¹ Upstream-Cylinder and Downstream-Cylinder Influence on the ² Hydrodynamics of a Four-Cylinder Group

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4 ABSTRACT

The wave interaction at low Keulegan-Carpenter numbers with a group of four large 5 cylinders arranged in the form of a square with one diagonal along the direction of wave 6 propagation is studied with focus on the hydrodynamic effects of the most upstream and 7 the downstream cylinders in the group. This is studied by removing them and comparing 8 the wave forces and the free surface elevations around the three remaining cylinders with 9 the four cylinder configuration. The theoretically predicted wave near-trapping in the case 10 of the four cylinder group is also investigated for low and high steepness incident waves. 11 The numerical results are compared with analytical formulae based on potential theory and 12 differences are observed between the results for high wave steepnesses. It is observed that the 13 downstream cylinder has a significant influence on the wave forces acting on the cylinders in 14 the four cylinder group. It is also found that the numerical model correctly represents the 15 wave near-trapping predicted by the analytical formula at a low incident wave steepness. For 16 a high incident wave steepness, the diffraction regime is found to be different, with significant 17 wave radiation from the cylinders, consequently the conditions for wave near-trapping break-18 down. 19

²⁰ Keywords: cylinder groups, wave trapping, wave diffraction, Computational Fluid Dynamics

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21 INTRODUCTION

Coastal constructions such as wave energy devices operate under low Keulegan-Carpenter 22 numbers (KC=UT/D, where U is the magnitude of the horizontal particle velocity, T is the 23 wave period and D is the diameter of the cylinder) regimes and are designed with dimensions 24 such that their equivalent diameters D are comparable to the incident wavelength L such that 25 D/L > 0.2. Under these conditions, the diffraction effects dominate the wave interaction 26 process and significantly modify the wave field around the devices. The variation of the free 27 surface around a group of deployed devices is an important parameter for device operation 28 and the wave forces are important from a structural design perspective. This scenario can be 29 studied using wave interaction with groups of large cylinders in intermediate water depths. 30 At small distances of separation between the cylinders, each of the cylinders in the group 31 is influenced by the wave diffraction and reflection from the neighboring cylinders. These 32 interactions can lead to wave near-trapping. Wave near-trapping refers to the phenomenon 33 where only a small amount of scattered wave energy in the region between closely placed 34 cylinders is radiated outwards and a near standing wave is formed. The free surface is am-35 plified close to the cylinders and is associated with large pressures on the cylinders, resulting 36 in large wave forces on the cylinders. This phenomenon occurs for certain combinations of 37 incident wavelength, cylinder array arrangement and spacing. In the case of oscillating water 38 column wave energy devices, which operate on the principle of a water column being excited 39 by incident waves Evans (1978), this resonant phenomenon may be used to an advantage 40 when a deployed in a closely placed group. But, the occurrence of this phenomenon and the 41 potential increase in the wave forces on the devices due to wave near-trapping have to be 42 further studied. 43

Wave diffraction and multiple reflection amongst multiple cylinders placed in proximity has been studied using potential theory formulations by several authors such as Ohkusu (1974) Spring and Monkmeyer (1974) and Linton and Evans (1990) Walker and Taylor (2005). Malenica et al. (1999) estimated the second-order and third-order potentials to cal-

culate higher-order forces on a cylinder array. Although these methods have provided a 48 lot of information regarding the near-trapping phenomena at the first and the second or-49 der, the assumptions of a small incident wave amplitude, inviscid fluid and irrotational flow 50 limit the application of these methods. Further, the interaction of high steepness waves 51 with large cylinders can be significantly different from that with low steepness waves due 52 to the occurrence of non-linear wave-body and wave-wave interactions. Many authors have 53 studied the near-trapping phenomenon in the case of cylinder groups composed of four and 54 more cylinders in a polygonal formation (Evans and Porter (1997); Walker et al. (2008)), 55 demonstrating the importance of studying the wave diffraction effects in these cases. Huang 56 (2004) developed a semi-analytical method to study the wave diffraction around two, three 57 and four cylinders and computed the free surface elevations around the array and reported 58 higher interaction in the case of a three cylinder array compared to the four cylinder array. 59 Ohl et al. (2001) carried out experiments to study wave diffraction by an array of large cylin-60 ders and concluded that predictions from potential theory agreed well with the observations, 61 whereas the semi-analytical theory by Malenica et al. (1999) over predicted the second-order 62 contribution to the free surface elevations. Interaction of solitary waves with a group of 63 four cylinders was modeled numerically by Zhao et al. (2007) using generalized Boussinesq 64 equations. Since a solitary wave is only a crest propagating on the free surface, the interac-65 tion of periodic waves is different from the that of solitary waves and separate studies are 66 required. Experimental investigations by Barnard et al. (1983) reported the absence of the 67 theoretically predicted pronounced resonant response due to wave near-trapping. Duclos and 68 Clément (2004) showed that a small amount of disorder, of the order of 0.5% of the cylin-69 der spacing in their analysis, can substantially reduce the forces due to wave near-trapping. 70 Thus, wave interaction with an array of large cylinders at low KC numbers depends on many 71 factors including the arrangement of the cylinders, the number of cylinders and the incident 72 wave steepness. But the effect of wave steepness has not been the focus of previous stud-73 ies in current literature. In this regard, further insight can be obtained by studying wave 74

⁷⁵ interaction with a four cylinder array with cylinders at the vertices and oriented with one ⁷⁶ diagonal arranged in the direction of wave propagation for both low and high steepness inci-⁷⁷ dent waves. The investigation into the variation of the free surface elevation around the four ⁷⁸ cylinder array and the wave forces on the cylinders compared to the free surface variations ⁷⁹ and wave forces in the absence of the most upstream and downstream cylinders can provide ⁸⁰ further knowledge about the changes in the wave field in the different scenarios.

In this study, the open-source Computational Fluid Dynamics (CFD) model REEF3D 81 (Alagan Chella et al., 2015) is used to simulate the wave interaction with cylinder arrays with 82 three and four cylinders as shown in Fig. (1). The objective of the study is to investigate the 83 wave field around the array with four cylinders and three cylinders obtained by removing one 84 of the cylinders from the four cylinder array, evaluate the consequences of the arrangement 85 on the wave forces experienced by the cylinders and the difference between low and high 86 steepness wave interaction with the cylinder arrays. The most upstream and downstream 87 cylinders are removed from the arrangements in turns to obtain two arrangements of three 88 cylinders to obtain insights into the influence of these cylinders on the wave forces experienced 89 by the other cylinders in the array. The free surface in the vicinity of the cylinders and the 90 wave forces on the cylinders are computed for incident waves for two different incident 91 wavelengths at both low and high wave steepnesses are studied. The formula by Linton and 92 McIver (2001) is used for the validation of the numerical results for the four cylinder array 93 at a low incident wave steepness. 94

95 NUMERICAL MODEL

⁹⁶ Governing equations

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The incompressible Reynolds-averaged Navier-Stokes (RANS) equations together with the continuity equation are used in the numerical wave tank in REEF3D:

$$\frac{\partial u_i}{\partial x_i} = 0 \tag{1}$$

$$\frac{\partial u_i}{\partial t} + u_j \frac{\partial u_i}{\partial x_j} = -\frac{1}{\rho} \frac{\partial p}{\partial x_i} + \frac{\partial}{\partial x_j} \left[(\nu + \nu_t) \left(\frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} \right) \right] + g_i \tag{2}$$

where u is the velocity, ρ is the density of the fluid, p is the pressure, ν is the kinematic viscosity, ν_t is the eddy viscosity and g the acceleration due to gravity.

