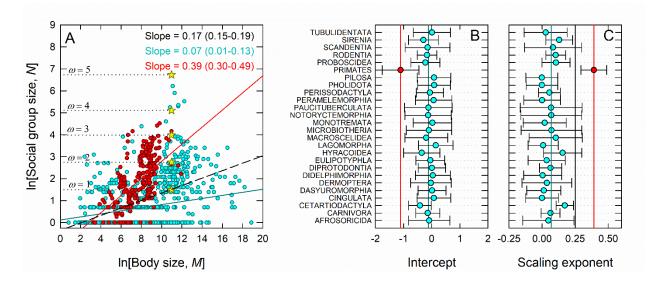
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Figure 4. Home range allometries in mammals, primates and humans. A) The scaling of home range size and body size; B) Intercepts for each order from the phylogenetic mixed model; C) Slopes for each order; D-F) The scaling of individual home range size and body size, and phylogenetic mixed models results; G-I) the scaling of social group size and body size, and mixed effect model results.

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Figure 5A shows that across mammals there is a noisy but statistically significant positive scaling 258 relationship between group size and body size, $N \propto M^{0.17}$ (Table 1), though shallower than the 259 null expectation of $N \propto M^{1/4}$. Figure 5C shows that primate group sizes increase with body size 260 significantly faster than all other mammal orders, where $N \propto M^{0.39}$, and significantly faster 261 than the null prediction (the vertical black like in Figure 5C). As this scaling is steeper than the 262 allometric null model, this means that in primate species individuals form groups that are larger 263 than simply the average density of individuals encountered in their home range over a 24 hour 264 265 period. In other words, this is strongly indicative of prosocial behavior as there must be additional behaviors that aggregate individuals into cooperative groups than simply shared 266 space and random encounters. On the other hand, in all other mammalian orders, the scaling 267 slope is less than 1/4 and so individuals form social groups at rates slower than the null model. 268 Group formation is much more limited and constrained in most other mammalian orders than 269 270 in primates. Figure 5A shows that largest group sizes of hunter-gatherers (levels 4 and 5; 271 regional and ethnolinguistic populations) are among the largest social groups of all mammals and primates. The only other mammals in Figure 5A with similar body sizes and social groups 272 273 are all marine mammals, including seven species of Delphinidae (Stenella attenuata; Delphinus 274 delphis; D. capensis; Peponocephala electra; Lissodelphis peronii; L. borealis; and S. longirostris). 275 Interestingly, the human body size of \sim 60 kg place them near the empirical apex of maximum group sizes observed at any body size suggesting the human ability to form large social groups 276 277 is partially a serendipitous function of having a body size near the midpoint of mammal body sizes, above which maximum group size declines rapidly. We discuss this further below. 278



280

Figure 5. Group size allometries in mammals, primates and humans. A) Group size and body size. B) Intercepts by order from the phylogenetic mixed model. C) Scaling exponents by order

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from the Bayesian phylogenetic mixed model. The vertical solid black line is the expectation from the null model, equation 2.

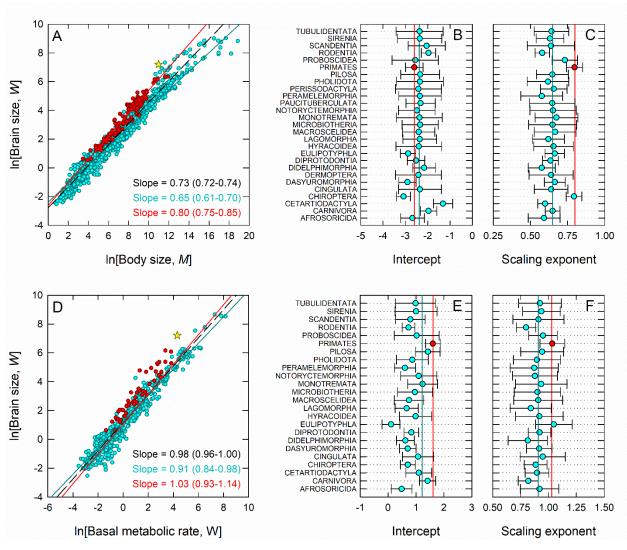
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286 d) Brain size and social networks of brains.

