

# Wind Tunnel Testing Airfoils at Low Reynolds Numbers

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This paper describes the wind tunnel testing methodology that has been applied to testing over 200 airfoils at low Reynolds numbers (40,000 to 500,000). The experiments were performed in the 2.8×4.0 ft (0.853×1.219 m) low-turbulence wind tunnel in the Subsonic Aerodynamics Research Laboratory at the University of Illinois at Urbana-Champaign (UIUC). The test apparatus, methodology, and data reduction techniques are described in detail, and the measurements are validated against benchmark data. New results on the AG455ct airfoil with a large 30%-chord flap, deflected over a wide range, are presented. The results show a dramatic increase in drag with higher flap deflections, and the flap efficiency reduces with large deflections up to 40 deg. Also, tests on a flat-plate airfoil with leading edge serration geometries were conducted to explore the effects on stall characteristics. The results support the conclusions of other researchers that leading edge serrations (protuberances like those found on the fins/flippers of some aquatic animals) lead to higher lift and softer stall. The results suggest that these characteristics are accompanied by lower drag in the stall and post-stall range.

## I. Introduction

Airfoil performance at low Reynolds numbers impacts the performance of a wide range of systems. The expanding role of unmanned aerial vehicles (UAVs) into unmanned aircraft systems (UAS) in military use<sup>1,2</sup> has led to growing interest in subsonic low Reynolds number aerodynamics.<sup>3-5</sup> Low Reynolds number aerodynamics of airfoils also apply to a host of other applications such as wind turbines,<sup>6-8</sup> motorsports, high altitude aircraft and propellers, natural flyers,<sup>9</sup> and subscale testing of many full scale systems.

Accurate measurements of low Reynolds number airfoil performance is key to understanding and improving the efficiency of low Reynolds number systems. Most aerodynamic performance measurement techniques for airfoils rely on using balance systems or pressure systems, or a combination of both.<sup>10-12</sup> The approach described in this paper uses a force balance approach to obtain lift and moment data and the wake rake method to obtain drag. Sections II and III of this paper describe this experimental approach and validation. Section IV presents first, data on an airfoil with large flap deflections, and second, data on a flat-plate airfoil as compared with one having a range of leading-edge serration geometries. The paper ends with conclusions that can be drawn from this research.

## II. Wind Tunnel Facility and Measurement Techniques

This section presents detailed descriptions of the UIUC low-turbulence subsonic wind tunnel facility, test section flow quality, lift, drag and moment measurement techniques, data acquisition equipment, and data reduction procedures that have been documented in Refs. 6,13-16.

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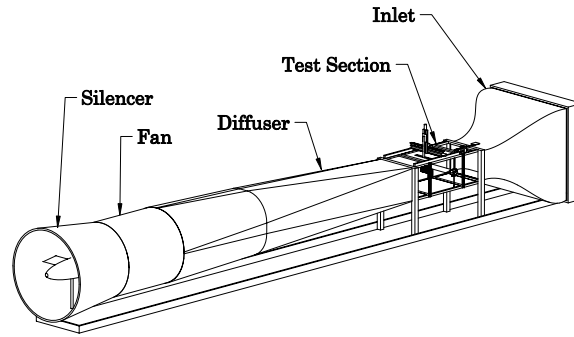


Figure 1. UIUC low-speed subsonic wind tunnel.

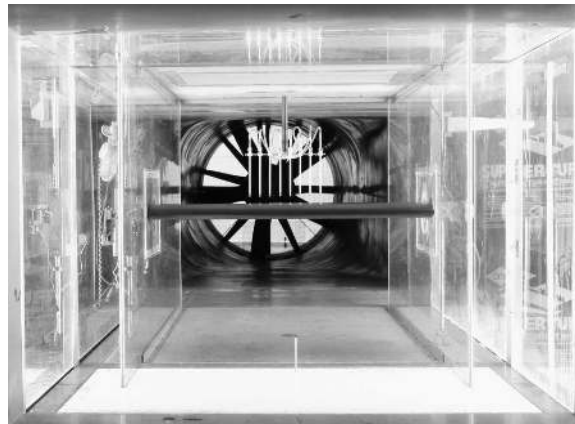


Figure 2. Photograph of wind-tunnel test section.

### A. Experimental Facility and Flow Quality Measurements

The low Reynolds number airfoil performance measurements described here were conducted in the UIUC low-turbulence subsonic wind tunnel shown in Fig. 1. The wind tunnel is an open-return type with a 7.5:1 contraction ratio. The rectangular test section is nominally  $2.8 \times 4.0$  ft ( $0.853 \times 1.219$  m) in cross section and 8-ft (2.438-m) long. Over the length of the test section, the width increases by approximately 0.5 in. (1.27 cm) to account for boundary-layer growth along the tunnel sidewalls. Test-section speeds are variable up to 160 mph (71.53 m/s) via a 125-hp (93.25-kW) AC motor connected to a five-bladed fan. For a Reynolds number of 500,000 based on an airfoil chord of 1 ft (0.305 m), the resulting nominal test-section speed is 80 ft/sec (24.38 m/s). Photographs of the test section and fan are presented in Figs. 2 and 3

Since low Reynolds number airfoil performance is highly dependent on the behavior of the laminar boundary layer, low turbulence levels within the wind-tunnel test section are necessary to ensure that laminar flow does not prematurely transition to turbulent flow. In order to ensure good flow quality in the test section, the wind-tunnel settling chamber contains a 4-in. (10.16-cm) thick honeycomb in addition to four anti-turbulence screens, which can be partially removed for cleaning. The turbulence intensity was measured and previously reported to be less than 0.1%,<sup>17</sup> which is sufficient for low Reynolds number airfoil measurements. Subsequent detailed measurements are show later in this section.

The experimental setup is depicted in Fig. 4. For the current tests, the 12-in. (0.305-m) chord, 33 5/8-in. (0.855-m) long airfoil models were mounted horizontally between two 3/8-in. (0.953-cm) thick, 6-ft (1.829-m) long Plexiglas<sup>®</sup> splitter plates to isolate the ends of the model from the tunnel side-wall boundary layers and the support hardware. For clarity, the Plexiglas splitter plates and the traverse enclosure box are not shown in Fig. 4. Gaps between the model and Plexiglas were nominally 0.05 in. (1.27 mm). The left-hand side of

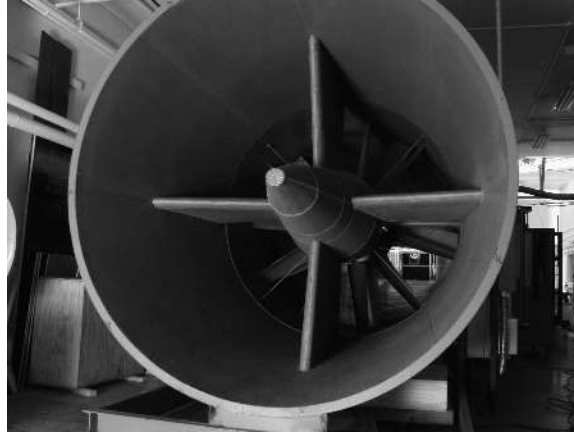


Figure 3. Photograph of wind-tunnel exit fan.

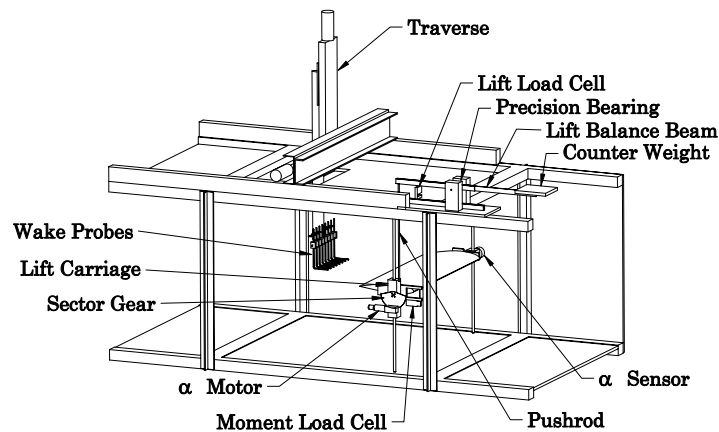


Figure 4. Experimental setup (Plexiglas<sup>®</sup> splitter plates and traverse enclosure box not shown for clarity).

the model was free to pivot (far side of Fig. 4). At this location, the angle of attack was measured using a precision potentiometer. The right-hand side of the airfoil model was connected to the lift carriage through two steel wing rods that passed through the wing-rod fixture and were anchored to the model through two set screws. At this side, the airfoil model was free to move vertically on a precision ground shaft, but not free to rotate. The lift carriage was linked to a custom load beam, as described later. Linear and spherical ball bearings within the lift carriage helped to minimize any frictional effects.

The two-axis traverse can be seen in Fig. 4, positioned above the wind-tunnel test section. Not shown is the pressure-sealed box that encloses the traverse system. The traverse was manufactured by LinTech and consists of horizontal and vertical screw-type linear positioning rails that operate in combination with two computer-controlled stepper motors. The rails are equipped with linear optical encoders that supply a feedback signal to the motor controller allowing the traverse to operate with virtually no error. Attached to the traverse is a 3-ft (0.914-m) long boom that extends down into the wind tunnel test section to support the eight side-by-side wake pitot probes [spaced 1.5 in. (3.81-cm) apart in the spanwise direction].

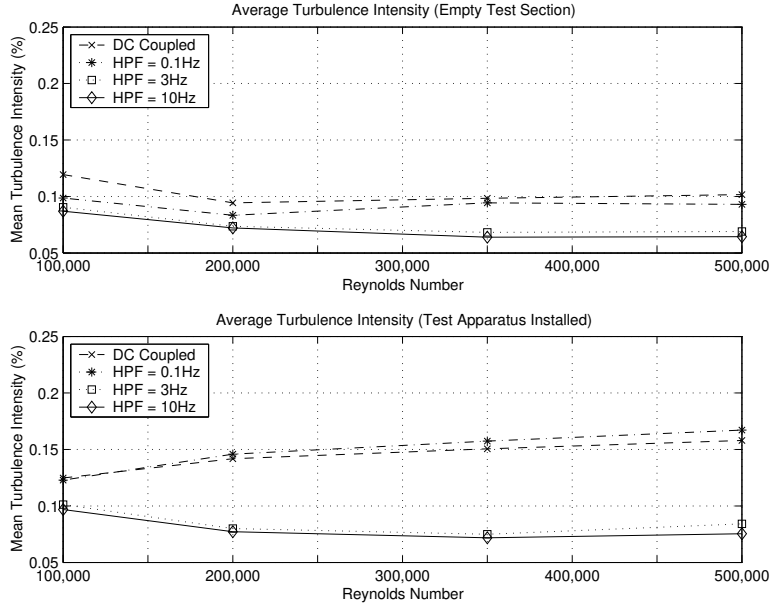


Figure 5. Turbulence intensity at tunnel centerline, empty test section and with rig in place.

### 1. Turbulence Intensity

The turbulence intensity was previously documented;<sup>17</sup> however, those measurements were with an empty tunnel test section. It is of interest to examine what effect, if any, the splitter plates and other test section components have on the turbulence intensity.

The turbulence intensity was measured using hot-wire anemometry. In particular, the hot-wire system was a TSI Incorporated IFA 100 anemometer in conjunction with a TSI Model 1210-T1.5 hot-wire probe. The probe makes use of a 1.5 micron platinum-coated tungsten wire. The probe was mounted in the tunnel end-flow orientation with the wire perpendicular to the tunnel floor in order to measure the axial turbulence intensity. A PC equipped with a data acquisition card was used to log the signal from the anemometer. A Hewlett-Packard HP 35665A Dynamic Signal Analyzer, which performed an FFT (Fast Fourier Transform) analysis, was employed to allow the turbulence spectrum to be monitored over a broad range of frequencies.

The hot-wire probe was calibrated in the UIUC low-speed subsonic wind tunnel. The tunnel speed was set using static pressure probes inside the tunnel, and the corresponding (average) output of the anemometer was recorded. From these data, a curve fit was generated that was used to measure the fluctuating velocity with the hot-wire probe. Corrections were made to the signal to account for changes in temperature and density between the time the probe was calibrated and the time the measurements were made. A more detailed description of the methods used is found in Ref. 18.

The turbulence intensity was calculated from data using a total of 50,000 samples with a sample frequency of 10,000 Hz and is shown in Fig. 5 for the case in which the tunnel was empty and that in which the full measurement apparatus was installed. As compared with the baseline empty tunnel, turbulence levels observed with the test apparatus installed are relatively unchanged at  $Re = 100,000$  but increase at higher Reynolds numbers. These effects all but disappear when the high-pass filter is set above 3 Hz. The main effect of the test rig appears to be added velocity fluctuations in the very low frequency range. Figure 6 shows the power spectra between 0 and 100 Hz for the  $Re = 350,000$  case both for the empty tunnel and for that with the test apparatus installed. Measurements were taken over a wide range of frequencies (up to 6,400 Hz), but in all cases the interesting features ranged between 0 and 100 Hz. Apart from the peaks in power at 56 and 79 Hz, the turbulent power spectrum is similar in magnitude for both configurations. It is only in the range from 0 to 25 Hz that there is a noticeable offset between the empty-tunnel test section and the installed-apparatus section. In general, these turbulence levels are considered to be sufficiently low for taking low Reynolds number airfoil measurements.

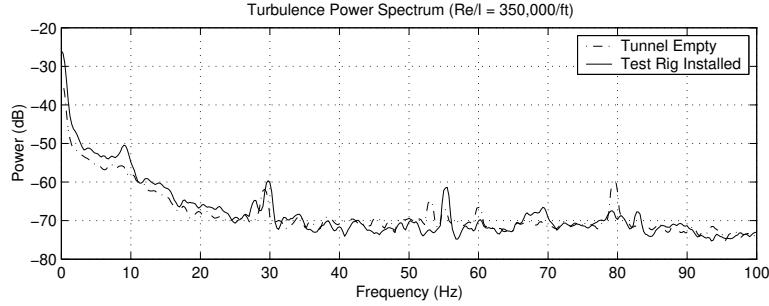


Figure 6. Power spectrum comparison between empty tunnel and installed test apparatus cases for  $Re = 350,000$ .