¹⁰³ The projection method (Chorin, 1968) is used for pressure treatment and a preconditioned ¹⁰⁴ BiCGStab solver (van der Vorst, 1992) is used to solve the resulting Poisson pressure equa-¹⁰⁵ tion. Turbulence modeling is carried out using the two equation k- ω model proposed by ¹⁰⁶ Wilcox (1994) with transport equations for turbulent kinetic energy k and specific turbu-¹⁰⁷ lence dissipation rate ω given by:

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$$\frac{\partial k}{\partial t} + u_j \frac{\partial k}{\partial x_j} = \frac{\partial}{\partial x_j} \left[\left(\nu + \frac{\nu_t}{\sigma_k} \right) \frac{\partial k}{\partial x_j} \right] + P_k - \beta_k k \omega$$
(3)

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$$\frac{\partial\omega}{\partial t} + u_j \frac{\partial\omega}{\partial x_j} = \frac{\partial}{\partial x_j} \left[\left(\nu + \frac{\nu_t}{\sigma_\omega} \right) \frac{\partial\omega}{\partial x_j} \right] + \frac{\omega}{k} \alpha P_k - \beta \omega^2 \tag{4}$$

where, P_k is the production rate and closure coefficients $\sigma_k = 2$, $\sigma_\omega = 2$, $\alpha = 5/9$, $\beta_k = 9/100$, $\beta = 3/40$. Wall functions for k and ω are defined as follows:

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$$k = \frac{u_T}{\sqrt{\beta_k}}, \qquad w = \frac{k^{1/2}}{(\beta_k)^{1/4} \kappa y} \tag{5}$$

where κ is the Karman constant, u_T is the friction velocity (Wilcox, 1994). The turbulence production based on the strain rate in the numerical wave tank results in overproduction of turbulence because of the large strain in the flow due to wave propagation. Eddy viscosity is bounded as shown by Durbin (2009) are used to avoid this as shown below:

$$\nu_t = \min\left(\frac{k}{\omega}, \sqrt{\frac{2}{3}}\frac{k}{|\mathbf{S}|}\right) \tag{6}$$

where \mathbf{S} stands for strain from the source terms in the transport equations. The strain tensor is defined as:

$$S_{ij} = \frac{1}{2} \left(\frac{\partial u_j}{\partial x_i} + \frac{\partial u_i}{\partial x_j} \right) \tag{7}$$

In a two-phase CFD model, the large difference in density at the interface between air and water causes an overproduction of turbulence at the interface because the standard k- ω model does not account for the free surface where the turbulent eddies from the water are dissipated. This effect accounted for by defining the specific turbulent dissipation term around the interface ω_s as shown by Naot and Rodi (1982):

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$$\omega_s = \frac{c_{\mu}^{-\frac{1}{4}}}{\kappa} k^{\frac{1}{2}} \cdot \left(\frac{1}{y'} + \frac{1}{y^*}\right)$$
(8)

where $c_{\mu} = 0.07$ and $\kappa = 0.4$. The variable y' is the virtual origin of the turbulent length scale, and was empirically found to be 0.07 times the mean water depth Hossain and Rodi (1980). Including the distance y^* from the nearest wall gives a smooth transition from the free surface value to the wall boundary value of ω .

132 Free Surface

The free surface is determined with the level set method, where the zero level set of the signed distance function $\phi(\vec{x}, t)$ is used to represent the interface between air and water (Osher and Sethian, 1988). The level set function gives the shortest distance from the interface for all the points in the flow domain. The sign of the function distinguishes between the two fluids across the interface as shown in Eq. (9):

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$$\phi(\vec{x},t) \begin{cases} > 0 & if \ \vec{x} \ is \ in \ phase \ 1 \\ = 0 & if \ \vec{x} \ is \ at \ the \ interface \\ < 0 & if \ \vec{x} \ is \ in \ phase \ 2 \end{cases}$$
(9)

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The level set function is moved under the influence of an external velocity field u_j with the convection equation in Eq. (10):

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$$\frac{\partial \phi}{\partial t} + u_j \frac{\partial \phi}{\partial x_j} = 0 \tag{10}$$

The level set function loses its signed distance property on convection and is reinitialized after every iteration using a partial differential equation based reinitialisation procedure by Peng et al. (1999) to regain its signed distance property.

145 Discretization schemes

The fifth-order conservative finite difference Weighted Essentially Non-Oscillatory (WENO) 146 scheme proposed by Jiang and Shu (1996) is applied for the discretization of the convective 147 terms of the RANS equation. The level set function, turbulent kinetic energy and the spe-148 cific turbulent dissipation rate are discretized using the Hamilton-Jacobi formulation of the 149 WENO scheme by Jiang and Peng (2000). The WENO scheme is a minimum third-order 150 accurate and numerically stable even in the presence of large gradients. Time advancement 151 for the momentum and level set equations is carried out using a Total Variation Diminishing 152 (TVD) third-order Runge-Kutta explicit time scheme proposed by Shu and Osher (1988). 153 Adaptive time stepping is employed to satisfy the CFL (Courant-Friederichs-Lewy) criterion 154 based on the maximum velocities in the domain and the source term contributions to the 155 Navier-Stokes equations. This ensures numerical stability and accuracy throughout the sim-156 ulation with an optimal value of time step size. A first-order implicit Euler scheme is used for 157 the time advancement of the turbulent kinetic energy and the specific turbulent dissipation, 158 as these variables are mostly source term driven with a low influence of the convective terms. 150 Diffusion terms of the velocities are also subjected to implicit treatment in order to remove 160 the diffusion terms from the CFL criterion. 161

The numerical model uses a uniform Cartesian grid for the spatial discretization together with the Immersed Boundary Method (IBM) to represent the irregular boundaries in the domain. Berthelsen and Faltinsen (2008) developed the local directional ghost cell IBM to extend the solution smoothly in the same direction as the discretization, which is adapted to three dimensions in the current model. REEF3D is fully parallelized using the domain decomposition strategy and MPI (Message Passing Interface).

