

X-Ray Determination of Crystallite Size and Effect of Lattice Strain on the Debye-Waller Factors of Ni Nano Powders using High Energy Ball Mill

E Purushotham N Gopi Krishna*

Department of Physics, Kakatiya University, Warangal – 506 009, India

*E-mail : psm45456@gmail.com

Abstract

The synthesis of Ni nanocrystalline powder by high-energy ball milling has been investigated. Ni powders were ball milled in an argon inert atmosphere. The milled powders were characterized by X-ray diffraction and scanning electron microscopy measurements. The high-energy ball milling of Ni after 12 hours resulted in crystallite size of about 48 nm. The lattice strains in nickel (Ni) powders produced by milling have been analyzed by X-ray powder diffraction. The lattice strain (ϵ) and Debye-Waller factor (B) are determined from the half-widths and integrated intensities of the Bragg reflections. In Ni the Debye-Waller factor is found to increase with the lattice strain. From the correlation between the strain and effective Debye-Waller factor, the Debye-Waller factors for zero strain have been estimated for Ni. The variation of energy of vacancy formation as a function of lattice strain has been studied.

Keywords: X-ray diffraction, lattice strain, crystallite size, Debye-Waller factor, vacancy formation energy

1. Introduction

Nanocrystalline materials with average crystallite size of a few nanometers have been the interest of many investigators [1,3]. Nanocrystalline nickel has attracted much attention due to its commercial importance and particular properties [4,5]. There are different methods for producing nanocrystalline materials. High-energy mechanical milling is one of these techniques. In this process, nanometer sized grain structures can be obtained in metals, intermetallic compounds, composites and ceramics, after sufficient milling time [6,8]. The product of milling and formation mechanism depend on various parameters particularly chemical composition and type of powders [9]. There are many papers dealing with the influences of materials addition on the milling product. In this paper, Ni nanocrystalline powder was synthesized by ball milling and the effect of lattice strain on the Debye-Waller factor was investigated.

Nano particles of size < 100 nm in diameter that exhibit enhanced size-dependent properties compared to ultra-fine or larger particles of the same material. An accurate estimation of grain size/crystallite size become essential when such materials are produced with their crystallite size of the order of less than 100 nm. Though TEM is one of the powerful techniques for crystallite size measurement, it has certain limitations. Since TEM images represent only a local region, many samples and images are required to provide an average information for the entire sample. Not only this, the TEM sample preparation method is an involved and time consuming one. The XRD technique is free from these limitations. X-ray diffraction is, on the other hand, a simple and easier approach for determination of crystallite size of powder samples.

The Debye-Waller factor is an important lattice dynamical property. There is considerable X-ray work on the Debye-Waller factors of Ni [10]. But it is interesting to study the effect of lattice strains on the Debye-Waller factors of this metal. Inagaki *et al* [11,12] showed that in several non-metallic powders, the strains produced during grinding have a significant effect on the Debye-Waller factors measured from X-ray diffraction intensities. Sirdeshmukh *et al* [13] observed the effect of lattice strains on the Debye-Waller factors in semiconductor powder materials. Gopi Krishna and Sirdeshmukh [14] studied the effect of lattice strains on the Debye-Waller factor of ytterbium metal. In the present investigation the results of a systematic study of the effect of lattice strains on the Debye-Waller factors and crystallite size of face centered cubic Ni metal is reported. These results are being reported for the first time.

2. Experimental

The powder samples were obtained by gently filing highly pure Ni metal ingots with a jeweller's file. A part of this powder was used to prepare the initial sample. The remaining powder was subjected to milling in a ball mill for 4, 8, 12, 16 and 20 hours to produce strains. X-ray diffractograms were recorded with the initial sample and with samples prepared after each spell of milling. The XRD pattern of Ni is shown in Fig. 1. The diffractograms were obtained with a Philips CWU 3710 X-ray powder diffractometer in the 2θ range $20-120^\circ$ using filtered $\text{CuK}\alpha$ at a goniometer speed of 0.5° per minute and a chart speed of 20 mm/min. All measurements were made at room temperature. The observed integrated intensities have been corrected for thermal diffuse scattering using the method of Chipman and Paskin [15].

