

VLSI Physical Design: From Graph Partitioning to Timing Closure

Andrew B. Kahng • Jens Lienig
Igor L. Markov • Jin Hu

VLSI Physical Design: From Graph Partitioning to Timing Closure

 Springer

Andrew B. Kahng
University of California at San Diego
Departments of CSE and ECE
Mailcode #0404
La Jolla, California 92093
USA
abk@ucsd.edu

Jens Lienig
Dresden University of Technology
Electrical Engineering and
Information Technology
Helmholtzstr. 10
01069 Dresden
Germany
jens@ieee.org

Igor L. Markov
University of Michigan
Electrical Engineering and
Computer Science
2260 Hayward St.
Ann Arbor, Michigan 48109
USA
imarkov@eecs.umich.edu

Jin Hu
University of Michigan
Electrical Engineering and
Computer Science
2260 Hayward St.
Ann Arbor, Michigan 48109
USA
jinhu@eecs.umich.edu

ISBN 978-90-481-9590-9 e-ISBN 978-90-481-9591-6
DOI 10.1007/978-90-481-9591-6
Springer Dordrecht Heidelberg London New York

© Springer Science+Business Media B.V. 2011

No part of this work may be reproduced, stored in a retrieval system, or transmitted in any form or by any means, electronic, mechanical, photocopying, microfilming, recording or otherwise, without written permission from the Publisher, with the exception of any material supplied specifically for the purpose of being entered and executed on a computer system, for exclusive use by the purchaser of the work.

Cover design: eStudio Calamar S.L.

Printed on acid-free paper

Springer is part of Springer Science+Business Media (www.springer.com)

Foreword

Physical design of integrated circuits remains one of the most interesting and challenging arenas in the field of Electronic Design Automation. The ability to integrate more and more devices on our silicon chips requires the algorithms to continuously scale up. Nowadays we can integrate $2e9$ transistors on a single 45nm-technology chip. This number will continue to scale for the next couple of technology generations, requiring more transistors to be automatically placed on a chip and connected together. In addition, more and more of the delay is contributed by the wires that interconnect the devices on the chip. This has a profound effect on how physical design flows need to be put together. In the 1990s, it was safe to assume that timing goals of the design could be reached once the devices were placed well on the chip. Today, one does not know whether the timing constraints can be satisfied until the final routing has completed.

As far back as 10 or 15 years ago, people believed that most physical design problems had been solved. But, the continued increase in the number of transistors on the chip, as well as the increased coupling between the physical, timing and logic domains warrant a fresh look at the basic algorithmic foundations of chip implementation. That is exactly what this book provides. It covers the basic algorithms underlying all physical design steps and also shows how they are applied to current instances of the design problems. For example, Chapter 7 provides a great deal of information on special types of routing for specific design situations.

Several other books provide in-depth descriptions of core physical design algorithms and the underlying mathematics, but this book goes a step further. The authors very much realize that the era of individual point algorithms with single objectives is over. Throughout the book they emphasize the multi-objective nature of modern design problems and they bring all the pieces of a physical design flow together in Chapter 8. A complete flow chart, from design partitioning and floorplanning all the way to electrical rule checking, describes all phases of the modern chip implementation flow. Each step is described in the context of the overall flow with references to the preceding chapters for the details.

This book will be appreciated by students and professionals alike. It starts from the basics and provides sufficient background material to get the reader up to speed on the real issues. Each of the chapters by itself provides sufficient introduction and depth to be very valuable. This is especially important in the present era, where experts in one area must understand the effects of their algorithms on the remainder of the design flow. An expert in routing will derive great benefit from reading the chapters on planning and placement. An expert in Design For Manufacturability (DFM) who seeks a better understanding of routing algorithms, and of how these algorithms can be affected by choices made in setting DFM requirements, will benefit tremendously from the chapters on global and detailed routing.

The book is completed by a detailed set of solutions to the exercises that accompany each chapter. The exercises force the student to truly understand the basic physical design algorithms and apply them to small but insightful problem instances.

This book will serve the EDA and design community well. It will be a foundational text and reference for the next generation of professionals who will be called on to continue the advancement of our chip design tools.

Dr. Leon Stok
Vice President, Electronic Design Automation
IBM Systems and Technology Group
Hopewell Junction, NY

Preface

VLSI physical design of integrated circuits underwent explosive development in the 1980s and 1990s. Many basic techniques were suggested by researchers and implemented in commercial tools, but only described in brief conference publications geared for experts in the field. In the 2000s, academic and industry researchers focused on comparative evaluation of basic techniques, their extension to large-scale optimization, and the assembly of point optimizations into multi-objective design flows. Our book covers these aspects of physical design in a consistent way, starting with basic concepts in Chapter 1 and gradually increasing the depth to reach advanced concepts, such as physical synthesis. Readers seeking additional details, will find a number of references discussed in each chapter, including specialized monographs and recent conference publications.

