

# Visual Models of Morphogenesis

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# Outline

- ◆ Introduction
- ◆ Features of Models of Morphogenesis
- ◆ Space-Oriented Models
- ◆ Structure-Oriented Models
- ◆ Conclusion

# Introduction

- ◆ From 1952 to 1994 over 40 decades, scientists have developed several visual models of morphogenesis using database amplification and emergence.
- ◆ Database Amplification:  
is a process of creating complex images using small data sets
- ◆ Emergence:  
is a process in which a collection of interacting units acquires qualitatively new properties that can't be reduced to a simple superposition of individual contribution.
- ◆ Morphogenesis:  
The development of patterns and forms in the domain of living organisms.

# Features of Models of Morphogenesis

- ◆ The studying of morphogenesis has emphasized on two directions:
  - Substances chemically reacting.
    - ◆ (Alan Turing, 1952)  
Space-oriented
  - Rate of growth in various direction.
    - ◆ ( d'Arcy Thompson, 1952)  
Structure-oriented.

# Features of Models of Morphogenesis ( Cont. )

- ◆ Comparison between these two models:
  - ◆ The space-oriented models capture the flow of information in the medium but usually limited the capacity of describing expansion of the medium and of the structure embedded on it: Growth is limited to the boundary.
  - ◆ The structure-oriented models can simulate the expansion of whole structure but they do not inherently capture the information flow through the medium.

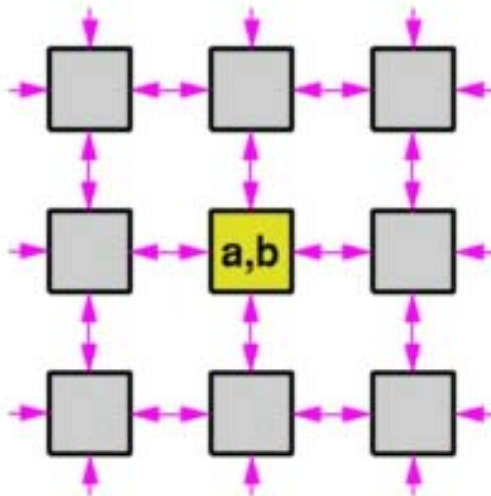
# Space-oriented models

## Reaction-Diffusion

- ◆ The first model was proposed by Alan Turing in 1952, known as reaction-diffusion model.
- ◆ Concepts of the reaction-diffusion model:  
Interaction between two or more morphogens that diffuser in a medium and enter into chemical reactions with each other.
- ◆ It can be represented by a system of partial differential equation.

# Reaction-Diffusion (Cont.)

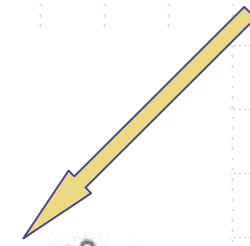
Each point can be characterized by two numbers  $a$  and  $b$ , which represents the concentrations of substances (morphogens)



$$\frac{\delta a}{\delta t} = f(a,b) + D_a \left( \frac{\delta^2 a}{\delta x^2} + \frac{\delta^2 a}{\delta y^2} \right)$$

$$\frac{\delta b}{\delta t} = g(a,b) + D_b \left( \frac{\delta^2 b}{\delta x^2} + \frac{\delta^2 b}{\delta y^2} \right)$$

Laplacian  
of  $a$  ( $\Delta a$ )



Reaction-diffusion model (Turing)

# Reaction-Diffusion(Cont. )

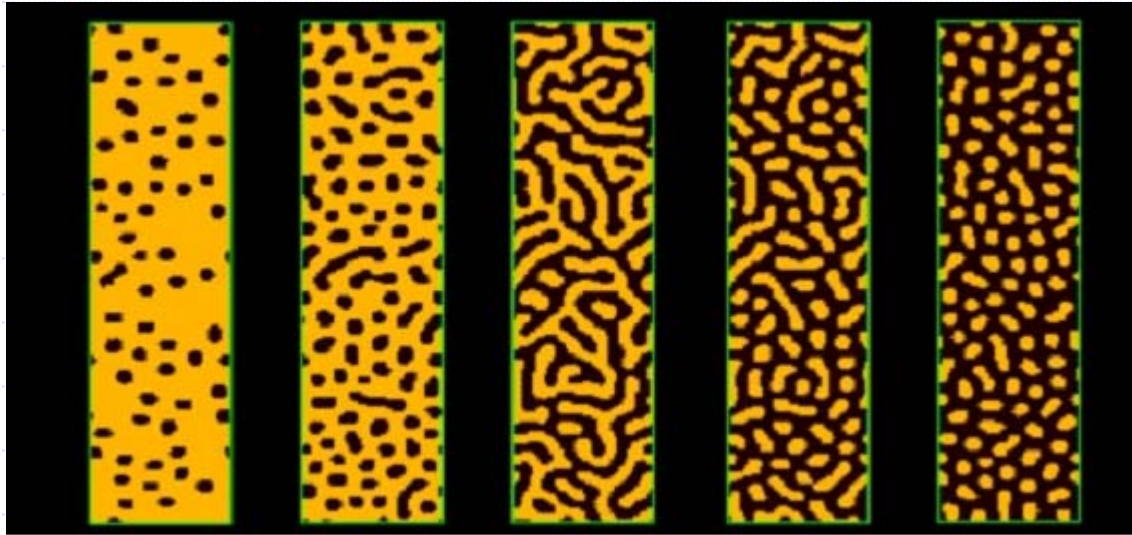
In the equations,  $f$  and  $g$  are functions,  $D_a$  and  $D_b$  are coefficients.