3. Analysis of Data

For the relative intensity method, the expression for the observed intensities I_0 is given by

$$I_0 = CL_p J F_T^2 \quad (1)$$

where L_p is the Lorentz-polarization factor, J , the multiplicity factor, F_T the structure factor and C is a constant. For a flat powder specimen, the absorption correction is independent of the angle θ , Klug and Alexander [16] and, hence, is lumped with the constant. The structure factor F_T in terms of the structure factor F for the static lattice is given by

$$F_T = F e^{-M} \quad (2)$$

We may also write Eq. (1) as

$$I_0 = I_c e^{-2B \left(\frac{\sin \theta}{\lambda} \right)^2} \quad (3)$$

where I_c is the intensity corresponding to the static lattice and is given by

$$I_c = L_p J F^2 \quad (4)$$

For crystals with fcc structure, the structure factor F is given by

$$F = 4f \quad (5)$$

f being the atomic scattering factor. Values of the atomic scattering factor were taken from Cromer and Waber [17] and International Tables for X-ray Crystallography [18], and have been corrected for dispersion, Cromer and Liberman [19]. The choice of the atomic scattering factors was guided by Cromer's [17] recommendation who suggested that the atomic scattering factors given in the International Tables for X-ray Crystallography [18] which are computed from the Hartree-Fock wave functions are the best for the lighter atoms or ions in the periodic table up to Rb^{+1} . For the heavier atoms or ions Cromer recommends the use of the Dirac-slater relativistic scattering factors given by Cromer and Waber [17].

From Eq. (3) it can be seen that $\log(I_0/I_c)$ is linearly related to $(\sin \theta / \lambda)^2$. By a least square treatment of data, B was determined. From the Debye-Waller theory

$$B = \left(\frac{8\pi^2}{3} \right) \langle u^2 \rangle \quad (6)$$

for a cubic crystal, where $\langle u^2 \rangle$ is the mean-square amplitude of vibration. Further, B , may also be expressed as

$$B = \left(\frac{6h^2}{mk_B T} \right) W(x) \quad (7)$$

where m is the mass, T the absolute temperature and h and k_B are the Planck and the Boltzmann constants respectively. The function $W(x)$ is given by

$$W(x) = \left[\frac{\phi(x)}{x^2} + \frac{1}{4x} \right] \quad (8)$$

where $\phi(x)$ is the Debye function and $x = \theta_M/T$, θ_M being the Debye temperature. Benson and Gill [20] have tabulated values of $W(x)$ for a wide range of x for small increments, from which θ_M can be obtained from the value of B .

Lattice strain and Particle size determination

When the size of the individual crystals is less than about 100nm the term "particle size" is usually used. When the crystallites of a material are smaller than 100nm, they have too small a number of parallel diffraction planes and so they produce broadened diffraction peaks instead of a sharp peak. Lattice strain present in the sample is another cause of broadening of Bragg diffraction peaks. In addition to this, there are instrumental factors such as unresolved α_1 and α_2 peaks, imperfect focusing which lead to the line broadening. There are various methods in practice to estimate the particle size. X-ray diffraction is a simpler and easier approach for the determination of precise particle size and the lattice strain in powder samples. The principle involved in the X-ray diffraction approach is precise quantification of the broadening of the Bragg diffraction peaks. Scherrer equation, Hall-Williamson method and Warren-Averbach method are some of the techniques based on this principle. Of the above methods, Scherrer equation method for the estimation of particle size does not take into account the broadening due to lattice strain present in the sample. As such in the present investigation, the lattice strains have been estimated using Hall-Williamson method. Recently, Bharati *et al* [21] have used this method to estimate the lattice strain and particle sizes of silver nano particles and composite silver nano particles. In this method the integral breadth of the diffraction peak is determined. The integral breadth is given by the integrated intensity divided by the maximum intensity. Thus, the observed peak broadening B_0 may be represented as

$$B_o = B_i + B_r \quad (9)$$

where B_o is the observed peak broadening in radians, B_i is the instrumental broadening in radians and B_r is the broadening due to the small particle size and lattice strain. The instrumental broadening has been estimated using a pure strain-free fine sodium chloride powder sample subjected to XRD under identical conditions as those for the strained metallic powders. Eq. (9) holds good if the diffraction peaks exhibit purely Cauchy profile. However, when the diffraction peaks are partly Cauchy and partly Gaussian for profiles, the following relation between B_o , B_i and B_r holds good, Bharati *et al* [21].

$$B_r = [(B_o - B_i) (B_o^2 - B_i^2)^{1/2}]^{1/2} \quad (10)$$

Now, according to Scherrer equation, the broadening due to small particle size may be expressed as

$$B_c = \frac{k\lambda}{t} \cos\theta \quad (11)$$

where B_c is the broadening solely due to small crystallite size, K a constant whose value depends on particle shape and usually taken as unity, t the crystallite size in nanometers, θ the Bragg angle and λ is the wavelength of incident X-ray beam in nanometers.

