

Yukawa alignment in the two-Higgs-doublet model

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(Received 10 August 2009; published 19 November 2009)

In multi-Higgs-doublet models the alignment in flavor space of the relevant Yukawa matrices guarantees the absence of tree-level flavor-changing couplings of the neutral scalar fields. We analyze the consequences of this condition within the two-Higgs-doublet model and show that it leads to a generic Yukawa structure which contains as particular cases all known specific implementations of the model based on Z_2 symmetries. All possible freedom in the Yukawa sector gets parametrized in terms of three complex couplings ς_f . In spite of having flavor conservation in the neutral scalar couplings, the phases of these three parameters represent potential new sources of CP violation.

DOI: 10.1103/PhysRevD.80.091702

PACS numbers: 12.60.Fr, 11.30.Hv, 12.15.Mm, 14.80.Cp

I. INTRODUCTION

The two-Higgs-doublet model (THDM) [1,2] constitutes one of the simplest extensions of the standard model (SM) and incorporates new and interesting phenomenological features. Many new-physics scenarios, including supersymmetry, can lead to a low-energy spectrum containing the SM fields plus only one additional scalar doublet. Therefore, the THDM is also a very convenient effective field theory framework to investigate low-energy effects of more generic dynamical settings. The extended scalar sector accommodates two charged and three neutral scalar fields, in addition to the three Goldstones needed to generate the gauge boson masses. This rich scalar spectrum provides a broad range of dynamical possibilities, such as potential new sources of CP symmetry breaking, including spontaneous CP violation, axion phenomenology or dark matter candidates, just to mention a few.

In the most general version of the THDM, the fermionic couplings of the neutral scalars are nondiagonal in flavor. The appearance of flavor-changing neutral current (FCNC) interactions represents a major shortcoming of the model. Since FCNC phenomena are experimentally tightly constrained, one needs to implement *ad hoc* dynamical restrictions to guarantee the suppression of the FCNC couplings at the required level. For instance, the assumption that the nondiagonal Yukawa couplings are proportional to the geometric mean of the two fermion masses, $g_{ij} \propto \sqrt{m_i m_j}$ [3], leads to a phenomenologically viable model usually known as “Type III” [4]. Models of this kind can be generated through particular textures of the Yukawa coupling matrices [3]. Another obvious possibility is to require the scalar boson masses to be heavy enough to suppress any low-energy FCNC effects induced through the scalar fields, but this drastically decreases the potential phenomenological relevance of the THDM.

A more elegant solution makes use of appropriately chosen discrete Z_2 symmetries such that only one scalar doublet couples to a given right-handed fermion field [5]. This guarantees the absence of FCNCs in the Yukawa

sector, but eliminates at the same time the possibility to have additional CP -violating phases beyond the standard Kobayashi-Maskawa one. There are several possible models of this type, corresponding to different explicit implementations of the Z_2 symmetry. The minimal supersymmetric extension of the SM corresponds at tree level with one particular choice, the so-called “Type-II” THDM, which is the default version adopted in the majority of phenomenological analyses.

Flavor conservation in the neutral scalar couplings can be enforced in a rather trivial way requiring the Yukawa coupling matrices to be aligned in flavor space. While this is also an *ad hoc* constraint, lacking a proper dynamical explanation (probably coming from a more fundamental high-energy theory), it leads to a much more general framework which contains as particular cases all known THDMs based on Z_2 symmetries. All possible freedom in the Yukawa sector gets parametrized in terms of three complex couplings ς_f ; their phases being possible new sources of CP violation. The general structure of this “aligned” THDM is discussed next, together with some relevant phenomenological implications.

