# White dwarf-main sequence binaries from LAMOST: the DR5 catalogue

J.-J. Ren,<sup>1\*</sup> A. Rebassa-Mansergas,<sup>2,3</sup> S. G. Parsons,<sup>4</sup> X.-W. Liu,<sup>5</sup> A.-L. Luo,<sup>1</sup> X. Kong,<sup>1,6</sup> H.-T. Zhang<sup>1</sup> <sup>1</sup>Key Laboratory of Optical Astronomy, National Astronomical Observatories, Chinese Academy of Sciences, Beijing 100012, P. R. China

<sup>2</sup>Departament de Física, Universitat Politècnica de Catalunya, c/Esteve Terrades 5, E-08860 Castelldefels, Spain

<sup>3</sup>Institute for Space Studies of Catalonia, c/Gran Capità 2-4, Edif. Nexus 201, 08034 Barcelona, Spain

<sup>4</sup>Department of Physics and Astronomy, University of Sheffield, Sheffield S3 7RH, UK

<sup>5</sup>South-Western Institute for Astronomy Research, Yunnan University, Kunming, Yunnan 650091, P. R. China

<sup>6</sup> University of Chinese Academy of Sciences, Beijing 10049, P. R. China

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#### ABSTRACT

We present the data release (DR) 5 catalogue of white dwarf-main sequence (WDMS) binaries from the Large Area Multi-Object fiber Spectroscopic Telescope (LAMOST). The catalogue contains 876 WDMS binaries, of which 757 are additions to our previous LAMOST DR1 sample and 357 are systems that have not been published before. We also describe a LAMOST-dedicated survey that aims at obtaining spectra of photometrically-selected WDMS binaries from the Sloan Digital Sky Survey (SDSS) that are expected to contain cool white dwarfs and/or early type M dwarf companions. This is a population under-represented in previous SDSS WDMS binary catalogues. We determine the stellar parameters (white dwarf effective temperatures, surface gravities and masses, and M dwarf spectral types) of the LAMOST DR5 WDMS binaries and make use of the parameter distributions to analyse the properties of the sample. We find that, despite our efforts, systems containing cool white dwarfs remain under-represented. Moreover, we make use of LAMOST DR5 and SDSS DR14 (when available) spectra to measure the Na  $\lambda\lambda$  8183.27,8194.81 absorption doublet and/or  $H\alpha$  emission radial velocities of our systems. This allows identifying 128 binaries displaying significant radial velocity variations, 76 of which are new. Finally, we crossmatch our catalogue with the Catalina Surveys and identify 57 systems displaying light curve variations. These include 16 eclipsing systems, two of which are new, and nine binaries that are new eclipsing candidates. We calculate periodograms from the photometric data and measure (estimate) the orbital periods of 30 (15) WDMS binaries.

**Key words:** binaries: close – binaries: spectroscopic – white dwarfs – stars: low-mass

#### INTRODUCTION 1

Detached binary stars containing a white dwarf (WD) primary and a main sequence companion star are referred to as WD-main sequence (WDMS) binaries. Depending on the orbital separations of the main sequence binaries from which they descend, the previous evolution of WDMS binaries follows two main different paths. Thus, in approximately 75 per cent of the cases the orbital separations are wide enough for the WD precursors to evolve as single stars (de Kool 1992; Willems & Kolb 2004). In the remaining cases the main sequence binary components are close enough for the systems to experience dynamically unstable mass transfer interactions when the more massive star evolves into a red giant or asymptotic giant. This generally results in a common envelope (CE) phase (Iben & Livio 1993; Webbink 2008) in which friction of the binary components with the material of the envelope leads to a dramatic decrease of the binary separation. The orbital energy released during this process is used to eventually expel the envelope (Passy et al. 2012; Ricker & Taam 2012). Close WDMS binaries that evolve through a CE phase are known as post-CE binaries or PCEBs. Whilst, stricly speaking, a PCEB refers to any type of binary that evolved through CE evolution - e.g. hot subd-

<sup>\*</sup> E-mail: jjren@nao.cas.cn (JJR).

warf B stars with close low-mass main sequence companions (Han et al. 2002, 2003; Heber 2016) – in this work we will only consider a PCEB as a close WDMS binary.

The orbital period distribution of WDMS binaries is bi-modal. Numerical simulations predict the orbital periods of wide systems that did not evolve through a CE to range between a few hundred to several thousand days (Willems & Kolb 2004; Camacho et al. 2014; Cojocaru et al. 2017). This is observationally confirmed by Farihi et al. (2010). The observed PCEB orbital period distribution displays a clear concentration of systems at  $\sim 8 \,\mathrm{h}$ (Miszalski et al. 2009; Nebot Gómez-Morán et al. 2011), although PCEBs with periods as long as 10 days have been also identified (e.g. Rebassa-Mansergas et al. 2012b).

After the CE phase, PCEBs evolve to even shorter orbital periods through angular momentum loss driven by magnetic braking and/or gravitational wave emission. Therefore, they may undergo a second phase of CE evolution, leading to double-degenerate WDs 2017;(Rebassa-Mansergas et al. Breedt et al. 2017:Kilic et al. 2017), or enter a semidetached state and become cataclysmic variables (Gänsicke et al. 2009: Pala et al. 2017) or super-soft X-ray sources (Parsons et al. 2015b). Double degenerate WDs, cataclysmic variables and super-soft X-ray sources are considered to be possible progenitors of type Ia supernova (Langer et al. 2000; Han & Podsiadlowski 2004; Wang et al. 2010; Wang & Han 2012), which are of important interest for cosmological studies

Thanks to the Sloan Digital Sky Survey (SDSS; York et al. 2000; Stoughton et al. 2002) the number of spectroscopically confirmed WDMS binaries has dramatically increased during the last decade (Silvestri et al. 2006: Rebassa-Mansergas et al. 2007;Heller et al. 2009; Rebassa-Mansergas et al. 2010, 2012a; Liu et al. 2012; Rebassa-Mansergas et al. 2013b; Li et al. 2014; Rebassa-Mansergas et al. 2016a). Thus, the current most updated SDSS WDMS catalogue includes 3294 binaries<sup>1</sup>, which is by far the largest and most homogeneous sample of compact binaries in the literature (Rebassa-Mansergas et al. 2016a). Among the  $3\,294$  SDSS WDMS, observational follow-up studies have resulted in the identification of  $\sim 1000$  wide binaries that did not interact and more than 200 PCEBs (Rebassa-Mansergas et al. 2007; Schreiber et al. 2008, 2010; Rebassa-Mansergas et al. 2011, 2016a), of which 90 have available orbital periods (Rebassa-Mansergas et al. 2008; Nebot Gómez-Morán et al. 2011; Rebassa-Mansergas et al. 2012b) and 71 are eclipsing (Nebot Gómez-Morán et al. 2009; Pyrzas et al. 2009, 2012; Parsons et al. 2013a, 2015a).

The superb sample of SDSS WDMS binaries has led to many and diverse advances in the field of astrophysics. Among these we emphasise the following: providing constraints on theories of CE evolution (Davis et al. 2010; Zorotovic et al. 2010; De Marco et al. 2011), analysing the Galactic properties of WDMS binaries through population synthesis studies aimed at reproducing the ensemble properties of the observed population (Toonen & Nelemans 2013; Camacho et al.

2014; Zorotovic et al. 2014; Cojocaru et al. 2017), testing the age-metallicity relation in the solar neighbourhood (Rebassa-Mansergas et al. 2016b), identifying pulsating lowmass WDs in detached WDMS binaries (Pyrzas et al. 2015), providing evidence for disrupted magnetic braking (Schreiber et al. 2010; Zorotovic et al. 2016), studying the origin of low-mass WDs (Rebassa-Mansergas et al. 2011), investigating the age-rotation-activity relation of low-mass M stars (Rebassa-Mansergas et al. 2013a; Skinner et al. 2017), constraining the critical binary star separation for a planetary system origin of WD pollution (Veras et al. 2018), testing the mass-radius relation of low-mass main sequence stars and WDs (Parsons et al. 2012a,b, 2017) and investigating the origin of circumbinary giant planets around PCEBs (Zorotovic & Schreiber 2013; Marsh et al. 2014; Parsons et al. 2014; Schleicher et al. 2015; Bours et al. 2016).

However, despite the importance of the SDSS WDMS binary sample, it is important to emphasise that it suffers from serious selection effects (Rebassa-Mansergas et al. 2016a). This is because the SDSS focused mainly on spectroscopic observations of quasars and galaxies, which overlap in colour space with hot WDs (Richards et al. 2002; Smolčić et al. 2004). Hence, WDMS containing cool WDs and early-type companions are under-represented. In order to overcome this issue, Rebassa-Mansergas et al. (2012a) presented a dedicated survey within SEGUE (The Sloan Extension for Galactic Understanding and Exploration; Yanny et al. 2009) that obtained spectra for 291 WDMS binaries containing cool WDs and/or early type companions. Moreover, Rebassa-Mansergas et al. (2013b) photometrically selected 3419 WDMS candidates for containing cool WDs.