Similarly, according to Wilson [22], the broadening due to lattice strain may be expressed by the relation,

$$B_s = \varepsilon \tan\theta \quad (12)$$

where B_s is the peak broadening due to lattice strain and ε the strain distribution within the material and θ is the Bragg angle. Based on Eqs. (11) and (12) the total peak broadening B_r may be expressed as,

$$B_r = \frac{k\lambda}{t \cos\theta} + \varepsilon \tan\theta \quad (13)$$

which can be written as

$$B_r \cos\theta = \frac{k\lambda}{t} + \varepsilon \sin\theta \quad (14)$$

The plot of $B_r \cos\theta/\lambda$ versus $\sin\theta/\lambda$ is a straight line with slope equal to ε and hence the particle size 't' can be estimated from the intercept. Typical Hall-Williamson plot between $B_r \cos\theta/\lambda$ and $\sin\theta/\lambda$ is shown in Fig. 2.

The lattice strains were determined from the plot of $B_r \cos\theta/\lambda$ against $\sin\theta/\lambda$ following standard procedures [23]. The measured half-widths were corrected for instrumental broadening with reference to a pure strain-free silicon powder. The variation of particle size with milling time is within the limits of experimental errors. This shows that while the milling is enough to create strains, it affect the particle size to a measurable extent. A typical Hall-Williamson plot is shown in Figure 2 for Ni after grinding for 12 hours.

4. Results and discussion

The values of the lattice strain, crystallite size, root mean square amplitude of vibrations, Debye-Waller factor and Debye temperature of Ni powders, ground for different durations, obtained in the present study are given in Table 1. For the comparison the scan electron microscopy (SEM) morphology of powder particles 0 hours and after 20 hours of milling is shown in Figure 3.

As the objective of the present work is to investigate the strain dependence of Debye-Waller factors, the variation of the lattice strain (ε) and Debye-Waller factor (B) for different milling times for fcc metal Ni is shown in Figure 3. Both lattice strain and Debye-Waller factor increase with milling time. This is similar to the observations of Inagaki *et al* [11,12], Sirdeshmuch *et al* [13] and Gopi Krishna and Sirdeshmukh [14]. The Debye-Waller factor increases with milling time and lattice strain in a slightly non-linear fashion and crystallite size decreases with milling time. An extrapolation of the B versus ε curve to $\varepsilon = 0$ gives the values of Debye-Waller factor 0.37 \AA^2 . The zero-strain values of Debye-Waller factor is less than the values for the initial samples. The zero strain Debye-Waller factor of 0.37 \AA^2 for Ni is close to the value of 0.39 \AA^2 obtained by Paakkari [10] using powder X-ray diffraction. Thus, the Debye-Waller factors of Ni powder samples carry an effect due to lattice strain. While comparing the Debye-Waller factors calculated from the lattice dynamical models with experimental results, Vetelino *et al* [24] have attributed the difference to inaccuracies in the experimental values caused by neglecting the TDS corrections. The repeated milling of the powder sample leads to lattice distortion which gives rise to microstrains in the lattice. These microstrains increase the contribution of static component of Debye-Waller factor. Thus both lattice strain and the observed Debye-Waller factor, which is the sum of static and thermal components, increase with milling time. Thus, whenever Debye-Waller factors are determined from X-ray intensities on powder samples, it is desirable to make an estimate of the lattice strain and if the strain is large, a suitable correction is to be made as done in the present study. The Debye

temperatures derived from the zero strain values of Debye-Waller factor of Ni is 405K. This value agrees well with the values of 397K [10], obtained for Ni from the powder X-ray diffraction.

Glyde [25] derived the following relation between the energy of vacancy formation (E_f) and the Debye temperature (θ) of a solid. The relation is

$$E_f = A(k/h)^2 M\theta^2 a^2 \quad (15)$$

where a is the interatomic spacing, A a constant shown to be equal to 1.17×10^{-2} , M the molecular weight and h and k are the Planck's and the Boltzmann's constants, respectively. Glyde recommended the use of X-ray based values in eq. (15). The validity of eq.(15) was verified for a number of fcc, bcc and hcp metals [26]. Therefore, the X-ray Debye temperatures obtained in the present work have been used to study the variation of vacancy formation energy as a function of lattice strain in Ni. The values of vacancy formation energies are also included in Table 1.

