

VAPOR-LIQUID EQUILIBRIA FOR THE NITROGEN-METHANE-CARBON DIOXIDE SYSTEM*

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Vapor-liquid equilibrium data for the nitrogen-methane-carbon dioxide system were measured by static method at -40°C to 0°C and up to 100 atm. The applicability of the BWR equation for this ternary system was examined. A marked improvement in the equilibria was obtained by introducing correction factors determined from the data of each prediction of vapor-liquid binary system.

In a previous paper²⁾, we showed that vapor-liquid equilibrium relations for systems consisting of carbon dioxide and light hydrocarbon could not be well predicted by the BWR equation¹⁾. In such a case, the BWR equation was sufficiently improved by introducing a correction factor, m_{c_j} into the constant, A_0 . According to Stotler and Benedict⁴⁾, the constant, A_0 , for a multicomponent system is formulated as follows^{2,3)}

$$A_0 = \sum_i^N x_i^2 A_{0i} + 2 \sum_i^N \sum_{\substack{j \neq i \\ j > i}}^N x_i x_j m_{ij} \sqrt{A_{0i} A_{0j}} \quad (1)$$

where m_{ij} is the correction factor and has been shown to be less than unity in general^{2,3)}. The usefulness of m_{ij} is recognized for several binary systems containing carbon dioxide^{2,3,5)} and hydrogen sulfide³⁾. However, application of m_{ij} to ternary systems seems to have been slight.

The purpose of the present work is to check the usefulness of m_{ij} for the nitrogen-methane-carbon dioxide system, whose vapor-liquid equilibrium data have been determined by static method. The equilibrium cell used here was the same one described in a previous paper²⁾. Gas chromatography was adopted to analyse equilibrium composition. The experimental results at various pressures and temperatures are listed in **Table 1** and are compared with predicted K -values by the BWR equation in **Table 2**. The correction factors used in this calculation were determined based on the vapor-liquid equilibrium data of each binary system^{2,4)} and are presented in **Table 3**. As shown in Table 2, the original BWR equation predicts erroneous K -values for this ternary system. However, the modified BWR equation containing m_{ij} is shown to be successful.

Table 1 Vapor-liquid equilibrium data for the $\text{N}_2\text{-CH}_4\text{-CO}_2$ system

| y_{N_2} | y_{CH_4} | x_{N_2} | x_{CH_4} |
|------------------|-------------------|------------------|-------------------|
| | 0°C | 60 atm | |
| 0.229 | 0.046 | 0.037 | 0.013 |
| 0.169 | 0.116 | 0.032 | 0.033 |
| 0.124 | 0.170 | 0.023 | 0.052 |
| 0.072 | 0.237 | 0.015 | 0.075 |
| | 0°C | 80 atm | |
| 0.306 | 0.064 | 0.079 | 0.026 |
| 0.253 | 0.120 | 0.071 | 0.050 |
| 0.205 | 0.169 | 0.060 | 0.077 |
| 0.182 | 0.196 | 0.057 | 0.091 |
| 0.149 | 0.237 | 0.049 | 0.112 |
| 0.100 | 0.290 | 0.038 | 0.146 |
| 0.075 | 0.315 | 0.030 | 0.165 |
| 0.061 | 0.334 | 0.024 | 0.179 |
| 0.047 | 0.344 | 0.020 | 0.190 |
| | 0°C | 100 atm | |
| 0.381 | 0.007 | 0.141 | 0.004 |
| 0.316 | 0.070 | 0.132 | 0.039 |
| 0.247 | 0.123 | 0.126 | 0.082 |
| 0.220 | 0.149 | 0.125 | 0.103 |
| 0.200 | 0.158 | 0.120 | 0.115 |
| | -20°C | 60 atm | |
| 0.342 | 0.195 | 0.052 | 0.038 |
| 0.174 | 0.374 | 0.032 | 0.110 |
| 0.113 | 0.439 | 0.024 | 0.131 |
| | -20°C | 80 atm | |
| 0.525 | 0.062 | 0.102 | 0.022 |
| 0.439 | 0.144 | 0.094 | 0.046 |
| 0.372 | 0.210 | 0.086 | 0.072 |
| 0.289 | 0.297 | 0.075 | 0.117 |
| 0.259 | 0.324 | 0.071 | 0.135 |
| 0.230 | 0.348 | 0.065 | 0.153 |
| 0.169 | 0.409 | 0.054 | 0.206 |
| 0.127 | 0.456 | 0.047 | 0.240 |
| 0.092 | 0.494 | 0.035 | 0.282 |
| 0.066 | 0.510 | 0.028 | 0.312 |
| | -20°C | 100 atm | |
| 0.393 | 0.182 | 0.136 | 0.097 |
| 0.331 | 0.239 | 0.131 | 0.143 |
| 0.301 | 0.259 | 0.127 | 0.163 |
| 0.277 | 0.280 | 0.123 | 0.178 |