Chapter 2 covers netlist partitioning. It first discusses typical problem formulations and proceeds to classic algorithms for balanced graph and hypergraph partitioning. The last section covers an important application – system partitioning among multiple FPGAs, used in the context of high-speed emulation in functional validation.

Chapter 3 is dedicated to chip planning, which includes floorplanning, power-ground planning and I/O assignment. A broad range of topics and techniques are covered, ranging from graph-theoretical aspects of block-packing to optimization by simulated annealing and package-aware I/O planning.

Chapter 4 addresses VLSI placement and covers a number of practical problem formulations. It distinguishes between global and detailed placement, and first covers several algorithmic frameworks traditionally used for global placement. Detailed placement algorithms are covered in a separate section. Current state of the art in placement is reviewed, with suggestions to readers who might want to implement their own software tools for large-scale placement.

Chapters 5 and 6 discuss global and detailed routing, which have received significant attention in research literature due to their interaction with manufacturability and chip-yield optimizations. Topics covered include representing layout with graph models and performing routing, for single and multiple nets, in these models. State-of-the-art global routers are discussed, as well as yield optimizations performed in detailed routing to address specific types of manufacturing faults.

Chapter 7 deals with several specialized types of routing which do not conform with the global-detailed paradigm followed by Chapters 5 and 6. These include non-Manhattan area routing, commonly used in PCBs, and clock-tree routing required for every synchronous digital circuit. In addition to algorithmic aspects, we explore the impact of process variability on clock-tree routing and means of decreasing this impact.

Chapter 8 focuses on timing closure, and its perspective is particularly unique. It offers a comprehensive coverage of timing analysis and relevant optimizations in placement, routing and netlist restructuring. Section 8.6 assembles all these techniques, along with those covered in earlier chapters, into an extensive design flow, illustrated in detail with a flow chart and discussed step-by-step with several figures and many references.

This book does not assume prior exposure to physical design or other areas of EDA. It introduces the reader to the EDA industry and basic EDA concepts, covers key graph concepts and algorithm analysis, carefully defines terms and specifies basic algorithms with pseudocode. Many illustrations are given throughout the book, and every chapter includes a set of exercises, solutions to which are given in one of the appendices. Unlike most other sources on physical design, we made an effort to avoid impractical and unnecessarily complicated algorithms. In many cases we offer comparisons between several leading algorithmic techniques and refer the reader to publications with additional empirical results.

Some chapters are based on material in the book *Layoutsynthese elektronischer Schaltungen – Grundlegende Algorithmen für die Entwurfsautomatisierung*, which was published by Springer in 2006.

We are grateful to our colleagues and students who proofread earlier versions of this book and suggested a number of improvements (in alphabetical order): Matthew Guthaus, Kwangok Jeong, Johann Knechtel, Andreas Krinke, Nancy MacDonald, Jarrod Roy, Yen-Kuan Wu and Hailong Yao.

Images for global placement and clock routing in Chapter 8 were provided by Myung-Chul Kim and Dong-Jin Lee. Cell libraries in Appendix B were provided by Bob Bullock, Dan Clein and Bill Lye from PMC Sierra; the layout and schematics in Appendix B were generated by Matthias Thiele. The work on this book was partially supported by the National Science Foundation (NSF) through the CAREER award 0448189 as well as by Texas Instruments and Sun Microsystems.

We hope that you will find the book interesting to read and useful in your professional endeavors.

Sincerely,

Andrew, Jens, Igor and Jin

Table of Contents

1	Introduction.....	3
1.1	Electronic Design Automation (EDA).....	4
1.2	VLSI Design Flow.....	7
1.3	VLSI Design Styles	11
1.4	Layout Layers and Design Rules.....	16
1.5	Physical Design Optimizations	18
1.6	Algorithms and Complexity	20
1.7	Graph Theory Terminology.....	24
1.8	Common EDA Terminology.....	26
	Chapter 1 References.....	30
2	Netlist and System Partitioning	33
2.1	Introduction.....	33
2.2	Terminology.....	34
2.3	Optimization Goals.....	35
2.4	Partitioning Algorithms	36
2.4.1	Kernighan-Lin (KL) Algorithm	36
2.4.2	Extensions of the Kernighan-Lin Algorithm	41
2.4.3	Fiduccia-Mattheyses (FM) Algorithm.....	41
2.5	A Framework for Multilevel Partitioning	47
2.5.1	Clustering.....	48
2.5.2	Multilevel Partitioning	48
2.6	System Partitioning onto Multiple FPGAs.....	50
	Chapter 2 Exercises.....	53
	Chapter 2 References.....	54
3	Chip Planning	57
3.1	Introduction to Floorplanning	58
3.2	Optimization Goals in Floorplanning.....	59
3.3	Terminology.....	61
3.4	Floorplan Representations.....	63
3.4.1	Floorplan to a Constraint-Graph Pair.....	63
3.4.2	Floorplan to a Sequence Pair	64
3.4.3	Sequence Pair to a Floorplan	65
3.5	Floorplanning Algorithms	68
3.5.1	Floorplan Sizing	69
3.5.2	Cluster Growth	73
3.5.3	Simulated Annealing	77
3.5.4	Integrated Floorplanning Algorithms.....	81
3.6	Pin Assignment	82
3.7	Power and Ground Routing	86
3.7.1	Design of a Power-Ground Distribution Network	87
3.7.2	Planar Routing	87
3.7.3	Mesh Routing.....	89
	Chapter 3 Exercises.....	91
	Chapter 3 References.....	92