¹⁶⁸ Wave generation and absorption

The numerical wave tank uses the relaxation method (Larsen and Dancy, 1983) for wave generation and absorption. This method requires a certain length of the wave tank to be reserved as wave generation and absorption zones. Relaxation functions are used to moderate the velocity and the free surface using a wave theory in the relaxation zones with Eq. (11):

$$u_{relaxed} = \Gamma(x)u_{analytical} + (1 - \Gamma(x))u_{computational}$$

$$\phi_{relaxed} = \Gamma(x)\phi_{analytical} + (1 - \Gamma(x))\phi_{computational}$$
(11)

where $\Gamma(x)$ is the relaxation function and $x \in [0, 1]$ is the *x*-coordinate scaled to the length of the relaxation zone. The relaxation function proposed by Jacobsen et al. (2012), shown in Eq. (12) is used in the numerical model.

$$\Gamma(x) = 1 - \frac{e^{(1-x)^{3.5}} - 1}{e - 1}$$
 (12)

The numerical model can simulate waves defined by several wave theories such as linear, 179 2nd-order Stokes, 5th-order Stokes, Cnoidal and solitary wave theory depending on the case 180 being studied. The wave theory used for wave generation by the relaxation method is chosen 181 according to the wave steepness and the water depth in the simulation. In the current study, 182 waves with steepness H/L = 0.003 are generated using the linear theory and with steepness 183 H/L = 0.06 and 0.10 are generated using the 5th-order Stokes wave theory. Typically, the 184 wave generation zone is one wavelength long and the absorption zone is two wavelengths 185 long. In the wave generation zone, the computational values of velocity and free surface are 186 raised to the analytical values prescribed by wave theory. The generation zone releases waves 187 into the working zone of the tank, where the objects to be studied are placed. The relaxation 188

function in the generation zone also absorbs reflections from structures in the wave tank and 189 prevents them from affecting the generated waves. At the end of the tank, the wave enters 190 the numerical beach. Here, the computational values of velocity and free surface are reduced 191 to zero in a smooth manner. This simulates the effect of a beach, where the wave energy 192 is removed from the wave tank and avoids reflections. In a three-dimensional numerical 193 wave tank, the relaxation functions for wave generation and absorption form the boundary 194 conditions at the two ends of the tank. No-slip wall boundary conditions are enforced on 195 the side walls and the bottom of the wave tank. The top of the wave tank is open to the 196 atmosphere and symmetry boundary condition is applied. 197

198 CALCULATION OF WAVE FORCES

¹⁹⁹ Numerical evaluation of wave forces

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The numerical model evaluates the wave force F on an object as the integral of the pressure p and the surface normal component of the viscous shear stress tensor τ on the object according to Eq. (13):

$$F = \int_{\Omega} (-\mathbf{n}p + \mathbf{n} \cdot \tau) d\Omega \tag{13}$$

where **n** is the unit normal vector pointing into the fluid and Ω is the surface of the object. This is readily accomplished by the numerical model as the values for the pressure and shear stress are available at every point in the domain at any given time of the simulation. The no-slip wall boundary condition is applied on the surface of the object and the effect of the boundary layer is modeled through the wall laws in the turbulence model.

209 Analytical formula for wave forces

Potential theory is used to obtain the wave diffraction potential and calculate the force on a single cylinder using the equation presented by MacCamy and Fuchs (1954), shown in Eq. (14):

$$|F| = \left|\frac{4\rho gia \ tanh(kd)}{k^2 H_1'(kr)}\right| \tag{14}$$

where $i = \sqrt{-1}$, a is the incident wave amplitude, $k = 2\pi/L$ the wave number, d the water 214 depth and H'_1 the first derivative of the Hankel function of the first kind and r the radius of 215 the cylinder. The parameter kr represents the ratio of the diameter of the cylinder to the 216 incident wavelength and thus a measure of the diffraction, with higher values of kr signifying 217 a stronger diffraction regime. 218

An extension of the diffraction theory proposed by Linton and McIver (2001) to calculate 219 wave forces on multiple cylinders placed in proximity is presented in Eq. (15): 220

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$$A_{m}^{l} + \sum_{\substack{j=1\\ \neq l}}^{N} \sum_{n=-M}^{M} A_{j}^{n} Z_{n}^{j} e^{i(n-m)\alpha_{jl}} H_{n-m}(kR_{jl}) = -I_{l} e^{im(\frac{\pi}{2}-\beta)}$$

$$l = 1, \dots, N, \ m = -M, \dots, M.$$
(15)

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where, M is the order of the solution, N is the number of cylinders, I is the incident wave 224 potential, β is the angle of wave propagation with respect to the x-axis, H is the Hankel 225 function of the first kind, R_{jl} is the length of the line joining the centers of the *j*th and the *l*th 226 cylinder, α_{jk} is the angle between the x-axis and the line joining the centers of the cylinders 227 and $Z = J'(kr_j)/H'(kr_j)$, where J is the Bessel function of the first kind. The unknown 228 coefficients A are to be evaluated. This results in a set of N(2M+1) equations. Linton and 229 McIver (2001) suggest that a value of M = 6 provides sufficiently accurate solutions and 230 is used in the equations to obtain the analytical prediction of wave forces for low steepness 231 incident waves. The unknown coefficients A are evaluated by solving Eq. (15) and the first-232 order wave force magnitudes $|F^{j}|$ on the *j*th cylinder are obtained using Eq. (16): 233

$$\left|\frac{F^{j}}{F}\right| = \frac{1}{2} \left|A_{-1}^{j} \pm A_{1}^{j}\right| \tag{16}$$

The subtraction of the coefficients on the right hand side gives the wave force along the 235 x-axis and the addition of the terms gives the wave force along the y-axis. In the current 236 study, the angle of incidence $\beta = 0$ and the waves propagate along the x-axis. 237

238 RESULTS AND DISCUSSION

Wave interaction with three arrangements of the cylinder array as shown in Fig. (1) with 239 two different incident wavelengths at small and large wave steepness are considered. The 240 first arrangement consists of four cylinders placed with a diagonal along the direction of wave 241 propagation (Fig. 1a). In the second arrangement, the downstream cylinder on the inline 242 diagonal is removed, resulting in a triangular arrangement of three cylinders (Fig. 1b) and in 243 the third setup, a triangular arrangement is obtained by removing the upstream cylinder on 244 the inline diagonal (Fig. 1c). Cylinders of diameter D = 0.60 m are arranged at the vertices 245 of a square of side 2D=1.20 m in a water depth of d=0.60 m. The center-to-center distance 246 is taken to be 2D to maintain the same distance used in the results presented by Linton and 247 Evans (1990). Also, in the case of wave energy device arrays, this is a suitable of separation 248 between devices in a group. The numerical wave tank used for the simulations is 16 m long, 249 8 m wide and 1.20 m high with a grid size of dx = 0.025 m resulting in 9.83 million cells. 250 The computational grid around a cylinder in the wave tank is shown in Fig. (2). The width 251 of the wave tank is chosen such that the reflections from the side walls of the tank do not 252 significantly influence the results in the wave tank. The outer surface of the cylinders closest 253 to the wall (2 and 4) are 2.55D from the wall and the surface of the cylinders in the center 254 (1 and 4) are 6.16D from the side wall. An overview of the simulations carried out is listed 255 in Table 1. According to the equations by Linton and Evans (1990), wave interaction with 256 the arrangement of four cylinders in Fig. (1a) results in wave near-trapping for a diffraction 257 parameter kr = 1.70. Thus, simulations are carried out for kr = 0.94 to simulate the 258 wave interaction away from wave near-trapping (setup A1) and for kr = 1.70 (setup B1) to 259 simulate wave near-trapping at a low incident wave steepness of H/L = 0.004. Further, the 260 wave interaction for the same values of the diffraction parameter kr is simulated at a higher 261 wave steepness of H/L = 0.060 to investigate the differences in the diffraction regime and 262 wave forces from that seen for the low incident wave steepness. 263