A central aspect of group living is cooperation and the increased potential for information 287 sharing among group members. One of the potential cognitive benefits of group living is the 288 ability to interact with more brains. In mammals brain size, W, scales with body size as 289 $W \propto M^{3/4}$ (Burger et al., 2019). We see this empirically in figure 6A, where $W \propto M^{0.73}$ (see 290 Table 1). In Figure 6C the BPMM shows that primate brain size (red data point and vertical line) 291 increases with body size significantly faster than other mammals (vertical blue line) (see ESM 292 for full results). Therefore, in primates, brains constitute an increasing proportion of body size 293 as body size increases, with the notable exception of Chiropterans (see Smaers et al., 2012). 294 Although the human brain is large for a mammal of 60,000 g at ~1,350 g, there are several 295 large-bodied mammalian species that have brains absolutely larger than humans, including 26 296 marine species of Cetartiodactlya (whales and dolphins) and both extant species of 297 Proboscidea; Loxodonta Africana and Elephas maximus. 298

Consequently mammalian brain size increases linearly with basal metabolic rate, $W \propto B^1$ as 299 300 shown in Figure 6D and Table 1; the faster the metabolic rate the larger the brain. Figure 6E shows that primate brains are significantly more expensive to support per gram than other 301 302 mammal brains, and Figure 6F shows that primate brain size increases significantly faster with basal metabolic rate than other mammals (see ESM for full results). Metabolically expensive 303 primate brains thus become increasingly expensive with size. Figure 6A shows that while 304 human brains are particularly metabolically expensive, so are those of several larger-bodied 305 primates, including Pongo pygmaeus, Papio Anubis, P. hamadryas, P. papio, Cercocebus 306 307 torguatus, Erythrocebus patas, and Hylobates lar.

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Figure 6. Brain size allometries in mammals, primates and humans. Red data points, lines, and 310 311 text are non-human primates, blue are non-primate mammals, and yellow diamonds are human. The red and blue lines are the scaling estimates from Bayesian phylogenetic mixed 312 models and the dashed black line and text is the OLS model estimate of the slope. A) Scaling of 313 basal metabolic rate in watts and body size in grams; B) Intercepts from the phylogenetic mixed 314 model by order; C) Scaling exponents from the Bayesian phylogenetic mixed model by order; D-315 316 F) Scaling of brain size in grams and body size, and Bayesian phylogenetic mixed model results; G-I) Scaling of brain size and basal metabolic rate, and Bayesian phylogenetic mixed model 317 318 results.

- 320 To consider how brain allometry scales up in social groups we combine the allometric scaling of
- brain size, W, and social group size, N, to define the collective brain mass of a social group as
- G = NW. An allometric null model for collective brain mass is then

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$$G = NW = \lambda HW \propto M^{-3/4} M^1 M^{3/4} \propto M^1$$
(3)

325

Thus, the null model predicts collective brain mass within species-specific social groups 326 327 increases linearly with body size. If so, this would have important consequences for group cognition as average brain size increases sublinearly with body size. Therefore, as body size 328 increases brains would be connected within larger social networks, allowing for greater 329 connectivity. However, Figure 7A shows that the scaling of collective brain mass across 330 331 mammals is sublinear and significantly less than 1 (see Figure 7C), both in the OLS model $G \propto M^{0.87}$ and the BPMM, $G \propto M^{0.72}$. However, for primates the scaling is superlinear, 332 $G \propto M^{1.20}$, and significantly greater than 1 (the vertical black line in Figure 7C) (see ESM for full 333 details). Primate collective brain mass increases with body size much faster than other 334 335 mammals (~1.7-fold). In addition, primates are the only mammalian order to scale significantly differently than all other mammalian orders (Figure 7C). Hunter-gatherers exhibit among the 336 largest collective brain masses of any mammal or primate (Figure 7A). As with social group size, 337 338 the only other mammals with similar-sized collective brain masses are species of the 339 Delphinidae family. The phylogeny of collective brain mass across mammals is shown in Figure 340 8.