The Large sky Area Multi-Object fiber Spectroscopic Telescope (LAMOST) survey is a large-scale spectroscopic survey which follows completely different target selection algorithms than SDSS, hence opening the possibility for identifying WDMS binaries that help in overcoming the selection effects of the SDSS sample. Ren et al. (2013, 2014) identified a total of 121 LAMOST WDMS binaries from the data release (DR) 1 of LAMOST (Luo et al. 2012). They found that the intrinsic properties of the LAMOST WDMS binary sample were different from those of the SDSS population. In particular, LAMOST WDMS binaries are found at considerably shorter distances and are dominated by systems containing early-type companions and hot WDs (Ren et al. 2014). LAMOST WDMS thus represent an important addition to the current known spectroscopic catalogue of SDSS WDMS binaries. However, the number of WDMS containing cool WDs remains still under-represented, and the number of LAMOST WDMS binaries identified so far is rather small.

Here we present an updated LAMOST WDMS binary catalogue based on the most recent DR of LAMOST – DR5, to thus increase the current small number of LAM-OST WDMS binaries. Moreover, we present a dedicated LAMOST survey for obtaining spectra of as many as possible photometrically selected SDSS WDMS binaries from Rebassa-Mansergas et al. (2013b) that presumably contain cool WDs. We measure the stellar parameters from the LAMOST spectra of all our identified objects and perform a statistical analysis of their intrinsic properties. We also determine the radial velocities (RVs) of each binary with the

<sup>&</sup>lt;sup>1</sup> https://sdss-wdms.org/

aim of detecting PCEBs. Finally, we cross-match our sample with photometric data from the Catalina Sky Survey (CSS) and Catalina Real Time Transient Survey (CRTS; Drake et al. 2009) in order to search for WDMS binaries displaying light curve variations (e.g. eclipsing systems).

#### 2 THE DR5 OF LAMOST

LAMOST is a quasi-meridian reflecting Schmidt telescope of  $\sim 4$  meter effective aperture and a field of view of 5 degrees in diameter (Wang et al. 1996; Su et al. 2004; Cui et al. 2012). LAMOST is located in Xinglong station of National Astronomical Observatories of Chinese Academy of Sciences. Being a dedicated large-scale survey telescope, LAMOST uses 4000 fibres to obtain spectra of celestial objects as well as sky background and calibration sources in one single exposure. To that end, LAMOST uses 16 fiber-fed spectrographs each accommodating 250 fibers. Each spectrograph is equipped with two CCD cameras of blue and red channels that simultaneously provide blue and red spectra of the 4000 selected targets, respectively. The LAMOST spectra cover the entire optical wavelength range ( $\simeq 3700-9000$ Å) at a resolving power  $R \sim 1800$ .

From 2012 September, LAMOST has been carrying out a five-year Regular Survey. Before that, there was a one-year Pilot Survey preceded by a two-year commissioning phase. The LAMOST Regular Survey consists of two components (Zhao et al. 2012): the LAMOST Extra-Galactic Survey of galaxies (LEGAS) that aims at studying the large scale structure of the universe, and the LAMOST Experiment for Galactic Understanding and Exploration (LEGUE) that aims at obtaining millions of stellar spectra in order to study the structure and evolution of the Milky Way (Deng et al. 2012). LEGUE is sub-divided into three sub-surveys: the spheroid, the anticentre (Liu et al. 2014; Yuan et al. 2015; Xiang et al. 2017) and the disc surveys. The five-year Regular Survey finished in June 16th 2017 and the spectra have been released internally to the Chinese scientific community through the DR5 of LAMOST<sup>2</sup>. The raw spectra are processed with the LAMOST two-dimensional (2D) pipeline (Luo et al. 2012, 2015), which includes dark and bias subtractions, cosmic ray removal, one-dimensional (1D) spectral extraction, merging sub-exposures (note that each plate is generally observed consecutively for a minimum of three times), and finally, splicing the sub-spectra from the blueand red channels of the spectrographs, respectively. The LAMOST 1D pipeline is then carried out to perform spectral classification and to measure the redshift (or radial velocity) of each spectrum. There are 4119 plates observed in LAMOST DR5, thus including a total of 8952297 spectra, of which 7 930 178 are stars, 152 608 are galaxies, 50 132 are quasars, and 819 379 are classified as unknowns.



Figure 1. A WT decomposition example of a LAMOST DA/M binary (J161713.52+215517.5). The top panels show the blue (left) and red (right) spectrum of the binary. The vertical grey dashed lines indicate the spectral regions selected to perform the wavelet transform (the 3910–4422Å range in the blue and the 6800–8496Å range in the red). The bottom panels display the approximation coefficients (CA) as a function of data number of points after applying the WT (5th iteration in blue, left panel; 7th iteration in red, right panel).

#### 3 THE LAMOST DR5 WDMS BINARY CATALOGUE

In this section we describe how we identify WDMS binaries within LAMOST DR5 and we estimate the completeness of the sample.

#### 3.1 Identification of WDMS binaries

In Ren et al. (2014) we developed a fast and efficient routine based on the wavelet transform (WT; Chui 1992) to identify WDMS binaries from LAMOST DR1. The analysis unit of the WT is the local flux of the spectrum, i.e. the selected spectral features. In other words, the WT recognises the spectral features rather than the global continuum of a given spectrum. This is done by decomposing a considered spectral range (covering the desired spectral features) into approximation signals, often referred to as approximation coefficients. The wavelength values under the considered spectral region are converted into data points. This decomposition process can be iterated by decomposing the approximation coefficients into successive approximation coefficients (thus reducing by half the number of data points in each iteration) until the decomposition level is satisfactory. This occurs when the spectral features of a WDMS binary spectrum can be identified in the approximation coefficients as compared to a non-WDMS binary spectrum in which the approximation coefficients are dominated by continuum emission and/or by spectral features different from those of WDMS binaries. The outcome of a WT can be hence considered as a smoothed version of the spectrum (for comparative purposes). Because of its high efficiency in identifying spectral features, the WT is very suitable to identify WDMS binaries among low signal-to-noise (SN) ratio spectra

WDMS binaries containing a DA (hydrogen-rich) WD and a low-mass main sequence star have two obvious spectral features: the Balmer lines in the blue band arising from

<sup>&</sup>lt;sup>2</sup> http://dr5.lamost.org/

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**Table 1.** The catalogue of LAMOST DR5 WDMS binaries, including a total of 1150 spectra of 876 unique targets. Here we list the coordinates, SDSS ugriz magnitudes (when available), LAMOST spectral identifiers (plate, spectrograph, fibre IDs and modified Julian date MJD), signal-to-noise ratio in five different bands (SN<sub>u</sub>, SN<sub>g</sub>, SN<sub>r</sub>, SN<sub>i</sub>, SN<sub>z</sub>) and stellar parameters (the WD effective temperature, surface gravity and mass, and the spectral type of the M dwarf companion). We also provide Simbad classifications (when available) and indicate if the target is identified by the WT (fWT=1, yes; 0, no), if it is a photometrically selected SDSS WDMS binary that obtained a LAMOST spectrum (fPhot=1, yes; 0, no), if it is part of the SDSS DR12 WDMS spectroscopic catalogue (fSDSS=1, yes; 0, no), if it is a WDMS binary candidate (fCAND=1, candidates; 0, genuine DA/M) and/or if it is part of the LAMOST DR1 WDMS binary catalogue (fDR1=0, not in DR1; 10, in DR1 genuine DA/M sample, not in DR1 DA/M candidate sample; 11, in DR1 DA/M candidate sample). The entire table is provided in the electronic version of the paper. We use '-' to indicate that no magnitude or stellar parameter is available.

