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4 **Weather and Road Geometry Impact on Longitudinal Driving Behavior:**
5 **Exploratory Analysis Using an Empirically Supported Acceleration Modeling**
6 **Framework**
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10 5 S. H. Hamdar* (hamdar@gwu.edu), L. Qin and A. Talebpour
11 6

12 7 **ABSTRACT**
13 8

14 9 The objective of this paper is to quantify and characterize driver behavior under different
15 10 roadway geometries and weather conditions. In order to explore how a driver perceives the
16 11 rapidly changing driving surrounding (i.e. different weather conditions and road geometry
17 12 configurations) and executes acceleration maneuvers accordingly, this paper extends a Prospect
18 13 Theory based acceleration modeling framework. A driving simulator is utilized to conduct 76
19 14 driving experiments. Foggy weather, icy and wet roadway surfaces, horizontal and vertical
20 15 curves, and different lane and shoulder widths are simulated while having participants driving
21 16 behind a yellow cab at speeds/headways of their choice. After studying the driving trends
22 17 observed in the different driving experiments, the extended Prospect Theory based acceleration
23 18 model is calibrated using the produced trajectory data. The extended Prospect Theory based
24 19 model parameters are able to reflect a change in risk-perception and acceleration maneuvering
25 20 when receiving different parameterized exogenous information. The results indicate that drivers
26 21 invest more attention and effort to deal with the weather challenges (statistically significant
27 22 changes in behavior) compared to the effort to deal with the road-geometry conditions.
28 23 Moreover, the calibrated model is used to simulate a highway segment and observe the produced
29 24 fundamental diagram. The preliminary results suggest that the model is capable of capturing
30 25 driver behavior under different roadway and weather conditions leading to changes in capacity
31 26 and traffic disruptions.
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7 **Keywords:** Car Following; Driving Simulator; Prospect Theory; Road Geometry; Safety;
8 Weather.

List of Figures

1	
2	
3	
4	1
5	
6	2
7	
8	3
9	Figure 1 Schematic of Prospect Theory Based Acceleration Model. 31
10	4
11	Figure 2 (a) Raw Data of Speed Profile Selected for the Lead Vehicle Based on NGSIM Data
12	5 (FHWA, 2005), (b) Speed Profile of the Lead Vehicle Defined in the Driving Simulator. 32
13	
14	6
15	Figure 3 (a) Jersey Barrier, (b) Undivided Road, (c) 9ft Wide Lane with Metal Barrier, (d) 10ft
16	7 Wide Lane with Metal Barrier, (e) No Hard Shoulders, (f) 3ft Wide Hard Shoulder, (g)
17	8 Mountainous Terrain, and (f) Rolling Terrain. 33
18	
19	9
20	Figure 4 Visibility Distance (a) 65.62ft, (b) 164ft, (c) 328ft, and (d) 656.2ft. 34
21	10
22	Figure 5 Minimum Time-To-Collision and Maximum Deceleration of the Follower. 35
23	
24	11
25	Figure 7 Two Examples of Drivers' Acceleration behavior in Moderately Challenging (a), and
26	12 Extremely Challenging (b) driving conditions. 37
27	
28	13
29	Figure 9 Simulated Flow Density Diagrams Based on the Average Calibrated Acceleration
30	14 Model Parameters in Normal (a), Moderately Challenging (b), and Challenging (c) Driving
31	15 Conditions. 39
32	16
33	
34	17
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37	
38	
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List of Tables

1	
2	
3	
4	1
5	
6	2
7	Table 1 Main Events Used in the Driving Experiments 40
8	3
9	Table 2 Length of Horizontal Curve Section..... 41
10	4
11	Table 3 Design of Vertical Curve Sections..... 42
12	5
13	Table 4 Test Variables in Each Driving Scenario..... 43
14	6
15	Table 5 Driving Simulator Output..... 44
16	7
17	Table 6 Experiment Sample..... 45
18	8
19	Table 10 Cross Comparison of Dependent and Independent Variables. 49
20	9
21	
22	10
23	11
24	12
25	
26	
27	
28	
29	
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5 1 **Weather and Road Geometry Impact on Longitudinal Driving Behavior:**
6 2 **Exploratory Analysis Using an Empirically Supported Acceleration**
7 3 **Modeling Framework**
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12 7 **1.0 INTRODUCTION AND MOTIVATION**
13 8

14 9 Environmental conditions have been identified to have major impacts on driver behavior.
15 10 Examples of different environmental conditions are weather-related and roadway geometry-
16 11 related factors. For instance, it has been shown that reduced visibility has a substantial impact on
17 12 traffic flow dynamics (Hoogendoorn et al. (2010) while the geometry of the road layouts leads to
18 13 changes in driving behavior (McLean (1981). Moreover, weather condition and road geometry
19 14 are the two congestion and crash triggering factors. Empirical evidence suggests that the
20 15 likelihood of rear-end crashes increases during abnormal weather or at accident prone sections
21 16 (Brackstone, et. al., 2009, Winsum, 1999; Knuiman et al., 1993; Karlaftis and Golias, 2002;
22 17 Polus et al., 2005). However, little effort has been made to quantify their effects on driving
23 18 behavior (in the micro scale) and congestion and safety (in the macro scale). Therefore, more
24 19 detail behavioral bases studies are required to describe the driver behavior in different weather
25 20 and roadway conditions.
26 21

27 22 Driver behavior is subject to change according to the surrounding environment. While it is
28 23 expected that different driving environments impose different changes to the driving behavior of
29 24 an individual, the magnitude of deviation from normal driving behavior varies among drivers.
30 25 Comprehensive study of the effect of certain driving environments on driving behavior has been
31 26 presented in the literature (Brackstone et al., 2009); however, little effort has been presented to
32 27 quantify the effects of different weather conditions and road geometrical configuration on
33 28 driving behavior. The main objective of this paper is to explore how a driver perceives the
34 29 dynamic changing driving surroundings (i.e. different weather conditions and road geometrical
35 30 configurations) and executes acceleration maneuvers accordingly. Specifically, this study
36 31 presents an effort to quantify the changes in drivers' car-following behavior under different
37 32 roadway geometries and weather conditions. Accordingly, this study presents an extension to the
38 33 Prospect Theory based car-following model of Hamdar et al. (2008, 2015). Prospect theory) is
39 34 commonly considered as one of the most powerful descriptive theories of human decision-
40 35 making. Hamdar et al. (2008) has first put forward an acceleration model, which adopts Prospect
41 36 Theory to reflect the psychological and cognitive aspects of the decision making process. In this
42 37 Prospect Theory based acceleration model, time is divided into different acceleration instances,
43 38 and at each time instance, driver may accelerate, decelerate or keep his or her current speed. In
44 39 other words, drivers make decisions on acceleration choices, and their choices are based on an
45 40 evaluation of gains and losses. This paper builds on this acceleration model that translates this
46 41 utility-based concept into longitudinal driving behavior. The presented model extends the current
47 42 Prospect Theory logic by considering the effect of the external driving environment while
48 43 keeping the adopted probabilistic nature of human judgment. A driving simulator is used to test
49 44 individual driving behavior in different environmental situations and then use the data obtained
50 45 from the driving experiments to calibrate the micro acceleration model.
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4 1 The structure of the remainder of this paper is as follows. First a background review on the
5 2 effects of weather and road geometry on driver behavior is presented. This section is followed by
6 3 the modeling framework and the related parametric sensitivity analysis. Experimental setup and
7 4 data collection procedures are presented next followed by a thorough numerical analysis. The
8 5 numerical results including the calibration results are presented next. The concluding remarks
9 6 and the future research directions are presented last.
10 7

11 8 **2.0 BACKGROUND**

12 9
13 10 This section presents a review of the literature focused on the impact of different weather and
14 11 road geometry characteristics on driver behavior. Note that this section does not provide any
15 12 background on car-following behavior and microscopic simulation models. A comprehensive
16 13 study of these models can be found at Hamdar et al. (2008, 2015) and Talebpour et al. (2011).
17 14

18 15 **2.1. Weather**

19 16
20 17 Multiple studies have focused on the statistical relationships between different traffic measures
21 18 and different surrounding weather conditions. The overall findings of these macro level studies
22 19 denote that visibility impairment, precipitation, and temperature extremes may affect driver
23 20 behavior and vehicle maneuverability. Chen et al. (1995) found that weather and road surface
24 21 conditions bring about some differences in car-following behavior. Based on recorded traffic
25 22 data, Ibrahim and Hall (1994) found that free-flow speed reduces 1.9 mph in light snow, 3.1 to
26 23 6.2 mph in heavy rain, and 23.6 to 31 mph during heavy snow. Liang et al. (1998) conducted a
27 24 study to investigate the impact of visibility on speed. Through data collection, they found that
28 25 average speed reduces 11.9 mph during snow events.
29 26

30 27 Another group of studies have focused on the concepts and theories of car following to
31 28 understand drivers' car following behavior, their headway selection and how the choice of
32 29 headway affects safety (Brackstone, et. al., 2009, Winsum, 1999). It was suggested that drivers'
33 30 car following behavior can be affected in dense fog resulting from obscure scenery (Evans,
34 31 2004). Evans (2004) also observed that drivers tended to follow the lead vehicles much closer
35 32 from the fear of losing a reference when driving in foggy weather. Hawkins (1988) reported a
36 33 significant increase in distance headways when visibility distance was 150 m. Van Der Hulst et
37 34 al. (1998) studied driving behavior in fog with a visibility distance of 150 m. They noted that due
38 35 to the difficulty in anticipation, drivers increase time headway under low visibility conditions.
39 36 They also found that drivers' reactions to decelerations of the leader were very accurate even at
40 37 low visibility levels. Broughton et al. (2007) employed a high-fidelity driving simulator to
41 38 measure the car-following behavior under three visibility conditions. Two distinctive driving
42 39 styles were identified in their studies: laggers and non-laggers driving styles; the laggers stopped
43 40 following the leader within visible distances and instead dropped back to some larger distance
44 41 headways, accompanied by increases in speed variability, whereas the non-laggers remained in a
45 42 true car following mode with a visible leader ahead of them. Hoogendoorn et al. (2010) also
46 43 conducted a set of driving simulation experiments and suggested that fog led to a decrease in
47 44 speed as well as in acceleration rate. A substantial increase in distance to the lead vehicle was
48 45 also observed in the experiments.
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4 1 The friction coefficient of the road surface, which influences vehicle's maneuverability, has been
5 2 widely studied. Perrin and Martin (2002) analyzed traffic flow in Salt Lake Valley, Utah during
6 3 winter. The results indicated that start-up delays on snowy pavement and wet pavement was 23%
7 4 and 5% higher, respectively, than the delays observed on dry pavement. As friction and
8 5 precipitation types are highly correlated, Wu et al. (2009) presented a novel car-following model
9 6 according to the relationship between vehicle deceleration and passenger comfort levels. In this
10 7 model, the friction coefficient between vehicles and road surface is considered and experiments
11 8 with this model showed high compatibility with real-life observations. Wallman et al. (1997)
12 9 found that average speed reduces by 10% to 30% in icy and snowy weather conditions
13 10 respectively. Tanaka et al. (2010) studied the influence of different road surfaces through car-
14 11 following platoon experiments and they discovered a significant difference in driving behavior
15 12 between icy and dry roadway surfaces. In addition, safe driving in adverse weather conditions
16 13 also requires full detection of pavement markings. Retro-reflectivity of pavement markings
17 14 varies as weather condition changes. Zwahlen et al. (1995) stated that obliteration of pavement
18 15 markings heavily influences drivers' detection distances and thus affect their perception and
19 16 behavior.

2.2. Road Geometry

20
21 Roadway layouts, including lane and shoulder width, median existence, horizontal and vertical
22 alignment, also have considerable impact on driving behavior. Roadway geometry affects
23 drivers' perception of driving environment and therefore influences their driving behavior
24 (Janssen et al., 2006). Several studies showed that crash rate were associated with roadway
25 design (Knuiman et al., 1993; Karlaftis and Golias, 2002; Polus et al., 2005). However, only few
26 studies directly investigated the effects of a specific roadway design elements on driving
27 behavior through controlled manipulations (Martens et al., 1997; Stamatiadis et al., 2007). In this
28 paper and based on the above studies, horizontal and vertical alignments, lane width, shoulder
29 widths, and median existence are considered as the geometric features of interest. Note that in
30 this study, a roadway feature at a given candidate location is considered deficient if its value at
31 that location is less than the recommended design value and criteria according to the AASHTO
32 Green Book (2001).