## 2. Freestream Velocity

The variation of velocity in the test section of the UIUC low-speed subsonic wind tunnel was obtained by comparing the dynamic pressure (directly related to velocity) at a pitot-static probe mounted near the entrance of the splitter plates with that measured by a downstream probe. The upstream probe was located at the centerline of the tunnel in the spanwise direction ( $X = 0$ ), 0.97 ft (0.296 m) below the centerline of the tunnel in the vertical direction [ $Y = -11.66$  in. (0.296 m)], and 1.323 ft (0.403 m) upstream of the quarter-chord location of the airfoil model when mounted in the test section. The downstream probe was traversed in the  $X$ - $Y$  plane perpendicular to the freestream and coincident with the quarter chord. Measurements were made both with the test section empty and with the test apparatus installed.

The measurement plane extended from 5.5 in. (13.97 cm) above the tunnel centerline to 14.5 in. (36.83 cm) below in the vertical direction  $Y$ , and from 10.5 in. (26.67 cm) to the left of the tunnel centerline to 10.5 in. (26.67 cm) to the right in the horizontal direction  $X$ . A grid spacing of 1 in. (2.54 cm) was used for the measurements, resulting in a total of 462 measurement points for each case tested.

Three differential-pressure transducers were used for the measurements. One transducer measured the upstream dynamic pressure  $Q_u$  by measuring the pressure difference across the total pressure and static pressure ports of a pitot-static probe. A second pressure transducer was configured to measure the difference between the upstream and downstream total pressure  $\Delta P_0$ . A third transducer was configured to measure the difference between the upstream and downstream static pressure  $\Delta p$ . The change in dynamic pressure  $\Delta Q$  is just  $\Delta P_0 - \Delta p$ . Thus, the local dynamic pressure at each point is therefore

$$Q = Q_u + \Delta Q = Q_u + \Delta P_0 - \Delta p \quad (2.1)$$

For each Reynolds number tested, the tunnel speed was set using the upstream probe as the reference. Differences in temperature and ambient pressure were accounted for. The percent difference at each point was calculated according to

$$\Delta Q(\%) = \frac{Q - Q_u}{Q_u} \times 100\% \quad (2.2)$$

Figure 7 shows contours of  $\Delta Q$  for various Reynolds numbers plotted against its  $X$  and  $Y$  location for the case in which the wind tunnel was empty. For comparison, Fig. 8 shows  $\Delta Q$  plotted against its  $X$  and  $Y$  location with the test rig installed.

From Figs. 7 and 8, several observations can be made. First, for the empty test section case, there is a slight decrease in the test section flow speed at the location of the model relative to the upstream probe. When the test rig is installed, there is instead an increase in the flow speed. It is likely that the velocity measured at the location of the model is higher than the upstream velocity because of the growth of the boundary layer along the splitter plates, ceiling and floor as well as the blockage that occurs between the splitter plates and the tunnel sidewalls. This percentage increase in the flow speed grows larger as the Reynolds number is reduced, which is consistent with the thicker wall boundary layers at lower Reynolds numbers. As discussed later, this rise in velocity is accounted for in the airfoil-performance data-reduction procedure. Second, over the region where the model is located, the net change in flow speed is observed to

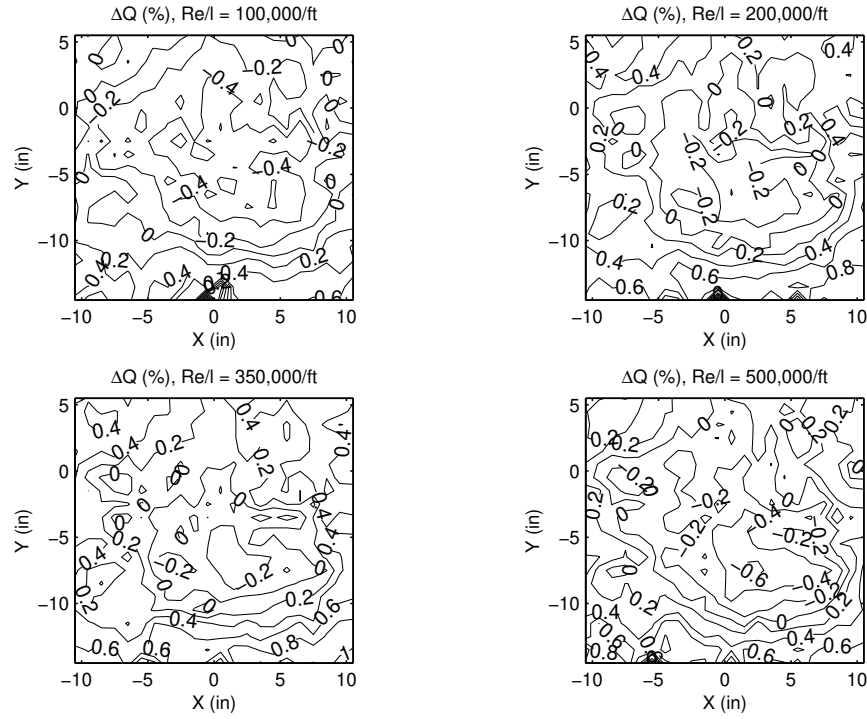


Figure 7. Dynamic pressure variation across the test section when empty.

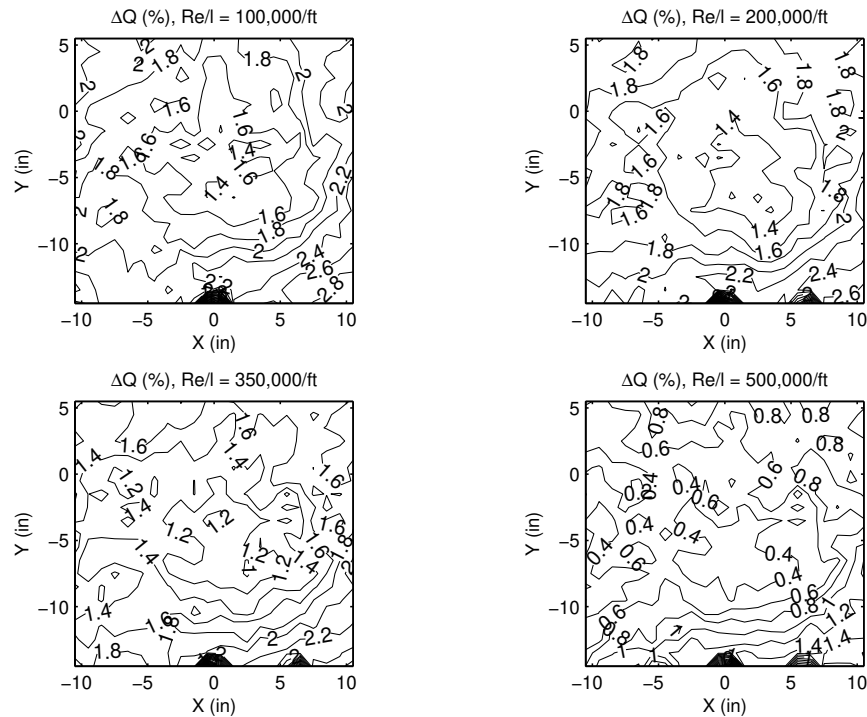
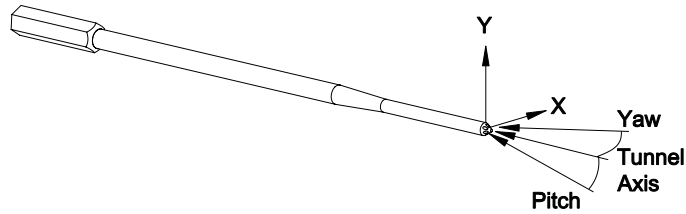


Figure 8. Dynamic pressure variation across the test section with the experimental rig installed.

be relatively small. For instance, Fig. 8 shows that at  $Re/l = 200,000/ft$  (656,168/m), the increase in the flow speed varies from approximately 1.4% to 1.8%, which is a relative difference of  $\pm 0.2\%$  in the working



**Figure 9.** Illustration of the seven-hole probe used for flow angle measurements.

range of the test section. As stated in Ref. 19, it is desirable for the variation in dynamic pressure in the working range of the test section to be less than 0.5% from the mean, i.e.,  $\pm 0.5\%$ . The results show that the flow is well within the “rule of thumb.” A third observation is the existence of a slight asymmetry in the flow, noticeable mainly in the  $+X:-Y$  quadrant (bottom right corner in Figs. 7 and 8). The asymmetry is present with the tunnel empty and with the test rig in place; hence, it is unrelated to the test rig. Moreover, the lines of constant  $Q$  are parallel to the tunnel floor at  $X = 0$  (centerline), so the effect is negligible with respect to the performance-measurement quantities in the center region of the test section.

### 3. Freestream Flow Angularity

Just as it is important to have uniform flow velocity in the wind-tunnel test section, it is equally important to have the flow parallel to the axial direction.<sup>19</sup> For the most part, pitot-static probes are insensitive to flow angles in the range of  $\pm 12$  deg, so a large flow angle is required to introduce an error in the dynamic pressure measurements. Similarly, large flow angles are required to introduce errors into total head measurements. Apart from pressure measurements, a small change in pitch angle contributes to a change in the effective angle of attack of the airfoil model, and thereby such an error can skew the lift and drag measurements when they are plotted versus the angle of attack.

The flow angularity in the test section of the UIUC low-speed subsonic wind tunnel was measured using an Aeroprobe Corporation Model S7TC317 seven-hole probe as shown in Fig. 9. The probe has a total-head port located at the center, and six chamfered ports were equally spaced circumferentially around the center. Each port of the seven-hole probe was connected to the high-pressure side of an MKS Model 220CD 1-mm Hg pressure transducer. The reference side of each pressure transducer was left open to ambient pressure. The probe was mounted in the wind tunnel on a special two-beam sting attached to the computer-controlled LinTech traverse. The flow measurements were all taken with the test rig installed in the wind-tunnel test section, without the model. A more detailed description of the use of the seven-hole probe is found in Ref. 20.

The seven-hole probe was traversed in a plane perpendicular to the freestream flow over the range from  $X = \pm 6.5$  in. (16.51 cm) to  $Y = \pm 10$  in. (25.4 cm). The traverse was not extended to the edges of the test section because of equipment limitations. Traversing this central core was acceptable because one would expect to find the largest flow angle variation in the center of the test section rather than along the walls, where at a minimum the flow is parallel to the wall (yaw or pitch is thereby zero). A grid spacing of 1 in. (2.54 cm) was used, resulting in a grid of 252 sample locations for each case tested. The seven-hole probe tip was located approximately 1.5 chord lengths behind the quarter chord of the airfoil model. To set the tunnel speed, one pitot-static probe was located at  $X = 0$ ,  $Y = -11.66$  in. (29.62 cm). For redundancy, an additional probe was located at  $X = 5$  in. (12.7 cm),  $Y = -11.66$  in. (29.62 cm). Both pitot-static probes were mounted at the same streamwise location, 1.323 ft (3.36 cm) upstream of the location of the quarter chord of the airfoil model.

Calibration curves supplied by the probe manufacturer were used to determine the flow angle at each location. Three such curves were provided, each of which covers a particular angle of attack range, namely, 0 to 5 deg, 5 to 10 deg, or 10 to 15 deg. Because the flow angles measured never exceeded 1 deg, only the first curve was needed. Figures 10–12 show the measured flow angle at each point plotted against its  $X$  and  $Y$  coordinate.

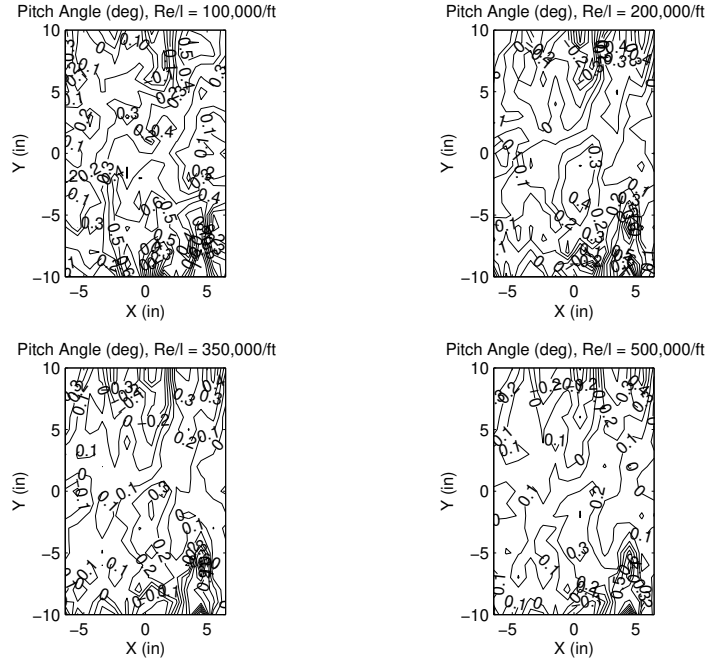


Figure 10. Pitch angle variation across the test section with the experimental rig installed.

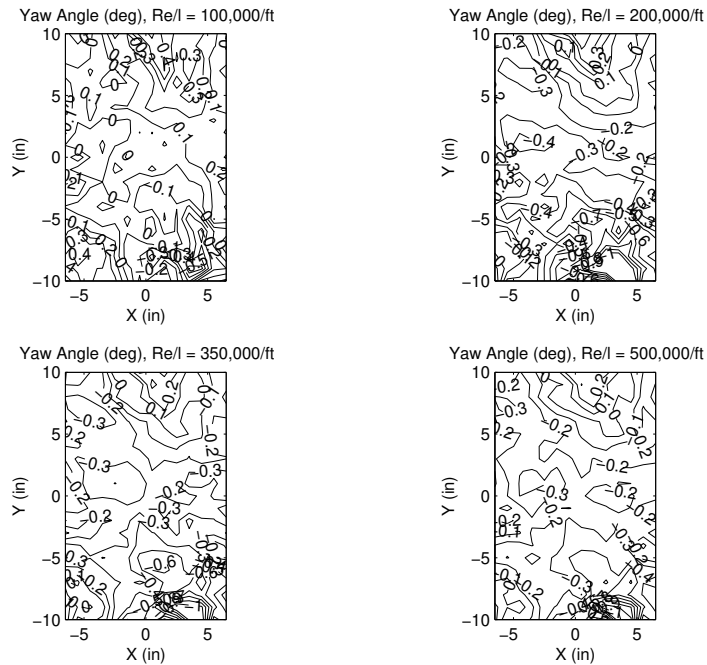


Figure 11. Yaw angle variation across the test section with the experimental rig installed.