At first, the numerical computation of the wave forces on cylinders is validated by sim-

ulating wave interaction with a single cylinder and a group of four cylinders (setup A1) 265 with low steepness incident waves (H/L = 0.004) of wavelength L = 2.00 m and height 266 H = 0.008 m. The numerical results for the single cylinder $F_0 = 16.20$ N are compared with 267 the analytically expected values using the MacCamy-Fuchs theory $F_{0t} = 15.90$ N in Eq. (14) 268 in Fig. (3) with only a difference of 1.8%. In the case of the four cylinders, the computed 269 forces on each of the cylinders is compared with the analytical prediction using Eq. (16) in 270 Fig. (4) and a good agreement is seen for all the four cylinders, with differences less than 271 2.0%. 272

In the following sections, the wave interaction with the three setups illustrated in Fig. (1) is investigated with low and high steepness waves for two different wavelengths.

²⁷⁵ Wave interaction with incident waves of low steepness, H/L = 0.004

The wave forces on cylinders for the setups A1, A2 and A3 with incident wavelength 276 L = 2.00 m and height H = 0.008 m resulting in a low wave steepness of H/L = 0.004 and 277 diffraction parameter kr = 0.94 are computed as listed in Table (1). The computed wave 278 forces on each cylinder are scaled to the numerically determined force on a single cylinder, 279 $F_0 = 16.20$ N and presented in Fig. (5). It is seen from Fig. (5a) that cylinder 1 experiences 280 the highest wave forces in both setups 1 and 2. It is also observed that in the presence of 281 the downstream cylinder 3, in setup 1, the wave force on the upstream cylinder 1 is higher 282 with $1.30F_0$ compared to $1.15F_0$ in the absence of the downstream cylinder 3 in setup 2. In 283 the case of cylinders 2 and 4, the highest wave forces are experienced in setup 3, when the 284 upstream cylinder 1 is removed from the arrangement as seen in Fig. (5b). In the presence 285 of the upstream cylinder 1, cylinders 2 and 4 experience similar wave forces for both setups 286 1 and 2. From Fig. (5c), the downstream cylinder 3 experiences the highest wave forces in 287 the presence of the upstream cylinder 1 and lower forces in the absence of the upstream 288 cylinder. Thus, in the four cylinder arrangement shown in Fig. (1a), the presence of the 289 upstream cylinder reduces the wave forces on cylinders 2 and 4 behind it, but leads to a 290 higher wave force on the downstream cylinder 3. From the results presented above, this can 291

be attributed to the increased total pressure acting on the downstream cylinder 3 due to the 292 inline presence of the upstream cylinder 1. Further, the diffraction parameter is changed to 293 kr = 1.70 and the wave forces on the cylinders for the setups B1, B2 and B3 with incident 294 wavelength L = 1.11 m and height H = 0.004 m (H/L=0.0036) are computed. In this 295 arrangement, the equations by Linton and McIver (2001) predict large wave forces on the 296 cylinders in setup 1, due to near-wave trapping. The numerical results follow with this 297 prediction and the wave forces on all four cylinders in setup 1 experiences larger forces than 298 the wave force computed for a single cylinder, $F_0 = 3.90$ N. In the case of cylinder 1, the 299 wave force is $2.00F_0$ in setup 1, whereas it is lowered to $1.30F_0$ when the downstream cylinder 300 is removed in setup 2 as seen in Fig. (6a). For cylinders 2 and 4, the wave forces are similar 301 $(1.10F_0)$ in all the three setups from Fig. (6b). The downstream cylinder 3 also experiences 302 similar forces of $1.60F_0$ both in the presence and absence of the upstream cylinder in Fig. (6c). 303 So, under conditions resulting in near wave trapping for the four cylinder arrangement, the 304 wave forces on the upstream cylinder is highly influenced by the presence of the downstream 305 cylinder but the effect of the upstream cylinder on the other cylinders in the arrangement is 306 negligible. 307

From the simulations presented above, it is observed that the wave forces on cylinders 308 in different arrangements is influenced both by the neighboring cylinders and the incident 309 wavelength. The effect of wave near-trapping for setup 1 for diffraction parameter kr =310 1.70 predicted by the analytical formula (Eq. 16) is replicated in the simulation for setup 311 B1. Under conditions resulting in near-trapping of incident waves for the four cylinder 312 arrangement, the wave force on the upstream cylinder is two times the force on a single 313 cylinder. On the hand, the force on cylinder 1 is reduced in the absence of the downstream 314 cylinder 3 in setup B2. The wave forces on the other cylinders are slightly influenced by the 315 presence of the upstream cylinder and experience forces higher than the force on a single 316 cylinder in all the arrangements. With diffraction parameter kr = 0.94, there is no near-317 trapping of waves in setup A1 and the presence of the upstream cylinder influences all the 318

other cylinders in the arrangement as seen from the results for setups A2 and A3. The upstream cylinder itself experiences higher wave forces in the presence of the downstream cylinder. In addition, the downstream cylinder experiences higher forces in the presence of the upstream cylinder. So, away from conditions leading to wave near-trapping, the neighboring cylinders have a significant influence on the wave forces experienced by a cylinder in the group.

To obtain a better understanding of the wave regime around the cylinders, the free 325 surface elevation around the cylinder arrays is studied when the incident wave crest is in the 326 region enclosed by the cylinders. The diffracted waves in the region between the cylinders 327 in setups B1-B3 is presented in Fig. (7). In setup B1 with four cylinders (Fig. 7a and 7b), 328 a higher free surface elevation in the region in between the cylinders is seen along with a 329 deep trough in front of cylinder 3. The wave near-trapping in this case results in large 330 variations in the free surface in the region in between the region. The large difference in 331 the free surface elevations correspond to large differences in the pressure around cylinders 332 1 and 3, resulting in large forces on the cylinders. On removing the downstream cylinder 3 333 from the arrangement in setup B2 (Fig. 7c and 7d), the region in between the cylinders has 334 lower free surface elevations than in setups B1 and B2. In the absence of the downstream 335 cylinder 3, wave trapping in the region between the cylinders does not occur and cylinder 336 1 experiences lower forces. The free surface elevation in the immediate vicinity of cylinders 337 2 and 4 is largely unaltered from the pattern seen for setup B1. In Fig. (7e and 7f), when 338 cylinder 1 is removed, the high free surface elevation is around cylinders 2 and 4 is similar to 339 setup B1 except for the lower free surface elevation in the region in the center. This shows 340 that the pressure difference around cylinders 2 and 4 is similar in all the three arrangements 341 and justifies the similar wave forces computed using Eq. (13) for cylinders 2 and 4 for all 342 the arrangements. The free surface elevation around the downstream cylinder is also similar 343 to to that in setup B1, corresponding to similar pressure differences and resulting in similar 344 forces on the downstream cylinder 3 in both setups B1 and B3. 345

₃₄₆ Wave interaction with incident waves of high steepness, H/L = 0.06

In order to investigate the difference in the wave interaction with the cylinder groups under the influence of high steepness incident waves, simulations are carried out with the same wavelengths as in the previous section but with a higher incident wave steepness of H/L = 0.06.