II. THE TWO-HIGGS DOUBLET MODEL

In its minimal version, that we are going to consider here, the THDM is an $SU(3)_C \otimes SU(2)_L \otimes U(1)_Y$ theory with the fermion SM content (without right-handed neutrinos) and two scalar doublets $\phi_a(x)$ ($a = 1, 2$) with hypercharge $Y = \frac{1}{2}$. The charge-conjugate fields $\tilde{\phi}_a(x) \equiv i\tau_2 \phi_a^*$ are also $SU(2)$ doublets with $Y = -\frac{1}{2}$. The neutral components of the two scalar doublets acquire vacuum expectation values $\langle 0 | \phi_a^T(x) | 0 \rangle = \frac{1}{\sqrt{2}} (0, v_a e^{i\theta_a})$. Without loss of generality, we can enforce $\theta_1 = 0$ through an appropriate $U(1)_Y$ transformation, leaving the relative phase $\theta \equiv \theta_2 - \theta_1$. The gauge boson masses, which receive contributions from the two vacuum expectation values v_a , are given by the same expressions than in the SM, with $v \equiv \sqrt{v_1^2 + v_2^2}$.

Using a global $SU(2)$ transformation in the scalar space (ϕ_1, ϕ_2) , it is possible to define a basis of scalar doublet fields (the so-called Higgs basis) such that only Φ_1 has nonzero vacuum expectation value ($\tan\beta \equiv v_2/v_1$):

$$\begin{pmatrix} \Phi_1 \\ -\Phi_2 \end{pmatrix} \equiv \begin{bmatrix} \cos\beta & \sin\beta \\ \sin\beta & -\cos\beta \end{bmatrix} \begin{pmatrix} \phi_1 \\ e^{-i\theta}\phi_2 \end{pmatrix}. \quad (1)$$

This has the advantage that the three Goldstone fields $G^\pm(x)$ and $G^0(x)$ get isolated as components of Φ_1 :

$$\begin{aligned} \Phi_1 &= \begin{bmatrix} G^+ \\ \frac{1}{\sqrt{2}}(v + S_1 + iG^0) \end{bmatrix}, \\ \Phi_2 &= \begin{bmatrix} H^+ \\ \frac{1}{\sqrt{2}}(S_2 + iS_3) \end{bmatrix}. \end{aligned}$$

The physical scalar spectrum contains 5 degrees of freedom: the charged fields $H^\pm(x)$ and three neutral scalars $\varphi_i^0(x) = \{h(x), H(x), A(x)\}$, which are related through an orthogonal transformation with the S_i fields: $\varphi_i^0(x) = \mathcal{R}_{ij}S_j(x)$. The form of the \mathcal{R} matrix is fixed by the scalar potential, which determines the neutral scalar mass matrix and the corresponding mass eigenstates. In general, the CP -odd component S_3 mixes with the CP -even fields $S_{1,2}$ and the resulting mass eigenstates do not have a definite CP quantum number. If the scalar potential is CP symmetric this admixture disappears; in this particular case, $A(x) = S_3(x)$ and

$$\begin{pmatrix} H \\ h \end{pmatrix} = \begin{bmatrix} \cos(\alpha - \beta) & \sin(\alpha - \beta) \\ -\sin(\alpha - \beta) & \cos(\alpha - \beta) \end{bmatrix} \begin{pmatrix} S_1 \\ S_2 \end{pmatrix}. \quad (2)$$

III. YUKAWA INTERACTIONS

The most general Yukawa Lagrangian is given by

$$\begin{aligned} \mathcal{L}_Y &= -\bar{Q}'_L(\Gamma_1\phi_1 + \Gamma_2\phi_2)d'_R - \bar{Q}'_L(\Delta_1\tilde{\phi}_1 + \Delta_2\tilde{\phi}_2)u'_R \\ &\quad - \bar{L}'_L(\Pi_1\phi_1 + \Pi_2\phi_2)l'_R + \text{H.c.}, \end{aligned} \quad (3)$$

where Q'_L and L'_L denote the left-handed quark and lepton doublets. All fermionic fields are written as N_G -dimensional flavor vectors; i.e., $d'_R = (d'_R, s'_R, b'_R, \dots)$ and similarly for u'_R, l'_R, Q'_L and L'_L . The couplings Γ_a, Δ_a and Π_a are $N_G \times N_G$ complex matrices in flavor space. In the Higgs basis, the Lagrangian takes the form

$$\begin{aligned} \mathcal{L}_Y &= -\frac{\sqrt{2}}{v} \{ \bar{Q}'_L(M'_d\Phi_1 + Y'_d\Phi_2)d'_R \\ &\quad + \bar{Q}'_L(M'_u\tilde{\Phi}_1 + Y'_u\tilde{\Phi}_2)u'_R + \bar{L}'_L(M'_l\Phi_1 + Y'_l\Phi_2)l'_R \\ &\quad + \text{H.c.} \}, \end{aligned} \quad (4)$$

where M'_f ($f = d, u, l$) are the nondiagonal fermion mass

matrices, while the matrices Y'_f contain the Yukawa couplings to the scalar doublet with zero vacuum expectation value.