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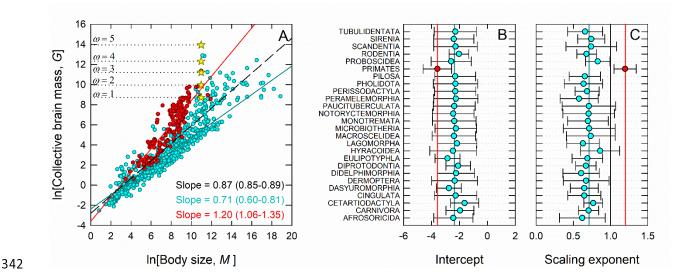
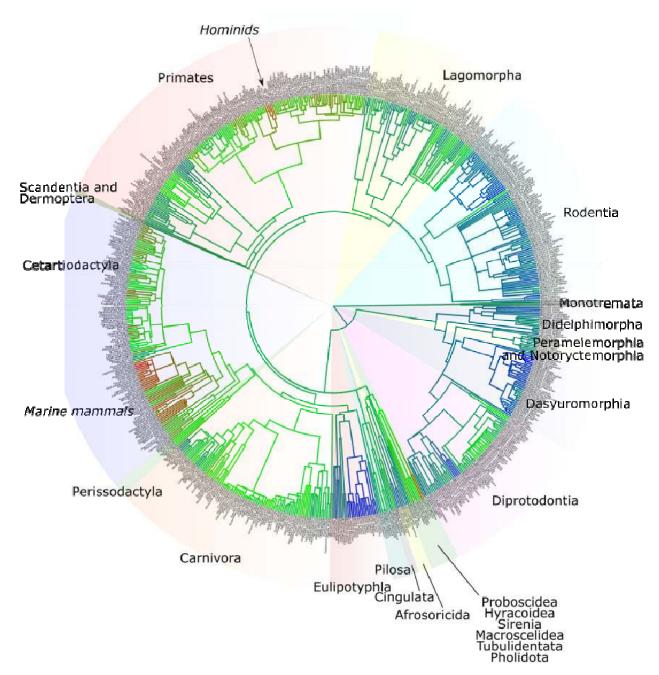


Figure 7. Collective brain size allometries in mammals, primates and humans. A) Collective brain size and body size. B) Intercepts by order from the phylogenetic mixed model. C) Scaling exponents by order from the Bayesian phylogenetic mixed model. The vertical solid black line is the expectation from the null model, equation 3.

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348

- 349 Figure 8. The phylogeny of group brain networks in mammals using continuous character
- 350 mapping. Colored sectors denote mammal orders.

351

352 3. Discussion

Primate species form social groups that are among the largest for their body size among mammals. The allometric scaling of primate group size is unique among mammals and the data show that group size increases with body size almost twice as fast than in other mammals

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(Figures 6A and C). The data show that this occurs because primates support greater densities 356 357 of individuals than most other mammals (Figures 3A and 4D). The analysis of the null model we derive in this paper from ecological theory shows that primates form groups faster than would 358 be expected from the random encounter rates of individuals within shared home ranges. As 359 360 species in all other mammal orders tend to form groups slower than the null expectation, the results we report here show a strong statistical signature of a generalized primate prosociality 361 not found in other mammals and which results in the unique allometry of social group scaling in 362 primates. 363