Jname	fWT	fPhot	fSDSS	fCAND	fDR1	R	А	Dec	u	Err	g	Err	r	Eri	r i	Err	Z	Err
						(*	°)	(°)	(mag)	(mag)	(mag)	(mag)	(mag)	(mag)	(mag)	(mag)	(mag)	(mag)
J000448.23+343627.	1 1	0	0	0	00	1.200999	99-34	4.6076320	_	-	-	-	-	_	· _	-	-	-
J000612.32 + 340358.	31	1	0	0	00	1.551339	97 34	4.0661980	18.954	0.029	18.327	0.008	17.794	0.008	8 16.535	0.005	15.713	0.007
J000729.32+023124.	51	0	0	0	00	1.872192	20 2	2.5234990	19.912	0.042	19.092	0.010	18.379	0.008	3 17.494	0.007	16.937	0.011
J001258.26+062617.	9 1	0	0	0	00	3.242754	42 6	5.4383056	18.505	0.016	17.987	0.006	18.001	0.007	7 17.528	0.007	17.088	0.011
J001733.59+004030.	4 1	0	1	0	00	4.389970	)5 (	0.6751216	20.200	0.051	19.517	0.014	18.982	0.013	3 17.925	0.009	17.166	0.014
J001752.63+332424.	9 1	1	0	0	00	4.469310	05 33	3.4069250	18.582	0.015	17.625	0.005	16.519	0.004	15.616	0.004	15.069	0.005
J001752.63+332424.	) 1	1	0	0	00	4.469310	)5 33	3.4069250	18.582	0.015	17.625	0.005	16.519	0.004	15.616	0.004	15.069	0.005
J002237.90+334322.	1 1	0	0	0	10	5.657942	20 33	3.7228090	19.548	0.033	17.361	0.005	15.985	0.003	8 14.590	0.004	13.858	0.004
J002407.31+054856.	4 1	1	0	0	00	6.030470	00 5	5.8156830	17.068	0.008	16.393	0.004	15.851	0.004	4 14.808	0.004	14.128	0.004
J002633.13+390904.	) 1	1	0	0	00	6.638082	24 39	9.1511210	16.348	0.006	15.905	0.003	16.011	0.004	15.831	0.004	15.327	0.005
J002633.14+390904.	) 1	1	0	0	00	6.638503	30 39	9.1508170	16.348	0.006	15.905	0.003	16.011	0.004	15.831	0.004	15.327	0.005
MJD P	ate		spID	fiberID	$SN_u$	$SN_q$	$SN_r$	$SN_i$	$SN_z$	$T_{\rm eff WD}$	Err	$\log g_{\rm V}$	ND	Err	M <sub>WD</sub>	Err	Sp S	imbad
						0				(K)	(K)	(d	ex) (c	lex) (	(M <sub>☉</sub> )	M <sub>☉</sub> )		
56948 M3100	1N35M	2	05	156	8.66	33.80	30.05	49.00	32.49	16717	245	8	.02 (	0.06	0.63	0.03	4 -	
56948 M3100	1N35M	2	01	139	3.92	12.66	22.09	47.00	50.04	28389	1448	7	.87 (	0.23	0.58	0.11	4 –	
55893 F9	302		01	235	1.72	2.52	4.11	7.63	6.58	-	-		-	-	-	-	1 –	
56602 EG0016051	1080655	5M01	02	066	1.52	3.01	2.25	3.48	3.23	_	_		_	-	-	_	4 –	
56978 EG0016391	1015102	2M01	05	141	1.52	5.07	7.31	16.86	14.32	_	_		_	-	-	_	3 D	A+dM
56952 M3100	5N35M	1	02	120	2.44	13.88	35.84	71.58	60.63	_	_		_	-	-	_	1 –	
57717 M3100	7N33B	2	10	109	3.66	16.36	34.31	71.88	63.27	29727	1312	8	.34 (	0.25	0.82	0.14	2 -	
56255 VB00'	'N33V1		03	085	2.23	3.49	2.78	1.72	3.15	_	-		_	-	-	_	– D	A+M
56621 EG002616	N03493	2B01	11	020	8.25	27.85	40.10	86.82	82.41	14899	395	8	.41 (	0.08	0.85	0.05	3 –	
57280 M3100	7N36M	1	11	163	1.80	3.81	4.02	4.78	4.40	-	-		_	_	-	-	9 D	A4.6
56911 HD002951	N38192	6B01	15	227	4.28	9.16	5.54	4.01	3.84	_	_		_	_	_	_	- D	A4.6



Figure 2. Example spectra of LAMOST DA/M binaries identified by the WT in descendant order of SN ratio (in the r band).

the WD and the molecular absorption bands in the red that are typical of M dwarfs. We hence applied the WT to the following spectral regions: the 3910–4422Å range in the blue band that covers the  $H\beta$  to  $H\epsilon$  Balmer lines and the 6800–8496Å range which covers a large number of TiO and VO molecular bands. By choosing these two spectral features we focus our search on the identification of WDMS binaries containing a DA WD and a M dwarf companion (hereafter DA/M binaries; see an example of WT applied to a DA/M binary in Figure 1). The main reason for this choice is that DA/M are by far the most common among WDMS binaries, including  $\sim 80$  per cent of all systems (Rebassa-Mansergas et al. 2016a). This is because of the following two reasons. First, DA WDs comprise  $\sim 80$  per cent of all single WDs (Kepler et al. 2015), hence it is not surprising that they are the most common WDs in binaries too. Second, because of selection effects, main sequence stars of spectral type earlier than M generally outshine the WDs in the optical, which implies only a handful of WDs with late K-type companions have been identified (Rebassa-Mansergas et al. 2016a). We will pursue the identification of LAMOST WDMS binaries harboring other WD types (DB, DQ, DZ, etc) as well as late K-type companions elsewhere. Of course, in order for our WT to efficiently identify DA/M binaries we require the two components (DA WD plus M dwarf) to be visible in the spectrum. This implies that systems in which one of the two components clearly dominates the spectral energy distribution will be harder (or even impossible) to detect. We note however that this issue makes the detection of such systems to be very difficult

by any method (see for example Rebassa-Mansergas et al. 2010).

After applying the WT method to the  $\sim 9$  million LAM-OST DR5 spectra, we obtained an initial list of 29269 WDMS binary candidate spectra that we visually inspected. This resulted in 776 spectra (579 unique systems) that we considered as genuine DA/M binaries, and 47 spectra (46 unique systems) that we catalogued as DA/M candidates. The majority of spectra selected by the WT that we did not consider DA/M binaries corresponded to single MS stars and to the superposition in the line of sight of two main sequence stars. Table 1 lists all the genuine and candidate DA/M binaries identified by the WT, where we also include LAM-OST spectroscopic identifiers and modified Julian dates of the observations. In Figure 2 we show four example spectra of LAMOST DA/M binaries of different SN ratio.

# 3.2 Completeness of the LAMOST DR5 DA/M binary sample

In Ren et al. (2014) we showed the WT method is highly efficient (~90 per cent) in identifying DA/M binaries and that the spectra it fails to identify are either clearly dominated by one of the stellar components and/or are associated to very low SN ratio (< 5). In order to estimate the completeness of the LAMOST DR5 DA/M binary catalogue (i.e. the number of DA/M binaries observed by LAMOST that the WT successfully identified), we cross-matched the entire ~9 million spectroscopic data base of LAMOST with the SDSS DR12 spectroscopic catalogue of WDMS binaries. We found 447 objects in common (583 LAMOST spectra).

111 (153 spectra) of the 447 objects (583 spectra) were non-DA/M binaries that the WT failed to identify for obvious reasons: the spectral features of these WDMS binaries were different from those of DA/M binaries. In order to compile a catalogue as complete as possible, we added the 111 objects (105 genuine WDMS, 143 spectra; 6 WDMS binary candidates, 7 spectra) to our list.

The remaining 330 systems were DA/M binaries (424 spectra), 233 (312 spectra) of which were identified by the WT and 97 (112 spectra) were missed. This translated into a completeness of  $\sim 70$  per cent, a value which is considerably lower than the  $\sim 90$  per cent claimed by Ren et al. (2014). We repeated the exercise excluding all spectra of SN ratio below 5 and found the number of DA/M binaries identified and missed by the WT were 156 (188 spectra) and 37 (42) spectra), respectively, i.e. a completeness of  $\sim 80$  per cent. We visually inspected the 42 missed spectra and realised that 19 of them were clearly dominated by the flux contribution of the WD and 15 by the flux contribution of the M dwarf. We also found 5 broken spectra. Excluding the broken spectra and those dominated by one of the stellar components, the completeness increased to  $\sim 98$  per cent. We added the 97 objects (93 genuine WDMS, 108 spectra; 4 candidate WDMS, 4 spectra) the WT missed to our list of LAMOST DR5 WDMS binaries.

We conclude the WT is highly efficient at identifying DA/M binaries and that the LAMOST DR5 DA/M binary catalogue is  $\sim$ 98 per cent complete. However, the completeness drops to  $\sim$ 70 per cent when considering spectra clearly dominated by the flux contribution of one of the stellar components and/or spectra of very low SN ratio (<5). Unfortu-



Figure 3. SDSS *gri* magnitude distributions of the 3 419 photometrically selected WDMS binaries of Rebassa-Mansergas et al. (2013b).

nately, identifying DA/M binary spectra of such characteristics is challenging for any method (Rebassa-Mansergas et al. 2010).

#### 4 A DEDICATED LAMOST SURVEY OF PHOTOMETRICALLY SELECTED SDSS WDMS BINARIES

The spectroscopic catalogue of SDSS WDMS binaries is severely biased against systems containing cool WDs and/or early type companions. This is mainly because SDSS dedicated most of its efforts to obtain spectra of quasars and galaxies, which overlap in colour space with WDMS binaries containing hot ( $\geq 10000-15000$  K) WDs and/or late type (>M3-4) companions. In order to overcome this selection effect, Rebassa-Mansergas et al. (2013b) developed a colour selection criteria that combines optical (SDSS ugriz) plus infrared (UKIRT Infrared Sky Survey yjhk, Two Micron All Sky Survey JHK and/or Wide-Field Infrared Survey Explorer  $w_1w_2$ ) magnitudes to photometrically select 3419 WDMS binary candidates for harboring cool WDs and/or dominant (M dwarf) companions in their spectra. Visual inspection of 567 photometric candidates with available SDSS spectra allowed Rebassa-Mansergas et al. (2013b) to conclude that 84 per cent of entire the photometric sample are expected to be genuine WDMS binaries, and that 71 per cent should contain WDs of effective temperatures below 10000-15000 K and M dwarf companions of spectral types concentrated at  $\sim$ M2–3.

In this section we present a dedicated LAMOST survey that so far has obtained spectra of 622 photometrically selected SDSS WDMS binaries.