In the basis of fermion mass eigenstates $d(x), u(x), l(x), \nu(x)$, with diagonal mass matrices M_f ($M_\nu = 0$), the corresponding matrices Y_f are in general nondiagonal and unrelated to the fermion masses. Thus, the Yukawa Lagrangian generates flavor-changing interactions of the neutral scalars because there are two different Yukawa matrices coupling to a given right-handed fermion field, which in general cannot be diagonalized simultaneously. The standard way to avoid this problem is forcing one of the two matrices to be zero; i.e., imposing that only one scalar doublet couples to a given right-handed fermion field [5]. This can be enforced implementing a discrete Z_2 symmetry, such that $\phi_1 \rightarrow \phi_1, \phi_2 \rightarrow -\phi_2, Q_L \rightarrow Q_L, L_L \rightarrow L_L$ and selecting appropriate transformation properties for the right-handed fermion fields. There are four nonequivalent possible choices, giving rise to the so-called type-I (only ϕ_2 couples to fermions) [6,7], type-II (ϕ_1 couples to d and l , while ϕ_2 couples to u) [7,8], leptophilic or type-X (ϕ_1 couples to leptons and ϕ_2 to quarks) and type-Y (ϕ_1 couples to d , while ϕ_2 couples to u and l) models [9–12]. The explicit implementation of the Z_2 symmetry is scalar-basis dependent. If the Z_2 symmetry is imposed in the Higgs basis, all fermions are forced to couple to the field Φ_1 in order to get nonvanishing masses. This *inert* doublet model provides a natural frame for dark matter [13–15]; note however that although Φ_2 does not couple to fermions, it does have electroweak interactions.

A softer and more general way to avoid tree-level FCNC interactions is to require the alignment in flavor space of the Yukawa couplings of the two scalar doublets. It is convenient to implement this condition in the form:

$$\begin{aligned} \Gamma_2 &= \xi_d e^{-i\theta} \Gamma_1, & \Delta_2 &= \xi_u^* e^{i\theta} \Delta_1, \\ \Pi_2 &= \xi_l e^{-i\theta} \Pi_1. \end{aligned} \quad (5)$$

The proportionality parameters ξ_f are arbitrary complex numbers. To simplify later equations, we have redefined these parameters introducing the explicit phases $e^{\mp i\theta}$ which cancel the relative global phases between the two scalar doublets. The Yukawa alignment guarantees that the Y'_f and M'_f matrices are proportional and, therefore, can be simultaneously diagonalized with the result:

$$Y_{d,l} = s_{d,l} M_{d,l}, \quad Y_u = s_u^* M_u, \quad s_f \equiv \frac{\xi_f - \tan\beta}{1 + \xi_f \tan\beta}. \quad (6)$$

In terms of the mass-eigenstate fields, the Yukawa interactions take then the form:

$$\begin{aligned}
\mathcal{L}_Y = & -\frac{\sqrt{2}}{v} H^+(x) \bar{u}(x) [\mathfrak{s}_d V M_d \mathcal{P}_R - \mathfrak{s}_u M_u V \mathcal{P}_L] d(x) \\
& -\frac{\sqrt{2}}{v} H^+(x) \mathfrak{s}_l \bar{\nu}(x) M_l \mathcal{P}_R l(x) \\
& -\frac{1}{v} \sum_{\varphi_i^0, f} \varphi_i^0(x) y_f^{\varphi_i^0} \bar{f}(x) M_f \mathcal{P}_R f(x) + \text{H.c.} \quad (7)
\end{aligned}$$

where V is the Cabibbo-Kobayashi-Maskawa quark-mixing matrix and $\mathcal{P}_{R,L} \equiv \frac{1}{2}(1 \pm \gamma_5)$ the chirality projectors.