364 Hunter-gatherers have a wide range of social group sizes (Figure 5A), including some of the largest observed in all mammals. The most common residential group sizes used during the 365 course of a year are the dispersed and aggregated bands (levels 2 and 3 in Table 2 and Figure 366 5A) that reflect the seasonal fission-fusion cycle of families as they aggregate into different 367 group sizes over the course of a year (Binford, 2001). Figure 5A shows the sizes of these groups 368 369 are much as expected for a primate of ~60 kg. However, because individual hunter-gatherer bands are embedded within larger social networks commonly of hundreds to thousands of 370 people, all of which interact at various rates (Hill et al., 2014), these social group sizes are 371 372 among the largest observed of any mammal species. While some mammal species aggregate 373 into large collectives of many thousands of individuals, such as herds of artiodactyls or colonies of chiropterans in roosts, these aggregations are not social networks of co-residing individuals, 374 but aggregations brought about by environmental conditions that are temporarily capable of 375 supporting large focal densities of individuals. Analogous aggregations in human societies may 376 be large-scale ritual events held over a number of days, or sporting events that aggregate tens 377 378 of thousands for short periods of time. Of course, the largest human social groups in the 21st 379 century connect billions of individuals though social media, cell phone networks, religious 380 identities, languages, or the politics of nation states.

The self-organization of hunter-gatherer meta-populations into a fluid arrangement where 381 families aggregate into different sizes of social groups at multiple levels results in a highly 382 383 flexible social organization. On the one hand, the number of co-residing families in a band is often no more than 3-6 (Hamilton et al., 2007b, 2018), perhaps 10-20 individuals (Hill et al., 384 2011), a size which may optimize group return rates while minimizing competition for finite 385 resources and the risk of free-riders, for example. On the other hand, by maintaining a fluid 386 387 structure of fission and fusion among meta-populations composed of hundreds of people with some form of shared identity, information flows at much larger scales, often including multiple 388 neighboring metapopulations (see Bird et al., 2019). Thus individuals living in small social 389 groups on a daily basis receive the long-term benefit of being embedded within a much larger 390 391 social network.

A consequence of the unique allometric scaling of primate group sizes is the similarly unique scaling of collective brain masses in social groups of primates (Figure 6A). This is because both social group size and brain size scale faster in primates than in all other mammals (Figure 6C)

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and so collective brain mass in primates diverges from all other mammals as body size 395 increases. Therefore, at all body sizes, primates have both larger brains and larger social 396 networks for that brain to interact with than other mammals. Importantly, the rate of 397 allometric increase of collective brain mass in primates is superlinear (i.e., slope > 1). This 398 399 means that in primate species increasingly larger brains are embedded within even larger social groups. Because group connectivity increases multiplicatively with size (i.e., $c \sim n^2$) then larger 400 401 brains have a multiplicatively greater potential for interaction than smaller brains. Across all 402 other mammal orders the collective brain mass within social groups increases sublinearly with body size (Figures 6A and C), because larger brains occur in social group sizes that increase with 403 body size only very shallowly (if at all) (Figure 6A and C). 404

Because the number of neurons scales positively with brain size in mammals (Herculano-405 406 Houzel, 2012; Herculano-Houzel et al., 2015), a social group with a larger collective brain mass can potentially recruit more brains with more neurons to perform a collective behavior, and so 407 it reasonable to hypothesize that larger social networks will have a greater potential for group 408 409 cognition and collective computation. If so, primates would be predicted to exhibit a greater 410 potential for group cognition than non-primate mammals. It is perhaps not surprising then that 411 the most evidence we have for advanced group cognition and collective computation in mammals comes from one of the largest-bodied primates. 412