#### 4.1 The LAMOST observations

Since 2014, the LAMOST target selection algorithm has incorporated the photometrically selected WDMS binary list

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of Rebassa-Mansergas et al. (2013b) with the aim of obtaining as many WDMS binary spectra as possible. As mentioned in Luo et al. (2015), the LAMOST observations are carried out using four different modes, i.e. the selected objects are observed using different plates according to their magnitudes: very bright plates (VB,  $r \leq 14$  mag), bright plates (B, 14 mag < r < 16.8 mag), medium-bright plates (M, 16.8 mag  $\leq r \leq 17.8$  mag) and faint plates (F, r >17.8 mag). LAMOST DR5 has made use of  $\sim 4000$  plates, of which 80 per cent are VB/B plates (46 per cent are VB plates), i.e. most of the observed targets have r magnitudes below 16.8. Fig 3 shows the qri magnitude distribution of the 3419 photometrically selected WDMS binaries of Rebassa-Mansergas et al. (2013b), where one can clearly see the number of systems with r < 16.8 mag is low (~17) per cent). Moreover, it is important to emphasize that, on occasions, the coordinates of the LAMOST plates and the WDMS binaries do not overlap (see Fig 4). Overall, this implies that only a small fraction of photometrically selected WDMS binaries has been so far observed by LAMOST.

# 4.2 The success rate of the SDSS photometric sample

The LAMOST observations above described resulted in a total number of 872 spectra of 622 unique sources from the Rebassa-Mansergas et al. (2013b)'s list. We visually inspected the spectra and identified 298 genuine WDMS binaries (436 spectra) and 41 (57 spectra) that we considered as WDMS binary candidates. The remaining sources were cataclysmic variables (7; 13 spectra), single M dwarfs (161; 214 spectra), quasars (23; 36 spectra), main sequence stars (16; 26 spectra), single WDs (4; 4 spectra), main sequence plus main sequence superpositions (11; 20 spectra), and unknown objects due to the bad quality of their spectra (61; 66 spectra).

If we exclude the 61 unknown sources we find that 60 per cent of the photometric candidates are indeed genuine WDMS binaries or WDMS binary candidates. This value is low compared to the 84 per cent of success rate claimed by Rebassa-Mansergas et al. (2013b) for the same sample. However, it is important to emphasise that Rebassa-Mansergas et al. (2013b) showed the success rate varies from 40 per cent up to 100 per cent depending on colour space and that the 84 per cent value represents an average success rate over the entire colour space. This can clearly be seen in Figure 5, where we illustrate the success rate in form of a density map in the g - r vs. r - i colour space. In this figure we also show the location of the genuine WDMS binaries observed by LAMOST DR5 (green solid dots) and those that we consider contaminants (i.e. non WDMS binaries). It becomes obvious that the contaminants are either located in areas of expected low success rate or concentrated at g - r < 1. At such red colours the WD contribution in the optical spectrum is expected to be rather low, which makes it difficult to judge simply by eye whether or not these objects are real WDMS binaries or single MS stars. Our visual inspection decided for the latter, although the former cannot be ruled out.

We checked how many of the 298 genuine WDMS binaries identified in this section were also found by the WT and realised that only 30 objects (a total of 49 spectra) were missing. We made use of this result to derive (in an alternative way) the completeness of the LAMOST DR5 WDMS binary catalogue, which results in this case in  $\sim 90$  per cent. This value is slightly lower than the 98 per cent we obtained before (see Section 3.2), however it confirms the WT is an efficient tool to identify WDMS binaries among large spectroscopic samples. We also found that 37 (52 spectra) of the 41 (57 spectra) WDMS binary candidates were not identified by the WT. Visual inspection revealed most of these candidate spectra were dominated by the flux of the M dwarf, some were broken, and others were of low SN ratio. Hence, it is not surprising that the WT was not successful at identifying these spectra.

Among the 30 objects the WT missed (49 spectra), 14 (25 spectra) were found cross-matching the entire LAMOST data base with the SDSS DR12 WDMS binary catalogue (see Section 3.2). Hence, we added to our list the remaining 16 WDMS binaries (24 spectra). In the same way, among the 37 WDMS binary candidates (52 spectra) the WT missed, 10 (11 spectra) were identified in Section 3.2. Thus, we added the remaining 27 (41 spectra) WDMS binary candidates to our LAMOST DR5 catalogue.

#### 5 THE FINAL CATALOGUE OF LAMOST DR5 WDMS BINARIES

The WT identified 579 genuine (776 spectra) and 46 candidate (47 spectra) WDMS binaries (Section 3.1). To this list we added 97 (112 spectra) DA/M binaries (93 genuine binaries, 108 spectra; 4 candidates, 4 spectra) and 111 (150 spectra) non DA/M binaries (105 genuine non DA/M, 143 spectra; 6 non DA/M candidates, 7 spectra) by crossmatching the SDSS DR12 WDMS catalogue with the entire LAMOST spectroscopic data base (Section 3.2). Finally, we added 16 (24 spectra) genuine and 27 (41 spectra) candidate DA/M binaries by visually inspecting the LAMOST spectra of 622 SDSS photometrically selected targets (Section 4). This brings the total number of genuine LAMOST DR5 WDMS binaries to 793 (1051 spectra) and 83 WDMS binary candidates (99 spectra), i.e. 876 objects and 1150 spectra. The entire catalogue is included in Table 1.

We compared our LAMOST DR5 catalogue to the one we presented in Ren et al. (2014) and found that 119 objects (194 spectra) were already identified in the DR1 of LAM-OST. Hence, the DR5 catalogue contains 757 (956 spectra) new entries. Moreover, we found that 400 (509 spectra) objects were already discovered in the SDSS DR12 catalogue of Rebassa-Mansergas et al. (2016a), which implies 357 (447 spectra) are new systems that have not been published before.

#### 6 CHARACTERIZATION OF THE LAMOST DR5 WDMS BINARY CATALOGUE

In this section we measure the WD stellar parameters and determine the M dwarf spectral subclass of all DA/M binaries that are part of our new LAMOST DR5 WDMS binary catalogue. We also describe the properties of the new DR5 sample by analysing the parameter distributions.



Figure 4. Galactic coordinates of the LAMOST DR5 plates (gray open circles) and the photometrically selected SDSS WDMS binaries of Rebassa-Mansergas et al. (2013b) (solid coloured dots; each colour is associated to a given r magnitude according the colour bar displayed in the bottom of the figure). The coloured dots with black edges illustrate those WDMS binaries with r < 16.8 mag.



Figure 5. The estimated success rate for selecting genuine WDMS binaries based on the colour selection criteria developed by Rebassa-Mansergas et al. (2013b) (black regions represent 100 per cent of success rate, white regions 0 per cent). The 873 spectra observed by LAMOST DR5 are indicated as solid dots (green for genuine WDMS binaries, red for contaminants).

#### 6.1 Stellar parameter determinations

We determined the stellar parameters following the decomposition/fitting routine described by Rebassa-Mansergas et al. (2007). The first step was to fit the DA/M binary spectrum with a two-component model using a set of observed M dwarf and WD templates, which allowed obtaining the spectral type of the M dwarf.



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Figure 6. Comparison between the WD parameters (effective temperature, surface gravity and mass) and M dwarf spectral subclass derived from SDSS and LAMOST spectra of common DA/M binaries.

Then, the best-fit M dwarf template was subtracted from the DA/M binary spectrum and the Balmer lines (H $\beta$  to H $\epsilon$ ) of the residual WD spectrum were fitted using a grid of DA WD atmosphere models (Koester 2010) to derive the WD effective temperature ( $T_{\rm eff}$ ) and surface gravity (log g). Given that the equivalent widths of the Balmer lines reach a maximum near  $T_{\rm eff} = 13\,000\,\mathrm{K}$  (with the exact value being a function of log g), the  $T_{\rm eff}$  and log g determined from Balmer line profile fits are subject to a degeneracy.



Figure 7. Parameter distributions (WD mass, top panel; WD effective temperature, top-middle panel; WD surface gravity, bottom-middle panel; secondary M dwarf spectral subtype, bottom panel) for the entire LAMOST DR5 DA/M binary catalogue (gray) and for the sub-sample of objects that were photometrically selected from the SDSS and observed by LAMOST (black).

That is, fits of similar quality can be achieved on either side of the temperature at which the maximum equivalent width is occurring. We broke this degeneracy fitting the entire WD residual spectrum (continuum plus Balmer lines).

It has been shown that one-dimensional WD model atmosphere spectra such as those used in this work yield overestimated log g values for WDs of effective temperatures below ~12 000 K (Koester et al. 2009; Tremblay et al. 2011). Therefore, we applied the corrections of Tremblay et al. (2013), which are based on three-dimensional WD model atmosphere spectra, to our WD parameter determinations. We then interpolated the  $T_{\rm eff}$  and log g values in the cooling sequences of Renedo et al. (2010) to derive the WD masses. In cases where more than one spectrum per target were available we averaged the stellar parameters (namely the  $T_{\rm eff}$ , log g and mass of the WD and the spectral type of the M dwarf). The stellar parameters are provided in Table 1 for each individual spectrum.

Given that a large number of LAMOST DA/M binaries have also been observed by SDSS, we decided to compare the stellar parameters determined here with those obtained fitting the SDSS spectra. We note that we applied the same fitting routine to both the LAMOST and SDSS spectra. The result can be seen in Figure 6, where we display only WDs with relative error in their effective temperatures

**Table 2.** KS and  $\chi^2$  probabilities. Sample 1 refers to the entire LAMOST DR5 catalogue excluding the SDSS photometrically selected objects observed by LAMOST, Sample 2 refers to the SDSS photometrically selected sample observed by LAMOST, Sample 3 refers to the LAMOST DR1 catalogue of Ren et al. (2014) and Sample 4 refers to the full LAMOST DR5 catalogue.