2.2.1. Horizontal Alignments

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35 Different road characteristics such as road curvature and gradient affect driving behavior
36 differently, as suggested by Rockwell (1972). Andueza (2000) developed a model to estimate
37 vehicular speed on curves and tangents of roads. The study found that drivers' choice of speed
38 within horizontal curves highly depended on the roadway features before the start point of the
39 curve. McLean (1981) studied the influences of rural road alignment on drivers' speed selection
40 behavior by collecting free-flow speed data at 120 curves with approach tangent sites on two-
41 lane rural highways. Their analysis suggested that the observed 85th percentile car speeds were
42 influenced by the desired speed. Bonneson et al. (2007) investigated the effects of horizontal
43 curves on driver behavior on rural two-lane highways. They proposed several criteria for
44 selecting curve advisory speed.

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4 1 In addition to speed, crash rate has been also investigated in this context. Significant positive
5 2 correlation has been identified between the road curvature and crash rates (Shankar et al., 1996).
6 3 A number of different indicators have been adopted to study the impact of road geometric
7 4 features on driving behavior. These indicators are summarized as follows:

- 9 5 • Bend numbers per kilometer (Barker, et al. 1999, Shankar, et al, 1995, Shankar, et al,
10 6 1996)
- 11 7 • Percentage of bend length to road length (Shankar, et al, 1996)
- 12 8 • Maximum and minimum radius of curvature (Shankar, et al, 1996)
- 13 9 • Cumulative absolute angle turned through per kilometer (Hughes, et al, 1996, Walmsley,
14 10 et al. 1998)

15 11 Furthermore, Crashes on horizontal curves have been recognized as a considerable safety
16 12 problem for many years. Zegeer et al. (1990) conducted a study on two-lane rural roads to
17 13 determine how horizontal curve features affect roadway crashes. They concluded that through
18 14 widening lanes or shoulders on curves, crashes can be radically reduced by as much as 33%.
19 15 Several other studies examined the relationship between specific levels of horizontal curve and
20 16 crash rate. These studies resulted in the following conclusions where crash rate tends to increase
21 17 for,

- 22 18 1) Curves of radii less than 1312ft (McLean, 1981; Choueiri and Lamm, 1987; and Krebs
23 19 and Kloeckner, 1977),
- 24 20 2) Curves of radii less than 1968ft on rural two-lane roads (Choueiri and Lamm, 1987;
25 21 Johnston, 1982), and
- 26 22 3) Curves over 3 degrees (1910ft) (Cirillo and Council, 1986).

27 23 28 24 **2.2.2. Vertical Alignment**

29 25 Yang and Peng (2010) identified the road gradient as an exogenous disturbance of longitudinal
30 26 driving behaviors in an error-able car-following model. Mullins and Keese (1961) also suggested
31 27 that rear-end accidents were common at vertical curve locations where unfavorable sight
32 28 conditions existed. Lefevre (1953) investigated driver behavior on two lane rural highways with
33 29 vertical curves, where the minimum sight distances ranged between 150 and 500ft. It was
34 30 observed that drivers invariably reduced the speeds as they approached vertical curves with short
35 31 sight distances. It was also found that speeds at the vertical curves (regardless of the sight
36 32 distance) appeared to be determined by present operating speeds. According to this study,
37 33 roadway crash rate was much higher on sag curves than on crest curves. Glennon (1985) noted
38 34 that crash rate at grade sections were much higher than crash rate at level sections. Their findings
39 35 showed that crash rate is higher at steep gradients and down-hill sections.

40 36 41 37 **2.2.3. Lane Width**

42 38 The effect of lane width on traffic flow efficiency as well as safety implications has been
43 39 investigated for many years. Harwood et al. (1990) suggested that the roadway capacity would
44 40 drop when the width of traffic lanes is below 12ft. Specifically, 11ft lanes have 3% less capacity
45 41 than 12ft lanes; 10 ft lanes have 7% less capacity than 12ft lanes; 9 ft lanes streets have 10% less
46 42 capacity than 12ft lanes. Narrower lanes are perceived as less tolerant and less secure. This led
47 43 drivers to adopt speed control to avoid dangerous or risky situations (Summala, 1996). De Waard
48 44 (1995) noted that driving on a narrow lane requires greater mental effort than driving on a wide
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4 1 lane, because drivers need to keep vehicles within the lane. Yagar and Van (1983) reported 1.1
5 2 mph reduction in average speed for every 1 foot reduction in lane width. Likewise, Heimbach et
6 3 al. (1983) found that during off-peak hours, if lanes narrowed by 1ft, speed would tend to reduce
7 4 0.6mph, when other factors are held constant. They showed that during peak hours, speed
8 5 decreases by 1mph per foot of lane width. Fitzpatrick et al. (2000) stated that 1 foot increase in
9 6 lane width would result is 2.9 mph increase in average speed. Vey and Ferreri (1968) also found
10 7 a direct relationship between lane width and speed: higher speeds were observed for 11ft lanes
11 8 compare to 10ft lanes.
12 9

13 10 Besides the impact of lane width on driving behavior and speed selection, lane width has an
14 11 effect on roadway safety. It has been demonstrated that the use of narrower lanes would lead to
15 12 more crashes if other roadway characteristics remain unchanged (Harwood, et al., 2000).
16 13 Heimbach et al. (1983) showed that crash rate increases as lane width decreases, but the
17 14 relationship is not linear. Karlaftis and Golias (2002) quantitatively assessed the effects of
18 15 various highway characteristics on crash rate using a crash database. They identified lane width
19 16 as one of the most important factors affecting crash rate on two-lane roadways.
20 17

21 18 **2.2.4. Shoulder Width**

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23 20 Shoulder width has also an impact on driving behavior. Yagar and Van (1983) found a small
24 21 increase in driving speed on 2-lane rural roads if a hard shoulder was added. Stamatiadis, et al.
25 22 (2009) suggested that wider shoulders give drivers a sense of security and much space to correct
26 23 their driving errors. However, narrow lanes demand more mental concentration and could
27 24 decrease the positive effects of wide shoulders on safety. In a study on safety relationships
28 25 between geometric characteristics and crashes, Zegeer and Deacon (1987) concluded that crash
29 26 rate decreased with increasing lane width and shoulder width. It was also observed that lane
30 27 width had a greater impact on crash rate compare to shoulder-width. After examining crash rate
31 28 on two-lane roads with three different shoulder widths (2, 4, and 8ft), Rinde (1977, in Dewar and
32 29 Olson, 2001) found that narrower shoulders led drivers to steer away from shoulders and drove
33 30 closer to the center of the road, which increases the likelihood of head-on collisions. Likewise,
34 31 Kraus et al. (1993) found that narrow shoulders might create a dangerous condition where
35 32 drivers don't have enough recovery area in case of lane deviation; therefore, this increases the
36 33 likelihood of off-road collisions. After analyzing data from 600 two-lane rural road sections in
37 34 Alabama, Michigan, and Washington, Miaou (1998) identified that 1ft increase in shoulder
38 35 widths would decrease approximately 9% run-off-the-road crashes. In a similar study for rural
39 36 two-lane roads in Washington and North Carolina, Council and Stewart (1999) found that
40 37 increasing the shoulder width by 1ft leads to 5% to10% reduction in crash rate at sections where
41 38 daily traffic volume exceeds 5,000. Using three-year data from Minnesota and Washington for
42 39 two-lane rural roads, Vogt and Bared (1998) suggested that a unit increase in shoulder width
43 40 significantly reduces crash rate. However, it is noteworthy that wide shoulders don't mean safer
44 41 situations to drivers. It has been shown that approximately 10% of fatal highway crashes are
45 42 related to vehicles stopped on shoulders (Hauer, 2000).
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4 **1 2.2.5. Median Existences**
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7 3 In the United States, rural two-lane roads sometimes lack physical objects that separate opposing
8 4 traffic streams. It has been confirmed that the existence of median on highways have substantial
9 5 influence on traffic flow operations and traffic safety. For example, Council and Stewart (1999)
10 6 examined the safety differences between divided two-lane and undivided four-lane rural
11 7 roadways. It was concluded that the existence of median barriers had positive effect on crash
12 8 rate. Fitzpatrick et al. (2000) pointed out that the presence of medians results in higher speeds
13 9 than where no median existed. The speed on streets without medians was about 38 mph, and the
14 10 speed was 42 mph with a raised median in urban areas. Tay and Churchill (2007) conducted a
15 11 study related to drivers' perception of median barriers. Specifically, speed data were collected on
16 12 freeways in the City of Calgary, Alberta with different types of longitudinal median barriers.
17 13 They found that drivers increased speed since they perceived the barriers as a protective device.
18 14 Another study conducted in Oregon suggested that crash rate would reduce if median barriers are
19 15 used (Strathman, et al., 2001).
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24 17 Most of these studies investigated the effects of weather and road geometry on average speed
25 18 and crash rate in a macro scale. However, understanding of the underlying mechanisms, which
26 19 lead to these changes in speed, flow, and crash rate, is essential to operate the transportation
27 20 facilities under adverse road and weather conditions. This paper mainly focuses on incorporating
28 21 the required parameters in a microscopic simulation model to capturing these mechanisms and
29 22 model drivers' responses to reduced visibility from fog, different friction coefficients, different
30 23 horizontal and vertical alignment, median types, and different lane and shoulder widths in real-
31 24 world conditions.
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34 25
35 26 **3.0 MODELING FRAMEWORK**
36 27

37 28 By reviewing the external factors of weather and road geometry, the objective is to investigate
38 29 drivers' responses to reduced visibility, different road surface conditions, different horizontal and
39 30 vertical curves, and different lane and shoulder widths in real-world conditions. This section
40 31 introduces a model to capture the drivers' decision making process after processing the external
41 32 information. Driving decisions are made based on drivers' current condition and the perceived
42 33 information obtained from the external environment. Therefore, a reasonable and realistic
43 34 drivers' decision representation should be dynamic rather than static. This study adopted the
44 35 Hamdar et al. (2008, 2015) model to capture the dynamics in the decision making process. The
45 36 decision making process in this model uses Kahneman and Tversky's Prospect Theory (1979).
46 37 Based on this theory, the decision maker first assigns different weights to different alternatives
47 38 considering corresponding gain and losses (framing or editing phase); and in then he/she
48 39 evaluates these alternatives based on the prospect index (evaluation phase). The prospect index is
49 40 calculated similar to the expected utility using subjective decision weights instead of expected
50 41 probability of each outcome. This approach allows risk-taking maneuvers when drivers are
51 42 uncertain of the leader's future behavior. Accordingly, crashes can be captured by this model
52 43 endogenously. Note that despite providing a realistic representation of car-following behavior
53 44 under normal conditions, most of other advanced car-following models introduce emergency
54 45 breaking mechanisms to preclude high-risk maneuvers (e.g. maneuvers that can lead to a crash)
55 46 in the simulation environment. Another advantage of the Prospect Theory based model is the
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4 1 inclusion of parameters that capture stochasticity and the distribution associated with the
5 2 acceleration values rather than simply looking at a deterministic acceleration value produced
6 3 through a given equation.
7 4

8 4
9 5 Driving in adverse weather condition as well as challenging roadway geometries involves
10 6 stochasticity and high-risk maneuvers. In fact, in extreme driving conditions, drivers are more
11 7 likely to make poor decisions due to the roadway condition, limited visibility, etc. Therefore,
12 8 from the modeling perspective, the car-following framework should be able to model the
13 9 occurrence of these high-risk maneuvers. Considering all these modeling requirements, Prospect
14 10 Theory based car-following model is an excellent modeling framework for the purpose of this
15 11 study.
16 12

17 12
18 13 Figure 1 illustrates the dynamic relationships inherent in the proposed Prospected Theory based
19 14 acceleration model. For every decision interval, drivers choose their acceleration based on
20 15 different value functions representing diverse driving environments. The final utility reflects a
21 16 speed-acceleration value that the driver considers to be safe over the anticipation time period.
22 17 The model calculates the state vector of the n^{th} vehicle at each time instance i :
23 18

$$s_{n,i} = [x_{n,i}, v_{n,i}, a_{n,i}] \quad (3.1)$$

24 18
25 19 Where $x_{n,i}$ is the position of the n^{th} vehicle (the following vehicle) at time instance i ; $v_{n,i}$ and
26 20 $a_{n,i}$ represent the n^{th} vehicle's velocity and acceleration at time instance i , respectively. The state
27 21 vectors $s_{n,i}$ is then applied to calculate the acceleration $a_{n,i+1}$.
28 22

