

ERRATA

1. In the paper: S. G. Mikhlin, "Variation-difference approximation," J. Sov. Math. 10, No. 5, 661-787 (1978), in Sec. 6 of Chap. 5, one estimate was made in not the best way and, as a result, the proof of fundamental inequality (3) for the case of degeneracy index $d = 1$ turned out to be incorrect. Here we present an improved estimate and by the same token eliminate the incorrectness mentioned. The paper's text on p. 721 line 5 to line 17 needs to be replaced by the following.

From the inequalities presented above it follows that

$$\int_{x_k}^{x_{k+1}} [u'(t)]^2 dt \leq Ch^{1-\frac{2}{v}-2d} [k^{-\frac{2}{v}-2d} \|f\|_v^2 + k^{-2d} \left\{ \int_{x_k}^{x_{k+1}} |g_1(t)|^v dt \right\}^{\frac{2}{v}}].$$

We take the polygonal line the same as in Sec. 4. Now

$$J_k = \int_{x_k}^{x_{k+1}} x^d \rho(x) (u'(x) - h^d u''(x))^2 dx \leq (k+1)^d h^{2d} \rho_1 \int_{x_k}^{x_{k+1}} (u'(x) - h^d u''(x))^2 dx \leq 2^d k^{2d} h^{2d} \rho_1 \int_{x_k}^{x_{k+1}} [u'(t)]^2 dt \leq Ch^{3-\frac{2}{v}-d} [k^{-\frac{2}{v}-d} \|f\|_v^2 + k^{-2d} \left\{ \int_{x_k}^{x_{k+1}} |g_1(t)|^v dt \right\}^{\frac{2}{v}}].$$

Summing and bearing in mind that the series $\sum_{k=1}^{\infty} k^{-\frac{2}{v}-d}$ converges, we obtain

$$J - J_0 = \sum_{k=1}^{2n-1} J_k \leq Ch^{3-\frac{2}{v}-d} [\|f\|_v^2 + \sum_{k=1}^{2n-1} k^{-2d} \left\{ \int_{x_k}^{x_{k+1}} |g_1(t)|^v dt \right\}^{\frac{2}{v}}].$$

We estimate the last sum by Hölder's inequality with indices $\frac{v}{v-2}$ and $\frac{v}{2}$:

$$\sum_{k=1}^{2n-1} k^{-2d} \left\{ \int_{x_k}^{x_{k+1}} |g_1(t)|^v dt \right\}^{\frac{2}{v}} \leq \left\{ \sum_{k=1}^{2n-1} k^{-\frac{dv}{v-2}} \right\}^{\frac{v-2}{v}} \left\{ \int_h^1 |g_1(t)|^v dt \right\}^{\frac{2}{v}}.$$

Since $v > 2$ and $d \geq 1$, the series $\sum_{k=1}^{\infty} k^{-\frac{dv}{v-2}}$ converges and the quantity on the right has the estimate $C \|g_1\|_v^2 \leq C \|f\|_v$. Finally,

$$J - J_0 \leq Ch^{3-\frac{2}{v}-d} \|f\|_v^2.$$

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2. In the paper: T. Ya. Kon'kova, "ALGOL procedure for solving certain problems of algebra, based on the application of a normalized process," J. Sov. Math., 7, No. 1, 24-28 (1977), the procedure iseigy (pp. 26-27) contains errors. We present a corrected text.