Intriguingly, Figure 5A suggests that the ability of humans to form large social groups may be 413 partially a function of its position on the mammal body size spectrum. The only other mammals 414 415 with similar-sized social groups are several species of Delphinidae, all of whom have similarsized bodies to humans. From the smallest terrestrial mammal, Suncus etruscus, the Estruscan 416 417 shrew at ~2 g, maximum social group size increases steadily up to the human body size of \sim 60,000 g, but thereafter declines rapidly. This suggests that while average group size may well 418 419 be a function of body size and ecology (as described in our model), as body size increases there are shifting trade-offs in the ability of ecosystems to support the largest aggregations of larger-420 bodied mammals: above a certain body size (apparently near the midpoint of the body size 421 spectrum) large groups are increasingly difficult to maintain and maximum group sizes decrease 422 monotonically. This may because about half of the mammal species with body sizes larger than 423 424 humans are marine mammals (data not shown), which have different ecological constraints to 425 maintaining aggregations than terrestrial mammals.

The estimated clade age of primates is on the order of \sim 53-88 MYA (Springer et al., 2012; 426 O'Leary et al., 2013), and so the distinctive evolutionary trajectory of primates was a pathway 427 428 that emerged early in the post-Cretaceous mammalian radiation. The hominin branch emerged 429 $^{\circ}$ 6-7 million years ago within the primate tree. Among other traits, the hominin clade saw not only increasing brain size but increasing neuroanatomical specialization (Lieberman, 2011) that 430 ultimately allowed for self-expression (Berwick and Chomsky, 2016; Tattersall, 2019) and the 431 432 transfer of social information among individuals through gestures, symbols, and language (Tomasello, 2010; Clark and Toribio, 2012; Everett, 2017). Some researchers suggest that 433

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modern human-like social complexity may have emerged with the first major expansion in
hominin brain size ~2 MYA with *Homo erectus* (*senso lato*) (Deacon, 1998; Wrangham, 2009;
Herculano-Houzel, 2016; Everett, 2017). However, the point at which complex social networks
of the form we see in ethnohistoric hunter-gatherers first appear in the archaeological record is
unclear.

It has been argued that the complexity, diversity, and specialization of the primate brain 439 evolved in response to the selective pressures of living in complex 3-dimensional, arboreal 440 environments (Passingham and Wise, 2012). Complex ecological environments are also 441 442 complex social environments as the successful exploitation of ecological niches necessarily involves the successful negotiation of conspecifics (Passingham, 2008; Passingham and Wise, 443 2012; Wittmann et al., 2018). Recent research in neuroscience suggests that the ability of 444 brains to restrict attention to a subset of stimuli in complex environments resulted in the 445 capacity for self-awareness of mental state, which in turn became awareness of the mental 446 447 state of others (Frith and Frith, 2006; Graziano, 2017). If this is an accurate mechanistic model, the results we show here suggest that the evolutionary consequences of these dynamics led to 448 feedbacks between group size and brain size that resulted in the unique allometries of group 449 size and collective brain mass in primate species. 450

451

452 **4. Conclusion**

The unique allometric scaling of group sizes in primates leads to the superlinear scaling of 453 454 collective brain masses. This superlinearity results from the faster allometric scaling of both brain size and group size in primates than other mammals. Thus primates have both larger 455 brains and larger social networks than other mammals of a similar body size. Consequently, as 456 large-bodied primates, human hunter-gatherers have the largest extended brain networks of 457 any mammal. These networks have grown in size, scale, and complexity over human 458 459 evolutionary history, particularly the last few thousand years to the extent that the majority of the human species is now connected globally by various overlapping social networks. 460 461 Ultimately, the scale of these networks have deep evolutionary roots in mammalian allometry, primate ecology, and the serendipity of human body size. 462

463

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Group size allometry in humans, primates, and mammals