29 22 3.1. Prospect Theory Model and Additional Parameters

30 23
31 24 A set of model parameters were incorporated in the extended Prospect Theory based model to
32 25 characterize the decision making circumstances. The extended value function adopted in this
33 26 paper is given by:
34 27

35 28 **Place Fig. 1**

$$U_{PT}(a_n) = \frac{\left(w^- + (1-w^-)\left(\tanh\left(\frac{a_n}{a_0}\right) + 1\right)\right)}{\psi} \times \frac{\left(\frac{a_n}{a_0}\right)}{\left(1 + \left(\frac{a_n}{a_0}\right)^2\right)^\gamma} \quad (3.2)$$

36 29 Where:

37 30 $U_{PT}(a_n)$ = The value function,

38 31 w^- = Weighing factor for the prospect theory value,

39 32 γ = Exponent of the prospect theory value mainly reflecting road impact,

40 33 a_0 = Acceleration normalizing factor,

41 34 ψ = Amplitude factor for the prospect theory value mainly reflecting weather influence.
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45 38 This extended value function was introduced based on the observations from the driving
46 39 simulator experiments. In general, it is expected that in favorable weather conditions, unlike
47 40 adverse weather conditions (e.g. foggy weather), drivers tend to avoid abrupt changes in
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1 acceleration and speed to enhance their comfort. Accordingly, this study defined the parameter ψ
2 to reflect this driver behavior. Lower ψ value results in an increase in the sensitivity to
3 acceleration/deceleration and results in less abrupt changes in acceleration and speed (for more
4 details see Section 5.4 and Figure 8). Moreover, the parameter γ is introduced to capture the
5 effects of roadway geometry on drivers' acceleration choices. Drivers tend to predict the
6 roadway geometry and adjust their acceleration and speed to enhance safety. Therefore, drivers
7 put more effort on acceleration/speed choices while dealing with a challenging roadway
8 geometry. Lower values of γ increases the sensitivity to roadway geometry and results in more
9 conservative acceleration choices by drivers (for more details see Section 5.4 and Figure 8). A
10 detailed discussion on the effect of these parameters are presented in Section 5.4.

11
12 The drivers will gain U_{PT} by choosing a_n as the acceleration unless they involve in a crash.
13 Hamdar et al. (2008, 2015) used the crash seriousness term, $k(v, \Delta v)$, to determines the disutility
14 resulting from the crash,

$$U(a_n) = (1 - p_{n,i})U_{PT}(a_n) - p_{n,i}w_c k(v, \Delta v) \quad (3.3)$$

15
16 where $p_{n,i}$ is the probability of being involved in a rear-end collision. $U_{PT}(a_n)$ is derived from
17 equation 3.2 and w_c is a crash weighting parameter which is lower for aggressive drivers.
18 Capturing the stochastic nature of the acceleration choice, Hamdar et al. (2008, 2015) obtained
19 the logistic functional form as follow,
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$$f(a_n) = \begin{cases} \frac{e^{(\beta_{PT} \cdot U(a_n))}}{a_{\max}} & a_{\min} \leq a_n \leq a_{\max} \\ \int_{a_{\min}}^{a_n} e^{(\beta_{PT} \cdot U(a'))} & \\ 0 & \text{Otherwise} \end{cases} \quad (3.4)$$

23
24 where β_{PT} is the sensitivity of choice to the total utility. In ideal conditions, the follower can
25 drive at his/her desired speed to follow the leader. Desired speed is the speed drivers would drive
26 on a straight and level road section in clear day and without traffic disruptions. However, a
27 driver's real travel speed is restricted by those aforementioned external factors as well as the
28 leader's behavior. Accordingly, drivers may accelerate or decelerate until they obtain an
29 acceptable utility corresponding to the driving environment; if the surrounding conditions
30 change, the utility function is also subject to change. Therefore, drivers always evaluate to what
31 extent they need to regulate their current speed to adapt to the new upcoming driving
32 environment.

33 34 4.0 EXPERIMENTAL SET-UP

35
36 Once the hypotheses on the impact of different weather and roadway condition on acceleration
37 behavior are defined within the Prospect Theory based modeling framework, a numerical study
38 supporting such hypotheses is needed. Using a driving simulator is an alternative for on-road
39 tests when researchers wish to use more controlled circumstances, or manipulate specific test
40 conditions. Driving simulators are useful tools for the studies of driving behavior and traffic

1 safety. By providing feedback in the form of visual, motion, and audio cues to drivers, a driving
2 simulator can give drivers the impression that they are driving an actual vehicle in the real world.
3 By simulating vehicle motion based on the driver operations, the vehicle kinematic data can in
4 turn be used to extract trajectory data, which in turn can be used to analyze driving behavior.
5 This section introduces the procedures related to the driving experiment set-up.

6 7 **4.1. 3-D Driving Simulator**

8
9 The simulator software used in this study was originally developed for the National Highway
10 Traffic Safety Administration in the 1980's. It is a product of Systems Technology, Inc. on low-
11 cost techniques for creating laboratory test relevant to the psychomotor and cognitive activities
12 of real world driving. The version currently in use of our studies is STISIM Drive Build 1.02.07.
13 The vehicle dynamics program in use is VDANL Drive version 6.0.30 and it allows for user-
14 specifiable, realistic steering and speed control characteristics.

15
16 The STISIM Driving simulator is the main apparatus applied in this study. Driving performances
17 of many subject populations have been studied in driving simulators (Lee, et al., 2005,
18 Shechtman, et al., 2007). A total of 36 students and staff from the George Washington
19 University, 26 male and 10 female, with different driving experience participated in the
20 experiments. Note that this sample mostly consists of younger drivers. Upon the participants'
21 arrival in the laboratory, a questionnaire was completed by each participant, which includes
22 several questions about their individual background and driving experience. In addition, each
23 participant was briefed on the requirements of the driving test. They were instructed to follow
24 their normal driving acceleration behavior. Since this paper focuses on acceleration behavior, the
25 drivers were instructed to follow a "yellow cab" without performing any lane-changing.

26
27 The participants' average age was 24.8 years (std 4.02 years), ranging from 20 to 35 year. Every
28 participant had a valid US driving license with 6 years of driving experience on average (std 4.50
29 years). None of the participants had previous experience with the driving simulator or reported
30 any history of visual problems. Among 36 participants, 6 (1 female, 5 males) had road crashes in
31 the past 5 years and one (male) refused to answer the corresponding "crash history" question.
32 The 26 males and 10 females were randomly assigned to two or three of the 15 experimental
33 scenarios (5.5 minutes each with around 3 minutes of pre-experiment driving and 1.5 minute of
34 post-experiment driving: around 10 minutes of total driving using the simulator). Details about
35 these experiments are presented in the next section. With this assignment, each experiment had at
36 least 3 participants (1 female participant and 2 male participants).

37 38 **4.2. Driving Scenarios and Data Collection**

39 40 **4.2.1. Generic Environmental Settings**

41
42 The simulation scenarios in this study consisted of different weather conditions and road
43 geometric configurations. In standard scenario, the test route was an 8000ft stretch of a four-lane
44 roadway through a rural landscape. A series of metal median barriers with the dimensions of 10ft
45 long, 1.5ft wide and 1.5ft high were displayed in the middle of the roadway. In the standard
46 scenario, the lane width and the shoulder width of the roadway in both directions were 12ft and

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4 1 6ft, respectively. Speed limit signs of 65 mph, white dashed lines as the lane markings and white
5 2 solid line at edge were posted throughout the scenario. The stripes of lane marking are 10ft long
6 3 and were separated by 10ft interval. The line width of the edge lines and lane markings were all
7 4 0.33ft. The cross-slopes for the travel lanes of both sides were set to slope down 1 percent from
8 5 the roadway center to its edge. As for the cross-slope of shoulders on both sides, it was set to 2
9 6 percent grade sloping down from the center of the roadway to the roadway's outer edges. Just
10 7 past the shoulders on both sides, there were 10ft wide fore-slopes that had 5 percent grade
11 8 sloping downward. The weather condition for the standard scenario was set to a clear day with
12 9 blue skies with no wind that may influence vehicle maneuverability. The simulator was
13 10 programmed to simulate a rural environment. Table 1 presents the events used in use in the
14 11 experiments.
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19 13 The traffic condition consisted of multiple vehicles traveling on both directions of the road.
20 14 Steady streams of oncoming vehicles were created throughout each simulation. There was also
21 15 steady traffic traveling in the same direction as the driver in both the center lane and side lane. In
22 16 addition, one lead “yellow cab” vehicle was programmed to travel on the side lane throughout
23 17 the simulation of the standard scenario. In order to make the movement of the lead vehicle as
24 18 generic as possible, the traffic data collected in the Federal Highway Administration’s Next
25 19 Generation Simulation project (FHWA, 2005) were adopted to define the speed profile of the
26 20 lead vehicle in this study. There were three data sets collected from 4:00 PM to 4:15 PM (data set
27 21 1), 5:00 PM to 5:15PM (data set 2) and 5:15PM to 5:30PM (data set 3) on 13th of April, 2005.
28 22 The NGSIM data were recorded at every 1/10 second and when selecting the speed data from the
29 23 NGSIM data pool, the authors always ensured that there were at least five vehicles in front of the
30 24 lead vehicle and at least 5 vehicles behind the lead vehicle; this guarantees a "car-following"
31 25 scenario. Finally, Vehicle ID 482, Vehicle ID 1014 from data set 1, vehicle ID 606 from data set
32 26 2, and Vehicle ID 100, Vehicle ID 306 from data set 3 were selected as the data samples in the
33 27 studies. The sequentially combined speed-time relationships of these five vehicles are presented
34 28 in Figure 2a. Due to the limitation of the STISIM Drive, the simulator only allows the speed of
35 29 the lead vehicle change 15 times during one single simulation. Therefore, the leader’s speed was
36 30 linearly smoothed (the speed of a vehicle can only be changed linearly in the driving simulator)
37 31 according to the selected NGSIM data. Figure 2b demonstrates the resulting speed profile.
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43 33 **Place Table 1**

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45 35 **Place Figure 2**

46 36 47 37 **4.2.2. Test Variables**

48 38
49 39 It was observed that median existence (Council and Stewart, 1999) and median type (Tay and
50 40 Churchill, 2007) affects drivers’ behavior and accordingly affects traffic efficiency and safety.
51 41 Two different median types: metal median barrier and concrete median barrier (Figures 3a and
52 42 3c) were used in the experiment. Undivided road was also tested in this study (Figure 3b).
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56 44 The lane width of a roadway also greatly affects the safety and comfort of drivers. Although 12ft
57 45 lane width is desirable on both rural and urban roadways, there are circumstances where much
58 46 narrower lane widths are used. For instance, the use of 10ft lane is acceptable when the traffic
59 47 volumes are low in some area. AASHTO Green Book (2001) notes that lane widths substantially
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4 1 less than 12ft are considered adequate for a wide range of volume, speed, and other conditions.
5 2 Actually, 9ft, 10ft, and 11ft lane widths are all in use depending on the road condition (*e.g.*
6 3 traffic demand, topographical constraints, etc.) and construction cost. In the experiments, 9ft and
7 4 10ft lane widths were tested for a long straight section of four-lane roadway (Figures 3c and 3d).
8 5 A standard lane width of 12ft will always be used in our simulation when testing other external
9 6 factors (*e.g.* visibility distances, friction coefficients of roadway surface, horizontal curves, and
10 7 vertical curves). Similarly, 0ft and 3ft shoulder widths were also tested in the experiment
11 8 (Figures 3e and 3f).
12 9

13 10 According to the literature, horizontal curve is one major location of traffic crashes and smaller
14 11 curve radius results in higher crash rate (Choueiri and Lamm, 1987). The transverse stability
15 12 (includes slippage and overturn) happens before the longitudinal stability on a curve based on the
16 13 vehicle steering theory. The drivers' comfort is also a decision factor in calculating the curve
17 14 radius. When designing the roadway layouts in mountainous area (Figure 3g), six different
18 15 horizontal curves were adopted. Three smooth horizontal curves were also used in the case of
19 16 rolling terrain scenario (Figure 3h).
20 17