the reaction components are capture by function  $f$  and  $g$ . The diffusion components are represented by the remaining terms.

These substances diffuser and reaction with each other over the time according to the partial differential equations.



# Examples:



Reaction-diffusion pattern

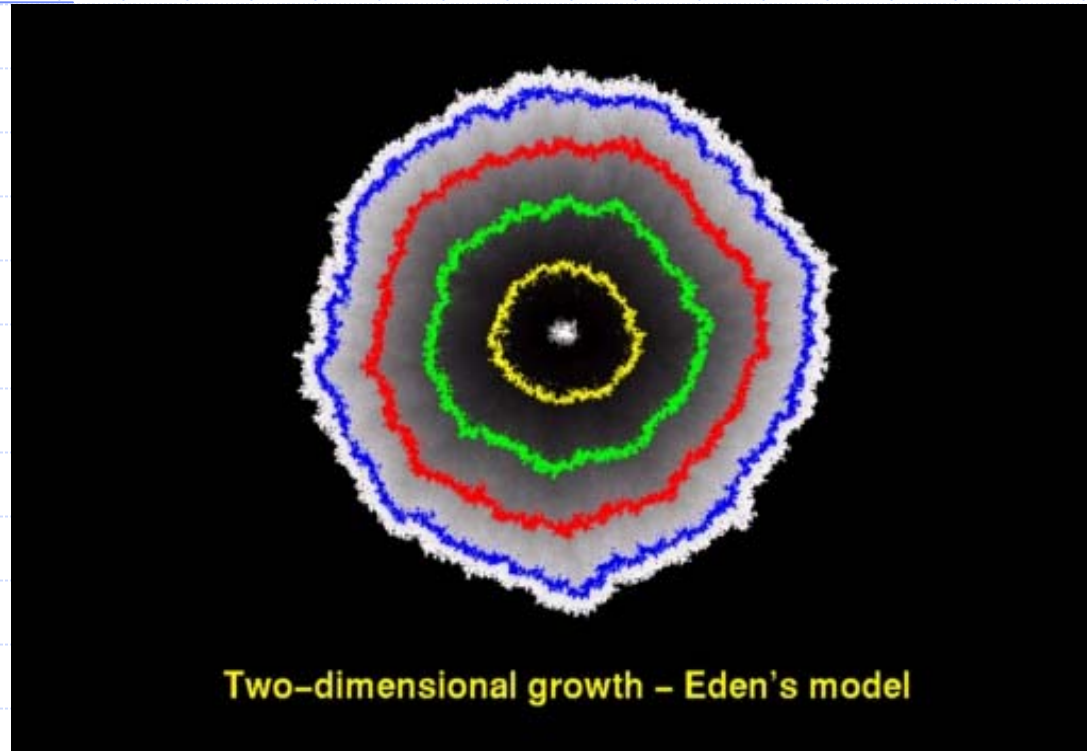
[reaction-diffusion2.mpeg](#)

# Space-Oriented Models

## Diffusion-Limited Accretive Growth

- ◆ It focus on the structure and its gradual expansion along the border.
- ◆ Eden's model:
  - proposed by Eden in 1960.
  - Reaction-diffusion takes places in a square grid.
  - A single initial particle is placed in the center of the grid.
  - The subsequent particles are attached one by one to randomly chosen points on the border of the structure formed in the previous steps.

# Eden's model:



The colors indicate the state of the structure at different points in time.  
The structure developing according to Eden's model is roughly circular.

# Diffusion-Limited Accretive Growth ( Cont. )

## ◆ Improvements:

- The growth rate depends on the local concentration of nutrients that diffuse from a surrounding exterior source and are consumed by the growing structure.
- Expanding to three dimensions.