4	Global and Detailed Placement	95
4.1	Introduction.....	95
4.2	Optimization Objectives	96
4.3	Global Placement.....	103
	4.3.1 Min-Cut Placement	104
	4.3.2 Analytic Placement	110
	4.3.3 Simulated Annealing.....	117
	4.3.4 Modern Placement Algorithms	120
4.4	Legalization and Detailed Placement	122
	Chapter 4 Exercises.....	125
	Chapter 4 References	126
5	Global Routing	131
5.1	Introduction.....	131
5.2	Terminology and Definitions	133
5.3	Optimization Goals.....	136
5.4	Representations of Routing Regions	138
5.5	The Global Routing Flow	140
5.6	Single-Net Routing	141
	5.6.1 Rectilinear Routing.....	141
	5.6.2 Global Routing in a Connectivity Graph	146
	5.6.3 Finding Shortest Paths with Dijkstra's Algorithm.....	149
	5.6.4 Finding Shortest Paths with A* Search	154
5.7	Full-Netlist Routing	155
	5.7.1 Routing by Integer Linear Programming	155
	5.7.2 Rip-Up and Reroute (RRR)	158
5.8	Modern Global Routing	160
	5.8.1 Pattern Routing	161
	5.8.2 Negotiated Congestion Routing.....	162
	Chapter 5 Exercises.....	164
	Chapter 5 References	165
6	Detailed Routing	169
6.1	Terminology.....	169
6.2	Horizontal and Vertical Constraint Graphs	172
	6.2.1 Horizontal Constraint Graphs	172
	6.2.2 Vertical Constraint Graphs.....	173
6.3	Channel Routing Algorithms	175
	6.3.1 Left-Edge Algorithm	175
	6.3.2 Dogleg Routing	178
6.4	Switchbox Routing	180
	6.4.1 Terminology	180
	6.4.2 Switchbox Routing Algorithms	181
6.5	Over-the-Cell Routing Algorithms	182
	6.5.1 OTC Routing Methodology	183
	6.5.2 OTC Routing Algorithms.....	184
6.6	Modern Challenges in Detailed Routing	185
	Chapter 6 Exercises.....	187
	Chapter 6 References	188

7	Specialized Routing	191
7.1	Introduction to Area Routing	191
7.2	Net Ordering in Area Routing.....	193
7.3	Non-Manhattan Routing.....	195
	7.3.1 Octilinear Steiner Trees	195
	7.3.2 Octilinear Maze Search	197
7.4	Basic Concepts in Clock Networks.....	197
	7.4.1 Terminology	198
	7.4.2 Problem Formulations for Clock-Tree Routing.....	201
7.5	Modern Clock Tree Synthesis.....	203
	7.5.1 Constructing Trees with Zero Global Skew.....	203
	7.5.2 Clock Tree Buffering in the Presence of Variation	212
	Chapter 7 Exercises.....	215
	Chapter 7 References	217
8	Timing Closure	221
8.1	Introduction.....	221
8.2	Timing Analysis and Performance Constraints	223
	8.2.1 Static Timing Analysis.....	224
	8.2.2 Delay Budgeting with the Zero-Slack Algorithm	229
8.3	Timing-Driven Placement.....	233
	8.3.1 Net-Based Techniques	234
	8.3.2 Embedding STA into Linear Programs for Placement .	237
8.4	Timing-Driven Routing	239
	8.4.1 The Bounded-Radius, Bounded-Cost Algorithm.....	240
	8.4.2 Prim-Dijkstra Tradeoff.....	241
	8.4.3 Minimization of Source-to-Sink Delay.....	242
8.5	Physical Synthesis	244
	8.5.1 Gate Sizing.....	244
	8.5.2 Buffering.....	245
	8.5.3 Netlist Restructuring.....	246
8.6	Performance-Driven Design Flow.....	250
8.7	Conclusions.....	258
	Chapter 8 Exercises.....	260
	Chapter 8 References	262
A	Solutions to Chapter Exercises	267
	Chapter 2: Netlist and System Partitioning	267
	Chapter 3: Chip Planning.....	270
	Chapter 4: Global and Detailed Placement	273
	Chapter 5: Global Routing.....	276
	Chapter 6: Detailed Routing.....	280
	Chapter 7: Specialized Routing	284
	Chapter 8: Timing Closure	292
B	Example CMOS Cell Layouts.....	299