21 18 **Place Figure 3**

22 19
23 20 **Place Table 2**

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25 22 **Place Table 3**

26 23
27 24 A roadway horizontal curvature consists of tangents (straight sections of road), curves (sections
28 25 of roadway with a constant curvature) and spirals. The roadway will remain straight until the
29 26 start of the curve is reached, and then will bend to the direction specified. The values of radius
30 27 and deflection angle of horizontal curves used in the experiments are shown in Table 2. The
31 28 Vertical Curve event in this simulator was selected to examine the elevation impact on driving
32 29 behavior. A combination of constant grade sections with a vertical curve was used to create
33 30 uphill and downhill segments. Table 3 presents the vertical curves applied in mountainous and
34 31 rolling terrain.
35 32

36 33 It was confirmed in the literature that reduced visibility conditions have huge impact on rear-end
37 34 crash rate (see background section for more details). In order to see the weather influence on
38 35 longitudinal driving behavior, this study utilized the driving simulator-based method where
39 36 foggy condition was simulated. The trajectory data of the subject vehicle and the lead yellow cab
40 37 vehicle were analyzed in order to determine how drivers react when driving in varying reduced
41 38 visibility conditions. Constant fog density was considered throughout each driving test and was
42 39 adjusted to present four different sight distances (65.62ft, 164ft, 328ft and 656.2ft) (Figure 4).
43 40 Note that the different levels of fog were operationally defined as the mean distance at which
44 41 drivers could detect an object on a straight road.
45 42

46 43 Road surface condition also affects driver behavior. Drivers often become more cautious and/or
47 44 nervous when encountering unusual roadway surface conditions (*e.g.* wet or icy conditions). The
48 45 Road Surface Attribute event in STISIM Drive was used to define different road surface
49 46 conditions. In this driving experiment, two different road surface conditions were created to

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4 1 simulate wet and icy roadway surfaces. When driving on normal roadway surfaces, the vehicle
5 2 tires had enough traction to respond to steering input. However, when the friction coefficient
6 3 reduced to 0.2 (icy condition) and 0.4 (wet condition), drivers found that the vehicle was harder
7 4 to control and less responsive.
8 5

9 6 Table 4 presents the summery of all 15 scenarios suggested in this section. Note that in all of the
10 7 14 scenarios (excluding the standard scenario), only one external factor was changed. The
11 8 standard scenario consists of two-lane rural road marked with single white edge lines and
12 9 separated by metal median barrier.
13 10

14 11 **Place Figure 4**
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17 14 **5.0 NUMERICAL ANALYSIS**

18 15 In this section, the results of driving simulator experiments are presented and the impacts of the
19 16 external factors on longitudinal driving behavior are discussed in detail. The effects of the
20 17 weather-related and the roadway geometry related factors on the microscopic traffic performance
21 18 measures (speed, spacing ...etc.) are discussed first. The discussion continues by introducing the
22 19 method used to calibrate the extended Prospect Theory based model parameters. The calibration
23 20 results are presented next followed by a limited simulation study.
24 21

25 22 **5.1 Exploratory Insight**

26 23 The average speed is calculated for each group in the 15 experiments. The average choice of
27 24 time headway and the corresponding standard deviation is also calculated for each experiment. In
28 25 addition, three deceleration instances are analyzed: deceleration of the leader from high speed to
29 26 medium speed (63ft/s to 30.5ft/s), from medium speed to relatively low speed (31ft/s to 15ft/s),
30 27 and from low speed to extremely low speed (15.2ft/s to 1.88ft/s). Note that three acceleration
31 28 instances, in each experiment, are also selected to evaluate the drivers' response to the
32 29 acceleration behavior of the leader.
33 30

34 31 **Place Table 4**
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37 34 **5.1.1 Choice of speed and time headway**

38 35 Car-following performance under the 15 different scenarios are measured on a stretch of road
39 36 during 5.5 minutes of experiments. Table 5 presents the corresponding statistics. Excluding the
40 37 standard scenario (standard scenario was used to familiarize the drivers with the simulator), the
41 38 results reveal that participants tend to choose lower speed when traveling on narrower lanes or
42 39 narrow shoulders. Similarly, the average speed under wet (23.94ft/s) and icy (23.94ft/s) road
43 40 surface conditions are slightly lower than other conditions. The results show that fog density has
44 41 little to no effect on the drivers' choice of speed (average speeds in four different foggy
45 42 conditions were all about 24ft/s). However, the standard deviations of speed in foggy conditions
46 43 were greater than standard condition, except for the third case (VD = 328ft). Note that drivers
47 44 were advised to follow a yellow cab in a car-following scenario. The driving pattern of the
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4 1 yellow cab was identical in all scenarios. Therefore, drivers had to choose similar speed values to
5 2 keep up with the driving pattern of the yellow cab. Low visibility, however, could introduce
6 3 more uncertainties that lead to more fluctuations in driving speed (higher standard deviation) in a
7 4 car-following scenario.
8 4
9 5

10 6 When looking at longitudinal driving behavior, safe time headway, considering the speed and
11 7 deceleration capability, is a major factor to prevent rear-end crashes. Choice of time headway is
12 8 also affected by different weather and roadway conditions. When traveling on the undivided
13 9 roadway, the participants had the smallest time headway (4.71s).
14 9
15 10

16 11 Driver behavior in foggy conditions can vary based on the fog density. In low and very low
17 12 visibilities, drivers tend to keep their distance from the leader; therefore, very high time
18 13 headways were observed. As the visibility distance increases, drivers tend to consider the leader
19 14 in their decision making process; therefore, a decrease in time headways was observed
20 15 (compared to low and very low visibilities). Note that the average time headway when visibility
21 16 is 656.2ft is less than most of other scenarios. This finding is consistent with the findings of
22 17 previous studies: drivers keep short headways (to follow visible cues) under poor visibility
23 18 conditions (Evans, 2004). Moreover, maximum time headway was found on the rolling terrain (
24 19 10.14s); this observation suggests that following a leader on a stretch of rolling terrain requires
25 20 more effort and drivers often “lose” the leader (which leads to higher average time headway).
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30 22 **5.1.2 Reactions to deceleration**

31 23

32 24 The control of longitudinal speed involves continuous information processing, situation
33 25 judgment, and decision making in response to potential hazards and critical changes in traffic
34 26 circumstances. Drivers’ expectations and predictions about the new actions of other road users
35 27 (especially the leader) are essential for a timely reaction to potential hazards. Untimely detecting
36 28 or reacting to the decelerations of the leader may result in a rear-end collision. The possibility of
37 29 an imminent crash is often expressed as Time-to-Collision (TTC), which is defined as the ratio of
38 30 the distance between the lead vehicle and the following vehicle and the speed difference between
39 31 these two vehicles. Lower values of TTC indicate higher risk of a rear-end collision. Hayward
40 32 (1972) identified 4 seconds as the critical TTC below which the crash is imminent. Brown et al.
41 33 (2001) also suggested a TTC threshold of 3 seconds.
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45 35 Moreover, in this study, the maximum deceleration that was chosen by the follower is adopted as
46 36 an indicator of drivers’ aggressiveness. Note that, in this study, the maximum deceleration applied
47 37 by the leader is 16ft/s^2 . Comparisons are made between the choices of maximum deceleration of
48 38 the follower and the leader. Among all these tests (excluding the standard scenario), the
49 39 maximum deceleration was found in undivided roads, dense fog, and rolling terrain (above
50 40 20ft/s^2). High deceleration rates indicate that drivers could not effectively adjust their behavior
51 41 according to the leader and they had to reduce their speed in a very short time. In contrast, a
52 42 much proper deceleration was applied by the follower in the cases of 9ft lane width, divided road
53 43 with Jersey barriers, and icy surface.
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58 45 Figure 5 shows the minimum TTC and maximum deceleration that drivers applied when the
59 46 leader was decelerating. Minimum TTC is 2.93s (below 3 seconds), which happened in the case
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1 of undivided Road. Furthermore, the second minimum TTC is 3.02s, which belongs to the case
2 of dense fog condition where visibility distance is just 65.62ft (following the leader without clear
3 cues may lead to the lower TTC values in poor visibility conditions).

5.1.3 Reactions to Accelerations

4 Drivers' maximum acceleration and minimum distance headway are adopted to investigate the
5 risk associate with the acceleration maneuvers. A reasonable distance gap should be maintained
6 to prevent any rear-end crash. In this study, the maximum acceleration applied by the leader is
7 5.5ft/s². Planned comparisons are made between the choices of maximum acceleration of the
8 follower and the leader. The maximum acceleration in each scenario is presented in Figure 6.
9 Among all the experiments, the maximum acceleration was observed in the undivided road
10 scenario (11.03ft/s²). This observation indicates that driving on undivided roads is challenging
11 and drivers select high acceleration and deceleration rates (based on the findings of Section
12 5.1.2) to follow the leader. The maximum accelerations under icy road surface condition and
13 under the condition where the lane is 10ft wide are relatively low (4.23ft/s² and 3.71ft/s²
14 respectively). This indicates that drivers become more conservative facing challenging road
15 conditions. Similarly, the average maximum acceleration on road without hard shoulders and on
16 road with narrower shoulders (3ft wide) is lower than the leader's average acceleration.

17 **Place Table 5**

18 **Place Figure 5**

19 In four poor visibility conditions, the maximum accelerations are 5.23ft/s² (65.62ft visibility
20 distance), 4.27ft/s² (164ft visibility distance), 4.58ft/s² (328ft visibility distance), and 5.7ft/s²
21 (656.2ft visibility distance). The values suggest that drivers are less likely to use a high
22 acceleration rates when the leader is increasing its speed, since drivers' ability to anticipate is
23 impaired in the foggy weather.

24 The minimum distance headway is also presented in Figure 6. The smallest minimum distance
25 headway occurs in "Mountainous" road scenario (25.28ft) while the largest minimum distance
26 headway was observed in the "rolling terrain" scenario. These observations suggest that the
27 distance headway increases as the roadway geometry becomes more challenging. However,
28 observations suggest that in a very challenging roadway geometry, drivers tend to focus on the
29 driving environment rather than the car-following behavior.

30 The average distance headway during these "yellow cab" acceleration instances are also
31 calculated in order to evaluate drivers tendency to follow an accelerating lead vehicle. The
32 minimum averaged distance headway was observed in "the undivided road" experiment
33 (67.69ft). The second minimum average distance headway (86.59ft) was observed in the poor
34 visibility condition. As mentioned previously, drivers tend to maintain shorter distance headways
35 in poor visibility condition. The largest average distance headway was observed on the divided
36 road with Jersey barriers.

5.2 Model Calibration

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6 2 This study adopts a genetic algorithm based optimization method to calibrate the extended
7 3 Prospect Theory based model parameters to deal with the nonlinear nature of the acceleration
8 4 model and stochasticity in drivers' choice of acceleration. The sample data that are collected
9 5 from the driving simulator to calibrate the acceleration model include the trajectories of both the
10 6 leader and the follower. More details on the calibration process can be found in Qin (2012) and
11 7 Qin and Hamdar (2013).
12 8

13 9 **Place Figure 6**

14 10 15 11 **5.2.1 Calibration Results**

16 12
17 13 76 driving experiments in total are carried out on the driving simulator during the entire study.
18 14 However, only 66 driving dynamic data sets are adopted in the calibration work. Among the 10
19 15 excluded experiments, there were 3 overtaking behavior: one in the standard scenario and
20 16 another two in the undivided road scenarios. Four road edge excursions occurred: two on 9ft
21 17 wide traveling lane, one on 10ft traveling lane and one on the road with a narrower shoulder of
22 18 3ft. In addition, three rear-end collisions happened in the cases of mountainous areas, rolling
23 19 terrain and heavy foggy condition (65.62ft visibility distance). Out of 66 remaining data sets,
24 20 only 44 sets were kept after calibration. These sets satisfy the maximum error threshold of 33%
25 21 (Qin, 2012; Qin and Hamdar, 2013). The resulting calibrated nine parameters (ψ , γ , w^- , w_c , τ_{max} ,
26 22 α , β , τ_{corr} and RT) are analyzed by means of multivariate analysis of variance (MANOVA).
27 23 Accordingly, to reach statistically significant conclusions using the remaining 44 sets, results
28 24 obtained from the 15 different test scenarios are regrouped into three major groups:

- 29 25 1. Normal Conditions (NC) including the scenarios of standard scenario, Jersey barrier,
30 26 undivided road and rolling terrain;
- 31 27 2. Moderate Conditions (MC - moderately challenging conditions) including the scenarios
32 28 of 10ft lane width, 3ft shoulder width, wet road surface, 656.2ft visibility distance and
33 29 328ft visibility distance;
- 34 30 3. Extreme Conditions (EC - extremely challenging roadway conditions) including the
35 31 scenarios of 65.62ft visibility distance, 164ft visibility distance, mountainous areas, icy
36 32 road surface, 9ft lane and road without hard shoulders.