	Sample 1 vs. Sample 2	Sample 3 vs. Sample 4
WD $T_{\rm eff}$	0.09	0.35
WD $\log g$	0.66	0.46
WD mass	0.40	0.09
M dwarf Sp	0.93	0.56

below 10 per cent (128 objects), and absolute errors below 0.15 dex (in log g; 30 objects) and 0.1 M<sub> $\odot$ </sub> (in mass; 50 objects). Moreover, we only took into account DA/M binaries with available M dwarf spectral subclasses (318 objects). Visual inspection reveals the WD parameters are broadly consistent with each other. Quantitatively, if we define  $\tau$  (Gentile Fusillo et al. 2015):

$$\tau = \frac{SDSS \text{ value} - LAMOST \text{ value}}{\sqrt{SDSS \operatorname{error}^2 + LAMOST \operatorname{error}^2}}$$
(1)

then we find that the WD parameters show a comparable agreement ( $\tau < 2$ ) in 70 ( $T_{\rm eff}$ ), 77 (log g) and 82 (mass) per cent of the cases. We can conclude then that the WD parameters derived using LAMOST and SDSS spectra are indeed broadly in agreement.

Visual comparison of the M dwarf spectral subclasses obtained fitting the SDSS and LAMOST spectra (bottom left panel of Figure 6) seems to indicate a large spread of values for a given spectral subtype. However, only in 12 of the 318 cases considered the difference in spectral subtypes is larger than 2, and in 49 cases larger than 1. We visually inspected the LAMOST spectra of these 49 objects and found that they were either dominated by the WD contribution and/or of low SN ratio. These are clear cases in which we expect higher uncertainties in the determination of the M dwarf spectral subclasses. In order to quantitatively study the apparent disagreement further, we obtained the average LAMOST spectral subclass and its standard deviation fixing the SDSS spectral subclasses. The result is shown as red solid dots and red solid lines in the bottom left panel of Figure 6. It becomes clear that, in the majority of cases, the spectral subtypes agree well with each other and that the apparent scatter at a given spectral subtype is caused by isolated cases.

## 6.2 Properties of the LAMOST DA/M binary catalogue

In the previous section we determined the stellar parameters of our LAMOST DR5 DA/M binaries. This allows us to present here the corresponding stellar parameter distributions, which we show in Figure 7 in the following order: WD mass (top panel), WD effective temperature (topmiddle panel), WD surface gravity (bottom-middle panel) and M dwarf spectral subtype (bottom panel). Following Section 6.1, and in order to exclude values subject to large uncertainties, we exclude WDs with relative error in their effective temperatures above 10 per cent (we are left with 277 objects in the top-middle panel of Figure 7), and ab-



Figure 8. Cumulative parameter distributions of the SDSS photometrically selected sample observed by LAMOST (black dotted lines; left and middle-left panels), the complete DR5 LAMOST sample excluding the SDSS photometrically-selected ones (black solid lines; left and middle-left panels), the LAMOST DR1 catalogue of Ren et al. (2014) (gray dotted lines; right and middle-right panels) and the complete LAMOST DR5 catalogue (solid gray lines; right and middle-right panels).

solute errors above 0.15 dex in  $\log g$  (76 objects; middlebottom panel) and  $0.1 M_{\odot}$  in mass (116 objects; top panel). In the same way, we only consider DA/M binaries with well-determined M dwarf spectral subclasses (686 objects; bottom panel of Figure 7). Visual inspection of the parameter distributions reveals that the WDs are concentrated at  $\sim 0.6 \,\mathrm{M_{\odot}}$  (which is equivalent to say they are concentrated at  $\log g \sim 8 \,\mathrm{dex}$ ), with a steep decline towards higher and lower masses (being the latter WDs that are presumably part of close binaries, see Section 7 for a further discussion) and with typical effective temperature values between 10 000 and  $40\,000\,\mathrm{K}$  (with a peak at  $\sim 15\,000\,\mathrm{K}$ ). The M dwarf spectral types are concentrated between M1–M4, with a decline towards earlier and later types. For completeness, we also show in Figure 7 the parameter distributions that result from considering only the photometrically-selected SDSS DA/M binary sample that has been observed by LAMOST. We note that we did not include any DA/M binary considered as candidate in this exercise.

We run Kolmogorov-Smirnov (KS) tests to the WD cumulative parameter distributions and apply a  $\chi^2$  test to the cumulative spectral type distributions resulting from the SDSS photometrically-selected sample and the total sample of LAMOST DR5 DA/M binaries (excluding the SDSS photometrically selected ones). The cumulative distributions are shown in the left panels of Figure 8 and the results are given in Table 2. The probabilities obtained do not seem to indicate the two samples are statistically different, which is what we should expect given that the photometric sample is selected based on colour cuts that favour the detection of systems containing cooler WDs and/or earlier type companions. This may be a consequence of the fact that it is more difficult to derive reliable WD parameters for this type of systems. That is, cooler WDs are systematically fainter and hence their spectra are of lower SN ratio, which translates into larger parameter uncertainties. Hence the objects containing the coolest WDs either cannot be fitted because they are subject to too low SN spectra or the fitted values do not survive our quality cuts and are excluded from the analysis.



Figure 9. Left panel: The maximum Na I doublet RV shift measured vs. time span between the observed spectra (in days) for the 76 new PCEBs identified in this work. Right panel: The same but for H $\alpha$  emission. The numerical values of the RV shifts are provided in Table 4.

This, unfortunately, implies that our sample of LAMOST DR5 DA/M binaries with available stellar parameters is still biased against systems containing cool WDs.

We also run KS and  $\chi^2$  tests to the cumulative distributions resulting from the entire LAMOST DR5 DA/M sample and the LAMOST DR1 catalogue we presented in Ren et al. (2014). The distributions are shown in the right panels of Figure 8 and in Table 2 we provide the probabilities. Again, we find no strong indications for the DR1 and DR5 LAMOST populations to be statistically different.

### 7 IDENTIFICATION OF CLOSE WDMS BINARIES

In this section we aim at detecting PCEBs among the WDMS binaries identified in this work. To that end we require measuring the radial velocities (RVs) of at least one stellar component. WD RVs can be measured fitting the Balmer lines (Breedt et al. 2017) and/or employing cross-

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**Table 3.** Radial velocities measured from the Na1 $\lambda\lambda$  8183.27, 8194.81 absorption doublet and the H $\alpha$  emission for the LAMOST DR5 WDMS binaries. The Heliocentric Julian Dates (HJD) are also indicated. The last column lists the telescope used for obtaining the spectra (either LAMOST or SDSS). We use '-' to indicate that no radial velocity is available. The complete table can be found in the electronic version of the paper.

Jname	HJD	RV(Na I)	$\operatorname{Err}$	$RV(H\alpha)$	$\operatorname{Err}$	Telescope
	(days)	$(\mathrm{kms^{-1}})$	$(\mathrm{kms^{-1}})$	$(\mathrm{km}\mathrm{s}^{-1})$	$(\mathrm{km}\mathrm{s}^{-1})$	
J000448.23+343627.4	2456948.07023	-21.59	45.97	-96.14	17.32	LAMOST
J000448.23+343627.4	2456948.09106	-45.61	20.86	-93.60	18.83	LAMOST
J000448.23+343627.4	2456948.09341	-43.07	15.78	-62.27	24.84	LAMOST
J000448.23+343627.4	2456948.11661	-37.64	20.67	-76.21	19.09	LAMOST
J000612.32+340358.3	2456948.07026	-4.35	12.62	-12.92	10.50	LAMOST
J000612.32+340358.3	2456948.09109	39.19	12.72	14.71	10.45	LAMOST
J000612.32+340358.3	2456948.09344	30.75	11.87	9.55	10.28	LAMOST
J000612.32+340358.3	2456948.11664	64.64	12.63	26.05	10.43	LAMOST
J000729.32 + 023124.5	2455892.99443	14.98	14.38	—	—	LAMOST

**Table 4.** The 76 new PCEBs found in this work. The Flag column indicates whether the PCEBs are detected based on NaI and/or H $\alpha$  emission RV measurements (only from NaI: 10; only from H $\alpha$ ; 01; from both NaI and H $\alpha$ : 11). The maximum RV shifts are also indicated.