The contour plots of flow angle in the test section show that pitch and yaw angles are smallest at  $Re = 500,000$ , becoming more pronounced at lower Reynolds numbers. Pitch angle, the more important angle for airfoil testing, is generally between 0 and 0.2 deg ( $\pm 0.1$  deg) across the working region of the test section where the airfoil model is located. According to Ref. 19, a flow angle variation of  $\pm 0.2$  deg is acceptable, but  $\pm 0.1$  deg or better is the preferred. The current measurements meet this latter desired level of flow quality.



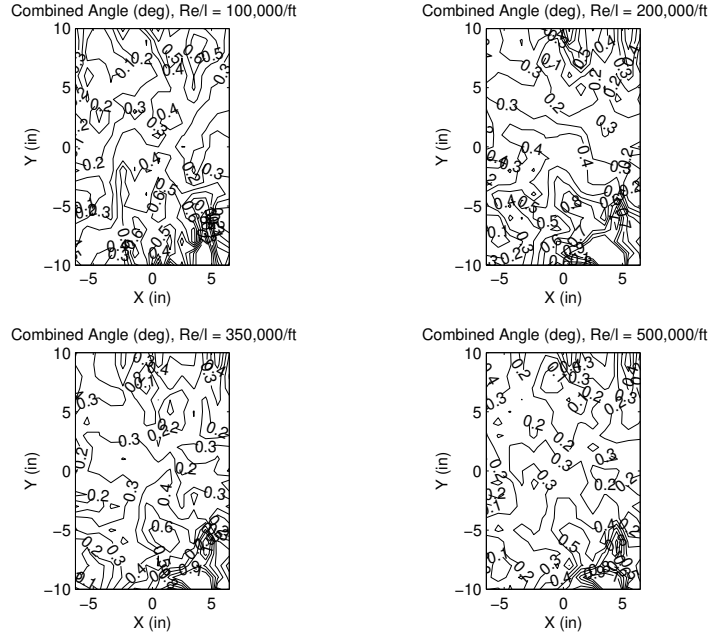


Figure 12. Combined pitch and yaw angle across the test section with the experimental rig installed.

It is worth noting that downstream of the pitot-static probes placed near the floor, relatively large flow angles were recorded locally. Flow angle perturbations due to probes near the wall, such as the dynamic pressure probes used to determine the flow speed during the airfoil tests, are of no concern because the corresponding flow is well below the working region of the test section where the model is located.

## B. Airfoil Models

In order to determine the accuracy of the wind-tunnel models, most all models that have been tested are digitized using a coordinate measuring machine (CMM) to determine the actual airfoil shape at the midsection of the model. Approximately 80 coordinates points are typically taken around the airfoil. The spacing is more or less proportional to the local curvature. Near the leading and trailing edges the spacing used is relatively small and then larger over the airfoil midsection. Measurements such as these can be found in Refs. <sup>13–16</sup>.

## C. Performance Data Measurement Techniques

As an overview to this section, the data acquisition process, which was largely choreographed by computer control, is briefly described. Two types of runs were performed: “lift runs” and “drag runs.” For the former, only lift and moment vs angle of attack data were taken for a fixed Reynolds number; whereas for the latter, drag data were included. Lift runs were extended to high angle of attack and sometimes into stall; drag runs were set to take data nominally over the low drag range, which for this work was defined as  $C_d$  approximately less than 0.05. For lift runs, data were taken for both increasing and decreasing angles of attack to document any aerodynamic hysteresis present. For drag runs, data were taken only for increasing angles of attack. For each angle of attack, the tunnel speed was checked and, if necessary, adjustments were made to maintain a fixed Reynolds number. In general, acquiring data during a lift run was a relatively quick process compared with acquisition during a drag run. Since no wake measurements were taken during a lift run, it was possible, for instance, to cover a full angle of attack range from  $-10$  to  $20$  deg and back in  $1$  deg increments in approximately  $20$  min. For a drag run, however, the time could range from  $1$  to  $6$  hr, depending principally on the width of the wake and desired angle of attack range. Details pertaining to the lift, drag, and moment measurements are described in more detail in the following sections.

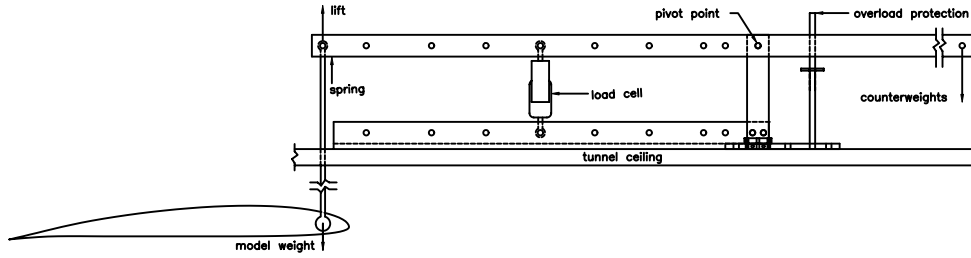


Figure 13. Lift beam balance assembly as viewed from the working side of the test section.

### 1. Lift Force Measurement

Figure 13 depicts a schematic of the lift beam balance that was integrated into the test section and oriented according to Fig. 4. The lift apparatus consisted primarily of a fulcrum supported beam restrained in rotation by a strain-gauge load cell. The lift load acting through a pushrod was applied to the beam and transferred to the load cell via a lever arrangement, as shown. For correct operation of the lift balance, the load cell was required to be in tension. To ensure this outcome, spring tension on the lift side of the beam and counterweight on the opposite end were used, and the amount of each depended on the model weight as well as the range of loads expected. Moreover, the mix of spring tension and counterweight changed in going from a calibration to a performance data run.

Depending on the Reynolds number of the test and expected range in lift coefficient, one of three possible load cells (Interface Inc. Models SM-10, SM-25, and SM-50) was inserted into one of nine possible load cell attachment holes, allowing for a variation in the operational range of the lift beam balance. This approach offered the ability to measure the small forces present at the lower Reynolds numbers range ( $Re \approx 60,000$ ) while retaining the capability to handle the larger lift forces occurring at the higher Reynolds numbers ( $Re \approx 500,000$ ). The resulting lift measurements were repeatable to within 0.01% of the rated output of the particular load cell used. Calibrations were performed frequently to minimize the effects of drift.

### 2. Drag Force Measurement

While the lift force on airfoils at low Reynolds numbers can be obtained with acceptable accuracy through a lift balance, drag force is often considerably much lower than the lift. As a result, profile drag is often best obtained by the momentum method instead of a force balance. For the current tests, the profile drag was determined through the method developed by Jones<sup>21</sup> (taken from Schlichting<sup>22</sup>).

After application of the two-dimensional momentum and continuity equations to a control volume shown in Fig. 14, the drag force per unit span can be calculated from

$$d = \rho \int_{-\infty}^{\infty} u_1(V_{\infty} - u_1)dy \quad (2.3)$$

Assuming that the location of the measurements is far enough behind the airfoil so that the static pressure has returned to upstream tunnel static pressure (i.e.,  $P_{s,1} = P_{s,\infty} = P_s$ ) and that the downstream flow outside the airfoil wake proceeds without losses (i.e., the total pressure remains constant along every streamline), the total pressure relationships from Bernoulli's equation are

$$P_s + \frac{1}{2}\rho u_1^2 = P_{0,1} \quad (2.4)$$

$$P_s + \frac{1}{2}\rho V_{\infty}^2 = P_{0,\infty} \quad (2.5)$$

Applying the above relationships to Eq. (2.3) and simplifying yields

$$d = 2 \int_{-\infty}^{\infty} \{ \sqrt{P_{0,1} - P_s} \sqrt{q_{\infty} - P_s} - (P_{0,1} - P_s) \} dy \quad (2.6)$$

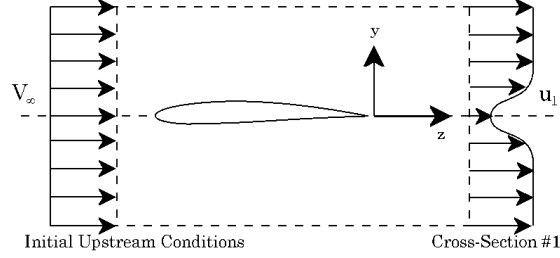


Figure 14. Control volume for the 2-D momentum deficit method to determine the profile drag.

$$P_{0,1} - P_s = P_{0,1} - P_s - P_{0,\infty} + P_{0,\infty} = q_\infty - \Delta P_0 \quad (2.7)$$

$$d = 2 \int_{-\infty}^{\infty} \sqrt{q_\infty - \Delta P_0} (\sqrt{q_\infty} - \sqrt{q_\infty - \Delta P_0}) dy \quad (2.8)$$

During the tests, to ensure that the wake had relaxed to tunnel static pressure, the wake measurements were performed 14.8 in (approximately 1.25 chord lengths) downstream of the trailing edge of the airfoil. Each vertical wake traverse consisted of between 20 and 80 total-head pressure measurements per probe (depending on wake thickness) with points nominally spaced 0.08 in. (2.03 mm) apart.

Pressure measurements within the wake were made using MKS Baratron Model 220 variable-capacitance differential pressure transducers with a full-scale range of 1-mm Hg (0.02 psia), having a resolution of 0.01% of full-scale reading and an accuracy of 0.15% of reading. All of the transducers were factory calibrated prior to the tests and checked during the tests.

In order to obtain an accurate value for the drag coefficient, wake profile measurements were taken at eight spanwise locations spaced 1.5 in. (3.81 cm) apart over the center 10.5 in. (26.67 cm) span of the model. The resulting eight drag coefficients were then averaged to obtain the drag at a given angle of attack. Figure 15 depicts a typical variation in the spanwise drag coefficient at Reynolds numbers from 100,000 to 500,000. For  $Re = 100,000$ , a component of the variation could be attributed to “scatter,” which is partly due to the unsteadiness in the wake and the difficulty in resolving such small pressure differences. At the higher  $Re$ 's, however, an intrinsic steady-state variation is present. For the interested reader, more documentation of this phenomenon is presented in Refs. 23 and 24.

### 3. Pitching Moment Measurement

Figure 16 shows a cut-away drawing of the system used to measure the moment produced by the airfoil model. A load cell (Interface Inc. Model MB-10) and connecting post served as a link between the free-member ‘A’ attached to the airfoil model and the fixed-member ‘B’ attached to the lift carriage. Because the load cell links the free and fixed members about a pivot point, it is subjected to any moment loads produced by the airfoil, thereby allowing the pitching moment of the airfoil to be measured. Also, in a manner similar to that employed on the lift balance, there are two sets of load cell attachment points, allowing for an expanded measurement range.

## D. Data Acquisition and Reduction

All analog data were recorded using a PC, and the data were digitized using a National Instruments NI PCI-6031E 16-bit analog-to-digital data acquisition board. The NI PCI-6031E has a resolution of 0.0015% of full-scale reading, 32 differential input channels, and two 16-bit digital-to-analog output channels. The 16-bit resolution of the board provided an accuracy of  $\pm 0.305$  mV when set for a full-scale range of  $\pm 10$  V.

At the low speeds required for low Reynolds number tests, small time-dependent fluctuations in tunnel speed were caused by inertia of both the fan drive system and the air. Thus, all quantities (dynamic pressure,

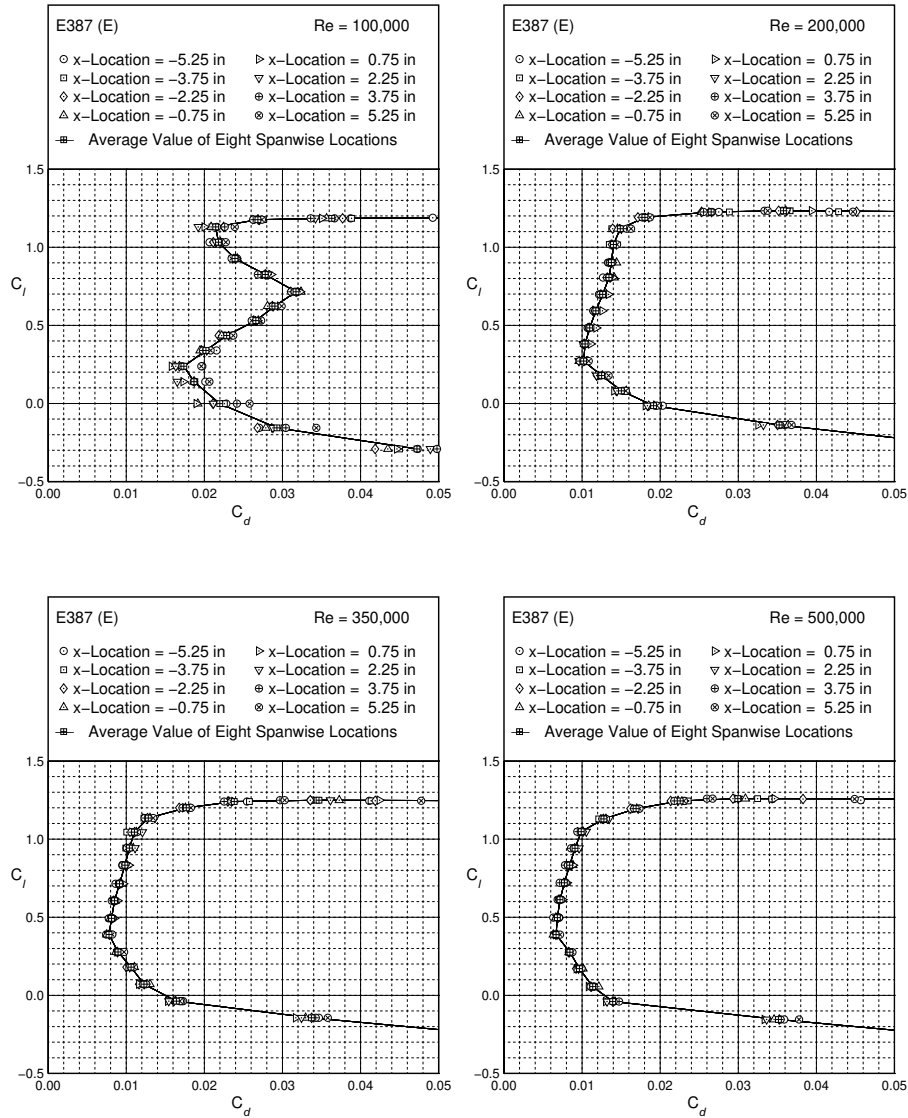


Figure 15. Drag results for the E387 (E) airfoil depicting typical spanwise drag variations for the eight spanwise stations for  $Re = 100,000, 200,000, 350,000,$  and  $500,000$ .