4. CONCLUSION

Ni powder was strained by milling for 20 hours. From a study of X-ray diffractograms recorded at different stages of milling, it is observed that milling for 20 hours has systematic effect on the particle size. However, the milling produces lattice strain and also enhances the effective Debye-Waller factor. By an extrapolation of the plot between the Debye-Waller factor and the lattice strain, the zero strain Debye-Waller factors are obtained for Ni. The variation of energy of vacancy formation as a function of lattice strain has been studied.

Acknowledgements The authors are grateful to the referee for suggestions. The authors thank University Grants Commission, New Delhi, for financial assistance under special assistance programme (SAP) No.F.530/8/DRS/2009(SAP-I).

Counts

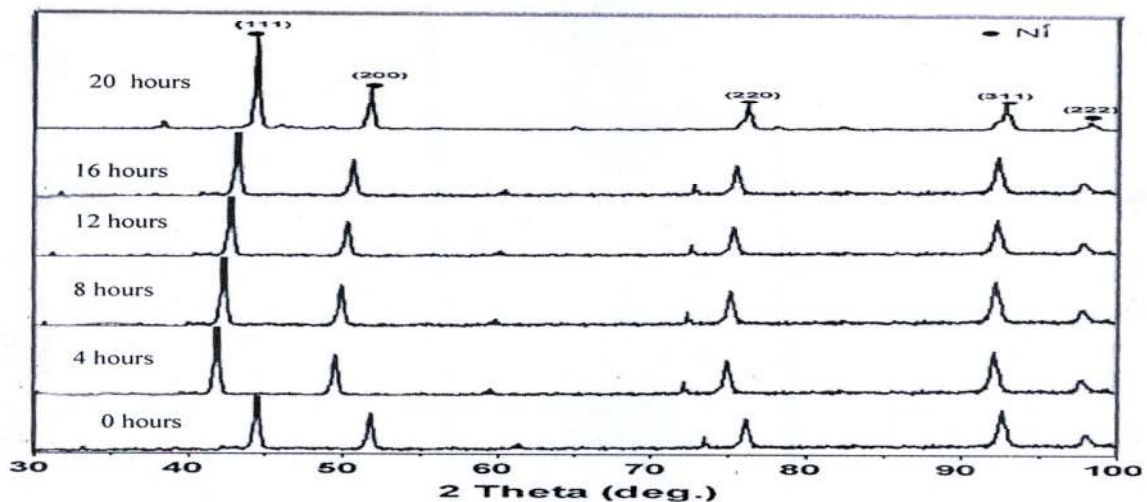


Figure 1. XRD pattern of Ni

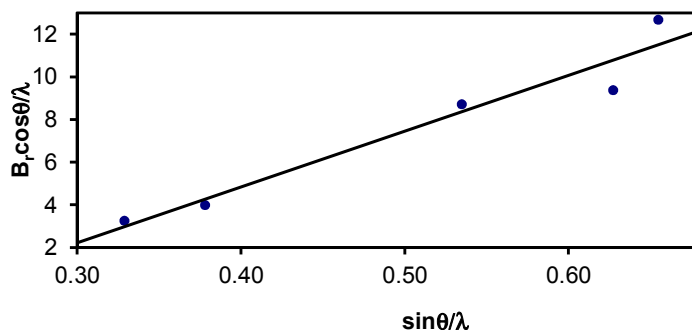


Figure 2. Plot of $B_r \cos \theta / \lambda$ Vs $\sin \theta / \lambda$ for Ni after milling for 12 hours.