Jname	Flag	RV shift	RV shift	Jname	Flag	RV shift	RV shift	Jname	Flag	RV shift	RV shift
		$(\rm km/s)$	$(\rm km/s)$			$(\rm km/s)$	$(\rm km/s)$			$(\rm km/s)$	$(\rm km/s)$
		Nai	$H\alpha$			Nai	$H\alpha$			Nai	$H\alpha$
J000612.32 + 340358.3	10	68.99	_	J093507.99 + 270049.2	11	248.88	182.41	J122514.92 + 292523.1	11	113.00	87.11
$J004751.47 {+} 340212.7$	01	_	70.77	J093809.28 + 143036.9	11	100.51	113.59	$J123339.40 {+} 135943.2$	11	133.43	106.79
J011739.90 + 340209.4	11	177.57	158.24	$J094101.91 {+} 510719.8$	01	_	59.05	J123642.53 + 580230.6	11	86.16	69.09
$\rm J011847.16{+}050531.2$	11	155.83	100.75	$J095641.79 {+} 013130.7$	01	_	87.01	J124831.79 + 435318.3	11	78.02	121.40
$J024924.76{+}071344.3$	01	_	118.56	J101356.31 + 272410.8	11	600.06	652.14	J124830.76 + 540803.6	11	83.12	219.67
$J025301.60 {-} 013006.8$	01	_	72.39	J101616.82 + 310506.5	11	114.66	66.68	$J132001.24{+}112805.3$	10	79.95	_
$J030944.99{+}285507.5$	10	58.73	_	$J103125.93 {+} 020751.4$	11	76.84	61.33	$J132341.89 {+} 541636.5$	10	137.35	_
${\scriptstyle J032750.32+222618.9}$	10	109.05	_	J104318.65 + 305012.9	10	146.37	_	J134051.00 + 321015.9	01	_	127.69
$\rm J050825.81{+}252050.8$	11	102.87	73.50	J104534.46 + 315740.6	01	_	80.16	$J135825.68{+}171204.1$	11	377.78	235.72
$J054119.24\!-\!051838.4$	11	154.71	167.96	J105352.90 + 340923.5	01	_	254.71	$J140115.68{+}214157.1$	10	49.64	_
$\rm J060040.31{+}312118.6$	10	45.48	-	J105657.35 + 330416.2	11	102.26	68.60	J142917.86 + 285103.0	10	90.38	_
$\rm J063840.55{+}130253.5$	01	_	101.87	J110827.40 + 303031.3	01	_	73.91	J144307.83 + 340523.5	01	_	94.57
$J073128.30 {+} 264353.6$	11	56.08	161.49	J111614.48 + 535720.9	01	_	74.54	J145248.79 + 234807.6	01	_	54.60
$\rm J081126.70{+}053912.9$	01	_	293.08	J112007.64 + 250221.3	11	193.70	204.91	J145430.02 + 203902.5	11	120.18	148.83
$J081654.35 {+} 354230.6$	10	146.69	_	J112124.82 + 273046.2	11	256.30	252.29	J151042.63 + 273509.9	10	90.99	_
$J082214.50 {+} 433343.6$	10	98.77	-	J113102.81 + 522645.3	01	_	74.78	$J153934.63 {+} 092221.5$	11	175.68	118.65
$\rm J082656.51{+}480545.7$	11	148.67	145.12	J113910.49 + 315013.1	10	121.59	_	J153914.69 + 263710.8	01	_	290.97
$\rm J082845.07{+}133551.6$	11	227.51	210.96	J114732.48 + 591735.1	10	60.98	_	J154101.07 + 294829.4	11	168.15	185.74
$\rm J083056.11{+}315941.9$	01	_	69.67	J114732.25 + 593921.9	10	106.47	_	J160645.02 + 284725.9	11	88.25	100.14
$J084418.12 {+} 340458.9$	11	122.49	105.03	J115057.60 + 282637.8	11	235.92	160.12	J165354.16 + 322937.6	01	_	75.64
$\rm J085024.05{+}054757.8$	10	37.21	_	J115026.28 + 302359.4	01	_	231.17	$J213136.72{+}002947.6$	10	74.41	_
$J085025.75 {+} 344053.2$	10	98.86	_	$J115113.14 {-} 011111.1$	01	_	168.85	$J224522.49 {+} 063817.2$	01	_	88.17
$J085414.26{+}211148.1$	11	233.93	149.53	J115510.86 + 271324.3	01	_	95.53	J224805.92 + 144328.3	01	_	66.04
$J085634.83 {+} 373913.4$	11	180.94	202.61	J121301.82 + 282310.0	11	389.86	388.75	$J234106.82 {+} 083550.3$	01	_	81.32
$\rm J090210.95{+}252913.3$	01	_	114.09	J122037.01 + 492334.0	10	76.86	-	${J235408.04}{+}{291623.1}$	01	_	54.65
${\scriptstyle J092712.02+284629.2}$	01	_	96.31								

correlation techniques (Anguiano et al. 2017). However, we expect the WD RV shifts to be smaller than those measured from their M dwarf companions, since the WDs are generally closer to the center of mass in this type of binaries. We hence measure the Na I  $\lambda\lambda$  8183.27, 8194.81 absorption doublet and the H $\alpha$  emission RVs arising from the M dwarf companions from all the LAMOST WDMS binary spectra identified in this work. We identify a PCEB when we detect more than  $3\sigma$  RV variation. Conversely, if no RV variation is detected from spectra taken separated by at least one night, the system is considered as a likely wide binary candidate that presumably evolved avoiding episodes of mass transfer. We fit the Na I  $\lambda\lambda$  8183.27, 8194.81 absorption doublet with a second-order polynomial plus a double-Gaussian line profile

of fixed separation, while the H $\alpha$  emission line (if present in the spectrum) is fitted with a second-order polynomial plus a single-Gaussian line profile (Rebassa-Mansergas et al. 2008; Ren et al. 2013). With the aim of increasing the SN ratio, the final released LAMOST DR5 spectra are the result of combining several different sub-exposure spectra (hereafter sub-spectra). Hence, we measure the RVs from all available sub-spectra as well as from the final combined spectra.

We cross-matched our LAMOST DR5 catalogue with the current newest spectroscopic data base of SDSS, i.e. DR14. This resulted in 685 additional spectra for 465 of our targets. Combining LAMOST DR5 and SDSS DR14 we thus gathered a total of 1835 spectra (1150 from LAMOST, 685 from SDSS) for measuring RVs. We derived at least Table 5. LAMOST DR5 WDMS binaries that display light curve variations as revealed by the Catalina photometric surveys. We provide notes on individual systems, classification and orbital periods obtained by calculating periodograms from the photometric data.

Object	Notes	Classification	Orbital Period
J000729.32+023124.5	Some faint points	Candidate new eclipser	?
J001752.63+332424.9	Reflection effect?	Candidate non-eclipser	6.4 hours?
J003033.11 + 070657.5	Seems to display variation	Candidate non-eclipser	1.2 hours? or double
J004232.56 + 415403.0	Reflection effect?	Non-eclipser	0.10312  days
J004751.47+340212.7	Large variations	Candidate non-eclipser	?
J005130.56 + 314555.9	Reflection effect?	Candidate non-eclipser	1.7 hours?
J010010.53 + 003739.1	Reflection effect?	Candidate non-eclipser	1.7 hours?
J011547.58 + 005350.0	Not many points	Candidate non-eclipser	1.2 hours?
J012549.89 + 330940.6	Variations	Non-eclipser	0.24244 days, or double
$J012550.48 \pm 280756.0$	Some faint points	Candidate new eclipser	?
J013157.96 + 084948.2	Reflection effect?	Candidate non-eclipser	2.3 hours?
J024924.77+071344.3	Variations	Non-eclipser	0.17334 days, or double
$J030308.35 \pm 005444.1$	Clear eclipser	Known eclipser [1]	0.13444 days
J042955.26 + 344734.3	Clear eclipser	New eclipser	0.30716 days
$1064959 81 \pm 424110 2$	Beflection effect?	Non-eclipser	0.24496 days
$1082145\ 27\pm455923\ 4$	Clear eclipser	Known eclipser [2]	0.50909 days
$108402885\pm5012382$	Variation	Candidate non-eclipser	1.2 hours? or double
$1085414\ 28\pm911148\ 9$	Reflection effect?	Non-eclipser	0.10215 dove
1085835 56J 981356 9	large variations	LARD?	0.10210 uays
1000812 04 060421 2	Clear colinsor	Known eclipsor [2]	0 14044 dovrs
1001916 27 + 924449 F	Beflection effect?	Non aclinear	0.14344 uays
$1091210.37 \pm 234442.3$	Kenection enect?	Non-eclipser	0.20500 days
J092712.02 + 284029.2	Variation	Candidate non-eclipser	3.1 nours! or double
J092741.73+332959.1	Clear eclipser	Known echpser [2]	2.30822 days
J093207.03 + 334805.9	Some faint points	Candidate new eclipser	1.7 days?
J093507.99+270049.2	Clear eclipser	Known eclipser [4]	0.20103 days
J093947.95+325807.3	Clear eclipser	Known eclipser [3]	0.33098 days
J094913.36+032254.5	Reflection effect?	Candidate non-eclipser	3.1 hours?
J095719.24 + 234240.7	Clear eclipser	Known eclipser [3]	0.15087 days
J095737.59 + 300136.5	Clear eclipser	Known eclipser [2]	1.92613 days
J101307.79 + 245713.1	Clear eclipser	Known eclipser [5]	0.12904 days
J104012.99 + 252559.9	Reflection effect?	Candidate non-eclipser	3.7 hours?
J110827.40+303031.3	Variation	Non-eclipser	0.81820 days, or double
J112007.64 + 250221.3	Some faint points	Candidate new eclipser	?
J112738.71+281532.7	Several faint points	Candidate new eclipser	?
J113102.81 + 522645.3	Variation	Candidate non-eclipser	2 hours? or double
J114224.71 - 022610.0	Variation	Non-eclipser	0.56112 days, or double
J114509.77 + 381329.2	Variation	Non-eclipser	0.19004  days,  or double
J114853.34 + 555217.0	Active star? Flares?	Active M dwarf?	?
J120020.81+363557.3	Some faint points	Candidate new eclipser	?
J121010.13+334722.9	Clear eclipser	Known eclipser [6]	0.12449  days
J121258.25-012309.9	Clear eclipser	Known eclipser [7]	0.33587  days
J122630.86+303852.5	Reflection effect?	Non-eclipser	0.25869 days
J123214.38+351324.8	Variation	Candidate non-eclipser	2.5 hours?
J132925.21+123025.4	Clear eclipser	Known eclipser [2]	0.08097 days
J134234.78+304849.2	Several faint points	Candidate new eclipser	1.66 days?
J135825.68+171204.1	Variation	Non-eclipser	0.16046 days, or double
J141811.97 + 204150.8	Reflection effect?	Candidate non-eclipser	2.6 hours?
J143547.87+373338.5	Clear eclipser	Known eclipser [8]	0.12563  davs
J143900.62 + 560219.0	Variation	Non-eclipser	0.34268 days, or double
J144307.83 + 340523.5	Shows big variations	Unclear	?
J144846.85+071304.3	Some faint points, real?	Candidate new eclipser	· ?
$J151426.90 \pm 285720.4$	Flares? CV?	Unclear	?
J152804 92+331012 1	Clear eclipser	New eclipser	: 0.21155 dave
$1154846\ 00\pm405798\ 7$	Clear eclipser	Known eclipser [8]	0.18552 days
1919300 40 + 040020 F	Many faint points	Candidate new colineer	0.10002 days
J212309.40+040929.0 1919591 09 010745 0	Reflection effect	Non aclinear	1 0.22022 dave
1022000 20 + 115707 0	Voniation	Non-eclipser	0.20302 uays
J233900.38+115707.2	Variation	Non-eclipser	0.12286 days, or double