The flavor alignment of the Yukawa couplings results in a very specific structure for the scalar-fermion interactions:

- (i) All fermionic couplings of the physical scalar fields are proportional to the corresponding fermion mass matrices.
- (ii) The neutral Yukawas are diagonal in flavor. The couplings of the physical scalar fields H , h and A are obviously proportional to the corresponding elements of the orthogonal matrix \mathcal{R} ,

$$\begin{aligned}
y_{d,l}^{\varphi_i^0} &= \mathcal{R}_{i1} + (\mathcal{R}_{i2} + i\mathcal{R}_{i3}) \mathfrak{s}_{d,l} \\
y_u^{\varphi_i^0} &= \mathcal{R}_{i1} + (\mathcal{R}_{i2} - i\mathcal{R}_{i3}) \mathfrak{s}_u^* \quad (8)
\end{aligned}$$

- (iii) The only source of flavor-changing phenomena is the quark-mixing matrix V , which regulates the quark couplings of the W^\pm gauge bosons and the charged scalars H^\pm .
- (iv) All leptonic couplings are diagonal in flavor. This is obviously related to the absence of right-handed neutrino fields in our low-energy Lagrangian. Since neutrinos are massless, the leptonic mixing matrix V_L can be reabsorbed through a redefinition of the neutrino fields: $\bar{\nu} \cdot V_L \rightarrow \bar{\nu}$.
- (v) The only new couplings introduced by the Yukawa Lagrangian are the three parameters \mathfrak{s}_f , which encode all possible freedom allowed by the alignment conditions. These couplings satisfy universality among the different generations: all fermions of a given electric charge have the same universal coupling \mathfrak{s}_f . Moreover, the parameters \mathfrak{s}_f are invariant under global $SU(2)$ transformations of the scalar fields, $\phi_a \rightarrow \phi'_a = U_{ab} \phi_b$ [16]; i.e., they are independent of the basis choice adopted in the scalar space.
- (vi) The usual models with a single scalar doublet coupling to each type of right-handed fermions are recovered taking the appropriate limits $\xi_f \rightarrow 0$ or $\xi_f \rightarrow \infty$ ($1/\xi_f \rightarrow 0$); i.e., $\mathfrak{s}_f \rightarrow -\tan\beta$ or $\mathfrak{s}_f \rightarrow \cot\beta$. The type-I model corresponds to $(\xi_d, \xi_u, \xi_l) = (\infty, \infty, \infty)$, type-II to $(0, \infty, 0)$, type-X to $(\infty, \infty, 0)$ and type-Y to $(0, \infty, \infty)$. The *inert* doublet model corresponds to $\mathfrak{s}_f = 0$ ($\xi_f = \tan\beta$).

TABLE I. Choices of couplings \mathfrak{s}_f which correspond to models with discrete Z_2 symmetries.

| Model | \mathfrak{s}_d | \mathfrak{s}_u | \mathfrak{s}_l |
|---------|------------------|------------------|------------------|
| Type-I | $\cot\beta$ | $\cot\beta$ | $\cot\beta$ |
| Type-II | $-\tan\beta$ | $\cot\beta$ | $-\tan\beta$ |
| Type-X | $\cot\beta$ | $\cot\beta$ | $-\tan\beta$ |
| Type-Y | $-\tan\beta$ | $\cot\beta$ | $\cot\beta$ |
| Inert | 0 | 0 | 0 |

The \mathfrak{s}_f values for all these particular models based on Z_2 symmetries are given in Table I.

- (vii) The \mathfrak{s}_f can be arbitrary complex numbers, opening the possibility to have new sources of CP violation without tree-level FCNCs.

The Yukawa alignment provides a general setting to discuss the phenomenology of THDMs without tree-level FCNCs, parametrizing the different possibilities through the three complex couplings \mathfrak{s}_f .

IV. QUANTUM CORRECTIONS

Quantum corrections could introduce some misalignment of the Yukawa coupling matrices, generating small FCNC effects suppressed by the corresponding loop factors. However, the special structure of the aligned THDM strongly constrains the possible FCNC interactions.