470 References

- Barton, R.A., 2012. Embodied cognitive evolution and the cerebellum. Philosophical Transactions of the
 Royal Society B: Biological Sciences. 367, 2097–2107.
- 473 Beauchamp, G., 2013. Social predation: how group living benefits predators and prey. Elsevier.
- 474 Berwick, R.C., Chomsky, N., 2016. Why only us: Language and evolution. MIT press.
- 475 Bettencourt, L.M., 2013. The origins of scaling in cities. Science. 340, 1438–1441.
- Bettencourt, L.M.A., Lobo, J., Helbing, D., Kühnert, C., West, G.B., 2007. Growth, innovation, scaling, and
 the pace of life in cities. Proceedings of the National Academy of Sciences. 104, 7301–7306.
- Binford, L.R., 2001. Constructing Frames of Reference: An Analytical Method for Archaeological Theory
 Building Using Ethnographic and Environmental Data Sets. University of California Press,
 Berkeley.
- Bird, D.W., Bird, R.B., Codding, B.F., Zeanah, D.W., 2019. Variability in the organization and size of
 hunter-gatherer groups: Foragers do not live in small-scale societies. Journal of Human
 Evolution. 131, 96–108.
- Brown, J.H., Burnside, W.R., Davidson, A.D., DeLong, J.P., Dunn, W.C., Hamilton, M.J., Mercado-Silva, N.,
 Nekola, J.C., Okie, J.G., Woodruff, W.H., 2011. Energetic limits to economic growth. BioScience.
 61, 19–26.
- 487 Brown, J.H., Gillooly, J.F., Allen, A.P., Savage, V.M., West, G.B., 2004. Toward a metabolic theory of 488 ecology. Ecology. 85, 1771–1789.
- Bullmore, E., Sporns, O., 2012. The economy of brain network organization. Nature Reviews
 Neuroscience. 13, 336.
- Burger, J.R., George, M.A., Leadbetter, C., Shaikh, F., 2019. The allometry of brain size in mammals.
 Journal of Mammalogy. 100, 276–283.
- Bürkner, P.-C., 2017. brms: An R Package for Bayesian Multilevel Models Using Stan. Journal of Statistical
 Software. 80, 1–28.
- 495 Christian, D., 2011. Maps of time: An introduction to big history. Univ of California Press.
- 496 Clark, A., Chalmers, D., 1998. The extended mind. Analysis. 58, 7–19.
- Clark, A., Toribio, J., 2012. Magic Words: How Language Augments Human Computation. In: Language
 and Meaning in Cognitive Science. Routledge, pp. 33–51.
- 499 Damuth, J., 1981. Population density and body size in mammals. Nature. 290, 699.
- Deacon, T.W., 1998. The symbolic species: The co-evolution of language and the brain. WW Norton &
 Company.
- 502 Dennett, D.C., 2017. From bacteria to Bach and back: The evolution of minds. WW Norton & Company.
- Dunbar, R.I., 1998. The social brain hypothesis. Evolutionary Anthropology: Issues, News, and Reviews:
 Issues, News, and Reviews. 6, 178–190.
- 505 Dunbar, R.I., Shultz, S., 2007. Evolution in the social brain. Science. 317, 1344–1347.
- 506 Elston, G.N., Benavides-Piccione, R., Elston, A., Zietsch, B., Defelipe, J., Manger, P., Casagrande, V., Kaas,
- 507 J.H., 2006. Specializations of the granular prefrontal cortex of primates: implications for 508 cognitive processing. The Anatomical Record Part A: Discoveries in Molecular, Cellular, and
- 509 Evolutionary Biology: An Official Publication of the American Association of Anatomists. 288, 26– 510 35.
- 511 Everett, D., 2017. How language began. London, UK: Profile Books.
- 512 Frith, C.D., Frith, U., 2006. The neural basis of mentalizing. Neuron. 50, 531–534.
- Fuster, J.M., 1999. Memory in the cerebral cortex: An empirical approach to neural networks in the
 human and nonhuman primate. MIT press.
- 515 Graziano, M.S., 2013. Consciousness and the social brain. Oxford University Press.