[1] Parsons et al. (2013b); [2] Parsons et al. (2013a); [3] Drake et al. (2010); [4] Drake et al. (2014); [5] Parsons et al. (2015a); [6] Pyrzas et al. (2012); [7] Parsons et al. (2012b); [8] Pyrzas et al. (2009)



Figure 10. Left panels: CSS light curves folded over the best orbital period determinations (see right panels) of the two new eclipsing DA/M binaries identified in this work. Top right panel: the results of a standard Lomb-Scargle periodogram applied to the CSS photometry of J042955.26+344734.3, peaking at 3.25556 cycles/day (corresponding to a period of 0.30716 d). Bottom right panel: displayed are the results obtained applying a box-search method (see Section 8 for details) to the CSS photometry of J152804.92+331012.1, resulting in an orbital period of 0.21155 days.

one Na1 $\lambda\lambda$  8183.27, 8194.81 absorption doublet and one H $\alpha$  emission RV of an accuracy better than 20 km s<sup>-1</sup> for 685 and 477 WDMS binaries in our catalogue, respectively. For 607 and 408 WDMS binaries we managed to measure at least two Na1 and H $\alpha$  RVs, respectively. The RVs are provided in Table 3 (for completeness, we also provide the RVs we measured with accuracies worse than 20 km s<sup>-1</sup>).

We identified 89 and 103 objects displaying more than  $3\sigma$  NaI and H $\alpha$  RV variation, respectively. If we only take into account systems with RVs taken on different nights (337 objects for NaI, 229 objects for H $\alpha$ ), we obtain a PCEB fraction of ~26 per cent based on the NaI RV measurements, or ~ 45 per cent based on the H $\alpha$  RV measurements. The PCEB fraction derived from the NaI RV analysis agrees well with those obtained in previous works from the SDSS WDMS sample (e.g. Nebot Gómez-Morán et al. 2011; Rebassa-Mansergas et al. 2016a). It has to be noted that the higher PCEB fraction derived by analysing the H $\alpha$  RVs needs to be taken with caution. This is because H $\alpha$  RVs are less robust for detecting RV variations due to magnetic activity effects (Rebassa-Mansergas et al. 2008).

The total number of unique PCEBs we have identified that results from excluding duplicated targets from both the Na I and H $\alpha$  PCEB lists is 128. Among these, four were previously identified by Ren et al. (2014) within the LAMOST DR1 catalogue and 50 by Rebassa-Mansergas et al. (2016a) within the SDSS DR12 sample (we note that two were both detected within the LAMOST DR1 and SDSS DR12 catalogues). Thus, we are left with 76 new PCEB identifications in this work. In table 4 we provide the object names of these 76 PCEBs and in Figure 9 we show their maximum radial velocity shift vs. time span between the observed spectra. It is worth mentioning that in ~1/2 of the cases the time span is over 1000 days. This is due to the fact that we combine LAMOST and SDSS spectra to detect close binaries, thus resulting in time baselines as long as  ${\sim}15$  years.

#### 8 ECLIPSING WDMS SYSTEMS

Following the approach presented in Parsons et al. (2013a) and Parsons et al. (2015a), we cross-matched our LAMOST DR5 WDMS binary catalogue with the photometric data from the Catalina Sky Survey (CSS) and Catalina Real Time Transient Survey (CRTS Drake et al. 2009). This allowed detecting WDMS binaries displaying light curve variations. During this process the raw CSS data were re-reduced by us to identify deeply eclipsing systems and to remove contaminated exposures.

Among the 876 unique WDMS binaries that form the DR5 LAMOST catalogue, 687 were observed by the Catalina surveys, of which 630 did not display light curve variations. The remaining 57 objects include 16 eclipsing systems, two of which are new (see the light curves in Figure 10), 9 new eclipsing candidates, 14 objects displaying reflection effects or irradiation effects, 14 candidates for displaying reflection or irradiation effects, one candidate low-accretion rate polar, one candidate active M dwarf and two systems displaying light curve variations which we are not able to classify. We provide additional notes and our classification for these 57 objects in Table 5.

We calculated Scargle (1982) periodograms from the Catalina photometric data with the aim of measuring the orbital periods of the 57 objects displaying light curve variations. This is a suitable method when analysing light curves displaying out-of-eclipse variations due to reflection or ellipsoidal modulation effects (see an example in the top right panel of Figure 10). In the absence of such variations, i.e. only the eclipses are sampled by the CSS data, we employed the box fitting method outlined by Parsons et al. (2013a). We first identify the in-eclipse points from the raw light curve and fold the data over a given orbital period. From the folded data we identify the first and last in-eclipse points and count the number of out-of-eclipse points in between. This procedure is repeated over a large range of adopted orbital periods, being the correct determination the value that results in zero out-of-eclipse points. The number of out-ofeclipse points as a function of the adopted orbital period for our newly identified eclipsing system J152804.92+331012.1 is shown in the bottom right panel of Figure 10.

For 30 systems we were able to determine precise values of the orbital periods. In additional 15 cases, we could only derive estimates of the orbital periods due to insufficient information provided by the periodograms. We note that since, a priory, we do not know whether the light curve variations are due to reflection of irradiation effects for our non-eclipsing systems, there is a possibility that the orbital periods are double the measured ones. We include our measured values of the orbital periods in Table 5. We note that, for the two new eclipsing systems found here, we were not able to derive accurate RVs due to the low SN ratio of their spectra, thus they are not included in our PCEB list.

### 9 SUMMARY AND CONCLUSIONS

The catalogue of WDMS binaries from LAMOST DR5 contains 876 objects and it is  $\sim 8$  times larger than our previous DR1 sample. 357 of these systems ( $\sim 40$  per cent of the catalogue) are new identifications that have not been published before. Moreover, 339 were observed as part of a dedicated LAMOST survey for obtaining spectra of WDMS binaries photometrically selected within SDSS that are expected to contain cool WDs and/or early type M dwarf companions.

We determined the stellar parameters (white dwarf effective temperatures, surface gravities and masses, and M dwarf spectral types) of our systems following a decomposition/fitting routine, and we used the corresponding parameter distributions to analyse the intrinsic properties of the LAMOST DR5 sample. We found that the population of cool WDs remains under-represented. This is most likely due to the fact that cool ( $T_{\rm eff} \lesssim 10\,000$  K) WDs are systematically fainter and hence associated to lower SN ratio spectra. This increases considerably the probability for our decomposition/fitting method to determine WD parameters associated to large uncertainties and, as a consequence, these objects are not taken into account in our analysis.

We measured the Na1 $\lambda\lambda$ 8183.27, 8194.81 absorption doublet and the H $\alpha$  emission radial velocities of each object in our catalogue from their LAMOST DR5 as well as SDSS DR14 spectra (when available). We detected 128 systems (76 of which are new identifications) displaying more than  $3\sigma$  radial velocity variations and hence classify these objects as PCEBs. The close binary fraction we derived is ~26 per cent, in agreement with previous studies.

By cross-matching our catalogue with the Catalina Surveys we found 57 systems displayed light curve variations. Among these we identified 16 eclipsing systems, two of which are new, and nine additional eclipsing WDMS binary candidates. By analysing the periodograms calculated from the photometric data we were able to determine the orbital periods of 30 objects and estimate the orbital periods of 15 additional systems.