37 33 Table 6 shows the three different driving conditions, in which the sample numbers are 11, 14 and
38 34 19 respectively. Figure 7 shows two examples of acceleration behaviors under different driving
39 35 conditions (moderate and extreme). This figure (7a and 7b) reveals that in moderate condition,
40 36 drivers use anticipation to provide a comfortable driving experience and avoid extreme
41 37 acceleration/deceleration values. Such extreme acceleration/deceleration rates are seen (even if
42 38 not frequently) in extremely challenging conditions. This finding does not mean however that the
43 39 acceleration distribution does not have a clear peak in extremely challenging conditions. As it
44 40 can be seen in Figures 7c and 7d, the moderately challenging conditions provide a less elaborate
45 41 peak and a "wider" distribution especially around the mean value. Actually, if looking at the
46 42 "peak" value, the acceleration value during moderately challenging conditions is greater than the
47 43 acceleration value in the extremely challenging conditions. However, this decrease in acceleration
48 44 rates used should not be explained as an increase in safety in extremely challenging conditions. Table 7
49 45 presents the calibration results for all three cases of normal, moderate, and extreme driving
50 46 conditions.
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6 2 **Place Table 6**

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8 4 **Place Figure 7**

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10 6 **5.3 MANOVA Test**

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12 8 In this section, the multivariate analysis of variance (MANOVA) of all 9 parameters is presented.
13 9 The MANOVA test is applied to explore how independent variables (IVs, the changes of
14 10 external factors) influence the response of the dependent variables (DVs, the changes of the 9
15 11 parameters in each condition). The test results reveal the statistically important independent and
16 12 dependent variables.

17 13
18 14 Since we are interested in understanding the similarities and differences between the three
19 15 different groups, the following hypotheses are considered,

- 20 16
21 17
 - 22 18 • Homogeneous variance and covariance matrix (note that the result of Box's Test ($p =$
23 19 0.163) for the covariance and Levene's Test for the variance indicate that these
24 20 hypotheses cannot be rejected. For more detail see Qin and Hamdar, 2013),
 - 25 21 • The dependent variables are normally distributed within groups.

26 22 The data structure of the MANOVA test is showed in the table 8, some of the calculations
27 23 involved in the MANOVA test are also listed as follows:

28 32
29 33
30 34 Level Mean
$$\bar{x}_i = \frac{1}{n} \sum_{j=1}^9 x_{ij} \quad (5.1)$$

31 35
32 36
33 37
34 38
35 39 Grand Mean
$$\bar{x} = \frac{\sum_{i=1}^3 \sum_{j=1}^9 x_{ij}}{\sum_{i=1}^3 n_i} \quad (5.2)$$

36 40
37 41
38 42 Sum of Squares for Total
$$SST = \sum_{i=1}^3 \sum_{j=1}^9 (x_{ij} - \bar{x})^2 \quad (5.3)$$

39 43
40 44
41 45 Sum of Squares for Error
$$SST = \sum_{i=1}^3 \sum_{j=1}^9 (x_{ij} - \bar{x}_i)^2 \quad (5.4)$$

42 46
43 47
44 48 Sum of Squares for Factor A
$$SSA = \sum_{i=1}^3 n_i (x_i - \bar{x})^2 \quad (5.5)$$

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50 54 The statistics of Multivariate Tests are calculated using SPSS. Table 9 shows the results of the
51 55 MANOVA test. The results reveal that the values of dependent variables significantly depend on
52 56 which test scenario. In other words, there exists a statistically significant difference between the
53 57 values of dependent variables under different conditions and external factors affecting the
54 58 extended Prospect Theory based model parameters. Meanwhile, these tests further prove that the
55 59 changes in the values of those dependent variables can be regarded as mainly caused by the
56 60

1 control factors in the driving experiments and the influences from stochastic factors during the
2 experiments can be excluded.

3
4 To determine how the dependent variables differ for each independent variable, Tukey's HSD
5 post-hoc test is performed. Table 10 shows the results of this test. Note that in this table NC, MC,
6 and EC represent Normal Condition, Moderate Condition, and Extreme Condition, respectively.
7 The major findings from the statistics presented in this table are as follows,

- 8 1. Mean Ψ (ψ) are statistically significantly different between Extreme Conditions &
9 Moderate Conditions ($p=0.80$),
- 10 2. Mean W_c (w^-) are statistically significantly different between Normal Conditions &
11 Moderate Road Conditions ($p=0.098$), and Normal Conditions & Extreme Conditions
12 with ($p=.005$),
- 13 3. Mean τ_{corr} are statistically significantly different between Moderate Conditions &
14 Extreme Conditions ($p=0.092$).

15
16
17 **Place Table 7**

18 19 **5.4 Parametric Framing during Different Weather/Geometry Conditions**

20
21 Before presenting the experimental design and the corresponding numerical results, different
22 hypotheses may be suggested within the modeling framework presented earlier. Such hypotheses
23 are related to the possible impact of the challenges faced during inclement weather conditions
24 and non-favorable roadway characteristics on some of the models' parameters defined and
25 calibrated in the previous sections.

26
27 In favorable weather conditions, drivers use smoother acceleration rates (less extreme with less
28 elaborate peak) to reach a desired speed (see Figure 7). In contrast, in unfavorable weather
29 conditions (e.g., poor visibility condition and slippery road surfaces), drivers sometimes resort to
30 abrupt and wider acceleration/deceleration choices in response to the challenging surrounding
31 environment. Accordingly, the parameter ψ is introduced in Equation 3.2 to characterize the
32 impact of weather on drivers' perceptions [of the driving environment. For illustration reasons,
33 Figures 8a shows three value functions representing three different weather conditions utilizing
34 different ψ values (called amplitude term). This figure reveals lower sensitivity to the
35 acceleration/deceleration values at higher values of ψ (which can be interpreted as wider
36 acceleration choices). Therefore, higher values of this parameter are expected for more
37 challenging roadway geometries, which is confirmed by the statistically significant calibration
38 results (compare the parameter values for moderate and extreme conditions in Table 7). Figure
39 8e reveals the models' capability of capturing drivers' wider acceleration/deceleration choices at
40 higher values of ψ .

41
42 Drivers predict the road geometrical configuration and regulate the speed and acceleration based
43 on their subjective expectation about the geometric features of the upcoming road sections.
44 When traveling on a road with a challenging geometry (e.g. a road section where a horizontal or
45 vertical curve exists, or when the travel lane or the hard shoulder is narrower than the normal
46 width), drivers need to invest more efforts to deal with the changes in geometry. Therefore, they

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4 1 are more likely to avoid high acceleration/deceleration rates and their expectations in gains may
5 2 increase. Accordingly, the parameter γ is introduced in Equation 3.2 to capture the effects of
6 3 roadway geometry on drivers' acceleration choices. Figure 8b shows three value functions
7 4 representing three different roadway geometries utilizing different γ values (called frequency
8 5 term). This figure reveals lower sensitivity to the acceleration/deceleration values at higher
9 6 values of γ (which can be interpreted as wider acceleration choices). Therefore, lower values of
10 7 this parameter is expected for more challenging roadway geometries, which is confirmed by the
11 8 calibration results (see Table 7). Figure 8f reveals the models' capability of capturing drivers'
12 9 narrower acceleration/deceleration choices at lower values of γ .

13 10
14 11 **Place Table 8**

15 12
16 13 **Place Table 9**

17 14
18 15 **Place Table 10**

19 16
20 17 Note that since drivers can anticipate the changes in roadway geometry and adjust their driving
21 18 behavior in advance accordingly, the effects of roadway geometry on driver behavior is more
22 19 limited compare to challenging weather conditions (in which drivers' anticipation ability is very
23 20 limited due to, for instance, the lack of visibility). This observation is also reflected in the
24 21 calibration results where calibrated γ values are not statistically different between normal,
25 22 moderate, and extreme weather conditions, whereas calibrated ψ values are statistically different
26 23 (see Table 10) between extreme and moderate conditions. This observation is in agreement with
27 24 observations of Ibrahim and Hall (1994), Broughton et al. (2007), McLean (1981), and
28 25 Heimbach et al. (1983).

29 26
30 27 Note that the ψ parameter in the normal conditions (NC) is not statistically different from ψ
31 28 parameter in the moderately challenging conditions (MC). Accordingly, the authors may
32 29 hypothesize that some level of weather related challenges may bring enough alert to smoothen
33 30 traffic (less elaborate peak with no extreme accelerations/decelerations) compared to the normal
34 31 conditions (with a self-confidence expressed by the drivers in normal conditions that may lead to
35 32 further disruption and less safe conditions). However, when the challenge is increased, the peak
36 33 of the distribution become more elaborate while extreme acceleration values are used (seen in the
37 34 change in the values of ψ) leading to less safe conditions (even if lower acceleration rates on
38 35 average are used). Even though such hypothesis is feasible, some caution is needed before fully
39 36 supporting it. For such purpose, additional data may need to be collected.

40 37
41 38 **Place Figure 8**

42 39 **5.5 Model Performance**

43 40
44 41 In this section, driver behavior under different roadway and weather conditions (i.e. normal,
45 42 moderate, and extreme conditions) is investigated through a set of simulations. A hypothetical
46 43 one-lane highway with an on-ramp (to produce disturbance in driving environment) is selected
47 44 for conducting simulations. The highway inflow rate is started from zero and increased until a
48 45 flow drop is observed in the merging section. After this point, the inflow rate is kept at flow drop
49 46 point until the end of the simulation. The ramp, however, has a constant inflow rate of 90 veh/hr.
50 47

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4 1 The maximum speed during the simulation is set based on the observed loop detector data in the
5 2 east-bound direction of I-290 near Chicago, IL in different roadway and weather conditions.
6 3 Specifically, the average speed is calculated during morning peak hours (7AM to 10AM) for a
7 4 day with heavy snow (representing an extreme condition), a day with low visibility (representing
8 5 a moderate condition), and a clear day (representing a normal condition). Based on these
9 6 observations, the maximum speed for the extreme conditions is set to 14 m/s, while the average
10 7 speeds for the moderate and normal conditions are set to 18 m/s and 21 m/s, respectively. Note
11 8 that through comparison of the fundamental diagrams for different weather conditions, the
12 9 performance of the microscopic model can be evaluated.

13 10
14 11 Figure 9 presents the simulation results for the first set of simulations. It is clear from this figure
15 12 that scatter in fundamental diagram increases as the roadway and weather conditions shift from
16 13 normal to extreme. Interestingly enough, the breakdown flow in all three roadway and weather
17 14 conditions is around 1800 veh/hr. However, despite similar breakdown flows, the breakdown
18 15 densities vary across different roadway and weather conditions. The highest breakdown density
19 16 is observed during the extreme condition and the lowest breakdown density is observed during
20 17 the normal condition. The difference in breakdown densities is mainly due to the difference in
21 18 maximum speeds and different slopes in the uncongested part of fundamental diagrams (compare
22 19 14 m/s for the extreme condition with 21 m/s for the normal condition).

23 20
24 21 Note that the presented results from both sets of simulations are in agreement with the real-world
25 22 observations where disturbances in driving condition have less influence on driving behavior in
26 23 normal roadway and weather conditions compare to extreme weather conditions. Moreover,
27 24 based on the calibrated parameter values, it is noticed that the parameter Ψ will increase when
28 25 the weather conditions get worse and the parameter γ will decrease when the road conditions get
29 26 worse. Through the series of driving experiment conducted, and the subsequent parameter
30 27 calibration, the hypotheses proposed in the Prospect Theory based model formulation part were
31 28 found to be valid. Therefore, it can be concluded that the extended Prospect Theory based
32 29 acceleration model's cognitive architecture are capable of jointly capturing the impact of two
33 30 main types of external driving factors: the weather-related factors (visibility distances and road
34 31 surface frictions), and the road-related factors (driving on undivided/divided road, lane width,
35 32 shoulder width, horizontal and vertical curvature).