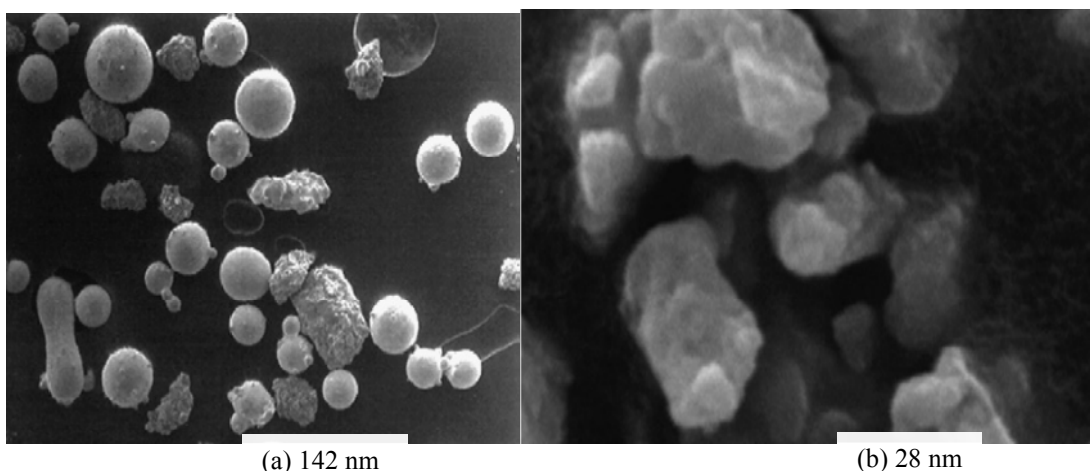


Figure 3. The Scan Electron Microscopy (SEM) morphology of powder particles (a) 0 hours and (b) after 20 hours of milling

Table 1. Values of lattice strain (ϵ), crystallite size (t), Debye-Waller factor (B), root mean square amplitudes of vibration $\langle u \rangle$, Debye temperature (θ_M) and energy of vacancy formation (E_f) of strained Nickel nano powders.

Metal	Milling time	$\epsilon \times 10^3$	$t(\text{nm})$	$\langle u \rangle (\text{\AA})$	$B(\text{\AA}^2)$	$\theta_M(\text{K})$	$E_f(\text{eV})$
Ni	0	1.11	145	0.00507 (3)	0.40 (2)	390 (5)	2.32
	4	1.89	114	0.00557(4)	0.44 (3)	372 (7)	2.11
	8	2.28	73	0.00608(1)	0.48 (1)	354 (3)	1.91
	12	2.85	46	0.00646 (5)	0.51 (4)	345(12)	1.81
	16	3.42	37	0.00697 (8)	0.55 (3)	333 (4)	1.69
	20	4.06	29	0.00747 (6)	0.59 (5)	321 (7)	1.57

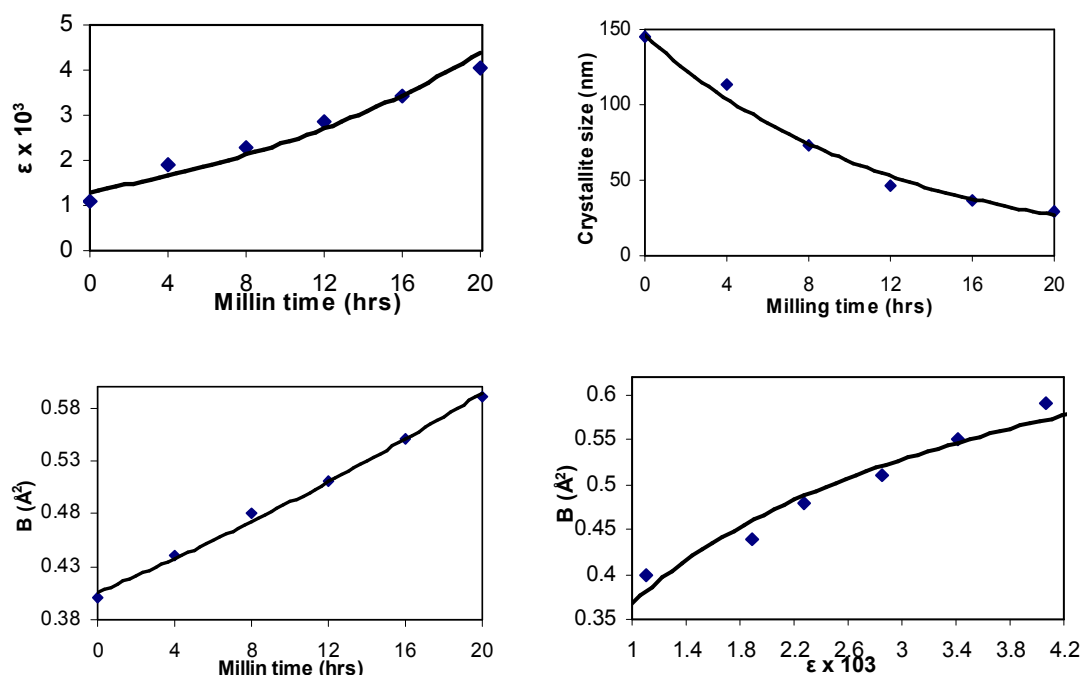


Figure 3. Milling time Vs lattice strain, Crystallite size and Debye-Waller factor and lattice strain Vs Debye-Waller factor curves for Ni