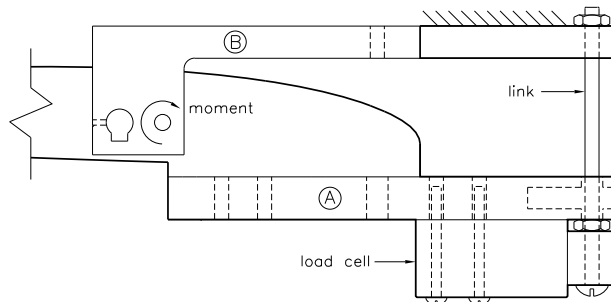


Figure 16. Moment measurement apparatus.

total pressure, lift, angle of attack, probe  $x-y$  position, and temperature) were measured simultaneously. Once a run started, the entire data acquisition process was completely automated as previously described. This

automation included setting and maintaining a constant Reynolds number within the test section, acquiring data, and plotting raw data graphically to the computer screen and numerically to a printer. All raw data were also saved to a separate output file for later in-depth data reduction.

Since the wind-tunnel model was mounted between splitter plates, the amount of flow (or spillage) between the splitter plates and the sidewalls of the test section could not be easily determined. Consequently, measurement of the freestream flow speed ahead of the splitter plates could not be used to determine the true freestream experienced by the model. Rather, the upstream dynamic pressure was measured between the two splitter plates 15.9 in. ahead of the quarter-chord point of the airfoil models and 5.2 in. above the test section floor. Since the upstream pitot-static probe was close to the leading edge of the airfoil, the measured velocity was corrected for circulation effects, as discussed later in this section.

In order to convert the upstream dynamic pressure into velocity, the air density was calculated from the ideal gas law

$$\rho = \frac{P_{atm}}{RT} \quad (2.9)$$

with ambient temperature obtained from an Omega Model CJ thermocouple (accurate to within 1 deg Rankine) located next to the wind tunnel. The velocity was then calculated from

$$V_{\infty} = \sqrt{\frac{2q_{\infty}}{\rho}} \quad (2.10)$$

The Reynolds number based on the airfoil chord is given by

$$Re = \frac{\rho V_{\infty} c}{\mu} \quad (2.11)$$

where  $\mu$  for air was calculated using the Sutherland viscosity law<sup>25</sup> expressed as

$$\frac{\mu}{\mu_0} = \left(\frac{T}{T_0}\right)^{3/2} \left(\frac{T_0 + S}{T + S}\right) \quad (2.12)$$

The physical boundaries of a closed test section restrict the flow and, as a result, produce extraneous forces on the model that must be subtracted out. These extraneous aerodynamic forces occur mainly because the velocity of the air increases as it flows over the model owing to the restraining effect of the wind-tunnel boundaries combined with the physical presence of the model and its wake. This effect is minimized when the model is small in relation to the size of the test section. Unfortunately, smaller models are more difficult to build accurately. Hence, 12-in. chord airfoil models were selected as a compromise, even though this required measuring smaller forces and a more complicated data reduction process.

In the following three sections, only an overview of the two-dimensional wind-tunnel corrections and their causes is presented.

### 1. Wind-Tunnel Boundary Corrections

The presence of the wind-tunnel walls increases the measured lift, drag, and pitching moment because of the increase in velocity at the model. More specifically, the lateral boundaries in a two-dimensional testing context cause four phenomena to occur<sup>19</sup>: buoyancy, solid blockage, wake blockage, and streamline curvature.

**Buoyancy:** Buoyancy is an additional drag force that results from a decrease in static pressure along the test section due to the growth of the boundary layer at the walls. Although buoyancy effects are usually insignificant even for airfoils tested within test sections having a constant area, the main effect of buoyancy was taken into account directly in corrections of the freestream velocity.

**Solid Blockage:** The physical presence of a model within a test section is known as solid blockage, which produces a decrease in the effective area. From the continuity and Bernoulli equations, the velocity of the air must increase as it flows over the model, increasing all aerodynamic forces and moments at a given angle of attack. Solid blockage is a function of the model size and test section dimensions.

$$\varepsilon_{sb} = \frac{K_1 M_v}{A_{ts}^{3/2}} \quad (2.13)$$

Wake Blockage: The second type of blockage is known as wake blockage, which results from a velocity within the airfoil wake that is lower than the freestream velocity. For closed test sections, in order to satisfy the continuity equation, the velocity at the model (outside of the wake) must increase. The effect of wake blockage is proportional to the wake size and thus to the measured drag force on the model.

$$\varepsilon_{wb} = \left( \frac{c}{2h_{ts}} \right) C_{d_u} \quad (2.14)$$

Streamline Curvature: Because of the physical constraints of the tunnel boundaries, the normal curvature of the free air as it passes over a lifting body (such as an airfoil) is altered, increasing the airfoil effective camber as the streamlines are “squeezed” together. For closed wind-tunnel sections, the increase in camber results in an increase in lift, pitching moment about the quarter-chord point, and angle of attack. The drag is unaffected by streamline curvature.

$$\Delta C_{l_{sc}} = \sigma C_l \quad (2.15)$$

$$\Delta \alpha_{sc} = \frac{57.3 \sigma}{2\pi} (C_l + 4 C_{m,c/4}) \quad (2.16)$$

where

$$\sigma = \frac{\pi^2}{48} \left( \frac{c}{h_{ts}} \right)^2 \quad (2.17)$$

## 2. Additional Velocity Corrections

When splitter plates are used, an additional velocity correction is required to correct for the so-called circulation effect.<sup>26</sup> As discussed previously, the freestream velocity must be measured between the splitter plates, and as a result the pitot-static tube used to measure dynamic pressure is influenced by the circulation on the airfoil model. Consequently, at the pitot-static tube, there is an induced velocity that depends on the amount of lift generated by the airfoil model—the greater the lift on the model (and thus the greater the circulation), the greater the induced velocity at the pitot-static tube. This circulation effect is, of course, also a function of the distance between the airfoil and the pitot-static tube. In most practical situations, however, the length of the splitter plates in front of the airfoil is usually small, since one of the main advantages of using splitter plates is to minimize the wall boundary-layer thickness at the model/wall juncture.

A detailed development of this correction procedure can be found in Ref. 26. To some degree, the effects of this correction can be gleaned from the results shown in Fig. 17 (taken from Ref. 15). Included in the figure are the reduced data for a prior version of the E387 airfoil, in particular model C, both with and without the circulation correction included. As clearly seen, this correction increases as the circulation increases, as one would expect, and overall the correction is substantial and should be included.

Finally, the velocity was also corrected to account for the boundary-layer growth along the tunnel walls, which resulted in a slightly higher than freestream velocity at the model. By using a second velocity measuring probe at the model quarter-chord point with the model removed and then measuring the upstream and downstream velocities simultaneously over a wide range in the Reynolds number, a calibration curve was obtained. Thus, for a measured upstream velocity, the actual velocity at the model could be calculated. The resulting velocity correction curve used to account for boundary-layer growth is shown in Fig. 18 and given by the equation

$$K_{vel} = 1.015755 - 0.0002391 V_u + 0.00001712 \sqrt{V_u} + \frac{0.1296}{\sqrt{V_u}} \quad (2.18)$$

## 3. Corrections to Measured Quantities

The measured quantities that must be corrected can be subdivided into two categories: stream and model quantities. The most important stream quantity is the velocity at the model. This velocity was obtained from the freestream velocity measurements and by applying the proper corrections to account for solid and

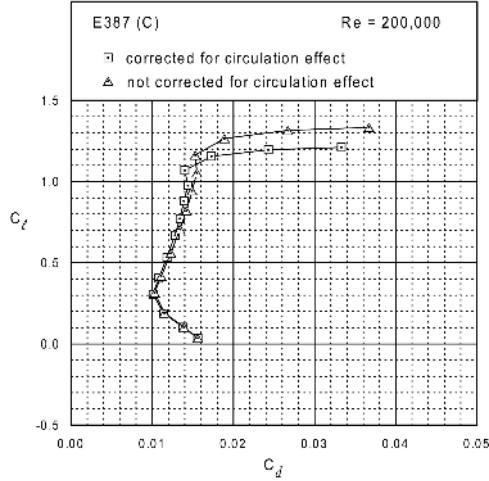


Figure 17. Drag polars for the E387 (C) with and without the necessary circulation correction (taken from Ref. 5).

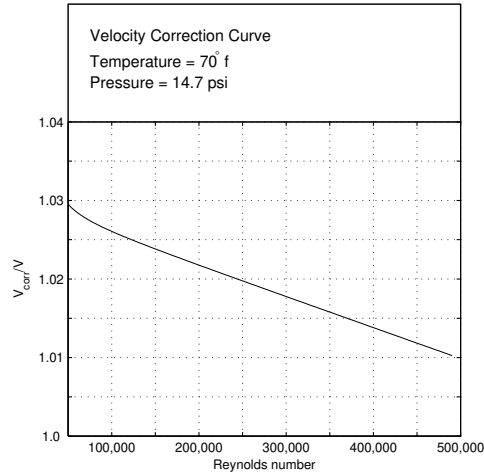


Figure 18. Velocity correction curve to account for boundary-layer growth between the splitter plates.

wake blockage as well as boundary-layer growth. Combining the velocity corrections in a single expression gives

$$V_c = V_u K_{vel} (1 + \varepsilon_{sb} + \varepsilon_{wb}) \quad (2.19)$$

Other freestream quantities, such as the Reynolds number and dynamic pressure, were then obtained directly from the corrected value of the velocity.

The model quantities of interest are the lift, drag, moment, and angle of attack, which were corrected in their nondimensional form to account for solid and wake blockage as well as streamline curvature. These correction equations for lift, drag, moment, and angle of attack are expressed as

$$C_l = C_{l_u} \frac{1 - \sigma}{(1 + \varepsilon_b)^2} \quad (2.20)$$

$$C_d = C_{d_u} \frac{1 - \varepsilon_{sb}}{(1 + \varepsilon_b)^2} \quad (2.21)$$

$$C_m = \frac{C_{m_u} + C_l \sigma(1 - \sigma)/4}{(1 + \varepsilon_b)^2} \quad (2.22)$$

$$\alpha = \alpha_u + \frac{57.3 \sigma}{2\pi} (C_{l_u} + 4 C_{m,c/4_u}) \quad (2.23)$$

It is important to note that the use of drag coefficient data is required to correct the model quantities since wake blockage is proportional to the measured drag coefficient. For the lift runs, however, drag was not measured, which has an effect on the lift data reduction. For the lift curves, the wake blockage correction was computed using a constant value for the drag coefficient of 0.04, which was representative for conditions close to maximum lift. This method ensured more accurate values for the maximum lift coefficients even though it overcorrected lift coefficient values in the normal low-drag operating range of the airfoil. This “overcorrection” was not significant, as can be seen by comparing lift data taken from a lift run with that from a drag run.

## E. Calibrations and Uncertainty Analysis

By applying the general uncertainty analysis presented in Coleman & Steele,<sup>27</sup> the uncertainties in the velocity, lift coefficient, and drag coefficient were found in a relatively straightforward manner. Further details describing the uncertainty analysis are presented in Ref. 23.

First, consider the case of measuring the upstream velocity, which is used to normalize the lift and drag forces. The highest uncertainty in the pressure readings due to fluctuations in flow angle is 1%, resulting in a freestream velocity uncertainty within 0.5%. If no errors related to the probes are included, the uncertainty in pressure readings and the velocity measurements reduce to less than approximately 0.5% and 0.3%, respectively.

The lift balance was calibrated over a range that depended on the loads expected for a given run—the higher the Reynolds number, the larger the range. Overall uncertainty in the lift coefficient is estimated to be 1.5%. The accuracy of the lift calibrations was the main contribution to this small error.

The drag measurement error comes from three sources: accuracy of the data acquisition instruments, the repeatability of the measurements, and spanwise variation in the downstream momentum deficit. Based partly on the error analysis method presented in McGhee<sup>11</sup> and Coleman & Steele,<sup>27</sup> the uncertainties caused by the instruments and measurement repeatability are less than 1% and 1.5%, respectively. Based on a statistical analysis of a representative low Reynolds number airfoil,<sup>15</sup> the uncertainties caused by the spanwise variations are estimated at 3% for  $Re = 100,000$  and reduce to approximately 1.5% at and above  $Re = 200,000$ .

For the angle of attack sensor, calibration measurements were taken at six different angles of attack incremented from 0 to 25 deg in 5-deg steps. Overall uncertainty in the angle of attack is estimated at 0.08 deg, based on the calibration results.

## III. Data Validation

In this section, data taken on the E387 are compared with results from NASA Langley taken in the Low-Turbulence Pressure Tunnel (NASA LTPT).<sup>11,28</sup> Four types of data are compared: surface oil flow visualization, lift data, moment data, and drag polars. In this order, these data are presented and discussed below.