36 33 37 34 **6.0 CONCLUSIONS AND FUTURE RESEARCH NEEDS**

38 35
39 36 This study characterizes the longitudinal driving behavior under different road-geometry and
40 37 weather conditions, as two factors that significantly affect congestion and safety in transportation
41 38 systems. A prospect theory based car-following model of Hamdar et al. (2008) is extended to
42 39 capture the behavioral dynamics resulting from these external factors. In order to test the
43 40 proposed expanded model, 15 driving experiments are designed and carried out using the
44 41 STISIM Drive simulator software. Throughout the test, 66 effective results are collected. The 66
45 42 car-following experiments conducted by 36 drivers are then used to calibrate the model using a
46 43 Genetic Algorithm. Based on the calibration results, the model performance and the features of
47 44 longitudinal driving behavior are discussed.

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4 1 The outcomes of the driving experiments are in accordance with the real-world observations. It is
5 2 found that the overall drivers' average speed, time headway, time to collision, and distance
6 3 headway are affected by both the roadway-related factors (lane width, shoulder width, median
7 4 existence, median type, horizontal curves and vertical curves) and weather related factors (foggy
8 5 weather and icy and wet road surface conditions). It has been confirmed that undivided road
9 6 causes drivers to adopt an aggressive driving strategy (less safety margins - like time headway,
10 7 large acceleration or deceleration are observed). Conversely, traveling on the divided road,
11 8 drivers adopt less aggressive behavior. The narrower lanes are also found to be one of the
12 9 influential factors that impact drivers driving style when following a leader. The most extreme
13 10 case of 9ft traveling lane increases the distance with the leader compared to the normal case.
14 11 Drivers driving on a road without hard shoulders are less likely to follow the leader at a
15 12 dangerously close distance. Inadequate visibility distance is also found to influence driving
16 13 behavior. Low visibility cause drivers to increase their distance with the leader, while in higher
17 14 visibility drivers tend to follow the leader more closely. It is evident that driving on slippery road
18 15 surfaces are much challenging and drivers become much vigilant. No apparent defensive or
19 16 aggressive driving styles are observed when driving in mountainous areas (horizontal curves and
20 17 vertical curves) and rolling terrains (vertical curves).
21 18

22 19 From the modeling perspective, Prospect Theory based acceleration model's cognitive
23 20 architecture distinguishes two main types of information corresponding to different value
24 21 functions: the weather-related information (visibility distances and road surface frictions), and
25 22 the road-related information (driving on undivided/divided road, lane width, shoulder width,
26 23 horizontal and vertical curvature). It is observed that parameters ψ , reflecting external weather
27 24 impact, increases as weather condition gets worse. On the other hand, γ , reflecting external road
28 25 impact, decreases when road condition gets worse. $W_c(w_c)$, which represents differences in
29 26 drivers' safety attitude or crash sensitivity with respect to the leader's speed estimations and
30 27 acceleration selections, is found to follow a decreasing pattern as the external driving
31 28 environment gets challenging. This finding indicates that drivers become more aggressive in
32 29 dealing with challenging roadway and weather conditions. Psychologically, drivers tend to
33 30 underestimate the losses caused by a rear-end collision under extreme conditions and
34 31 overestimate the crash losses when traveling under normal conditions. Finally, the simulation of
35 32 a real-world segment indicated the models capability of simulating driver behavior under
36 33 different roadway and weather conditions.
37 34

38 35 Note that extending the findings of this study to multilane highways with higher congestion level
39 36 while accounting for socio-demographic characteristics of drivers in their decision-making
40 37 constitute a future research direction to be adopted by the authors.
41 38

42 39 **Place Figure 9**
43 40

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4 1 are those of the author(s) and do not necessarily reflect the views of the National Science
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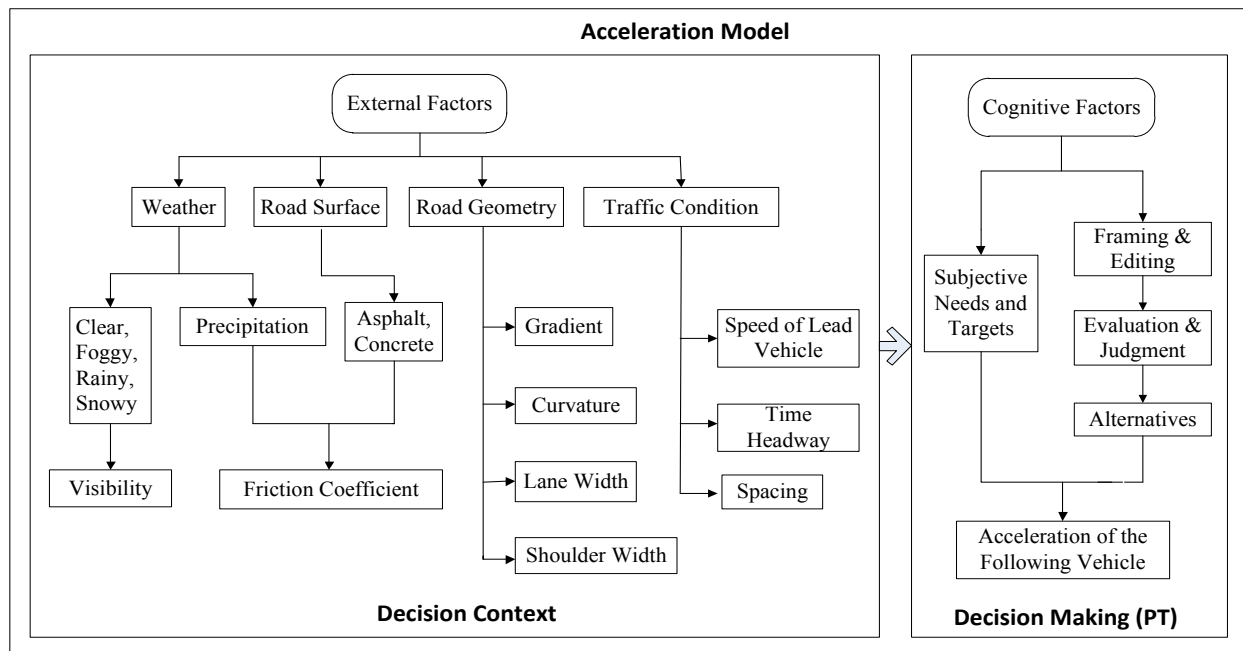
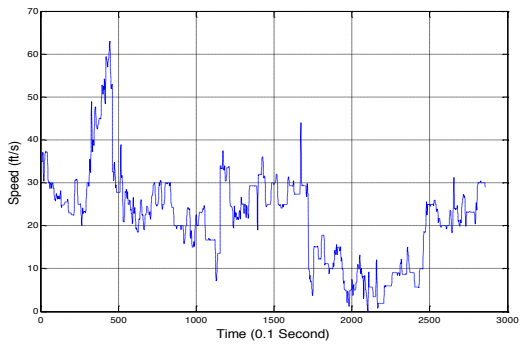
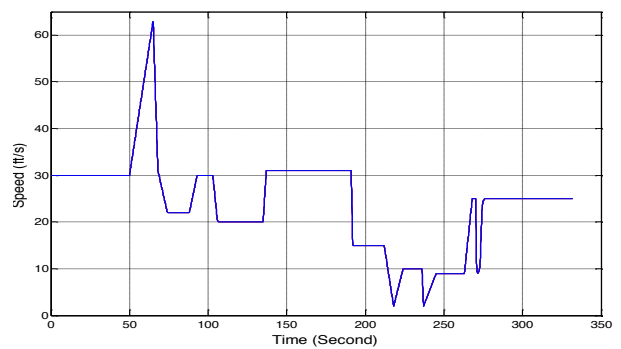


Figure 1 Schematic of Prospect Theory Based Acceleration Model.

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(b)

Figure 2 (a) Raw Data of Speed Profile Selected for the Lead Vehicle Based on NGSIM Data (FHWA, 2005), (b) Speed Profile of the Lead Vehicle Defined in the Driving Simulator.

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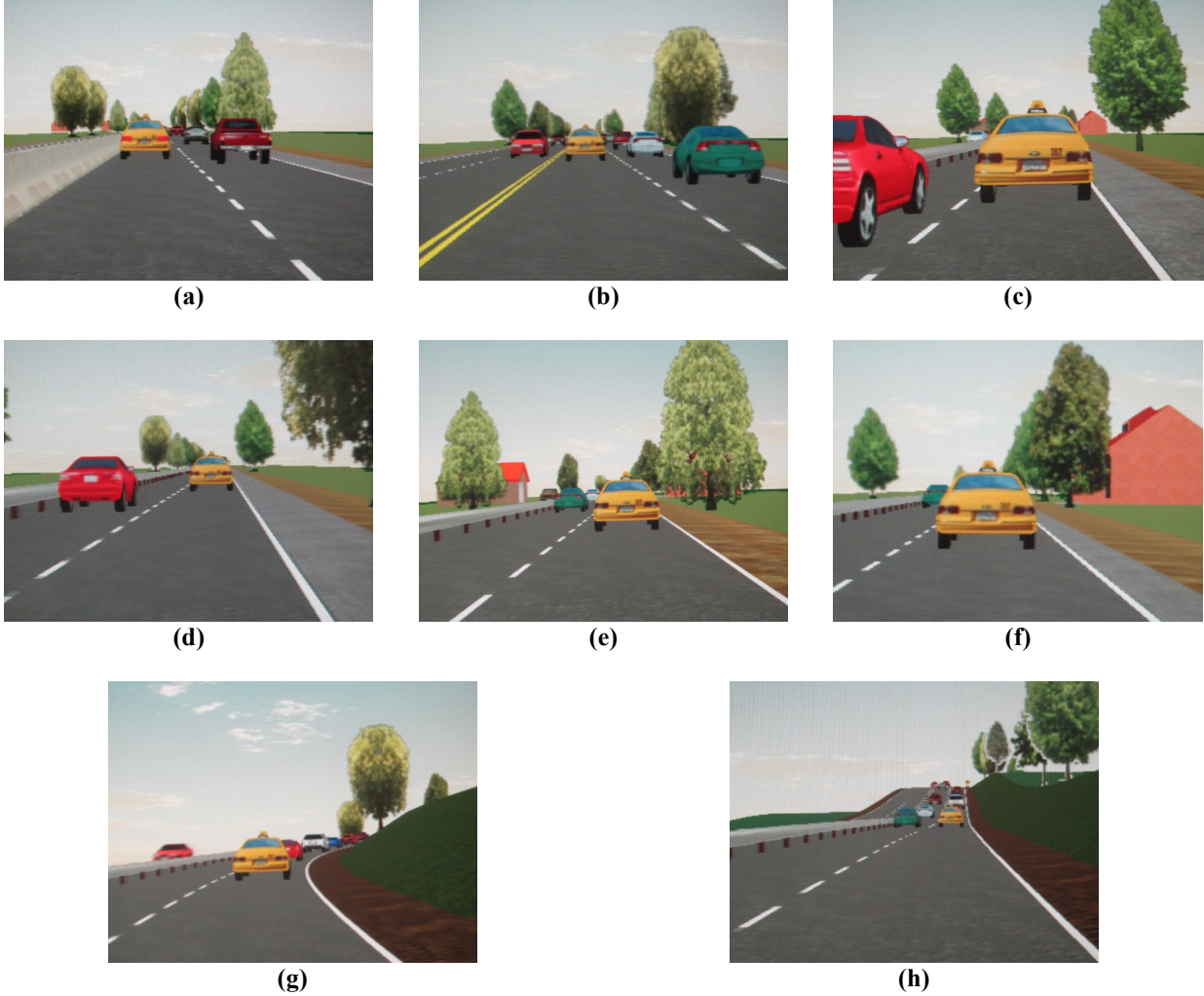


Figure 3 (a) Jersey Barrier, (b) Undivided Road, (c) 9ft Wide Lane with Metal Barrier, (d) 10ft Wide Lane with Metal Barrier, (e) No Hard Shoulders, (f) 3ft Wide Hard Shoulder, (g) Mountainous Terrain, and (h) Rolling Terrain.

