

# Vitrification and levitation of a liquid droplet on liquid nitrogen

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The vitrification of a liquid occurs when ice crystal formation is prevented in the cryogenic environment through ultrarapid cooling. In general, vitrification entails a large temperature difference between the liquid and its surrounding medium. In our droplet vitrification experiments, we observed that such vitrification events are accompanied by a Leidenfrost phenomenon, which impedes the heat transfer to cool the liquid, when the liquid droplet comes into direct contact with liquid nitrogen. This is distinct from the more generally observed Leidenfrost phenomenon that occurs when a liquid droplet is self-vaporized on a hot plate. In the case of rapid cooling, the phase transition from liquid to vitrified solid (i.e., vitrification) and the levitation of droplets on liquid nitrogen (i.e., Leidenfrost phenomenon) take place simultaneously. Here, we investigate these two simultaneous physical events by using a theoretical model containing three dimensionless parameters (i.e., Stefan, Biot, and Fourier numbers). We explain theoretically and observe experimentally a threshold droplet radius during the vitrification of a cryoprotectant droplet in the presence of the Leidenfrost effect.

cryopreservation | leidenfrost | film boiling | phase change | crystallization

Film boiling is a phenomenon of great interest that has applications in a variety of fields such as aerospace, cryogenics, and electronics. In addition, a similar phenomenon can be easily observed in daily life, e.g., the “dancing droplets” on a frying pan when the droplets come into contact with the pan that is much hotter than the boiling temperature of the droplets (1, 2). The droplets are heated and evaporate on the pan. As a result, they are provided with a levitation force by the generated vapor layer. This solid–liquid film boiling (or liquid–liquid film boiling) is usually caused by a huge temperature distinction between adjacent substances (3–7). Film boiling, also referred to as the Leidenfrost effect, generally impedes the heat transfer between neighboring materials due to the big thermal resistance induced by evaporated vapor layer (8, 9). A great amount of effort has been spent to understand the film boiling behavior of plates or spheres occurring at extremely high temperatures with strong evaporation of a liquid (10–12). On the other hand, when a liquid droplet falls into an extremely cold medium such as a cryogenic fluid (e.g., liquid nitrogen), the relatively hot droplet boils the surrounding medium. Unlike a droplet on the pan, the vapor from the medium, not from the droplet itself, levitates the droplet. Furthermore, abrupt phase change from liquid to solid occurs along with film boiling during cooling down of the droplets.

Here, we investigate the vitrification of a droplet via rapid freezing and its levitation by the Leidenfrost effect. In principle, vitrification implies the phase transition of a liquid to a glass (amorphous ice) with a very low degree of crystallization. To the best of our knowledge, there have been no prior attempts to examine the vitrification behavior of droplets that are ejected directly into liquid nitrogen and the accompanying Leidenfrost phenomenon on the surface of liquid nitrogen. In the current

study, we investigate the heat transfer and simultaneous phase change of a nanoliter volume droplet levitating on liquid nitrogen. Understanding the vitrification and film boiling phenomena is also of great importance to other broad applications, such as metallurgy, nuclear reactors, turbine machineries, and biopreservation (13–16). In particular, vitrification is regarded as the only feasible way to successfully cryopreserve human cells and tissues such as oocytes and brain tissue (17, 18).

Upon ejecting a droplet into liquid nitrogen, as demonstrated in Fig. 1A, the liquid nitrogen surrounding the droplet absorbs the heat from the liquid of relatively higher temperature and evaporates (14, 15, 19, 20). As soon as droplets are immersed in liquid nitrogen, the evaporated nitrogen results in a buoyant force and a pressure differential pushing droplets to the liquid nitrogen surface (i.e., levitation phenomenon; Fig. S1 and Video S1). This levitation continues until the droplet temperature reaches the Leidenfrost temperature (Fig. 1D; Video S1). Assuming that the static feature of the droplet primarily governs the entire system [as first reported by Frederking and Clark (21)], the flow behavior of nitrogen gas environing a droplet and following pressure development can be analytically modeled as an incompressible flow in cavities, Fig. 1B and C (also see SI Text). The vapor blanket acts as a heat-insulating layer, thereby hindering heat transfer for cooling.