## ◆ Example of growth of marine sessile organisms (proposed by Kaandorp) in three dimensions.

## ◆ [sponge.avi](#)

# Space-oriented Models

## Diffusion-Limited Aggregation

- ◆ It was introduced by Witten and Sander in 1983
- ◆ It captures diffusion of nutrients by simulating random movement of particles in a grid.
- ◆ The growing structure originates in a single fixed cell.
- ◆ Free particles move in the grid with the displacement direction chosen at random on each simulation step.
- ◆ Once a moving particle touches the structure, it sticks to it rigidly.
- ◆ Example: [dla.avi](#)

# Space-Oriented Models

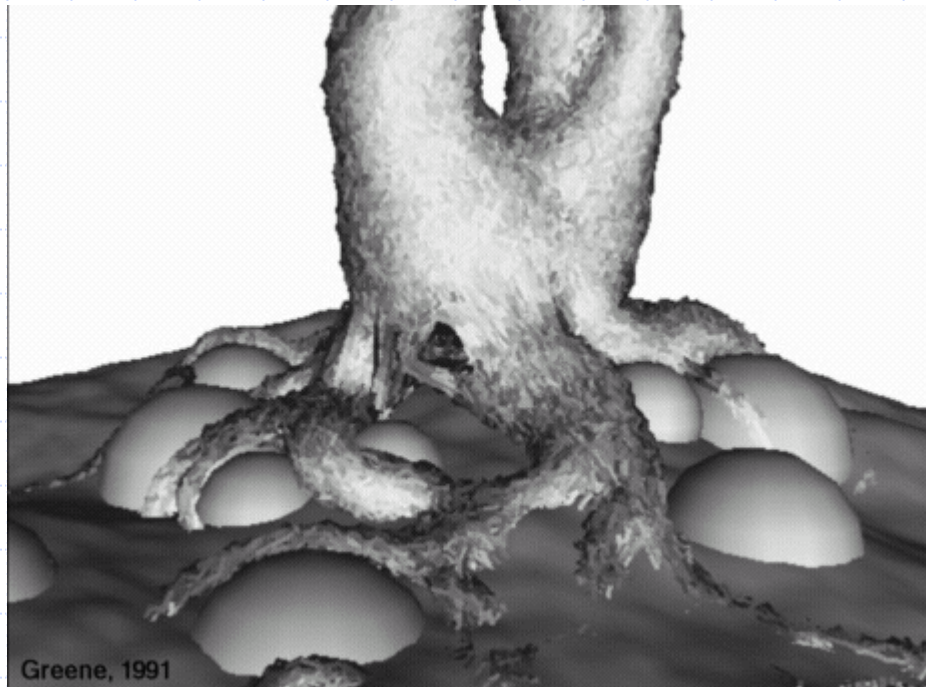
## Cellular Automata

- ◆ It was first introduced by Toffoli and Margolus in 1987.
- ◆ It can be considered a discrete-space counterpart of reaction-diffusion models.
- ◆ The space is presented by a uniform grid with each site or cell characterized by a state chosen from a finite set.
- ◆ Time advances in discrete steps.
- ◆ All cells change their states according to the same rule.
- ◆ The next state is a function of the previous state of a cell and its closed neighbors.
- ◆ Example: [maltese.avi](#)

# Space-Oriented Models

## Voxel Automata

- ◆ Three-dimensional extensions of cellular automata.
- ◆ By Greene 1991
- ◆ Example:



# Structure-Oriented Models

## L-Systems

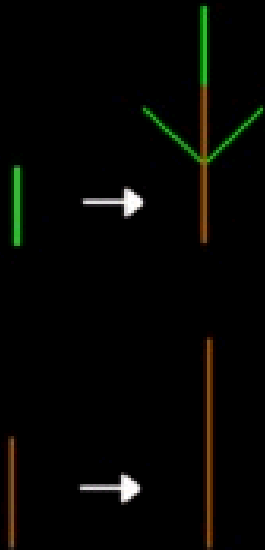
- ◆ previous models have two limitations:
  - The growth of a structure is controlled by environment. In contrast, it is determined largely by genetic factors
  - All models represent accretive growth. In contrast, the development patterns of higher organisms are often much more complicated.
  - Example:
    - [cpoundlf.avi](#)