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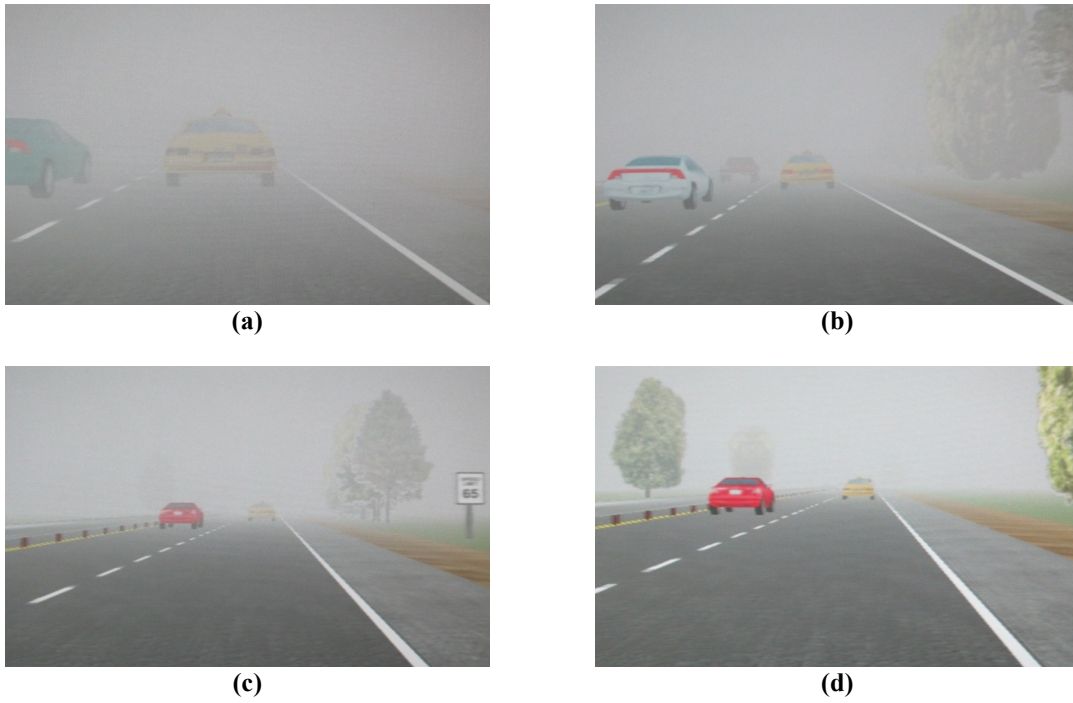


Figure 4 Visibility Distance (a) 65.62ft, (b) 164ft, (c) 328ft, and (d) 656.2ft.

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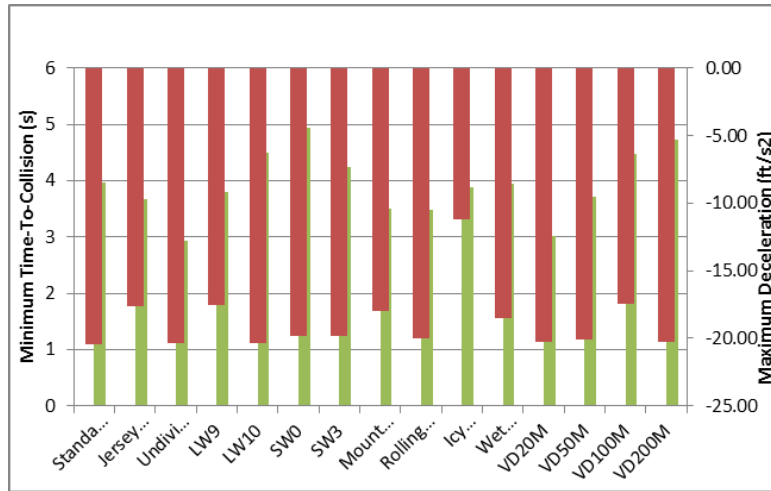


Figure 5 Minimum Time-To-Collision and Maximum Deceleration of the Follower.

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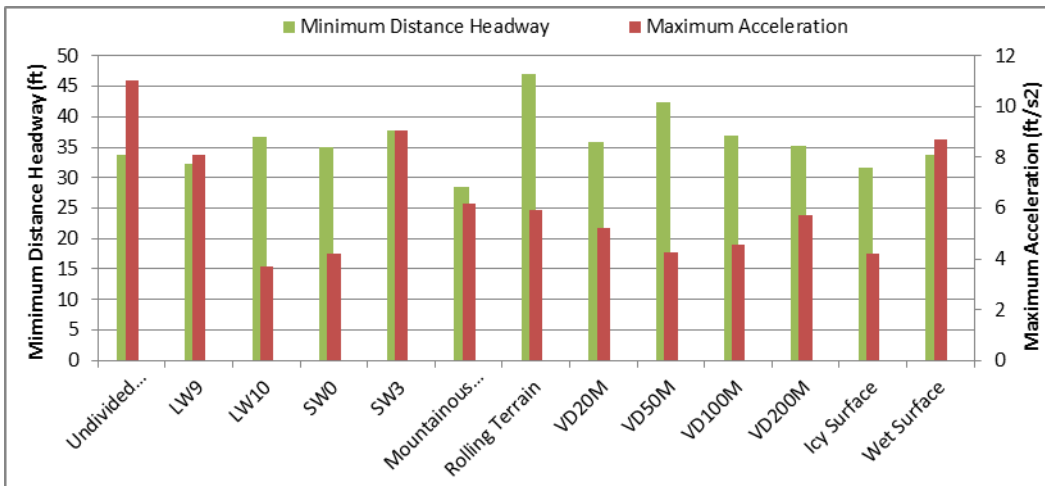


Figure 6 Maximum Acceleration and Minimum Distance Headway of the Follower.

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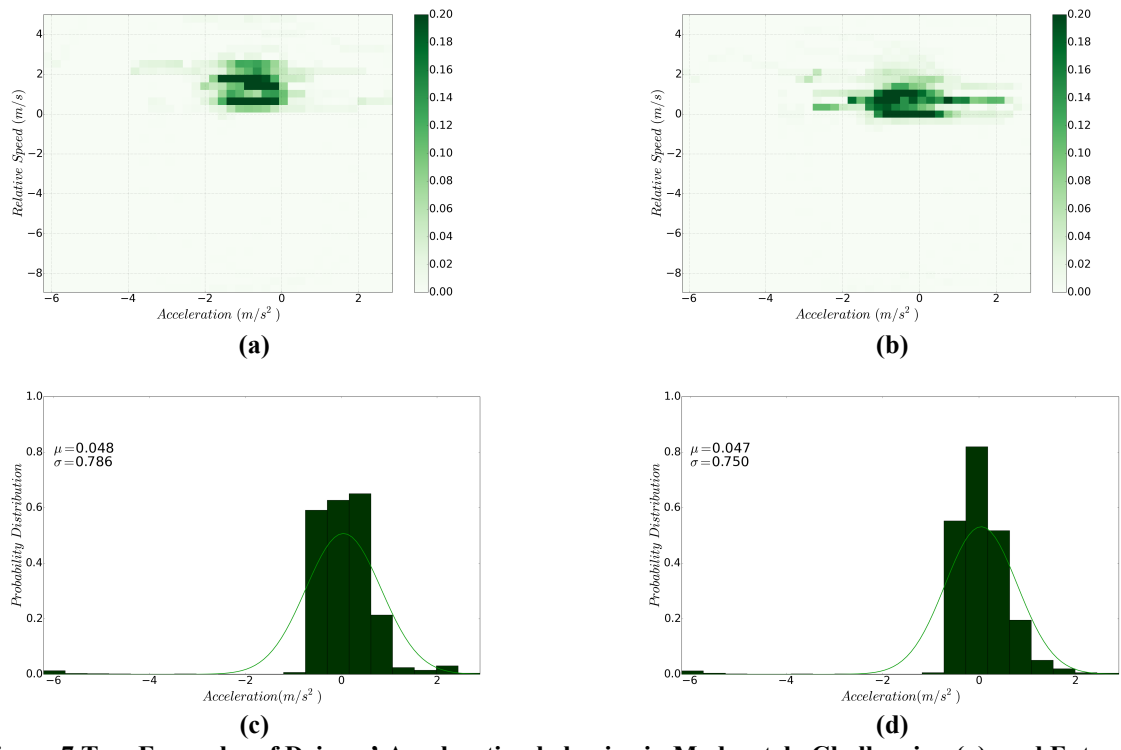
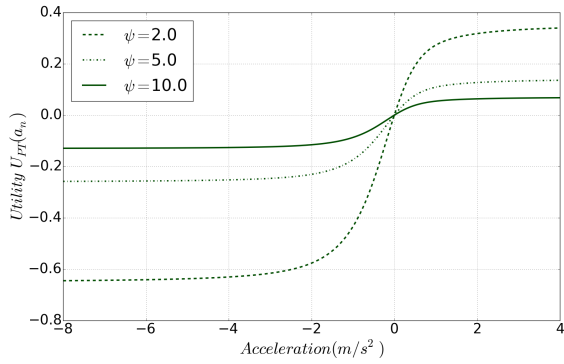
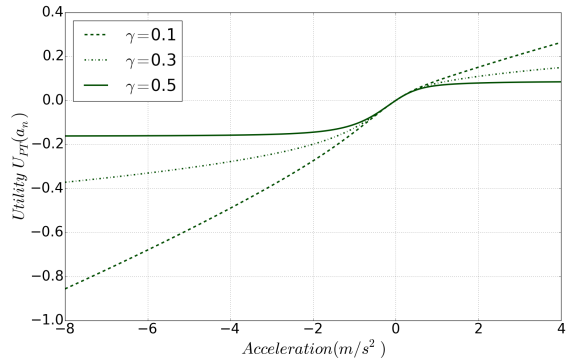


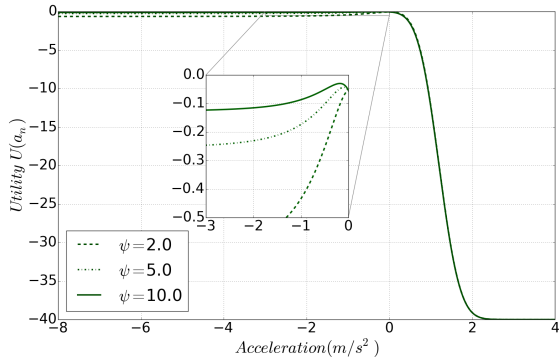
Figure 7 Two Examples of Drivers' Acceleration behavior in Moderately Challenging (a), and Extremely Challenging (b) driving conditions.



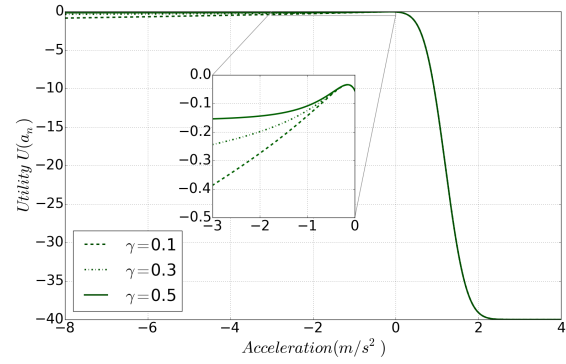
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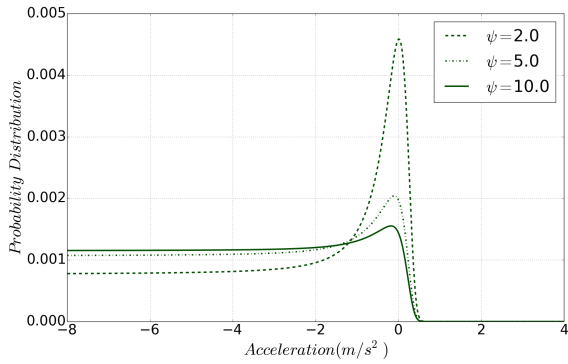
(b)



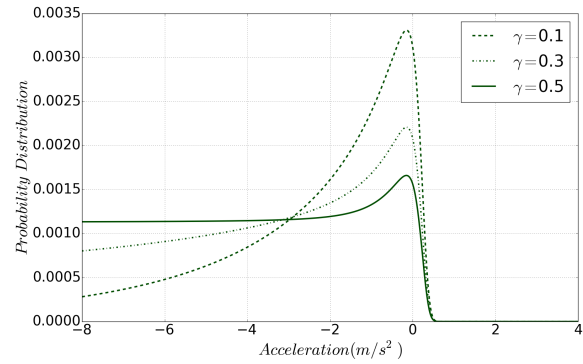
(c)



(d)