## Results and Discussion

Once the temperature of a liquid approaches its freezing point, solidification of the liquid (crystallization or vitrification) starts depending on cooling conditions such as cooling rate, nucleation sites, and pressure (22–24). To describe such a solidification process, two models, i.e., the Stefan and zone models, have been employed (25). Unlike the Stefan model, where the entire domain is sharply divided into solid and liquid subdomains by a moving phase interface, the zone model benefits from more efficiency in characterizing the crystallization process using a propagating zone. In the current study, the zone model is adopted by using the following nonisothermal kinetic equation proposed by Boutron and Mehl (13):

$$\frac{d\chi}{dt} = k_a \chi^{\frac{2}{3}} (1 - \chi) (T_f - T) e^{-Q/RT} \quad [1]$$

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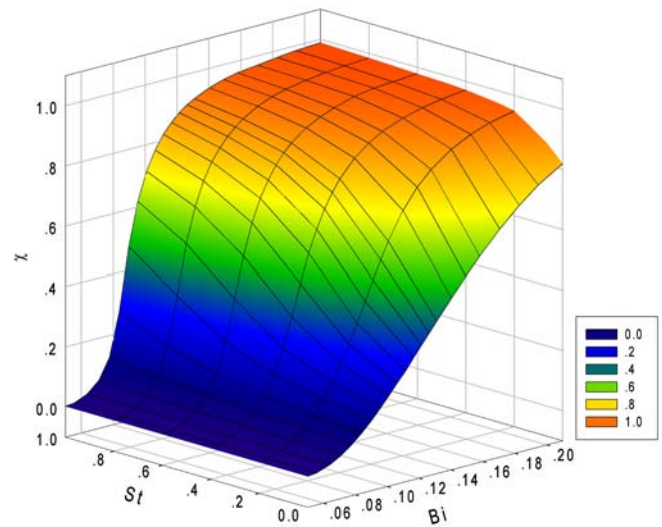




nitrogen ( $Bi < 1$ , i.e., heat transfer occurs faster inside the droplet), the range of the temperature variation across the droplet is narrow (Fig. 2C).

After calculating the final degree of crystallization of a droplet, we averaged the value using the relevant volume. The calculated degree of crystallization of droplets is found to be a strong function of the droplet size (Fig. 3A). As the droplet radius increases, the degree of crystallization also increases, especially between 0 and 0.2 dimensionless radii. The droplets with a low degree of crystallization after cooling can be regarded as vitrified droplets. During cooling, homogeneous ice nucleation first happens between homogeneous nucleation temperature  $T_h$  and the melting temperature  $T_m$  (e.g.,  $-42 \sim 0^\circ\text{C}$  for water), followed by heterogeneous ice nucleation in the range of the glass transition temperature ( $T_g$ ) to  $T_h$  (28). In the nucleation regimes, including the DTR as shown in Fig. 2A and B, the probability for a volume of ice crystal ( $V$ ) can be given by  $J(T, P) \times V \times \Delta t$ , where  $J(T, P)$  is the nucleation rate as a function of temperature  $T$  and pressure  $P$  (29). Rapid cooling can shorten the time duration in the nucleation regime ( $\Delta t$ ), thus decrease the probability of ice crystal nucleation. For instance, a cooling rate of  $\sim 10^8^\circ\text{C}/\text{min}$  allows the vitrification of pure water (30). It is noted that there exists a critical droplet size beyond which incipient nuclei grow leading to the formation of ice crystals. Otherwise, incipient nuclei collapse and an ice crystal is not created. The thermodynamic characteristic temperatures ( $T_g$ ,  $T_h$ , and  $T_m$ ) change along with the composition and concentration of solutes. In the current study, we took into account of cryoprotective agents (CPAs), which are chemicals used to minimize damage of cells or tissues during freezing.  $T_h$  and  $T_m$  decrease, while  $T_g$  increases, with increasing CPA concentration. By increasing CPA concentration,  $T_g$  and  $T_m$  become closer and eventually meet. As a result, a vitrified solid can be generated even at a slow cooling rate in the case of  $\sim 60\%$  wt/wt of CPAs (31). Fig. 3B–D shows the frozen droplets in the liquid nitrogen. As the droplet size increases, morphological changes are observed: Vitrified droplets are translucent with bright cores (Fig. 3B), but crystallized droplets contain granular particles inside (ice crystals) (Fig. 3C and D). In addition, it is shown that the large droplets have grain-like crystal particles due to the longer cooling time. The experimental results shown in Fig. 3B–D are found to be consistent with the numerical findings.