The wave forces on all the cylinders in setups C1, C2 and C3 (kr = 0.94) with incident 351 wavelength L = 2.00 m, height H = 0.12 m are presented in Fig. (8). From Fig. (8a), the 352 wave forces on the upstream cylinder 1 are higher $(1.60F_0)$ in the presence of the downstream 353 cylinder 3 in setup 1, than in the absence of the downstream cylinder 3 in setup 2 $(1.40F_0)$. 354 Cylinders 2 and 4 experience similar forces in all the three setups, almost the same force as 355 that on a single cylinder, $F_0 = 178.20$ N, but with slightly higher forces on cylinders 2 and 356 4 in the absence of the upstream cylinder as seen in Fig. (8b). The downstream cylinder 3 357 experiences a wave force of $0.75F_0$ in the presence of the upstream cylinder 1 and a lower 358 force of $0.55F_0$ in the absence of the upstream cylinder in Fig. (8c). It is also observed that 359 the wave forces on the downstream cylinder are the lowest in the group and lesser than the 360 force on a single cylinder. 361

Further, the wave forces computed on all the cylinders in setups D1, D2 and D3 (kr =362 1.70) with incident wavelength L = 1.11 m and height H = 0.066 m (H/L=0.06) are pre-363 sented in Fig. (9) scaled to $F_0 = 50.50$ N. The upstream cylinder 1 experiences wave forces 364 of about $1.20F_0$ both in the presence and absence of the downstream cylinder 3. Cylinders 365 2 and 4 experience similar forces of about $0.90F_0$ in all the arrangements. The downstream 366 cylinder 3 experiences wave forces of about $0.85F_0$. Thus, also in this case, the upstream 367 cylinder experiences the highest forces in all the arrangements and all the other cylinders 368 experience forces lower than F_0 for all arrangements. 369

From the simulations for high steepness incident waves, the upstream cylinder experiences the highest forces and all the other cylinders in the arrangement experience lower forces. The large wave forces on the cylinders seen in setup B1 with low incident wave steepness, due to wave near-trapping is not seen for the high steepness waves in setup D1 for the same diffraction parameter kr = 1.70. This points towards the break-down of the wave neartrapping condition at higher wave steepnesses.

Further insight is obtained regarding the wave diffraction effects for higher steepness 376 incident waves by studying the free surface elevations in the region around the cylinder arrays 377 for setups D1-D3, with incident wavelength L = 1.11 m and wave steepness H/L = 0.06 in 378 Fig. (10). The formation of multiple semi-circular diffracted waves around the cylinders in 379 all three setups is seen. For setup D1 (Fig. 10a), the region in between the cylinders does not 380 show large free surface elevations and it can be concluded that the near-trapping phenomenon 381 does not occur in this case. As a result, the cylinders do not experience extremely high wave 382 forces in comparison to the wave force on a single cylinder. When the downstream cylinder 383 3 is removed from the cylinder array in setup D2 (Fig. 10c), the wave diffraction patterns 384 around the cylinder is similar to that in setup D1 and the cylinders experience similar forces 385 in both arrangements. In Fig. (10e), on removing cylinder 1, high free surface are seen but 386 restricted to small regions around cylinder 2 and 4. The free surface elevations in front of 387 cylinder 3 is similar to that seen in setup D1 with four cylinders and thus, it experiences 388 similar forces in both arrangements. 389

³⁹⁰ Wave interaction with incident waves of very high steepness, H/L = 0.10

The deviation of the numerical results for wave forces from the prediction using the analytical formula is already seen at a higher wave steepness of H/L = 0.06 compared to H/L = 0.004. To further explore the effect of high steepness waves, simulations are carried out with an even higher steepness of H/L = 0.10 for both the incident wavelengths L = 2.00m (cases E1-E3) and L = 1.11 m (cases F1-F3) for all the three different configurations of the cylinders considered in the study.

The computed wave force on each cylinder in the three setups for an incident wave height H = 0.20 m and wavelength L = 2.00 m is presented in Fig. (11) and scaled to the wave force on a single cylinder $F_0 = 310.6$ N. It is seen from Fig. (11a) that the wave force on

the upstream cylinder 1 in the presence of the downstream cylinder 3 in setup 1 is slightly 400 higher $(1.25F_0)$ than in the absence the downstream cylinder in setup 2 $(1.07F_0)$. This is 401 similar to the observation made in cases C1-C3 for a wave steepness of H/L = 0.06. In the 402 case of cylinders 2 and 4, the similar wave forces are computed for setups 1 and 2 in the 403 presence and absence of the downstream cylinder. But slightly higher forces are experienced 404 in the absence of the upstream cylinder 1 from Fig. (11b). At this incident wave steepness, 405 the absence of the upstream cylinder slightly increases the total pressure on cylinders 2 and 406 4 resulting in higher wave forces. This is also similar to the trend seen in the case of incident 407 steepness H/L = 0.06 in cases C1-C3. The wave force on the downstream cylinder 3 in 408 the absence of the upstream cylinder 1 in Fig. (11c) is $0.67F_0$, slightly higher than $0.56F_0$ 409 computed in the presence of the upstream cylinder. 410

On the increase of the incident wave steepness for an incident wavelength of L = 2.00411 m, the computed wave forces are mostly seen to be lower than the analytical prediction, 412 which match the computed values at the lowest wave steepness of H/L = 0.004. This is 413 illustrated in Fig. (12) showing the variation of the wave force with respect to the incident 414 wave steepness, on each cylinder in the different setups presented in this paper. Generally, 415 the ratio F/F_0 reduces as the wave steepness H/L is increased from 0.004 to 0.06. On further 416 increase in the wave steepness to 0.10, the ratio of F/F_0 in each case is either similar to the 417 value at H/L = 0.06 or further lowered. 418