Group size allometry in humans, primates, and mammals

- Graziano, M.S.A., 2017. The Attention Schema Theory: A Foundation for Engineering Artificial
 Consciousness. Frontiers in Robotics and Al. 4.
 Hamilton, M.J., Buchanan, B., Walker, R.S., 2018. Scaling the size, structure, and dynamics of
 residentially mobile hunter-gatherer camps. American Antiquity. 83, 701–720.
- 520 Hamilton, M.J., Lobo, J., Rupley, E., Youn, H., West, G.B., 2016. The ecological and evolutionary 521 energetics of hunter-gatherer residential mobility. Evolutionary Anthropology: Issues, News, and 522 Reviews. 25, 124–132.
- Hamilton, M.J., Milne, B.T., Walker, R.S., Brown, J.H., 2007a. Nonlinear scaling of space use in human
 hunter–gatherers. Proceedings of the National Academy of Sciences. 104, 4765–4769.
- Hamilton, M.J., Milne, B.T., Walker, R.S., Burger, O., Brown, J.H., 2007b. The complex structure of
 hunter–gatherer social networks. Proceedings of the Royal Society of London B: Biological
 Sciences. 274, 2195–2203.
- Herculano-Houzel, S., 2009. The human brain in numbers: a linearly scaled-up primate brain. Frontiers in
 human neuroscience. 3, 31.
- Herculano-Houzel, S., 2012. The remarkable, yet not extraordinary, human brain as a scaled-up primate
 brain and its associated cost. Proceedings of the National Academy of Sciences. 109, 10661–
 10668.
- Herculano-Houzel, S., 2016. The Human Advantage: A New Understanding of How Our Brain Became
 Remarkable. MIT Press.
- Herculano-Houzel, S., Catania, K., Manger, P.R., Kaas, J.H., 2015. Mammalian Brains Are Made of These:
 A Dataset of the Numbers and Densities of Neuronal and Nonneuronal Cells in the Brain of
 Glires, Primates, Scandentia, Eulipotyphlans, Afrotherians and Artiodactyls, and Their
 Relationship with Body Mass. Brain, Behavior and Evolution. 86, 145–163.
- Hill, K.R., Walker, R.S., Božičević, M., Eder, J., Headland, T., Hewlett, B., Hurtado, A.M., Marlowe, F.,
 Wiessner, P., Wood, B., 2011. Co-residence patterns in hunter-gatherer societies show unique
 human social structure. Science. 331, 1286–1289.
- Hill, K.R., Wood, B.M., Baggio, J., Hurtado, A.M., Boyd, R.T., 2014. Hunter-gatherer inter-band
 interaction rates: Implications for cumulative culture. PLoS One. 9, e102806.
- 544 Hutchins, E., 1995. Cognition in the Wild. MIT press.
- 545 Hutchins, E., 2014. The cultural ecosystem of human cognition. Philosophical Psychology. 27, 34–49.
- 546 Jetz, W., Carbone, C., Fulford, J., Brown, J.H., 2004. The scaling of animal space use. Science. 306, 266– 547 268.
- Jones, K.E., Bielby, J., Cardillo, M., Fritz, S.A., O'Dell, J., Orme, C.D.L., Safi, K., Sechrest, W., Boakes, E.H.,
 Carbone, C., 2009. PanTHERIA: a species-level database of life history, ecology, and geography of
 extant and recently extinct mammals. Ecology. 90, 2648–2648.
- 551 Kelt, D.A., Van Vuren, D.H., 2001. The ecology and macroecology of mammalian home range area. The 552 American Naturalist. 157, 637–645.
- 553 Krause, J., Ruxton, G.D., Ruxton, G.D., 2002. Living in groups. Oxford University Press.
- 554 Krubitzer, L., 2009. In search of a unifying theory of complex brain evolution. Annals of the New York 555 Academy of Sciences. 1156, 44–67.
- Lieberman, D., 2011. The evolution of the human head. Harvard University Press.
- Muthukrishna, M., Doebeli, M., Chudek, M., Henrich, J., 2018. The Cultural Brain Hypothesis: How
 culture drives brain expansion, sociality, and life history. PLoS computational biology. 14,
 e1006504.
- O'Leary, M.A., Bloch, J.I., Flynn, J.J., Gaudin, T.J., Giallombardo, A., Giannini, N.P., Goldberg, S.L., Kraatz,
 B.P., Luo, Z.-X., Meng, J., Ni, X., Novacek, M.J., Perini, F.A., Randall, Z.S., Rougier, G.W., Sargis,
- 562 E.J., Silcox, M.T., Simmons, N.B., Spaulding, M., Velazco, P.M., Weksler, M., Wible, J.R.,