### A. Surface Oil Flow Measurements

Low Reynolds number airfoil flows are distinguished principally by the presence of a laminar separation bubble, which is the leading culprit in the degradation of low Reynolds number airfoil performance relative to the performance of airfoils at higher Reynolds numbers. When laminar separation bubbles do appear, they are caused by the inability of the flow to make a transition to turbulent flow in the attached boundary layer on the surface of the airfoil. Instead, the laminar flow separates before transition. When this happens, transition occurs in the free shear layer, and the so-called laminar separation bubble is formed when the turbulent flow reattaches to the airfoil surface downstream of the transition. For the most part, the resulting



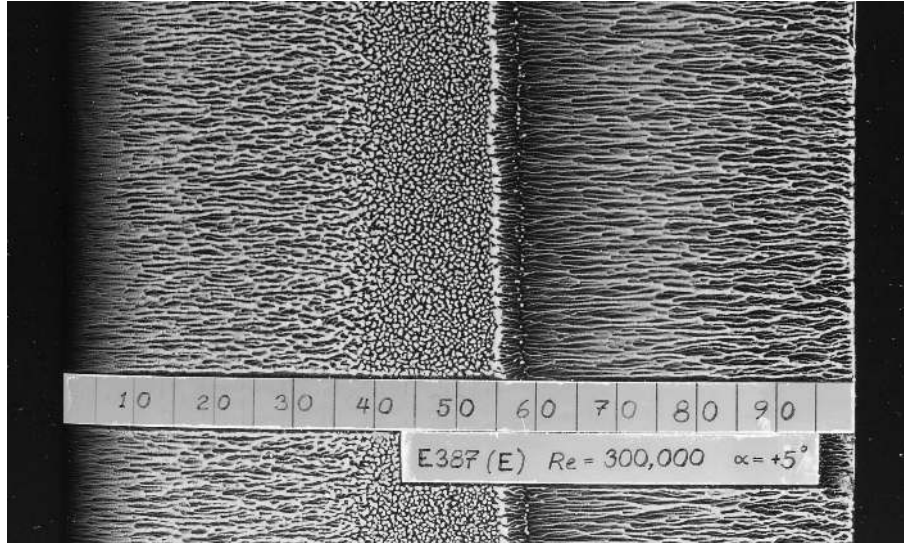


Figure 19. Representative upper-surface oil flow visualization on the E387 (E) airfoil.

pressure drag over the region of the laminar separation bubble is responsible for the relatively high drag that can sometimes accompany airfoils at low Reynolds numbers. The existence of a laminar separation bubble and its extent can be deduced by examining surface oil flow visualization, as was done in the study.

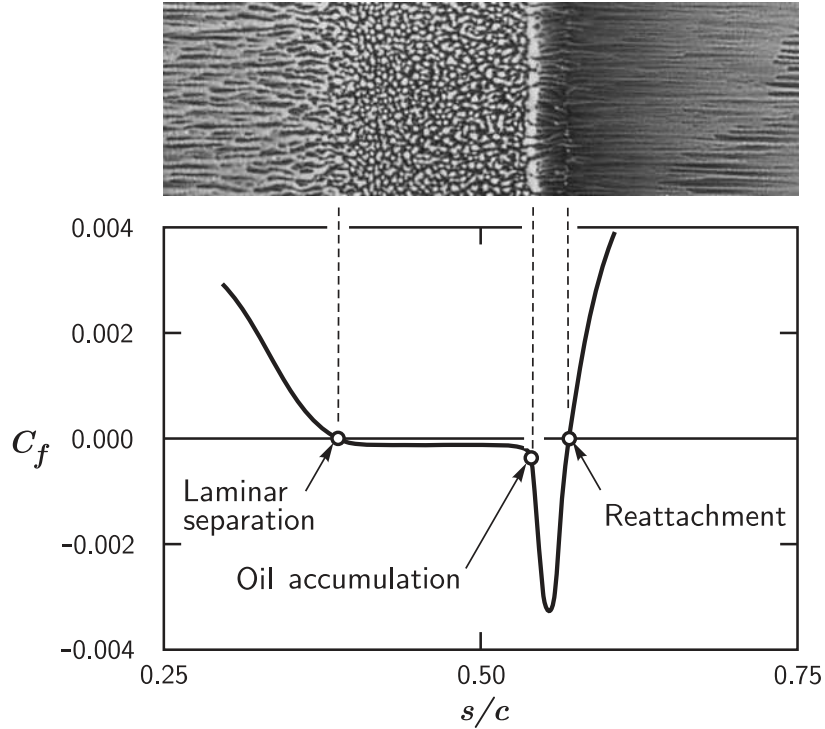
The surface oil flow visualization technique made use of a fluorescent pigment (Kent-Moore 28431-1) suspended in a light, household-grade mineral oil that was sprayed onto the surface of the model using a Paasche Model VL airbrush. The model was then subjected to 20–45 min of continuous wind-tunnel run time at a fixed speed and angle of attack. During this period, the oil moved in the direction of the local flow velocity at a rate dependent on the balance of forces dictated by the boundary-layer skin friction  $C_f$  and surface tension of the oil. As a result, discernible regions of the flow could be identified for comparison with the NASA LTPT data.<sup>11,28</sup>

Figure 19 is a photograph of the surface oil flow pattern made visible under fluorescent light. Figure 20 conceptually illustrates the connection between the salient surface oil flow features and the skin friction distribution. Note that the skin friction distribution, though conceptual, is consistent with the results of many computational studies.<sup>29–32</sup>

Several important flow features can be identified and related to the underlying skin friction and surface tension forces. In Fig. 19, laminar flow is seen to exist from the leading edge to approximately  $x/c = 40\%$ . The oil streaks are characteristically smooth in this region until laminar separation, which has been identified in Fig. 20 as the point where  $C_f = 0$ . (Note again that the flow shown in Fig. 20 is conceptual, and it is not intended to match Fig. 19 in detail.) Downstream of the point of laminar separation, the original airbrushed “orange-peel” texture that existed before running the tunnel test still exists, indicating that the flow is mainly stagnant in this region. This stagnant flow is consistent with the known behavior of the interior leading-edge region of a laminar separation bubble. As sketched, the magnitude of the  $C_f$  in this region is quite small because of the low flow speed and negative in sign because of reverse flow at the surface.

In the presence of a laminar separation bubble, transition takes place in the free shear layer above the airfoil surface. Downstream of this point, reattachment occurs in a process that is known to be unsteady as vortices are periodically generated and impinge on the airfoil surface at reattachment.<sup>32,33</sup> These unsteady vortices colliding with the surface lead to a relatively high shear stress that tends to scour away the oil at the mean reattachment point, pushing the oil upstream or downstream in a random walk of sorts. As seen in Fig. 20, the reattachment line is less distinct because the bulk of the oil has been pushed away, revealing the underlying black airfoil surface. In Fig. 19, the tunnel run time was long enough that the reattachment line at  $x/c = 58\%$  is even harder to see. In the original high-resolution color photographs that were archived, this feature is clear and easily quantifiable.

Downstream of reattachment, the boundary layer is, of course, turbulent. The high skin friction in this



**Figure 20.** Conceptual illustration of the relationship between the surface oil flow features and skin friction distribution in the region of a laminar separation bubble.

area relative to the laminar boundary layer tends to clear away more oil, again making the dark-colored surface downstream more visible than it was upstream, where it was laminar.

The remaining feature of the flow is a line where the oil tends to pool, termed here the “oil accumulation line.” This intrinsic feature of the oil flow has no direct connection to laminar flow, reverse flow in the bubble, or the ensuing turbulent flow downstream. However, it does have physical significance. The negative  $C_f$  spike shown in predictions and sketched conceptually in Fig. 20 is most likely responsible for generating the oil accumulation line. Assuming that this is the case, the fluctuating high skin friction that is generated over the unsteady reattachment zone will tend to push the oil upstream ahead of the mean reattachment point. At some location on the airfoil, however, the oil moving upstream will experience a balance of forces between the rapidly weakening skin friction force (at the edge of the negative  $C_f$  spike) and the surface tension or oil adhesion that is retarding its motion. Where these two forces balance, the oil accumulates into a line that becomes the single most visible feature of the oil flow. Moreover, there is speculation that this flow feature is further distinguished by sometimes being mislabeled as “reattachment” as will be discussed below.

The upper-surface oil flow features, as just described, were obtained over a range of angles of attack for Reynolds numbers of 200,000 and 300,000. These results are shown in Fig. 21 and compared with the NASA Langley LTPT data. Over the low drag range from  $-2$  deg to  $7$  deg, the agreement in the laminar separation line between the data sets is mostly within 1–2% of  $x/c$ , which is very near the uncertainty of the method. As previously discussed, the next feature to appear is the oil accumulation line. The UIUC oil accumulation line agrees fairly well with the “reattachment” line identified in the NASA experiment. It is believed, however, on the basis of the previous reasoning, that this label in the original reference<sup>11</sup> is a misnomer. Had the UIUC tests been performed for a longer time, the reattachment zone would be scoured clean with no distinguishing feature, leaving only the oil accumulation line to be labeled as the “reattachment line,” since one must exist. Hence, here and in prior UIUC work<sup>14</sup> there is speculation that such a scenario took place in the NASA study, i.e., the oil-accumulation line was misinterpreted as the reattachment line. Given this working assumption, the two results again are in good agreement.

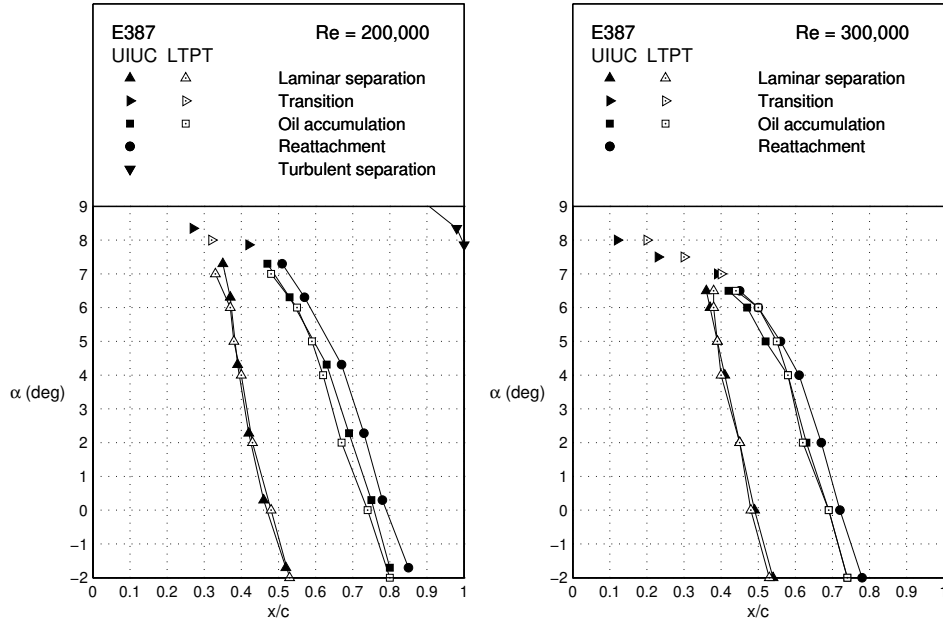


Figure 21. Comparison of major E387 (E) upper-surface flow features between UIUC and LTPT for  $Re = 200,000$  and  $300,000$ .

Moving further downstream, the UIUC reattachment data are plotted, but no direct comparison can be made because reattachment proper was not reported in the NASA study. However, close inspection of the data suggests that at a Reynolds of  $300,000$  and between  $5$  deg and  $7$  deg, the LTPT line merges with the UIUC reattachment line. Perhaps in this case, the measurements at Langley were indeed the reattachment points.

It is worth mentioning that surface oil flow data were not taken at a Reynolds number of  $100,000$  during these tests because the run times would be in excess of  $2$  hrs per data point. Over this period of time, the droplets of oil spray that initially give rise to the “orange peel” texture tend to smooth out. This reduces the contrast between the different regions of the flow, thereby making it difficult to ascertain the distinguishing features of the flow.

The conclusion to be drawn from this comparison of the oil flow visualization results is that the two facilities produce airfoil flows that are in close agreement. Moreover, assuming that the arguments regarding the oil accumulation line are correct, then the agreement is excellent and within the uncertainty of the measurements.

## B. Lift and Moment Data

Lift and moment data comparisons between the UIUC and NASA LTPT data are shown in Fig. 22. Discrepancies can be seen for a Reynolds number of  $100,000$  as well as in the stalled regime. For  $Re = 100,000$ , differences are most likely attributable to measurement accuracy. In stall for  $\alpha > 12$  deg, taking the NASA LTPT data as the benchmark, the UIUC data differ most likely as result of three-dimensional end effects. Nevertheless, the results show good agreement over the unstalled range, and this agreement improves with higher Reynolds number.