The wave forces computed for cases F1-F3 with an incident wave height of H = 0.055419 m, wavelength 1.11 m and wave steepness H/L = 0.1 are presented in Fig. (13), scaled to 420 the wave force on a single cylinder, $F_0 = 45.5$ N. Figure 13a shows that the force on the 421 upstream cylinder 1 is $1.23F_0$ in the absence of the downstream cylinder in setup 2, while 422 the wave force on cylinder 1 in the presence of the downstream cylinder is lower at $1.02F_0$. 423 In the case of cylinders 2 and 4, the wave forces are $0.90F_0$, $0.82F_0$ and $1.02F_0$ in setups 1, 424 2 and 3 respectively in Fig. (13b). Cylinders 2 and 4 experience higher forces in the absence 425 of the upstream cylinder in setup 3. The wave force on the downstream cylinder 3 is higher 426

in the absence of the upstream cylinder with forces of $0.67F_0$ and $0.76F_0$ computed in setup 427 1 and setup 3 respectively, shown in Fig. (13c). The results obtained for this steepness of 428 H/L = 0.10 for L = 1.11 m are qualitatively similar to the results obtained at H/L = 0.06. 429 The variation of the wave forces on each cylinder in the different setups for different 430 incident wave steepness is presented in Fig. (14). A large reduction is seen in the relative 431 wave force on cylinder as the wave steepness is increased from H/L = 0.004 to H/L = 0.06432 due to the breakdown of the wave near-trapping phenomenon in setup 1. Further increase 433 in the wave steepness to 0.10 results in some more reduction in the relative wave force on 434 cylinder 1. In setup 2, the change in the relative wave forces on changing the incident wave 435 steepness is not very significant. For cylinders 2 and 4, a slight reduction in the relative wave 436 forces is seen when the wave steepness is increased from H/L = 0.004 to 0.06 and on further 437 increase in H/L, the values for F/F_0 do not change significantly. As seen before, the change 438 in the setup have only a minor influence on the wave forces acting on cylinders 2 and 4. The 439 relative wave force on the downstream cylinder 3 is reduced significantly on increasing the 440 incident wave steepness from 0.004 to 0.06 due to the breakdown of the wave near-trapping 441 phenomenon and further increase in H/L leads to a small further reduction. The relative 442 wave forces on cylinder 3 the presence and absence of the upstream cylinder are seen to be 443 similar. This further supports the findings in previous sections that the wave forces on the 444 upstream cylinder are affected due to the presence of the downstream cylinder. 445

The difference in the wave diffraction regime at low and high incident wave steepnesses 446 is seen from the free surface elevations around the cylinder arrays. This difference results in 447 the different forces seen in the case of high steepness waves than that predicted by analytical 448 formula, that assumes low steepness incident waves. The formation of multiple semi-circular 449 diffracted waves around the cylinders in seen for higher incident wave steepness. On the other 450 hand, in the case of low steepness incident waves, the wave diffraction results in bending of 451 the waveform and for L = 1.11 m the phenomenon of near-trapping of waves is observed. 452 The formation of multiple diffracted waves at a higher incident wave steepness results in a 453

⁴⁵⁴ break down of the conditions leading to wave near trapping. Since potential theory assumes ⁴⁵⁵ a low incident wave steepness, formulae based on potential theory cannot account for the ⁴⁵⁶ diffraction effects at higher wave steepnesses. It is also observed that in the absence of the ⁴⁵⁷ downstream cylinder 3 in the four cylinder array, the wave forces on the upstream cylinder ⁴⁵⁸ 1 are reduced.

In the context of an array of oscillating water column wave energy devices, the phe-459 nomenon of wave near-trapping could lead to higher free surface oscillations in the vicinity 460 of the devices resulting in higher energy capture. The results presented above, though, show 461 that wave near-trapping breaks down on an increase in the incident wave steepness. Also, 462 the relative wave forces on each of the device is reduced on the increase of incident wave 463 steepness, even at conditions that theoretically lead to wave near-trapping. Thus, for the 464 structural design of the device, wave near-trapping is of concern only at very low incident 465 wave steepness. At higher wave steepnesses, the total force on the device forms the criterion 466 for the structural design of the device. Also, an advantage in terms of potential higher energy 467 capture due to wave near-trapping is only available at a very low incident wave steepness. 468 For further insight into the free surface variations in between the devices and the effect on 469 the energy captured by the devices, further research is needed using a representation of the 470 oscillating water column device in the wave tank. 471

472 CONCLUSION

The open source CFD model REEF3D is used to simulate wave interaction with arrays of 473 cylinders to study the change in the hydrodynamics and the wave forces in the presence and 474 absence of cylinders along the the direction of wave propagation. The numerical model was 475 validated using equations based on potential theory for low incident wave steepness for both a 476 single cylinder and an arrangement of four cylinders. The phenomenon of wave near-trapping 477 resulting in large free surface elevations in the vicinity of the cylinders and large wave forces 478 on the cylinders is observed at low wave steepness in accordance with analytical expectation. 479 The difference in the wave diffraction for different incident wavelengths and wave steepnesses 480

⁴⁸¹ is also studied and found that significant radiating waves are reflected from the cylinders at
⁴⁸² higher wave steepnesses, which are not observed at lower wave steepnesses. The phenomenon
⁴⁸³ of wave near-trapping is seen to breakdown for higher incident wave steepness due this
⁴⁸⁴ difference in the diffraction pattern.

The presence of the downstream cylinder generally results in a higher wave force on 485 the upstream cylinder with a 30% increase for low steepness waves and a 60% increase for 486 high steepness waves compared to the force on a single cylinder, at conditions away from 487 theoretical near-wave trapping. Under theoretical conditions for wave near-trapping, the 488 upstream experiences about two times the force on a single cylinder at low steepness and a 480 20% higher force for high steepness waves. However, at a higher incident wave steepness and 490 break-down of the near-trapping, though the wave forces on the upstream cylinder are the 491 highest in the array, the rest of the cylinders experience lower forces. It can be concluded 492 that the wave interaction with a four cylinder array with a given center-to-center distance 493 depends not only on the incident wavelength but also the incident wave steepness. The effect 494 of higher steepness incident waves cannot be effectively accounted for using formulae based 495 on potential theory. In context of oscillating water column wave energy devices, a potential 496 advantage for higher energy capture due to wave near-trapping is possible only at a very low 497 incident wave steepness. From the structural design point of view of the device, the total 498 force from a higher steepness wave would decide the design requirement and the effect of 499 wave near-trapping can be ignored as it breaks down at a higher incident wave steepness. 500

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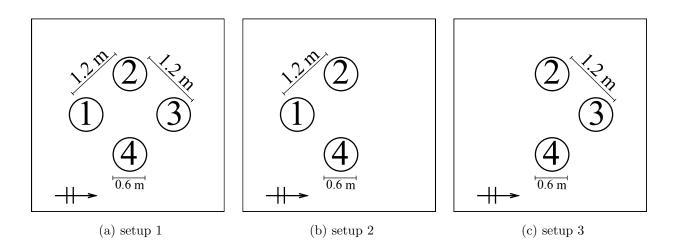