The Lagrangian of the aligned THDM is invariant under flavor-dependent phase transformations of the fermion mass eigenstates, $f_i(x) \rightarrow e^{i\alpha_i^f} f_i(x)$, provided the quark-mixing matrix is transformed as $V_{ij} \rightarrow e^{i\alpha_i^f} V_{ij} e^{-i\alpha_j^f}$. Here $f = d, u, l, \nu$, while the subindex i refers to the different fermion generations. Since the equivalent lepton mixing matrix has been reabsorbed into the neutrino fields, the redefined $\nu_i(x)$ fields have $\alpha_i^\nu = \alpha_i^l$. Owing to this symmetry, lepton-flavor-violating neutral couplings are identically zero to all orders in perturbation theory, because there is neither lepton mixing in the charged-current couplings in the absence of right-handed neutrinos. The usually adopted Z_2 symmetries are unnecessary in the lepton sector, making the model variants ‘‘Type-X’’ and ‘‘Type-Y’’ less compelling. From a phenomenological point of view, the coupling \mathfrak{s}_l can take any value. In fact, a leptophobic (or lepton-inert) model with $\mathfrak{s}_l = 0$ is a perfectly acceptable possibility, independently of the assumed structure of the quark couplings. Thus, one could easily evade all phenomenological constraints coming from leptonic or semi-leptonic processes.

In the quark sector the quark-mixing matrix can induce FCNC structures of the type $\bar{u}_i F_{ij}^u u_j$ or $\bar{d}_i F_{ij}^d d_j$. To preserve the symmetry under phase redefinitions of the quark fields, the matrices F_{ij}^q should transform as $F_{ij}^u \rightarrow e^{i\alpha_i^u} F_{ij}^u e^{-i\alpha_j^u}$ and $F_{ij}^d \rightarrow e^{i\alpha_i^d} F_{ij}^d e^{-i\alpha_j^d}$. This determines F_{ij}^q to adopt the forms $F_{ij}^u = \sum_k V_{ik} g(m_{d_k}) V_{kj}^\dagger$ and $F_{ij}^d = \sum_k V_{ik}^\dagger \tilde{g}(m_{u_k}) V_{kj}$,

or similar ones with more factors of V and V^\dagger . For $i \neq j$, the unitarity of V (GIM mechanism) makes necessary the presence of mass-dependent factors through the loop functions $g(m_{d_k})$ and $\tilde{g}(m_{u_k})$. The only possible local FCNC terms are then of the type ($n, m > 0$) $F^u = V(M_d)^n V^\dagger$ and $F^d = V^\dagger(M_u)^m V$ (or similar structures with additional factors of V and V^\dagger). Therefore, the flavor mixing induced by loop corrections has a very characteristic structure which resembles the popular minimal flavor violation scenarios [17]. Notice however that local FCNC terms shall disappear whenever the ς_f parameters approach any of the different sets of values given in Table I, because these limits are protected by corresponding Z_2 symmetries (provided the scalar potential is Z_2 symmetric). One-loop FCNC effects are then very constrained.

V. DISCUSSION

One of the most distinctive features of the THDM is the presence of a charged scalar. The process $e^+e^- \rightarrow H^+H^-$ provides a very efficient way to search for H^\pm without referring to any specific Yukawa structure. Assuming that $\text{Br}(H^+ \rightarrow c\bar{s}) + \text{Br}(H^+ \rightarrow \tau^+\nu_\tau) = 1$, the combined LEP data constrain $M_{H^\pm} > 78.6$ GeV (95% CL) [18]. The limit slightly improves if particular values of $B_\tau \equiv \text{Br}(H^+ \rightarrow \tau^+\nu_\tau)$ are assumed. The weakest limit of 78.6 GeV is obtained for $B_\tau \sim 0.4\text{--}0.5$, improving to 81.0 (89.6) for $B_\tau = 0$ (1) which corresponds to $\varsigma_l = 0$ ($\varsigma_{u,d} = 0$). These limits could be avoided for a fermiophobic (inert) THDM with $\varsigma_f \ll 1$. The charged scalar could then be detected through the decay mode $H^\pm \rightarrow W^\pm A$, provided it is kinematically allowed. Assuming a CP -conserving scalar potential, OPAL finds the (95% CL) constraints $M_{H^\pm} > 56.5(64.8)$ GeV for $12(15)$ GeV $< M_A < M_{H^\pm} - M_{W^\pm}$ [19].