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- Anguiano B., Rebassa-Mansergas A., García-Berro E., Torres S., Freeman K. C., Zwitter T., 2017, MNRAS, 469, 2102
- Bours M. C. P., Marsh T. R., Parsons S. G., et al., 2016, MNRAS, 460, 3873
- Breedt E., et al., 2017, MNRAS, 468, 2910
- Camacho J., Torres S., García-Berro E., Zorotovic M., Schreiber M. R., Rebassa-Mansergas A., Nebot Gómez-Morán A., Gänsicke B. T., 2014, A&A, 566, A86
- Chui C. K., 1992, Wavelets: A tutorial in theory and applications Cojocaru R., Rebassa-Mansergas A., Torres S., García-Berro E., 2017, MNRAS, 470, 1442
- Cui X.-Q., et al., 2012, Research in Astronomy and Astrophysics, 12, 1197
- Davis P. J., Kolb U., Willems B., 2010, MNRAS, 403, 179
- De Marco O., Passy J.-C., Moe M., Herwig F., Mac Low M.-M., Paxton B., 2011, MNRAS, 411, 2277
- Deng L.-C., et al., 2012, Research in Astronomy and Astrophysics, 12, 735
- Drake A. J., et al., 2009, ApJ, 696, 870
- Drake A. J., et al., 2010, preprint, (arXiv:1009.3048)
- Drake A. J., et al., 2014, ApJS, 213, 9
- Farihi J., Hoard D. W., Wachter S., et al., 2010, ApJS, 190, 275
- Gänsicke B. T., et al., 2009, MNRAS, 397, 2170
- Gentile Fusillo N. P., et al., 2015, MNRAS, 452, 765
- Han Z., Podsiadlowski P., Maxted P. F. L., Marsh T. R., Ivanova N., 2002, MNRAS, 336, 449
- Han Z., Podsiadlowski P., Maxted P. F. L., Marsh T. R., 2003, MNRAS, 341, 669
- Han Z., Podsiadlowski P., 2004, MNRAS, 350, 1301
- Heller R., Homeier D., Dreizler S., Østensen R., 2009, A&A, 496, 191
- Heber U., 2016, PASP, 128, 082001
- Iben Jr. I., Livio M., 1993, PASP, 105, 1373
- Kepler S. O., et al., 2015, MNRAS, 446, 4078
- Kilic M., Brown W. R., Gianninas A., Curd B., Bell K. J., Allende Prieto C., 2017, MNRAS, 471, 4218
- Koester D., 2010, Mem. Soc. Astron. Italiana, 81, 921
- Koester D., Kepler S. O., Kleinman S. J., Nitta A., 2009, in Journal of Physics Conference Series. p. 012006 (arXiv:0812.0491), doi:10.1088/1742-6596/172/1/012006
- Langer N., Deutschmann A., Wellstein S., Höflich P., 2000, A&A, 362, 1046
- Li L., Zhang F., Han Q., Kong X., Gong X., 2014, MNRAS, 445, 1331
- Liu C., Li L., Zhang F., Zhang Y., Jiang D., Liu J., 2012, MNRAS, 424, 1841
- Liu X.-W., et al., 2014, in Feltzing S., Zhao G., Walton N. A., Whitelock P., eds, IAU Symposium Vol. 298, Setting the scene for Gaia and LAMOST. pp 310–321 (arXiv:1306.5376), doi:10.1017/S1743921313006510
- Luo A.-L., et al., 2012, Research in Astronomy and Astrophysics, 12, 1243
- Luo A.-L., et al., 2015, Research in Astronomy and Astrophysics, 15, 1095
- Marsh T. R., et al., 2014, MNRAS, 437, 475
- Miszalski B., Acker A., Moffat A. F. J., et al., 2009, A&A, 496, 813
- Nebot Gómez-Morán A., et al., 2009, A&A, 495, 561
- Nebot Gómez-Morán A., et al., 2011, A&A, 536, A43
- Pala A. F., et al., 2017, MNRAS, 466, 2855
- Parsons S. G., et al., 2012a, MNRAS, 419, 304  $\,$
- Parsons S. G., et al., 2012b, MNRAS, 420, 3281
- Parsons S. G., et al., 2013a, MNRAS, 429, 256

Parsons S. G., Marsh T. R., Gänsicke B. T., Schreiber M. R., Bours M. C. P., Dhillon V. S., Littlefair S. P., 2013b, MNRAS, 436, 241

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- Parsons S. G., et al., 2014, MNRAS, 438, L91  $\,$
- Parsons S. G., et al., 2015a, MNRAS, 449, 2194
- Parsons S. G., et al., 2015b, MNRAS, 452, 1754
- Parsons S. G., et al., 2017, MNRAS, 470, 4473
- Passy J.-C., et al., 2012, ApJ, 744, 52
- Pyrzas S., et al., 2009, MNRAS, 394, 978
- Pyrzas S., et al., 2012, MNRAS, 419, 817
- Pyrzas S., et al., 2015, MNRAS, 447, 691
- Rebassa-Mansergas A., Gänsicke B. T., Rodríguez-Gil P., Schreiber M. R., Koester D., 2007, MNRAS, 382, 1377
- Rebassa-Mansergas A., et al., 2008, MNRAS, 390, 1635
- Rebassa-Mansergas A., Gänsicke B. T., Schreiber M. R., Koester D., Rodríguez-Gil P., 2010, MNRAS, 402, 620
- Rebassa-Mansergas A., Nebot Gómez-Morán A., Schreiber M. R., Girven J., Gänsicke B. T., 2011, MNRAS, 413, 1121
- Rebassa-Mansergas A., Nebot Gómez-Morán A., Schreiber M. R., Gänsicke B. T., Schwope A., Gallardo J., Koester D., 2012a, MNRAS, 419, 806
- Rebassa-Mansergas A., et al., 2012b, MNRAS, 423, 320
- Rebassa-Mansergas A., Schreiber M. R., Gänsicke B. T., 2013a, MNRAS, 429, 3570
- Rebassa-Mansergas A., Agurto-Gangas C., Schreiber M. R., Gänsicke B. T., Koester D., 2013b, MNRAS, 433, 3398
- Rebassa-Mansergas A., Ren J. J., Parsons S. G., Gänsicke B. T., Schreiber M. R., García-Berro E., Liu X.-W., Koester D., 2016a, MNRAS, 458, 3808
- Rebassa-Mansergas A., et al., 2016b, MNRAS, 463, 1137
- Rebassa-Mansergas A., Parsons S. G., García-Berro E., Gänsicke B. T., Schreiber M. R., Rybicka M., Koester D., 2017, MNRAS, 466, 1575
- Ren J., Luo A., Li Y., Wei P., Zhao J., Zhao Y., Song Y., Zhao G., 2013, AJ, 146, 82
- Ren J. J., et al., 2014, A&A, 570, A107
- Renedo I., Althaus L. G., Miller Bertolami M. M., Romero A. D., Córsico A. H., Rohrmann R. D., García-Berro E., 2010, ApJ, 717, 183
- Richards G. T., et al., 2002, AJ, 123, 2945
- Ricker P. M., Taam R. E., 2012, ApJ, 746, 74
- Scargle J. D., 1982, ApJ, 263, 835
- Schleicher D. R. G., Dreizler S., Völschow M., Banerjee R., Hessman F. V., 2015, Astronomische Nachrichten, 336, 458
- Schreiber M. R., Gänsicke B. T., Southworth J., Schwope A. D., Koester D., 2008, A&A, 484, 441
- Schreiber M. R., et al., 2010, A&A, 513, L7
- Silvestri N. M., et al., 2006, AJ, 131, 1674
- Skinner J. N., Morgan D. P., West A. A., Lépine S., Thorstensen J. R., 2017, AJ, 154, 118
- Smolčić V., et al., 2004, ApJ, 615, L141
- Stoughton C., et al., 2002, AJ, 123, 485
- Su D.-Q., Cui X.-Q., 2004, Chinese J. Astron. Astrophys., 4, 1
- Toonen S., Nelemans G., 2013, A&A, 557, A87
- Tremblay P.-E., Ludwig H.-G., Steffen M., Bergeron P., Freytag B., 2011, A&A, 531, L19
- Tremblay P.-E., Ludwig H.-G., Steffen M., Freytag B., 2013, A&A, 559, A104
- Veras D., Xu S., Rebassa-Mansergas A., 2018, MNRAS, 473, 2871
- Wang B., Han Z., 2012, New Astron. Rev., 56, 122
- Wang B., Li X.-D., Han Z.-W., 2010, MNRAS, 401, 2729
- Wang S.-G., Su D.-Q., Chu Y.-Q., Cui X., Wang Y.-N., 1996, Appl. Opt., 35, 5155
- Webbink R. F., 2008, in Milone E. F., Leahy D. A., Hobill D. W., eds, Astrophysics and Space Science Library Vol. 352, Astrophysics and Space Science Library. p. 233 (arXiv:0704.0280), doi:10.1007/978-1-4020-6544-6\_13
- Willems B., Kolb U., 2004, A&A, 419, 1057
- Xiang M.-S., et al., 2017, MNRAS, 467, 1890
- Yanny B., et al., 2009, AJ, 137, 4377
- York D. G., et al., 2000, AJ, 120, 1579

- Yuan H.-B., et al., 2015, MNRAS, 448, 855
- Zhao G., Zhao Y.-H., Chu Y.-Q., Jing Y.-P., Deng L.-C., 2012, Research in Astronomy and Astrophysics, 12, 723
- Zorotovic M., Schreiber M. R., 2013, A&A, 549, A95
- Zorotovic M., Schreiber M. R., Gänsicke B. T., Nebot Gómez-Morán A., 2010, A&A, 520, A86
- Zorotovic M., Schreiber M. R., García-Berro E., Camacho J., Torres S., Rebassa-Mansergas A., Gänsicke B. T., 2014, A&A, 568, A68
- Zorotovic M., et al., 2016, MNRAS, 457, 3867
- de Kool M., 1992, A&A, 261, 188

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