Fig. 1. Different arrangements used in the study

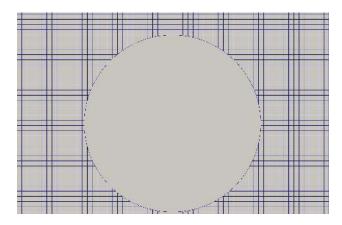


Fig. 2. Computational mesh around a cylinder in the numerical wave tank

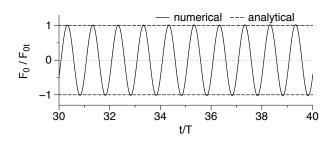


Fig. 3. Comparison of numerical and analytical wave forces on a single cylinder for H = 0.008 m and L = 2.00 m

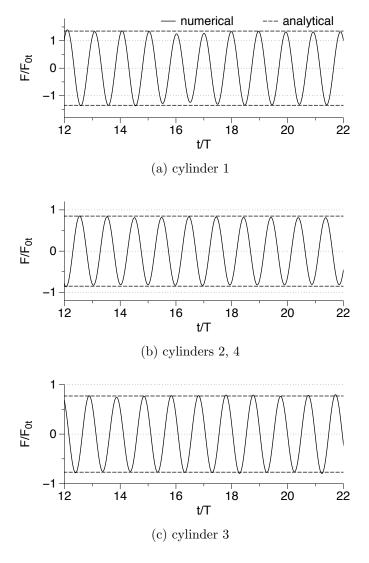


Fig. 4. Comparison of the numerical and analytical wave forces on the four cylinders in setup A1 with H = 0.008 m and L = 2.00 m for kr = 0.94

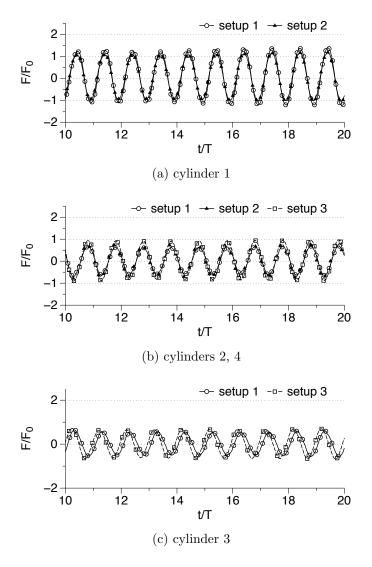


Fig. 5. Comparison of wave forces on each of the cylinders in setups A1, A2 and A3 for steepness H/L = 0.004 with H = 0.008 m and L = 2.00 m for kr = 0.94

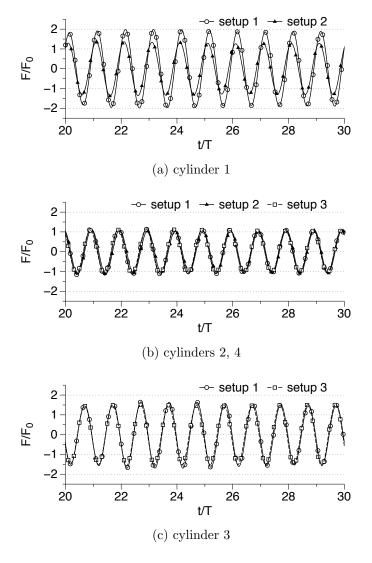


Fig. 6. Comparison of wave forces on each of the cylinders in setups B1, B2 and B3 for steepness H/L = 0.004 with H = 0.004 m and L = 1.11 m for kr = 1.70

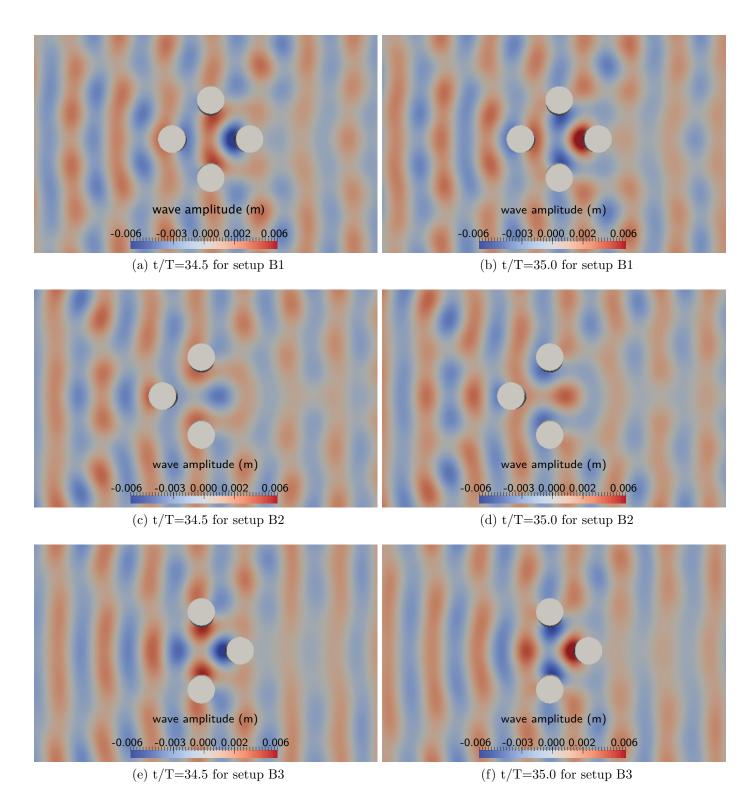


Fig. 7. Free surface elevations in the part of the domain around the cylinders for low steepness H/L = 0.004 in setups B1, B2 and B3 with H = 0.004 m, L = 1.11 m, for kr = 1.70

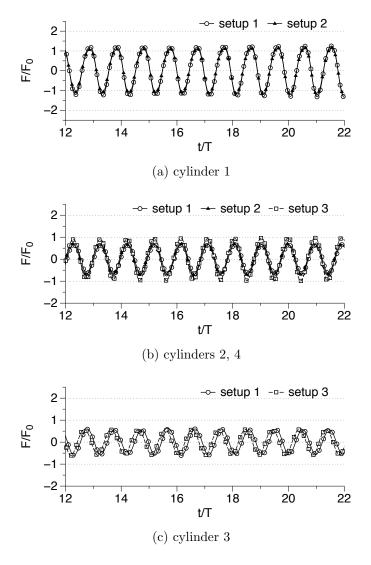


Fig. 8. Comparison of wave forces on each of the cylinders in setups C1, C2 and C3 for steepness H/L = 0.06 with H = 0.12 m and L = 2.00 m for kr = 0.94