References

- [1] Shengqi, C.H., Yanchun, Z.H., Yiyi, L., 1997. Mater. Sci. Tech. 13,86–90.
- [2] Froes, F.H., Senkov, O.N., Baburaj, E., 2001. Mater. Sci. Eng. A 301, 44–53.
- [3] Zhang, D.L., 2004. Prog. Mater. Sci. 49, 537–560
- [4] Klement, U., Erb, U., Aust, K.T., 1995a. Nanostruct. Mater. 6, 581–586.
- [5] Valiev, R.Z., Mishra, R.S., Groza, J., Mukherjee, A.K., 1996. Scripta Mater. 34, 1443–1448.
- [6] Pabi, S.K., Joardar, J., Murthy, B.S., 1996. J. Mater. Sci. 31, 3207– 3211.
- [7] Zakeri, M., Yazdani-Rad, R., Enayati, M.H., Rahimipour, M.R., 2005. J. Alloys Compd. 403, 258–261.
- [8] Mousavi, T., Karimzadeh, F., Abbasi, M.H. Mater. Sci. Eng., in press.
- [9] Suryanarayana, C., 2001. Prog. Mater. Sci. 46, 1–184.
- [10] Paakkari, T. (1974). *Acta Cryst.* A30, 83.
- [11] Inagaki, M. Furuhashi, H., Ozeki *et al.*, *J Mater Sci.* 6, (1971) 1520.
- [12] M Inagaki, H Furuhashi, T Ozeki and S Naka *J.Mater. Sci.* 8, (1973) 312.
- [13] Sirdeshmukh, D.B., Subhadra, K.G., Hussain, K.A., Gopi Krishna, N., and Rag-havendra Rao. B., *Cryst.Res.Technol* 28, (1993) 15.
- [14] Gopi Krishna, N., and Sirdeshmukh., D.B., *Indian J Pure & Appl Phys.*31, (1993)198.
- [15] Chipman, D.R., and Paskin, A., *J.Appl. Phys.* 30, (1959) 1938.
- [16] Klug, H.P., and Alexander, L.E., (1974). *X-ray Diffraction Procedures* (John Wiley and Sons, U.S.A.).
- [17] Cromer, D.T., and Waber, J.T., *Acta Cryst.* 18, (1965) 104.
- [18] International Tables for X-ray Crystallography (1968) Vol. III (Kynoch Press, Birmingham).
- [19] Cromer, D.T., and Liberman, D., *J. Chem. Phys.* 53, (1970) 1891.
- [20] Benson, G.C., and Gill, E.K., (1966) Table of Integral Functions Related to Debye-Waller factor, National Research Council of Canada, Ottawa.
- [21] Bharati, R., Rehani, P.B., Joshi, Kirit N., Lad and Arun Pratap, *Indian Journal of Pure and Applied Physics*, 44, (2006) 157-161.
- [22] Wilson, A.J.C., (1949). *X-ray Optics* (Methuen, London).
- [23] Kaelble, E.F., *Handbook of X-rays* (New York Mc Graw ill) (1967)
- [24] Vetelino, J.F., Gaur, S.P., Mitra, S.S., *Phys. Rev.* B5, (1972) 2360.
- [25] Glyde, H.R., *J.Phys and Chem Solids* (G.B) 28, (1967) 2061.
- [26] *Micro-and Macro-Properties of Solids* (Springer Series in Material Science) (2006)

The IISTE is a pioneer in the Open-Access hosting service and academic event management. The aim of the firm is Accelerating Global Knowledge Sharing.

More information about the firm can be found on the homepage:

<http://www.iiste.org>

CALL FOR JOURNAL PAPERS

There are more than 30 peer-reviewed academic journals hosted under the hosting platform.

Prospective authors of journals can find the submission instruction on the following page: <http://www.iiste.org/journals/> All the journals articles are available online to the readers all over the world without financial, legal, or technical barriers other than those inseparable from gaining access to the internet itself. Paper version of the journals is also available upon request of readers and authors.

MORE RESOURCES

Book publication information: <http://www.iiste.org/book/>

Academic conference: <http://www.iiste.org/conference/upcoming-conferences-call-for-paper/>

IISTE Knowledge Sharing Partners

EBSCO, Index Copernicus, Ulrich's Periodicals Directory, JournalTOCS, PKP Open Archives Harvester, Bielefeld Academic Search Engine, Elektronische Zeitschriftenbibliothek EZB, Open J-Gate, OCLC WorldCat, Universe Digital Library, NewJour, Google Scholar