CDF [20] and D0 [21] have searched for $t \rightarrow H^+b$ decays with negative results. CDF assumes $\text{Br}(H^+ \rightarrow c\bar{s}) = 1$ ($\varsigma_l \ll \varsigma_{u,d}$), while D0 adopts the opposite hypothesis $\text{Br}(H^+ \rightarrow \tau^+\nu_\tau) = 1$ ($\varsigma_l \gg \varsigma_{u,d}$). Both experiments find upper bounds on $\text{Br}(t \rightarrow H^+b)$ around 0.2 (95% CL) for charged scalar masses between 60 to 155 GeV. This implies $|\varsigma_u| < 0.3\text{--}2.5$, the exact number depending on the particular value of M_{H^\pm} within the analyzed range.

Weak decays provide valuable probes of virtual H^\pm contributions. The $\tau \rightarrow \mu/e$ lepton universality test

$|g_\mu/g_e| = 1.0000 \pm 0.0020$ [22] gives the lower bound $M_{H^\pm}/|\varsigma_l| > 1.78$ GeV (90% CL). Owing to the helicity suppression of the SM amplitude, the semileptonic decays $P^+ \rightarrow l^+\nu_l$ are more sensitive to H^+ exchange: $\Gamma(P_{ij}^+ \rightarrow l^+\nu_l)/\Gamma(P_{ij}^+ \rightarrow l^+\nu_l)_{\text{SM}} = |1 - \Delta_{ij}|^2$, with $\Delta_{ij} = (m_{P_{ij}^\pm}/M_{H^\pm})^2 \varsigma_l^* (\varsigma_u m_{u_i} + \varsigma_d m_{d_j}) / (m_{u_i} + m_{d_j})$. The correction Δ_{ij} is in general complex and its real part could have either sign. To determine its size one needs to know V_{ij} (extracted from P_{13} decays which are much less sensitive to scalar contributions) and a theoretical determination of the meson decay constant. From the present knowledge on $B^+ \rightarrow \tau^+\nu_\tau$ [23], we obtain $|1 - \Delta_{ub}| = 1.32 \pm 0.20$ which implies $M_{H^\pm}/\sqrt{|\text{Re}(\varsigma_l^* \varsigma_d)|} > 5.7$ GeV (90% CL). Using $f_{D_s} = 242 \pm 6$ MeV [24], the recent CLEO measurement $\text{Br}(D_s^+ \rightarrow \tau^+\nu_\tau) = (5.62 \pm 0.44)\%$ [25] implies $|1 - \Delta_{cs}| = 1.07 \pm 0.05$ and $M_{H^\pm}/\sqrt{|\text{Re}(\varsigma_l^* \varsigma_u)|} > 4.4$ GeV (90% CL).

FCNC processes induced at the quantum level, such as $b \rightarrow s\gamma$ or $P^0 - \bar{P}^0$ mixing, are also very sensitive to scalar contributions and provide strong constraints on the parameter space ($M_{H^\pm}, \varsigma_u, \varsigma_d$). In the CP -conserving limit, these type of transitions have been already analyzed within THDMs with discrete Z_2 symmetries [12,26] or adopting the ‘‘Type III’’ ansatz [4,26]. A detailed phenomenological analysis within the more general aligned THDM is under way. Of particular interest are the CP -violating effects induced by the complex phases of the ς_f parameters. They represent a new source of CP violation in the Yukawa sector which does not introduce any dangerous FCNC couplings at tree level. The structure of the aligned THDM at higher orders is also worth investigating. While loop corrections could generate some misalignment of the Yukawa structures, the resulting FCNC phenomena are strongly constrained by the symmetries of the aligned THDM Lagrangian. We plan to analyze these questions in future publications.

ACKNOWLEDGMENTS

This work has been supported in part by the EU Contract No. MRTN-CT-2006-035482 (FLAVIANet), by MICINN, Spain [grants FPA2007-60323 and Consolider-Ingenio 2010 CSD2007-00042 CPAN] and by Generalitat Valenciana (PROMETEO/2008/069).

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