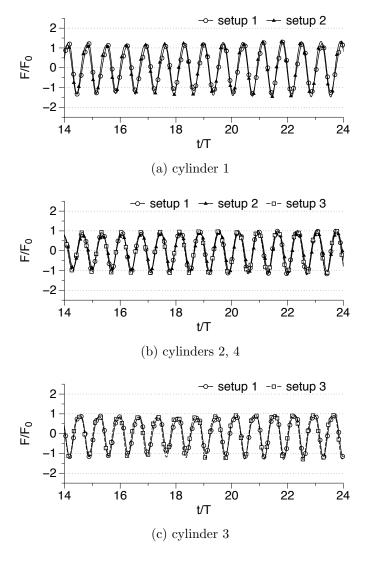
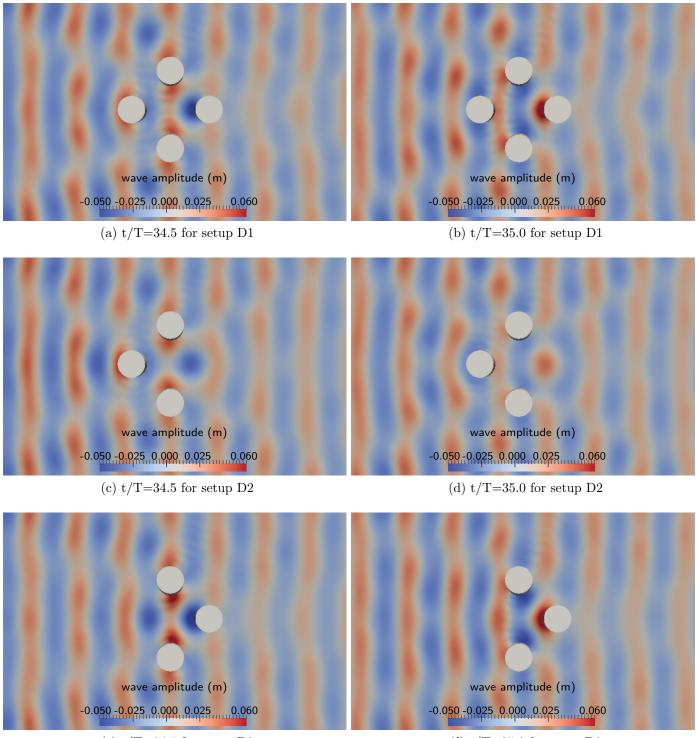


Fig. 9. Comparison of wave forces on each of the cylinders in setups D1, D2 and D3 for steepness H/L = 0.06 with H = 0.066 m and L = 1.11 m for kr = 1.70



(e) t/T=34.5 for setup D3 $\,$

(f) t/T=35.0 for setup D3

Fig. 10. Free surface elevation in the part of the domain around the cylinders for steepness H/L = 0.06 in setups D1, D2 and D3 with H = 0.066 m, L = 1.11 m for kr = 1.70

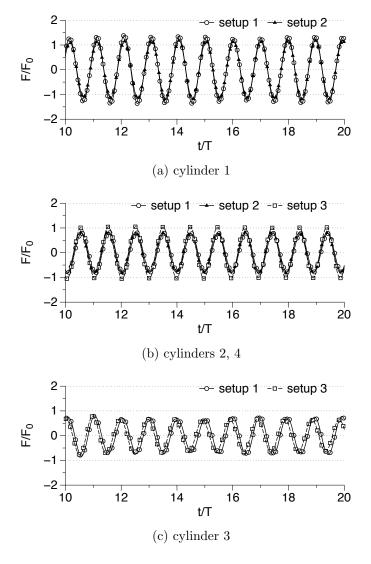


Fig. 11. Comparison of wave forces on each of the cylinders in setups E1, E2 and E3 for steepness H/L = 0.10 with H = 0.20 m and L = 2.00 m for kr = 0.94

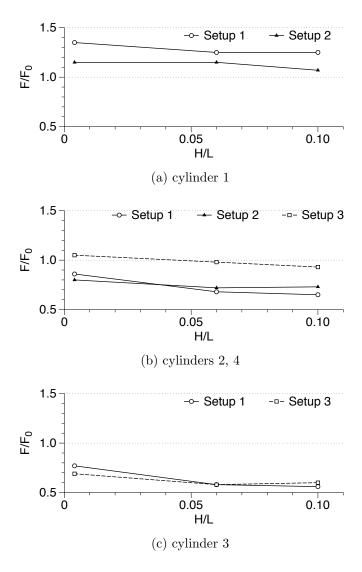


Fig. 12. Variation of the wave forces on the cylinders in different setups for different incident wave steepness with L = 2.00 m, kr = 0.94

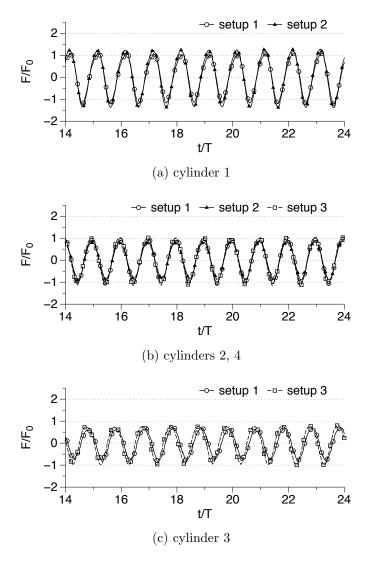


Fig. 13. Comparison of wave forces on each of the cylinders in setups F1, F2 and F3 for steepness H/L = 0.10 with H = 0.11 m and L = 1.11 m for kr = 1.70

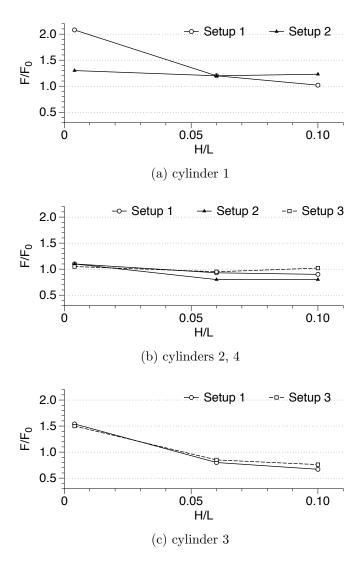


Fig. 14. Variation of the wave forces on the cylinders in different setups for different incident wave steepness with L = 1.11 m, kr = 1.70

Table 1. Details of the setups used in the different simulations

				- T			
No.	H(m)	L (m)	KC	H/L	kr	$F_0(N)$	Arrangement
A1							Setup 1
A2	0.008	2.00	0.04	0.004	0.94	16.20	Setup 2
A3							Setup 3
B1							Setup 1
B2	0.004	1.11	0.02	0.004	1.70	3.90	Setup 2
B3							Setup 3
C1							Setup 1
C2	0.120	2.00	0.66	0.06	0.94	178.20	Setup 2
C3							Setup 3
D1							Setup 1
D2	0.066	1.11	0.35	0.06	1.70	50.50	Setup 2
D3							Setup 3
E1							Setup 1
E2	0.20	2.00	1.10	0.10	0.94	310.60	Setup 2
E3							Setup 3
F1							Setup 1
F2	0.11	1.11	0.57	0.10	1.70	45.40	Setup 2
F3							Setup 3