Group size allometry in humans, primates, and mammals

- 563 Cirranello, A.L., 2013. The Placental Mammal Ancestor and the Post–K-Pg Radiation of 564 Placentals. Science. 339, 662–667.
- 565 Passingham, R., 2008. What is special about the human brain? Oxford University Press.
- Passingham, R.E., Wise, S.P., 2012. The neurobiology of the prefrontal cortex: anatomy, evolution, and
 the origin of insight. Oxford University Press.
- 568 Peters, R.H., 1986. The ecological implications of body size. Cambridge University Press.
- 569 Richerson, P.J., Boyd, R., 2005. Not by genes alone. Chicago: University of Chicago Press.
- Roth, G., Dicke, U., 2012. Evolution of the brain and intelligence in primates. Progress in Brain Research.
 195, 413–430.
- 572 Schneider, G.E., 2014. Brain structure and its origins: in development and in evolution of behavior and 573 the mind. MIT Press.
- 574 Silk, J.B., 2007. The adaptive value of sociality in mammalian groups. Philosophical Transactions of the 575 Royal Society B: Biological Sciences. 362, 539–559.
- Smaers, J.B., Dechmann, D.K.N., Goswami, A., Soligo, C., Safi, K., 2012. Comparative analyses of
 evolutionary rates reveal different pathways to encephalization in bats, carnivorans, and
 primates. Proceedings of the National Academy of Sciences of the United States of America.
 109, 18006–18011.
- 580 Smil, V., 2008. Energy in nature and society: general energetics of complex systems. MIT press.
- 581 Smil, V., 2019. Energy in world history. Routledge.
- Springer, M.S., Meredith, R.W., Gatesy, J., Emerling, C.A., Park, J., Rabosky, D.L., Stadler, T., Steiner, C.,
 Ryder, O.A., Janečka, J.E., Fisher, C.A., Murphy, W.J., 2012. Macroevolutionary Dynamics and
 Historical Biogeography of Primate Diversification Inferred from a Species Supermatrix. PLOS
 ONE. 7, e49521.
- 586 Striedter, G.F., 2006. Précis of principles of brain evolution. Behavioral and Brain Sciences. 29, 1–12.
- 587 Tattersall, I., 2019. The Minimalist Program and the Origin of Language: A View From
- 588 Paleoanthropology. Frontiers in Psychology. 10.
- 589 Tomasello, M., 2009. Why We Cooperate. MIT press.
- 590 Tomasello, M., 2010. Origins of Human Communication. MIT press.
- 591 Tomasello, M., 2014. A Natural History of Human Thinking. Harvard University Press.
- Whiten, A., Erdal, D., 2012. The human socio-cognitive niche and its evolutionary origins. Philosophical
 Transactions of the Royal Society B: Biological Sciences. 367, 2119–2129.
- Wittmann, M.K., Lockwood, P.L., Rushworth, M.F.S., 2018. Neural Mechanisms of Social Cognition in
 Primates. Annual Review of Neuroscience. 41, 99–118.
- 596 Woolley, A.W., Chabris, C.F., Pentland, A., Hashmi, N., Malone, T.W., 2010. Evidence for a Collective 597 Intelligence Factor in the Performance of Human Groups. Science. 330, 686–688.
- 598 Wrangham, R., 2009. Catching fire: how cooking made us human. Basic Books.