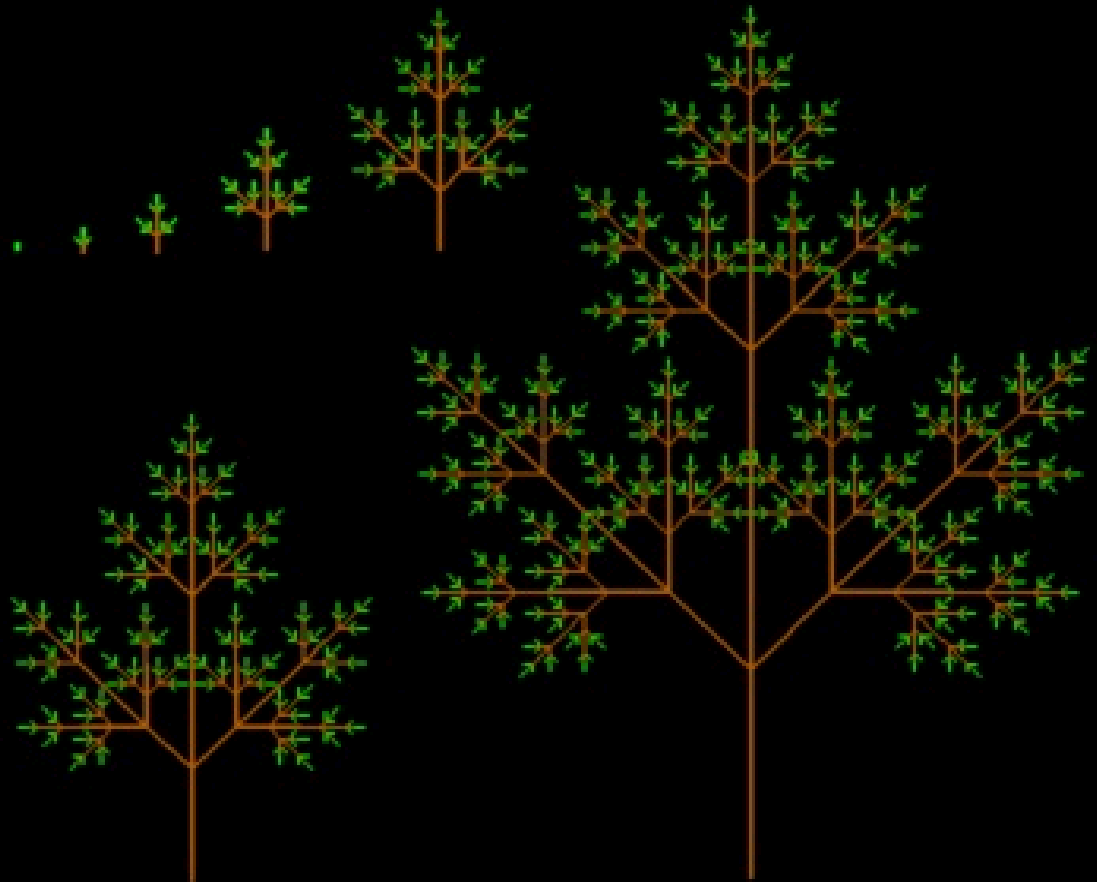
# L-Systems (Cont.)

- ◆ L-system was proposed by Lindenmayer in 1968.
- ◆ In biological terms, an L-System uses a small set of rules to locally add details to a structure
- ◆ In computer science terms, an L-System is a context-free, recursive, text substitution scheme, followed by geometric interpretation.
- ◆ A simple L-System starts with a seed, for example, the letter F, and has one rule to replace the existing seed. A simple replacement rule might be:  
F-F-FF+F-F-F.

# Plant development



productions

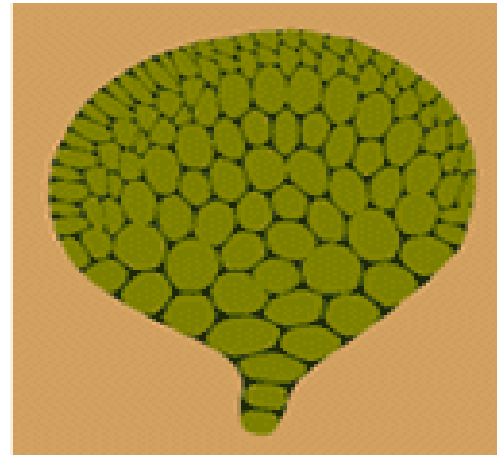


# Structure-Oriented Models

## Map L-Systems

- ◆ It is an advanced L-System
- ◆ Graphs with cycles.
- ◆ Was proposed by Fracchia, Prusinkiewicz, and de Boer in 1990
- ◆ Example:

Thalli of  
microsorium  
linguaeforme



# Structure-Oriented Models

## Mobile Cells in a Continuous Medium

- ◆ It was proposed by Fleischer and Barr in 1993.
- ◆ Focus on the generation of connectivity patterns during neural development.
- ◆ Discrete cells embedded in a continuous substrate.
- ◆ The action of cells are divided into continuous processes and discrete events.

# Conclusion

This paper presented a survey of selected models of morphogenesis that use computer graphics techniques to visualize the results of simulations.

These models can be used for image synthesis purposes and provide a research tool for studying morphogenesis in nature.

In the absence of formal measures of what makes two patterns look alike, visual inspection is a valuable method for comparing the models with reality.



***Thanks !***