(continued)

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| -40°C | | 60 atm | |
|-------|-------|---------|-------|
| 0.561 | 0.168 | 0.063 | 0.044 |
| 0.444 | 0.279 | 0.059 | 0.080 |
| 0.286 | 0.439 | 0.046 | 0.126 |
| 0.205 | 0.521 | 0.034 | 0.174 |
| 0.124 | 0.610 | 0.024 | 0.223 |
| -40°C | | 80 atm | |
| 0.682 | 0.060 | 0.104 | 0.023 |
| 0.574 | 0.176 | 0.100 | 0.064 |
| 0.464 | 0.279 | 0.086 | 0.108 |
| 0.332 | 0.406 | 0.086 | 0.197 |
| 0.285 | 0.449 | 0.083 | 0.228 |
| 0.247 | 0.486 | 0.066 | 0.236 |
| 0.185 | 0.541 | 0.064 | 0.318 |
| 0.121 | 0.589 | 0.059 | 0.398 |
| -40°C | | 100 atm | |
| 0.486 | 0.244 | 0.144 | 0.127 |
| 0.399 | 0.316 | 0.139 | 0.174 |
| 0.368 | 0.339 | 0.140 | 0.206 |
| 0.361 | 0.349 | 0.148 | 0.224 |
| 0.345 | 0.357 | 0.156 | 0.246 |

| System | 0°C and 80 atm | -40°C and 60 atm |
|----------------------------------|---------------------|---------------------|
| N ₂ -CH ₄ | 0.966 ⁴⁾ | 0.966 ⁴⁾ |
| CH ₄ -CO ₂ | 0.945 | 0.910 |
| N ₂ -CO ₂ | 1 | 1 |

Table 2 Comparison of predicted and experimental K -values for the N₂-CH₄-CO₂ system

| K_{N_2} | | | K_{CH_4} | | | K_{CO_2} | | |
|------------------|----------|-----------|------------|---------|---------|------------|---------|---------|
| Exp. | Calc. 1* | Calc. 2** | Exp. | Calc. 1 | Calc. 2 | Exp. | Calc. 1 | Calc. 2 |
| 0°C and 80 atm | | | | | | | | |
| 3.873 | 3.127 | 3.266 | 2.462 | 1.757 | 2.029 | 0.704 | 0.734 | 0.727 |
| 3.563 | 3.010 | 3.172 | 2.400 | 1.724 | 1.992 | 0.713 | 0.742 | 0.733 |
| 3.417 | 2.844 | 3.034 | 2.195 | 1.678 | 1.940 | 0.725 | 0.756 | 0.744 |
| 3.193 | 2.787 | 2.986 | 2.154 | 1.662 | 1.921 | 0.730 | 0.760 | 0.748 |
| 3.041 | 2.647 | 2.875 | 2.116 | 1.621 | 1.876 | 0.732 | 0.771 | 0.755 |
| 2.632 | 2.469 | 2.706 | 1.986 | 1.567 | 1.809 | 0.748 | 0.785 | 0.769 |
| 2.500 | 2.342 | 2.591 | 1.909 | 1.526 | 1.761 | 0.758 | 0.796 | 0.778 |
| 2.542 | 2.253 | 2.506 | 1.866 | 1.497 | 1.726 | 0.759 | 0.805 | 0.785 |
| 2.350 | 2.185 | 2.442 | 1.810 | 1.475 | 1.700 | 0.771 | 0.812 | 0.790 |
| -40°C and 60 atm | | | | | | | | |
| 8.905 | 6.302 | 7.546 | 3.818 | 2.048 | 3.189 | 0.303 | 0.341 | 0.322 |
| 7.525 | 5.949 | 7.278 | 3.488 | 2.005 | 3.112 | 0.322 | 0.348 | 0.326 |
| 6.217 | 5.065 | 6.416 | 3.484 | 1.869 | 2.858 | 0.332 | 0.373 | 0.342 |
| 6.029 | 4.500 | 5.711 | 2.994 | 1.780 | 2.642 | 0.346 | 0.393 | 0.358 |
| 5.167 | 4.083 | 5.219 | 2.735 | 1.714 | 2.486 | 0.353 | 0.410 | 0.372 |

* Calculated by the original BWR equation
 ** Calculated by the modified BWR equation

Nomenclature

A_o = constant of the BWR equation
 i, j = component i and j
 K = K -value (y/x)
 m_{ij} = correction factor for $i-j$ pair interaction
 N = number of component
 x = mole fraction of liquid phase
 y = mole fraction of vapor phase

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