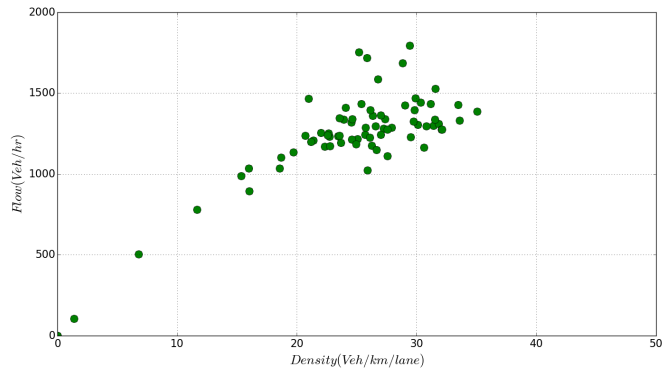
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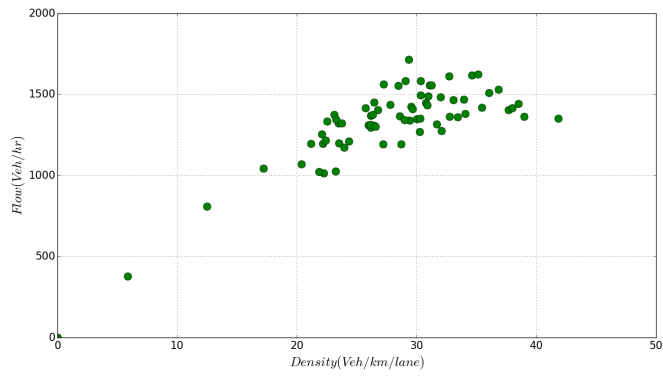
(f)

1 **Figure 8 (a) Value Functions (Equation 3.2) for Different Values of ψ , (b) Value Functions (Equation 3.2) for**
 2 **Different Values of γ , (c) Utility Functions (Equation 3.3) for Different Values of ψ and (d) Utility Functions**
 3 **(Equation 3.3) for Different Values of γ , (e) Probability Density Functions (Equation 3.4) for Different Values**
 4 **of ψ and (f) Probability Density Functions (Equation 3.4) for Different Values of γ .**

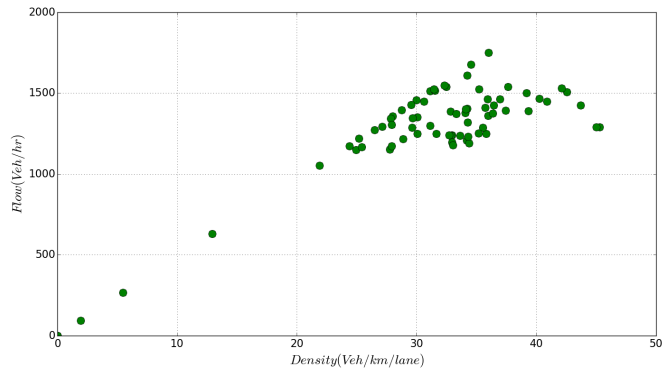
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(a)



(b)



(c)

Figure 9 Simulated Flow Density Diagrams Based on the Average Calibrated Acceleration Model Parameters in Normal (a), Moderately Challenging (b), and Challenging (c) Driving Conditions.

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Table 1 Main Events Used in the Driving Experiments

Event Abbreviation	Event	Event Description
A	Approaching Vehicle	Define oncoming traffic
V	Following Vehicle	Define traffic in the direction of the driver
BLDG	Buildings	Display buildings
BSAV	Dynamic Data	Begin saving dynamic data for the output file
R	Road	Display a specific roadway
C	Road Horizontal Curve	Add horizontal curves at desired location with desired length, curvature, and radius
VC	Road Vertical Curve	Add vertical curves at desired location with desired length, curvature, and radius
ES	End Simulation	Call the simulation to stop
JBAR	Jersey Barrier	Add desired barriers as the road median
FOG	Fog	Add a patch of fog to simulation scene
SIGN	Traffic Sign	Display a roadway sign
TREE	Trees	Display trees on the side of the road
RSA	Road Surface Attributes	Change the current road surface attributes

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Table 2 Length of Horizontal Curve Section.

Radius	$\alpha_1=10$ degree	$\alpha_2=20$ degree	$\alpha_3=30$ degree
984ft (300 m)	172ft	345ft	515ft
1968ft (600 m)	344ft	687ft	1030ft
3281ft (1000 m)	572ft	1145ft	1716ft

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Table 3 Design of Vertical Curve Sections.

Type	Stop Sight Distance (ft)	Upgrade	Downgrade	Vertical Curve Length (ft)
Simple Upgrade I	-	3%	-	500
Simple Upgrade II	-	4%	-	300
Simple Upgrade III	-	5%	-	200
Simple Downgrade I	-	-	-3%	500
Simple Downgrade II	-	-	-4%	300
Simple Downgrade III	-	-	-5%	200
Curve I	150	4%	-4%	134
Curve II	400	4%	-4%	963
Curve III	400	4%	-4%	843

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Table 4 Test Variables in Each Driving Scenario.

External Factors	Items	Specification		
<i>Road Geometry</i>	<i>Median</i>	10ft long, 2ft wide, 3ft high concrete barrier		
		10ft long, 1.5ft wide and 1.5ft metal barrier		
	Undivided Road (Double Solid Yellow Line)			
	<i>Lane Width (LW)</i>	LW = 9ft		
		LW = 10ft		
	<i>Shoulder Width (SW)</i>	SW = 0ft		
		SW = 3ft		
	<i>Mountainous Area</i>	HC = 172ft		VC = 134ft
		HC = 344ft		VC = 200ft
		HC = 515ft		VC = 300ft
		HC = 345ft		VC = 500ft
		HC = 687ft		
HC = 1716ft				
<i>Rolling Terrain</i>	HC = 572ft		VC = 500ft	
	HC = 1030ft		VC = 963ft	
	HC = 1145ft		VC = 843ft	
<i>Weather</i>	<i>Visibility Distance (VD)</i>	VD = 65.62ft		
		VD = 164ft		
		VD = 328ft		
		VD = 656.2ft		
	<i>Friction Coefficient (FC)</i>	FC = 0.2 (icy condition)		
FC = 0.4 (wet condition)				

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Table 5 Driving Simulator Output.

External Factors	Specification	Driver Performance					
		V _{ave}	StdV	DeltaV _{ave}	StdDeltaV	TH _{ave}	StdTH
Roadway Layouts	Standard Scenario	23.87	10.10	-2.78	12.00	4.92	6.95
	Jersey Barrier	24.06	10.68	-0.01	9.39	8.26	7.73
	Undivided Road	24.22	10.66	-0.14	7.24	4.72	6.58
	LW=9ft	23.92	11.16	-0.25	9.80	6.02	7.54
	LW=10ft	24.08	10.57	-0.06	8.14	6.17	9.06
	SW=0ft	23.89	10.20	-0.08	7.80	6.28	7.22
	SW=3ft	23.73	11.35	-0.10	10.77	9.42	18.10
	Mountainous	24.07	9.90	0.16	7.39	4.05	6.86
	Rolling Terrain	24.29	10.79	-0.09	9.00	10.14	8.46
Weather	VD=65.62ft	24.19	11.24	-0.34	9.80	8.07	7.98
	VD=164ft	24.00	11.01	-0.23	9.25	6.53	6.70
	VD=328ft	24.20	10.04	0.01	9.03	6.27	6.71
	VD=656.2ft	24.44	10.60	-0.04	7.88	5.46	7.19
	Wet Surface	23.94	10.31	-0.14	7.84	6.10	6.62
	Icy Surface	23.82	10.25	-0.21	7.87	5.68	6.93

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Table 6 Experiment Sample

Case	Value Label	N
1	Normal Conditions	11
2	Moderate Conditions	14
3	Extreme Conditions	19

Table 7 Descriptive Statistics of the Calibrated Parameters of the Extended Prospect Theory Based Acceleration Model

Parameters	Case	Mean	Std. Deviation
$\Psi (\psi)$	Normal Conditions	8.00	2.75
	Moderate Conditions	6.54	3.26
	Extreme Conditions	9.07	3.48
	Total	7.87	3.35
γ	Normal Conditions	0.16	0.08
	Moderate Conditions	0.14	0.11
	Extreme Conditions	0.14	0.08
	Total	0.15	0.09
$W_m (w^-)$	Normal Conditions	5.67	3.76
	Moderate Conditions	6.67	3.97
	Extreme Conditions	7.22	3.27
	Total	6.66	3.59
$W_c (w_c)$	Normal Conditions	97181.82	26407.64
	Moderate Conditions	78071.43	21585.12
	Extreme Conditions	69052.63	20416.42
	Total	78954.55	24618.91
α	Normal Conditions	0.14	0.20
	Moderate Conditions	0.08	0.12
	Extreme Conditions	0.07	0.08
	Total	0.09	0.13
β	Normal Conditions	5.52	2.66
	Moderate Conditions	7.38	3.22
	Extreme Conditions	5.67	3.51
	Total	6.18	3.26
τ_{max}	Normal Conditions	6.01	1.94
	Moderate Conditions	7.13	2.35
	Extreme Conditions	6.81	1.99
	Total	6.71	2.09
τ_{corr}	Normal Conditions	21.91	6.38
	Moderate Conditions	17.79	3.95
	Extreme Conditions	21.74	5.29
	Total	20.52	5.43
RT	Normal Conditions	1.09	0.92
	Moderate Conditions	1.45	0.73
	Extreme Conditions	1.40	0.85
	Total	1.34	0.82

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Table 8 Data Sample of MANOVA Test

Case	Parameters				Mean
	DV ₁	DV ₂	...	DV ₉	
IV ₁	x_{11}	x_{12}	...	x_{19}	\bar{x}_1
IV ₂	x_{21}	x_{22}	...	x_{29}	\bar{x}_2
IV ₃	x_{31}	x_{32}	...	x_{33}	\bar{x}_3
Mean	\bar{x}_1	\bar{x}_2	...	\bar{x}_9	\bar{x}

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Table 9 Multivariate Tests

Effect	Value	F	Hypo. df	Error df	<i>p</i>-value
Pillai's Trace	.791	2.473	18	68.000	.004
Wilks' Lambda	.350	2.531b	18	66.000	.003
Hotelling's Trace	1.453	2.584	18	64.000	.003
Roy's Largest Root	1.079	4.078c	9	34.000	.001

Table 10 Cross Comparison of Dependent and Independent Variables.

DV _s	(I) Case	(J) Case	Mean Difference (I-J)	Std. Error	p-value	95% Confidence Interval	
						Lower Bound	Upper Bound
ψ (ψ)	NC	MC	1.4643	1.3074	0.5070	-1.7149	4.6435
	NC	EC	-1.0684	1.2294	0.6630	-4.0579	1.9211
	MC	EC	-2.5327	1.1429	0.0800	-5.3119	0.2465
γ	NC	MC	0.0279	0.0369	0.7310	-0.0618	0.1177
	NC	EC	0.0215	0.0347	0.8100	-0.0628	0.1059
	MC	EC	-0.0064	0.0323	0.9790	-0.0848	0.0721
W_m (w^-)	NC	MC	-0.9987	1.4597	0.7740	-4.5483	2.5509
	NC	EC	-1.5483	1.3726	0.5030	-4.8861	1.7894
	MC	EC	-0.5496	1.2761	0.9030	-3.6526	2.5534
W_c (w_c)	NC	MC	19110.3896	9016.7356	0.0980	-2815.1637	41035.9429
	NC	EC	28129.1866	8478.6592	0.0050	7512.0474	48746.3258
	MC	EC	9018.7970	7882.3524	0.4930	-10148.3322	28185.9262
α	NC	MC	0.0573	0.0538	0.5420	-0.0736	0.1882
	NC	EC	0.0657	0.0506	0.4050	-0.0574	0.1888
	MC	EC	0.0084	0.0471	0.9830	-0.1060	0.1229
β	NC	MC	-1.8604	1.3009	0.3350	-5.0238	1.3030
	NC	EC	-0.1502	1.2233	0.9920	-3.1249	2.8244
	MC	EC	1.7102	1.1373	0.3000	-1.0553	4.4756
τ_{max}	NC	MC	-1.1195	0.8456	0.3900	-3.1758	0.9368
	NC	EC	-0.7962	0.7952	0.5800	-2.7298	1.1374
	MC	EC	0.3233	0.7393	0.9000	-1.4743	2.1209
τ_{corr}	NC	MC	4.1234	2.0992	0.1340	-0.9812	9.2279
	NC	EC	0.1722	1.9739	0.9960	-4.6277	4.9722
	MC	EC	-3.9511	1.8351	0.0920	-8.4135	0.5112
RT	NC	MC	-0.3591	0.3347	0.5360	-1.1728	0.4547
	NC	EC	-0.3091	0.3147	0.5920	-1.0743	0.4561
	MC	EC	0.0500	0.2926	0.9840	-0.6614	0.7614