## C. Drag Polars

Figure 23 shows a comparison between UIUC and NASA LTPT drag data for the Reynolds numbers of  $100,000$ ,  $200,000$ ,  $300,000$ , and  $460,000$ . To begin this discussion, data at a Reynolds number of  $200,000$  and  $300,000$  are considered. For these cases, the oil flow results were in close agreement as well as the lift data, which, taken together, suggest that the drag data should likewise be in good agreement. Indeed, for  $Re = 200,000$ , there is close agreement. However, for  $Re = 300,000$ , the agreement is not as good. As for the

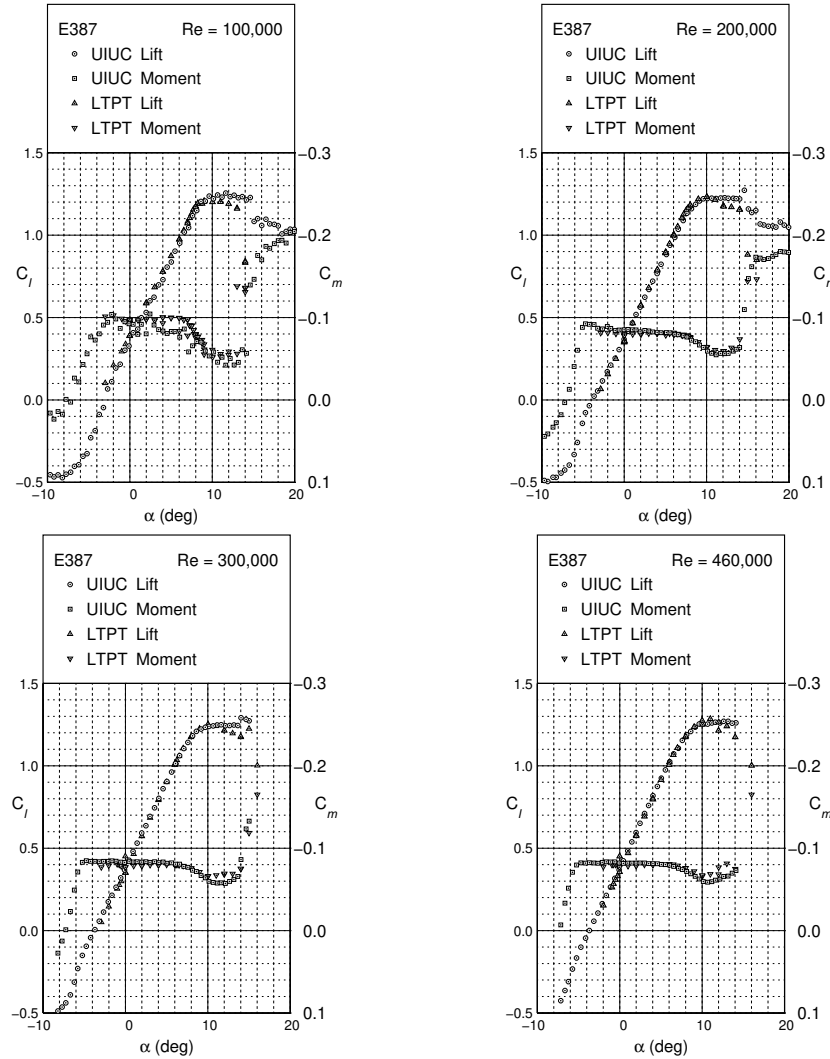


Figure 22. Comparison between UIUC and LTPT E387 lift and moment coefficient data for  $Re = 100,000$ ,  $200,000$ ,  $300,000$ , and  $460,000$ .

other cases, for a  $Re = 460,000$ , the agreement improves, while for  $Re = 100,000$ , there is less agreement. When these cases are studied in more detail, it is seen that the edges of the drag polar are in quite close agreement for each case, with the  $Re = 100,000$  perhaps being the exception.

There can be many reasons for the observed discrepancies, not the least of which is the fact that at low Reynolds numbers the drag data, when determined from downstream wake measurements, vary along the span—the further downstream, the more variation. The current measurements were taken 1.25 chord lengths downstream of the trailing edge, while those in the NASA study were taken 1.5 chord lengths downstream. Because of this variation in spanwise drag, ideally many wake profile measurements should be taken along the span and the resulting drag coefficients summed and averaged. This approach of performing multiple wake surveys was taken in the current study (as mentioned previously, eight wake surveys were taken), but in the NASA study, wake rake data were taken at only one station for the purpose of acquiring the full polar data reported. However, in the NASA study, some limited spanwise data were taken at angles of attack of 0 and 5 deg. For these cases, the degree of spanwise variation observed is quite similar to the current data shown in Fig. 15. Consequently, the discrepancies in part must be related to the variation in drag along the span. In the NASA study, had data been taken at many stations for all conditions, it is likely that better agreement would be observed.

For the Reynolds number of 100,000, which was not critical to the current investigation, the discrepancies are larger. This result cannot be attributed solely to spanwise drag variation. Figure 15 shows that at a  $C_l = 0.7$  and  $Re = 100,000$ , the eight  $C_d$  data points obtained from the eight wake measurements fall nearly one on top of the other. Therefore, the spanwise variation in drag is small on a percentage basis, and a similar variation in  $C_d$  was seen in the NASA data. Consequently, for  $Re = 100,000$ , the cause for the bulk of the difference in the drag measurements must be something other than spanwise drag variation.

When sources of error were being considered to explain the discrepancies, several factors were ruled out in light of the excellent agreement in surface oil flow visualization as well as lift and moment data. Of those that remained, no sources of uncertainty in the current data lingered after investigation. Thus, the state of the agreement for the Reynolds number of 100,000 remains unexplained. It is recognized that the source of this discrepancy might relate to some of the discrepancies for the higher Reynolds number cases, as well. Nevertheless, the agreement overall is good, especially in light of past historical comparisons of low Reynolds number airfoil data, which vary widely.<sup>13,34</sup>

#### D. Summary

Regarding the accuracy of the current data overall, first, it was shown that surface oil flow data obtained on the E387 airfoil exhibited excellent agreement with NASA LTPT data for  $Re = 200,000$  and  $300,000$ . Second, current lift data were shown to have good agreement with LTPT data for all Reynolds numbers up to stall, after which three-dimensional end effects and unsteady aerodynamics produced slight discrepancies. Third, the pitching moment data were shown to agree well with LTPT data over a broad range of angles of attack. Lastly, in support of the three previous conclusions, the drag data showed good agreement, with some discrepancies yet to be fully explained.

## IV. Recent Low Reynolds Number Airfoil Measurements

The UIUC experimental setup was used to measure the performance of an airfoil with very large flap deflections. Also, a flat plate was tested with leading edge serrations which have been shown to increase lift and soften airfoil stall characteristics.

### A. Performance with Large Trailing Edge Flap Deflections

Large flap deflections are used on many small model aircraft and UAVs for glide path control and extreme maneuvers. Data such as this is especially interesting because of the dearth of experimental measurements on low Reynolds number airfoils with large flap deflections. The specific flapped airfoil used for these tests was the AG455ct with a 30% chord flap. It was designed by Mark Drela for RC sailplanes, and the wind tunnel model was constructed by him. Figure 24 shows the true airfoil as compared with the digitized wind tunnel model center section. The average difference between the true airfoil and the digitized coordinates was 0.008 in. (0.20 mm) for the 12-in. (0.305 m) chord model.

Figures 25–27 show the polars and lift characteristics for the Reynolds of 100,000, 200,000 and 300,000 for the flap deflections of  $-15$ ,  $0$ ,  $15$ ,  $30$ , and  $40$  deg. The same data is shown in Figs. 28–31 for each respective flap position. The decrease in the flap effectiveness with higher flap angle is clearly seen, and this trend is consistent with the flap-effectiveness correction factor  $\tau$  found in Ref. 35. The increase in drag with higher flap deflection is dramatic, but no benchmark data exists for comparison (not the change the scale for  $C_d$  as the drag increases). It should be noted that for high flap deflections the wake is unsteady. Under such conditions, refinements to the wake rake method could be applied if the turbulence properties are known.<sup>20,36</sup> With the absence of this additional data in these tests, however, no such refinements were applied.

### B. Flat Plate Airfoils with Serrated Leading Edges

Saw-toothed structures (serrations) on the leading edge of the flippers of some aquatic animals have been shown to delay stall, increase maximum lift, and lower drag, and these characteristics together are believed to improve the maneuverability of the humpback whale and other aquatic animals.<sup>37–39</sup> Mutual interest<sup>40</sup> in these observations led to the current experiments and some preliminary results were reported previously.<sup>41</sup>

For these experiments, a flat-plate airfoil was used as the baseline, which is the airfoil configuration used on many popular light-weight flat-foam aerobatic RC models that have become quite popular.<sup>41</sup> The experiments were designed to determine if a simple serrated configuration could be used to increase performance, that is, increase lift, soften stall, and lower drag in the stall regime. The results presented here include only lift and moment characteristics.

Four serrated leading edge configurations were tested (as well as many other configurations not reported here). Each had an average chord of 12 in. (0.305 m); that is, the planform area of the wind tunnel models was the same for each case. A given test configuration was composed of the serrated leading-edge piece attached to a common aft flat plate. The resulting airfoil wind tunnel model was thus flat and had a serrated leading edge. The thickness of the wind tunnel model was a uniform 3/8-in (9.52-mm) thickness or 3.125% thick ( $= 0.375/12$ ).

The baseline flat-plate case is shown in Fig. 33. Figures 34–37 show the lift coefficient and moment coefficient measurements for the four configurations at Reynolds numbers of 40,000, 80,000, and 120,000. As seen in the data, the main effect of the serrations is to smooth out the stall characteristics and moment characteristics relative to the baseline flat plate. The change in the moment characteristics are particularly noteworthy because the lower pitching moment in the stalled region is suggestive of reduced separation into stall and thus lower associated drag. The results show the aerodynamics of a flat plate can be improved at low Reynolds numbers with serrations, and the larger and more coarse serrations (case D, Fig. 37) appear to be the most favorable.

## V. Conclusions

The wind tunnel test techniques described in this paper have been validated and used to test over 200 airfoils at low Reynolds numbers at UIUC. The approach relies on using a force balance method for lift and moment, and a wake rake method for airfoil drag. This paper presented new results on the AG455ct airfoil with a large 30%-chord flap deflected over a wide range that might be used for glide path control or extreme maneuvering. In a second series of tests, a flat-plate airfoil was tested with leading edge serration geometries to explore the effects on stall characteristics. The results support the conclusions of other researchers that leading edge serrations (protuberances like those found on the fins/flippers of some aquatic animals) leads to higher lift and softer stall. The results suggest that these characteristics are accompanied by lower drag in the stall and post-stall range, but drag data was not obtained in these conditions. Finally, the results from the experimental setup have been used in the design, test and validation of many airfoils used in low Reynolds number applications, and these data are readily available online and in the references provided here (see Refs. 13–16,34).

## Acknowledgments

The authors would like to thank Dr. Mark Drela of MIT for building the AG455ct flapped airfoil for these tests. Also we thank Camille Goudeseune of the University of Illinois for design and fabrication of constant-area leading edges, and Upper Canada Composites (<http://www.uppercanadacomposites.com/>) for the design and fabrication of flat plate wind tunnel model.

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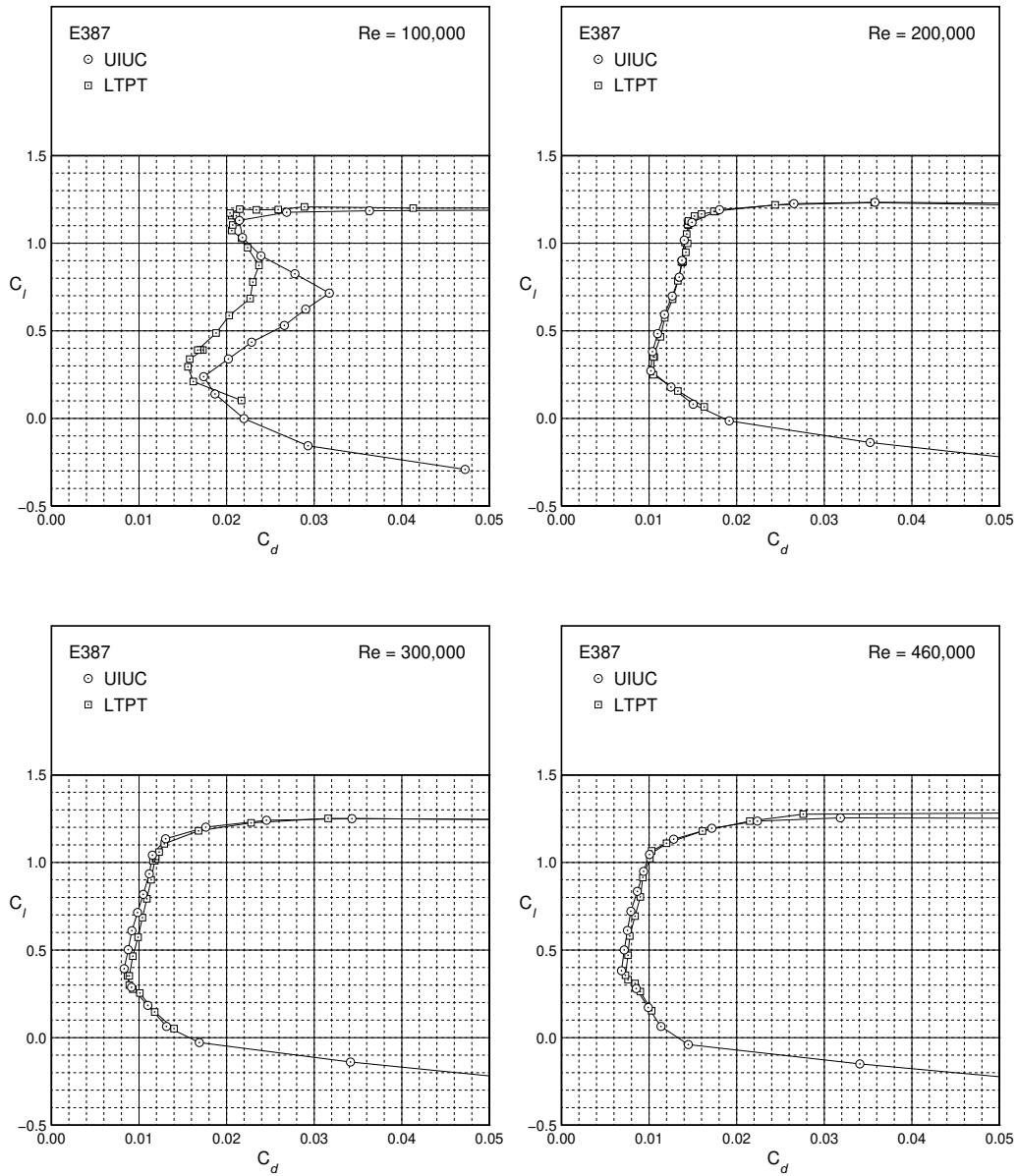


Figure 23. Comparison between UIUC and LTPT E387 drag coefficient data for  $Re = 100,000$ ,  $200,000$ ,  $300,000$ , and  $460,000$ .

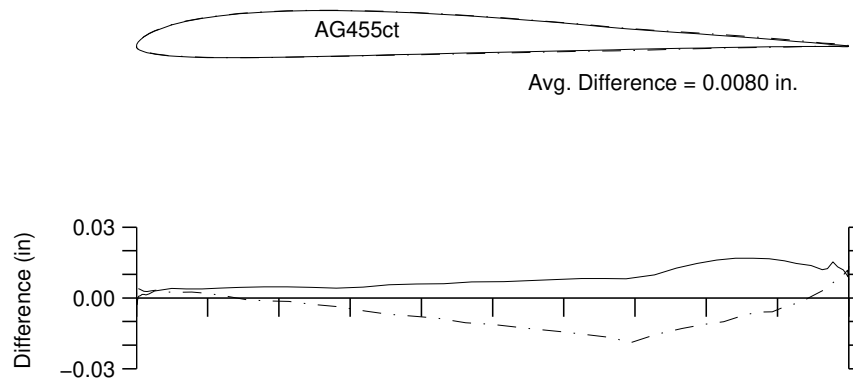


Figure 24. True AG455ct airfoil as compared with the digitized 12-in chord wind tunnel model (airfoil solid line is true, airfoil dot-dash line is measured).