Fig. 3E demonstrates the hovering time of droplets on liquid nitrogen. When droplets plummet into liquid nitrogen, three regimes are defined: a film boiling regime, a transition boiling regime, and a nucleate boiling regime. The evaporation rate of film boiling is known to be lower than that of peak nucleate boiling by more than one order of magnitude (14). During the transition from film boiling to nucleate boiling, the vapor blanket surrounding the droplet disappears. Subsequently, the droplet sinks beneath the liquid nitrogen. The temperature at the moment that film boiling changes into nucleate boiling corresponds to the Leidenfrost temperature. The hovering time is the elapsed time when the calculated temperature of droplets reaches the Leidenfrost temperature. The Leidenfrost time normalized by the diffusive characteristic time ( $t_c$ ) declines dramatically and approaches an asymptotic value ( $\sim 1.5$ ). As the size of the droplet increases, the influence of heat diffusion in the droplet strengthens. It is interpreted that the smaller droplets are more easily affected by external heat transfer than by internal heat diffusion because the Biot number ( $Bi$ ) gets smaller ( $\ll 1$ ). Similar to the change in crystallinity (Fig. 3A), the dimensionless Leidenfrost time drastically alters between 0 and  $\sim 0.2$  (Fig. 3E). Please note that thermodynamics and heat transfer between the droplet and liquid nitrogen modeled in this study play a more important role in determining the vitrification behavior and hovering time of the droplet than relevant hydrodynamics. The hydrodynamics of the convection film boiling is explained in *SI Text*. In addition,



**Fig. 4.** Plot of the degree of crystallization in the domain of the  $St$  and  $Bi$  numbers. The degree of crystallization increases with an increase in the  $St$  and  $Bi$  numbers. In particular, the degree of crystallization drastically rises with respect to the  $Bi$  number.

tion, the experimental and numerical results show the same trends (Fig. 3E).

By using two governing dimensionless parameters (i.e.,  $Bi$  and  $St$ ) in our system, we analyzed the characteristics of crystallization of droplets (i.e.,  $\chi$ ). That is, the degree of crystallization increases with an increase in either  $St$  or  $Bi$  (Fig. 4). In particular, we find that the crystallinity is a stronger function of  $Bi$  than  $St$ . This is attributed to the fact that the heat transfer at the interface between the droplets and the liquid nitrogen is more critical in determining the crystallization of droplets than the internal heat capacity of the droplets. Here, it is noted that, in the case of  $St = 0$ , it is identical to the uncoupled approach, where the energy equation [2] is decoupled from the kinetics of ice crystal formation (Eq. 1) (27).

In summary, we have theoretically analyzed the vitrification and Leidenfrost phenomena of droplets in liquid nitrogen using dimensionless physical parameters and compared the theoretical results with experimental data. This dimensionless analysis explains the simultaneous levitation and phase change of droplets.

## Methods

**Experimental Methods.** A valve-based droplet ejector with nozzle diameter  $150 \mu\text{m}$  (SMLD-5b, TechElan) was connected to a syringe through a needle and tubing, and the liquid was then loaded into the syringe. The air line was connected to the syringe to provide a pressure of  $34 \text{ kPa}$  to overcome the surface tension of a droplet at the orifice of the ejector (Fig. 1A). The ejector was controlled by a pulse generator (8112A 50 MHz, Hewlett-Packard). Droplets are generated to implement rapid cooling by using an air-pressure, pulse-controlled solenoid valve. Larger droplets were generated using a micropipette. Cryoprotectant,  $3 \text{ M } 1,2\text{-propanediol}$  (PrOH, EMD Chemicals), was employed to vitrify droplets. Blue food dye was used to stain the droplets. The generated droplets were plunged into a liquid nitrogen bath (glass Petri dishes, Pyrex). The liquid nitrogen container was covered with aluminum foil in a bid to prevent possible electrostatic interactions between the container and droplets. Right after the immersion of droplets, the levitation time of the droplets was measured until they sank into the liquid nitrogen bath. The frozen droplets were taken for imaging (Spot Advanced, Diagnostic Instruments, Inc.) under a microscope (Eclipse Ti-S, Nikon) using a polarized filter. Droplet sizes were measured based on recorded images.

**Numerical Simulations.** Finite element simulation was carried out to model the heat transfer, phase change, and Leidenfrost phenomena of droplets. To predict the temperature and degree of crystallization of droplets during cooling, we simultaneously calculated Eqs. 1 and 2 because they are coupled to each other. For the calculation, we assumed a spherical symmetry based on

the analytical solutions of fluid dynamics of the nitrogen vapor (*SI Text*). The fourth-order Runge–Kutta algorithm and the backward Euler method, which is an implicit method solving an equation set to move forward to a next time step during calculation, were employed for the numerical simulations.

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