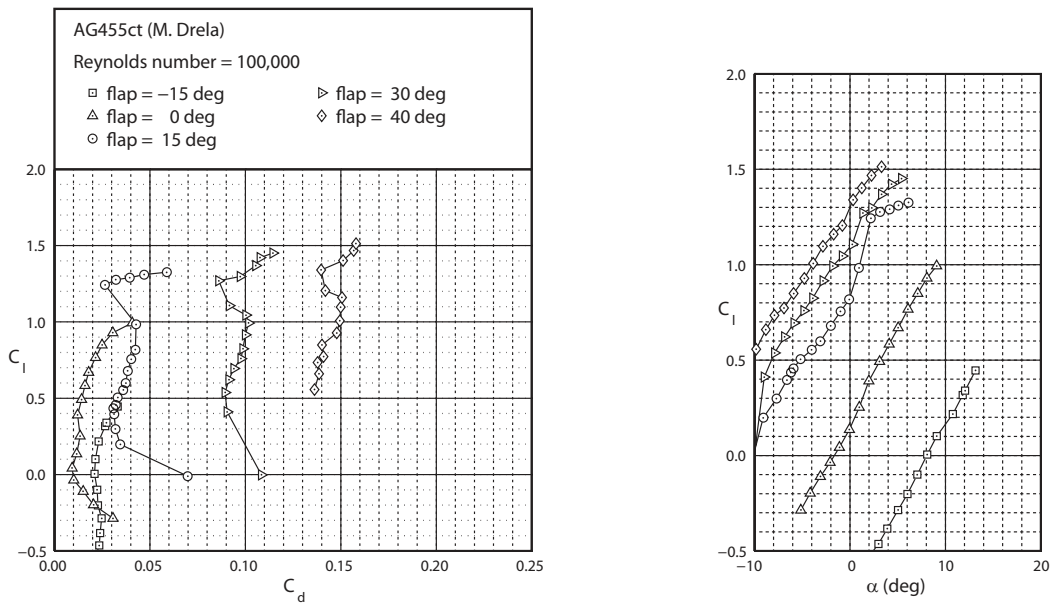


Figure 25. AG455ct airfoil polar for  $Re = 100,000$  and flap deflections of  $-15, 0, 15, 30,$  and  $40$  deg.

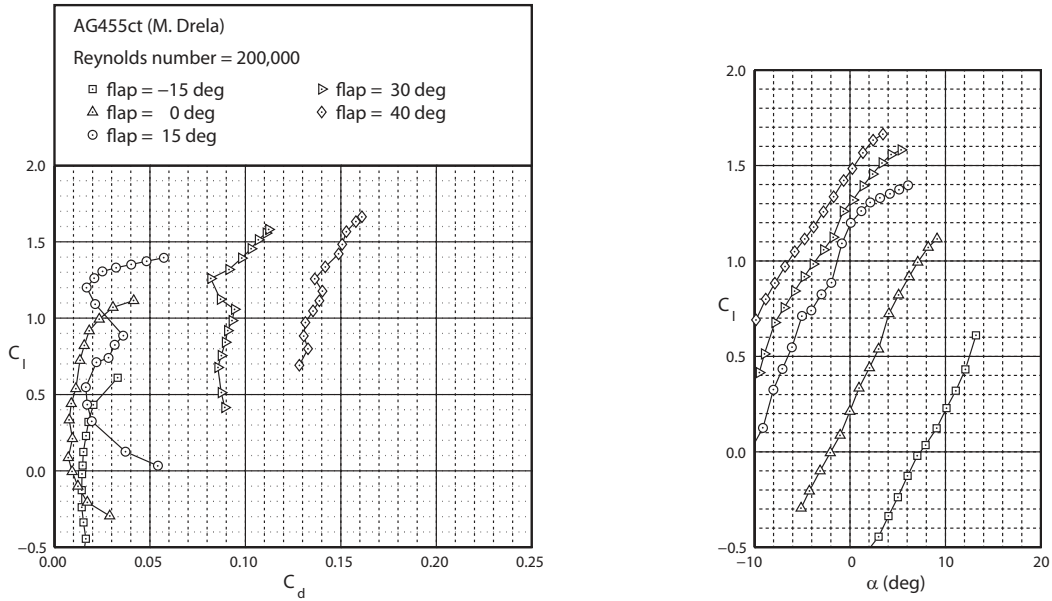


Figure 26. AG455ct airfoil polar for  $Re = 200,000$  and flap deflections of  $-15, 0, 15, 30,$  and  $40$  deg.

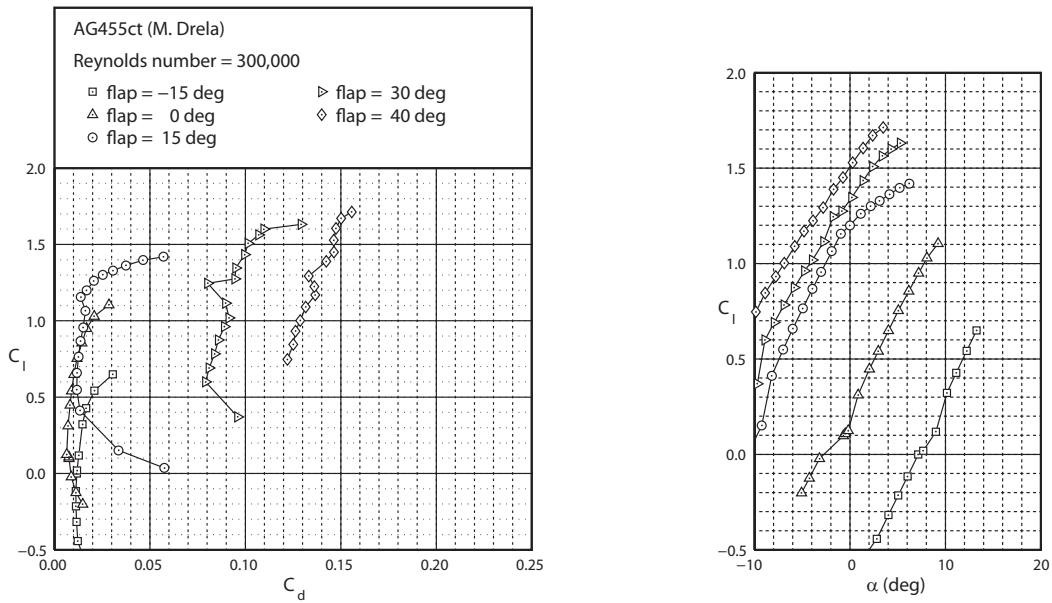


Figure 27. AG455ct airfoil polar for  $Re = 300,000$  and flap deflections of  $-15, 0, 15, 30,$  and  $40$  deg.

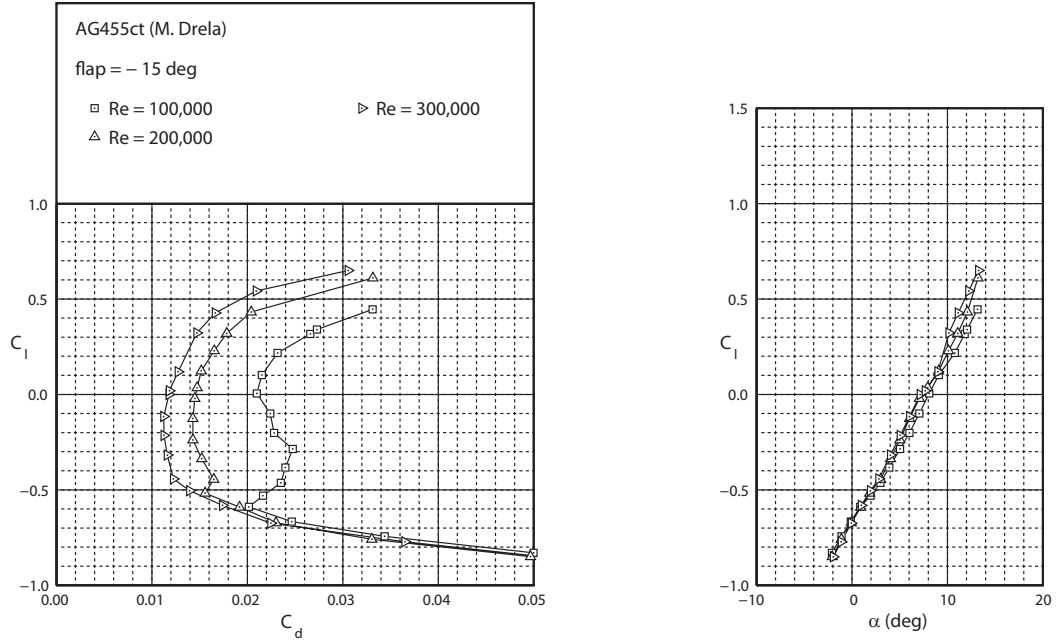


Figure 28. AG455ct airfoil polar for flap deflection of  $-15$  deg and  $Re = 100,000, 200,000$  and  $300,000$ .

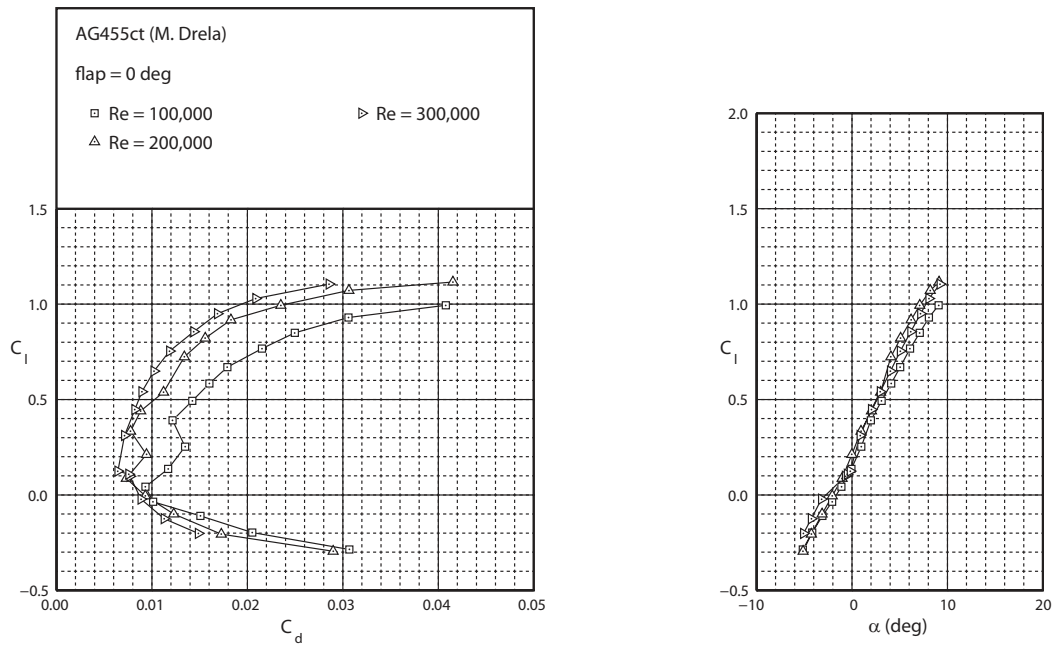


Figure 29. AG455ct airfoil polar for flap deflection of  $0$  deg and  $Re = 100,000, 200,000$  and  $300,000$ .

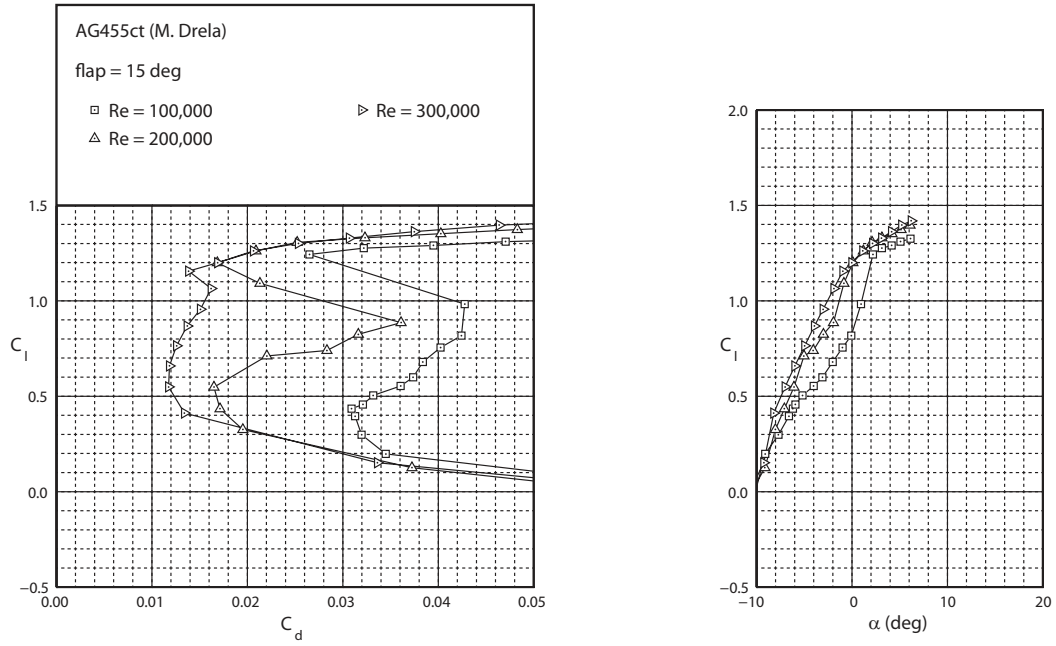


Figure 30. AG455ct airfoil polar for flap deflection of 15 deg and  $Re = 100,000, 200,000$  and  $300,000$ .

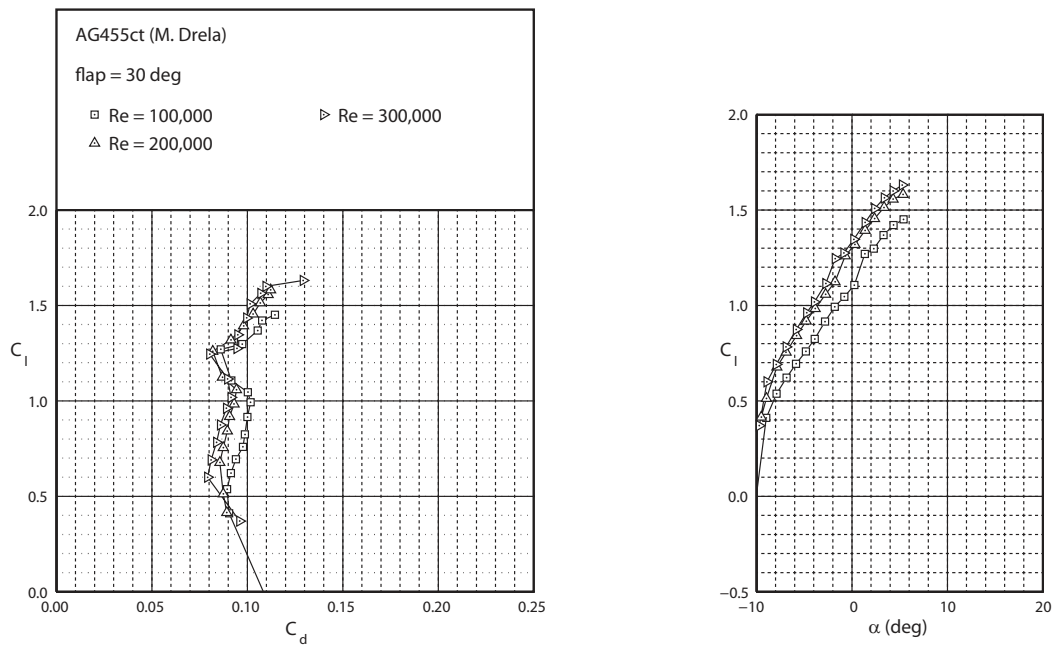


Figure 31. AG455ct airfoil polar for flap deflection of 30 deg and  $Re = 100,000, 200,000$  and  $300,000$ .

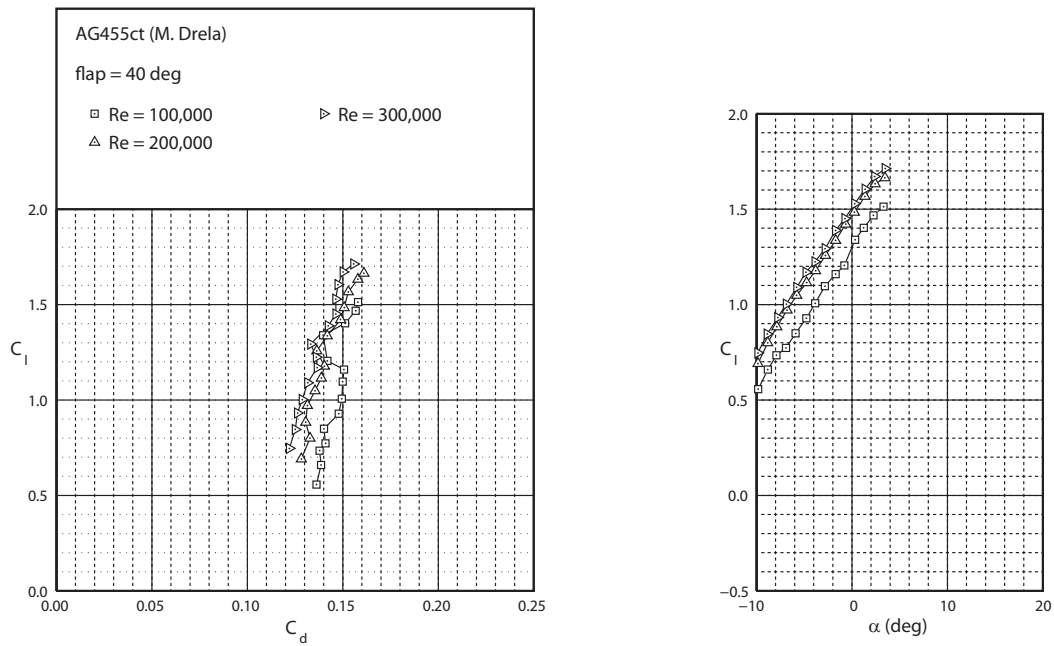


Figure 32. AG455ct airfoil polar for flap deflection of 45 deg and  $Re = 100,000, 200,000$  and  $300,000$ .

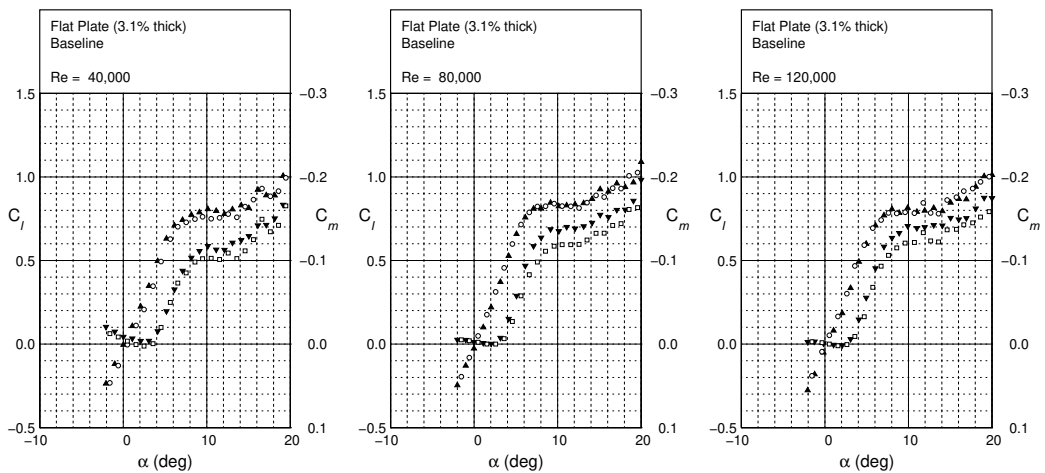


Figure 33. Lift and moment coefficient characteristics for the baseline flat plate (3.2% thickness).

Serrations A  
 Amplitude = 0.013c  
 Wavelength = 0.052c

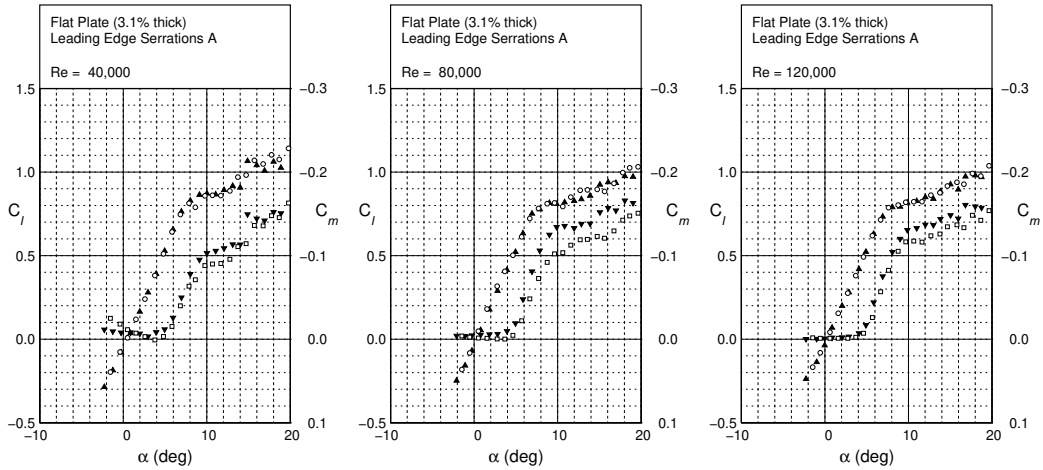
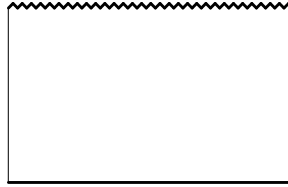


Figure 34. Lift and moment coefficient characteristics for a flat plate with leading edge serrations (case A).

Serrations B  
 Amplitude = 0.049c  
 Wavelength = 0.052c

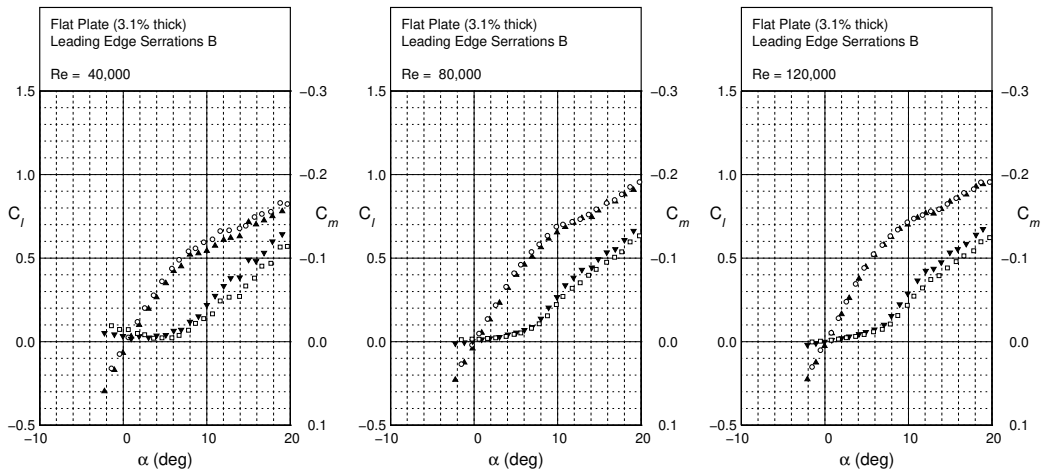
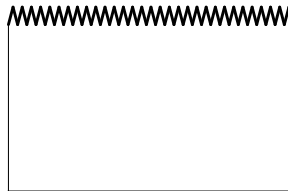


Figure 35. Lift and moment coefficient characteristics for a flat plate with leading edge serrations (case B).

Serrations C  
 Amplitude = 0.013c  
 Wavelength = 0.125c

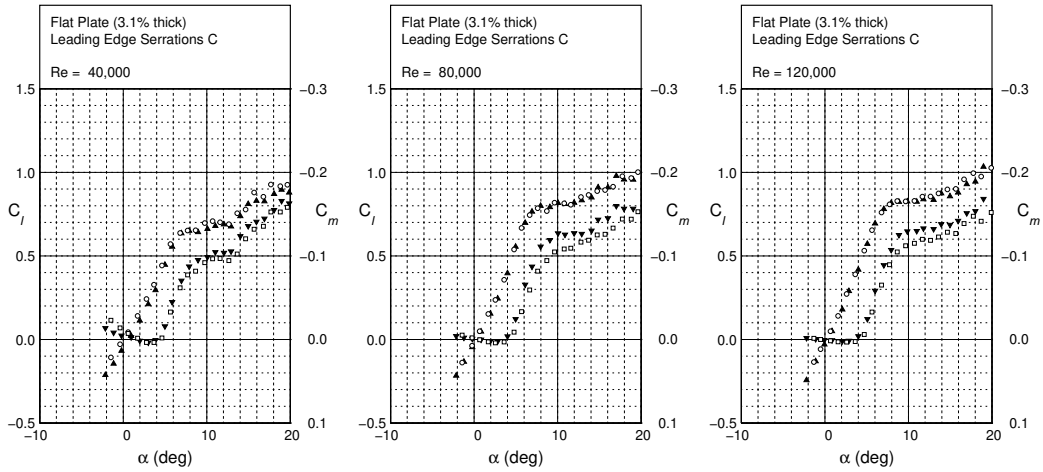
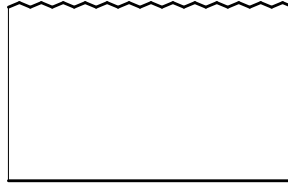


Figure 36. Lift and moment coefficient characteristics for a flat plate with leading edge serrations (case C).

Serrations D  
 Amplitude = 0.052c  
 Wavelength = 0.125c

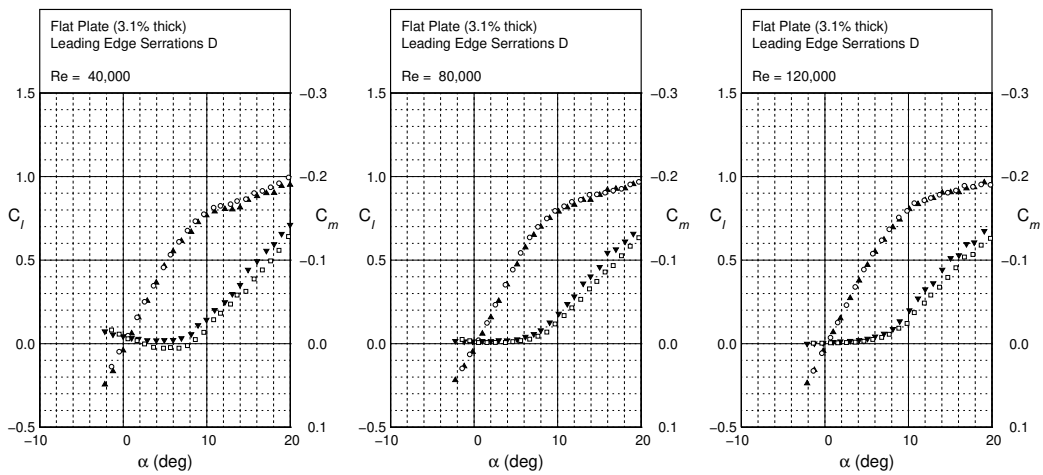
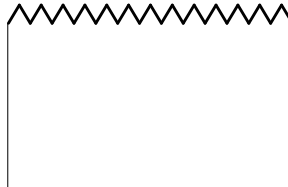


Figure 37. Lift and moment coefficient characteristics for a flat plate with leading edge serrations (case D).